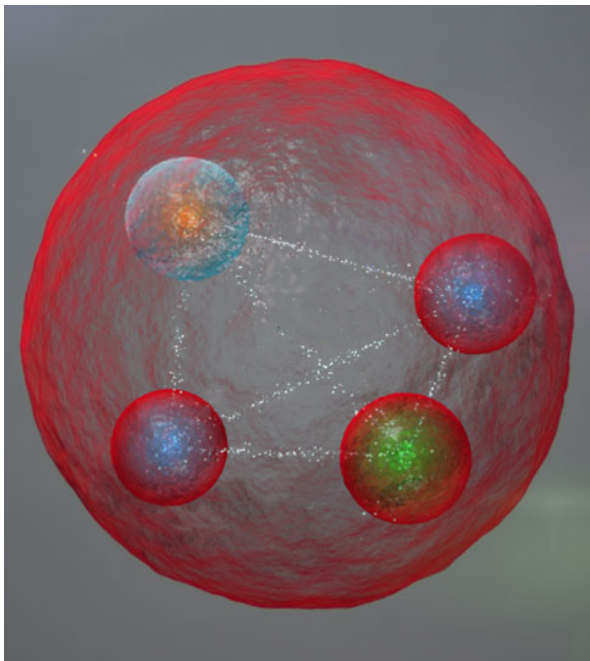


Tetraquarks and Pentaquarks

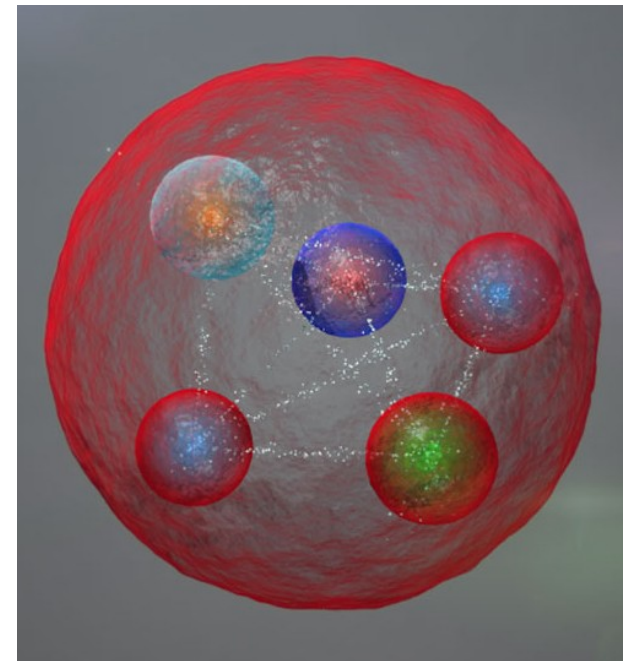
based in part on forthcoming IoP eBook by TG and Greig Cowan
also drawing extensively on [Rev. Mod. Phys. 90 \(2018\) 015003](#)

Tim Gershon
University of Warwick

Seminar at University of Birmingham
2nd May 2018



Tetraquarks and Pentaquarks



The birth of the quark model

- Nowadays, usual to think of hadrons as being either
 - $q\bar{q}$ mesons or qqq baryons ($\bar{q}\bar{q}\bar{q}$ antibaryons)
- But these are not the only options, as has been known since the start of the quark model

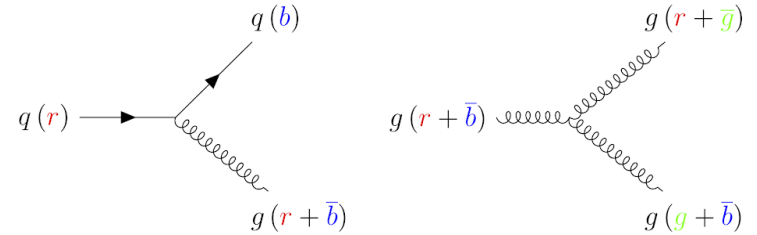
Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assuming that the lowest baryon configuration (qqq) gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration $(q\bar{q})$ similarly gives just **1** and **8**.

M. Gell-Mann, Phys. Lett. 8 (1964) 214

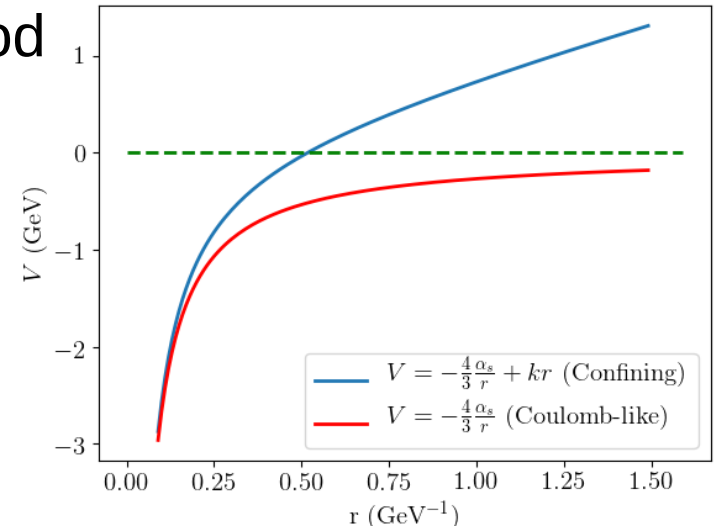
- **Where are the $qqqq$ tetraquarks and $qqqq\bar{q}$ pentaquarks?**

QCD basics

- Due to confinement, bound states must be colourless
 - rgb (baryons) or $r\bar{r}+g\bar{g}+b\bar{b}$ (mesons)
 - thus, $\bar{r} \equiv gb$, etc., as regards SU(3)
 - important for diquark model
 - baryons can be modelled as quark-diquark mesons



- Perturbative methods do not work at low energies
 - can use NRQCD based on an effective potential
 - lattice QCD important & predictive method
 - limited by available computing power
 - not a silver bullet to understand hadrons



Tetraquarks and Pentaquarks

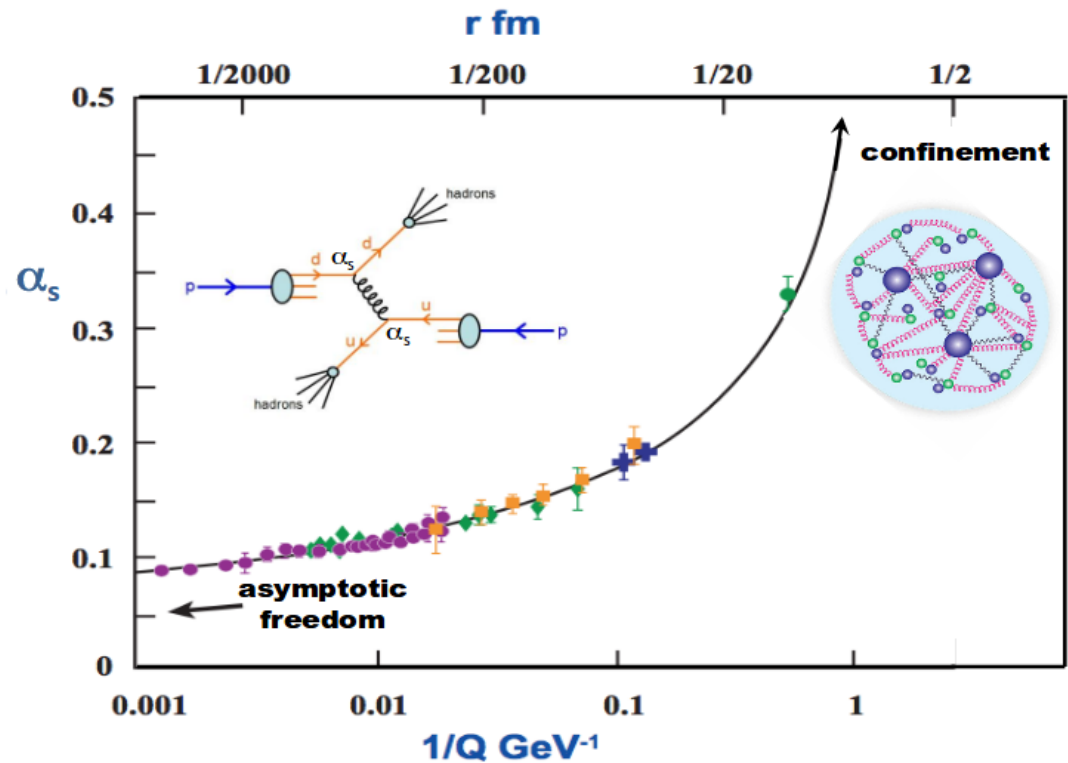
What do we learn from hadrons?

- New states, bound by QCD, do not test the SM per se
- Yet they do provide insight into a murky corner of the SM, namely confinement

Think you understand confinement?

Solve the Millennium prize!

<http://www.claymath.org/millennium-problems/yang--mills-and-mass-gap>



Rev. Mod. Phys. 90 (2018) 015003

What do we learn from hadrons?

- New states, bound by QCD, do not test the SM per se
- Yet they do provide insight into a murky corner of the SM, namely confinement
- **Understanding strong interactions could be important for new high energy phenomena**
 - Higgs boson as a composite state
 - Strong interactions in a dark sector (e.g. [arXiv:1602.00714](#))
 - Hadronic dark matter?
- Exotic spectroscopy is an open and fast moving field – exciting and fun to be involved
 - n.b. will use “exotic” to refer to anything that is not “conventional”

A stable sexaquark?

arXiv:1708.08951

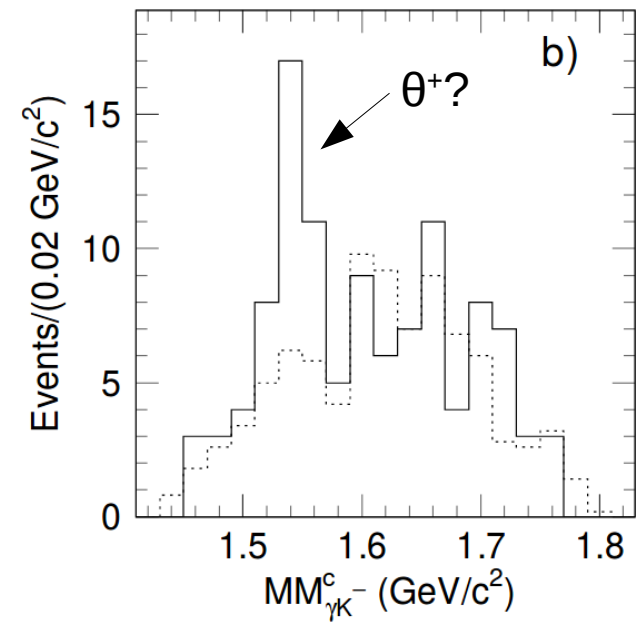
- The **uuddss** sexaquark S
 - with baryon number 2 (similar states sometimes called dibaryons)
 - **has a totally symmetric wavefunction, hence large binding energy**
 - if $m_S < m_d + m_e \sim 2(m_p + m_e)$ is completely stable
 - else if $m_S < m_p + m_e + m_\Lambda$ is effectively stable
 - **could be a dark matter candidate**
- This model has issues, but still interesting
 - Oxygen decay through $NN \rightarrow SX$ not seen in Super Kamiokande (arXiv:1803.10242)
- Dedicated searches possible (e.g. in Y decay at B factories)

Why is this relevant now?

- Searches for exotic hadrons have been ongoing for ~50 years *with light quarks*
 - some claimed signals for pentaquarks which led to nothing ...

LEPS collaboration
Phys.Rev.Lett. 91 (2003) 012002

- See also DIANA, CLAS, SAPHIR, NA49, HERMES, SVD, COSY-TOF, ZEUS, H1, ...
- Many peaks disappeared with more data and more careful analyses
- Non-observations in other experiments
- See hep-ph/0703004 for a review
- (Not all claims completely disproved yet)

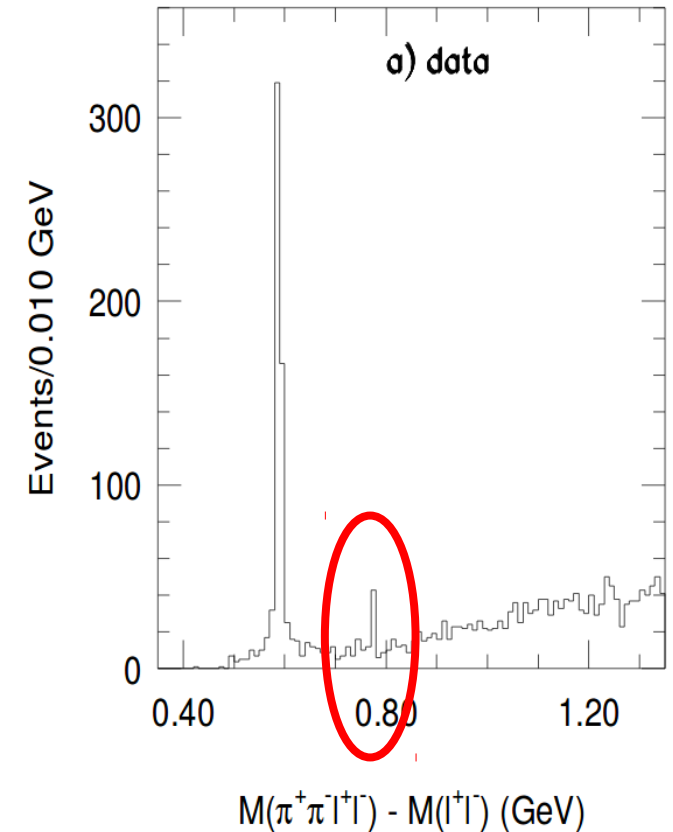


Why is this relevant now?

- Searches for exotic hadrons have been ongoing for ~50 years *with light quarks*
 - some claimed signals for pentaquarks which led to nothing ...
 - too many scalar states
 - with an unexpected pattern of masses ($K\bar{K}$ threshold effect?)
 - $\pi_1(1400)$, $\pi_1(1600)$ states with $J^{PC} = 1^{-+}$
 - i.e. manifestly exotic quantum numbers
 - difficult to make definitive claims in light hadron sector
 - states broad and overlapping
- New possibilities in latest generations of heavy flavour experiments, especially for $c\bar{c}$ (and related) states

X(3872)

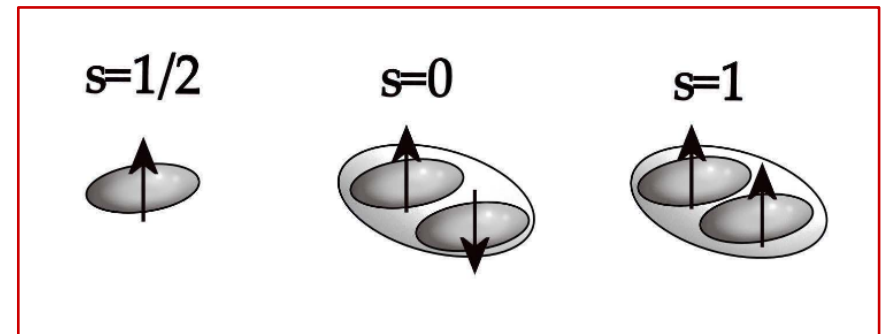
- Unexpected discovery by the Belle collaboration in 2003
 - $B^+ \rightarrow X(3872)K^+$, $X(3872) \rightarrow J/\psi\pi^+\pi^-$
 - Rapidly confirmed by
 - BaBar, CDF, D0
 - (later LHCb, CMS, ATLAS)
 - Produced in
 - B decay, pp & $p\bar{p}$ collisions
 - Decays to
 - $J/\psi\rho$, $J/\psi\omega$, $J/\psi\gamma$, $D\bar{D}^*$
- Does not fit conventional $c\bar{c}$ spectrum



Phys.Rev.Lett. 91 (2003) 262001

Conventional $q\bar{q}$ spectroscopy

- Define, as usual, intrinsic spin S , orbital angular momentum L , total angular momentum (“spin”) $J = L \oplus S$
- q & \bar{q} have opposite parity: $P = -1^{L+1}$
- charge conjugation: $C = (-1^S)(-1^L)$
- For $L=0$, have $J^{PC} = 0^{-+}$ (η_c), 1^{-} (J/ψ)



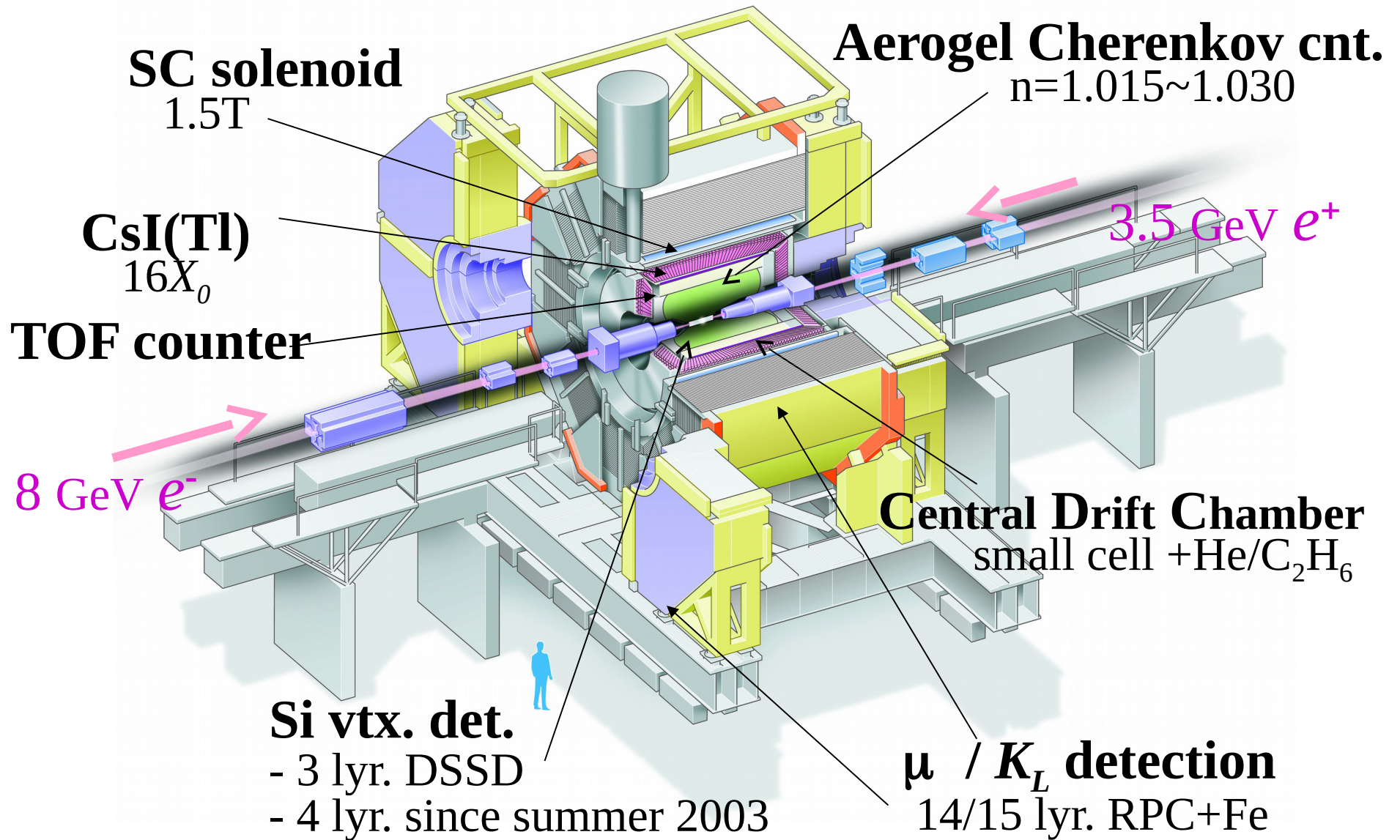
- For $L=1$, have $J^{PC} = 0^{++}$ (χ_{c0}), 1^{+-} (h_c), 1^{++} (χ_{c1}), 2^{++} (χ_{c2})
 - cannot get manifestly exotic quantum numbers (e.g. $J^{PC} = 0^{-}, 0^{+-}, 1^{-+}$) from $q\bar{q}$
- Other notations also used: $n^{2S+1}L_J$, $\psi(2S)$, $X(3872)$, ...
 - as usual in spectroscopy, $L = 0,1,2,3 \dots$ denoted S,P,D,F ...
- **Simple prediction for pattern of masses and quantum numbers**
 - need to measure both, as well as total widths, branching fractions, ...

Measuring quantum numbers

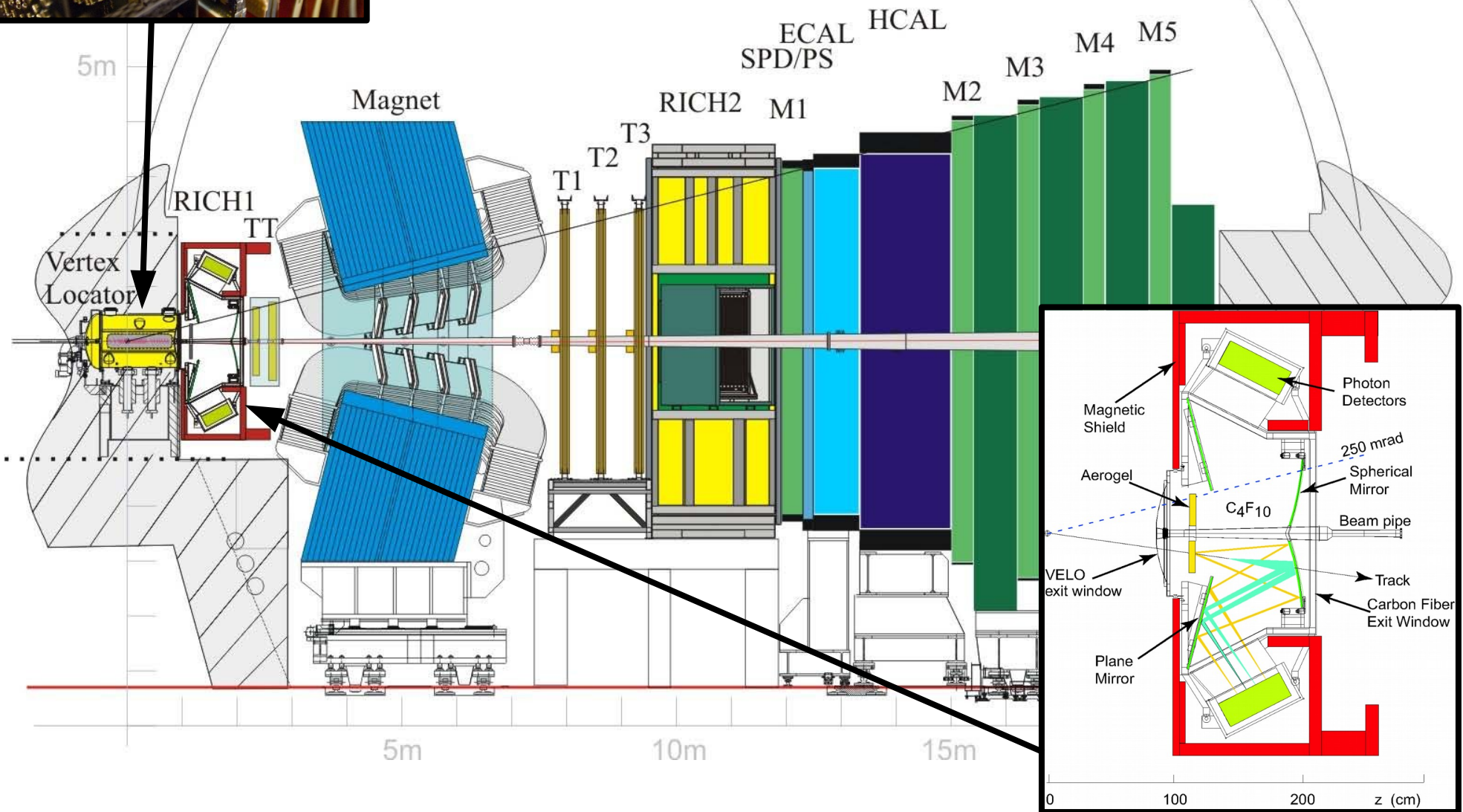
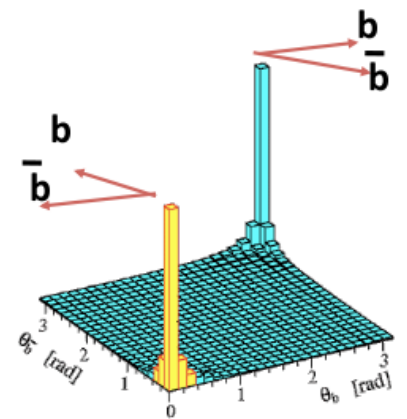
- Can be inferred from production or decay processes
 - both P and C conserved, since strong or electromagnetic processes
- Production
 - in e^+e^- collisions then $J^{PC} = 1^-$
 - in hadron collisions \rightarrow usually no information (unknown additional particles)
 - in B decay \rightarrow initial state constrained
- Decay
 - need to measure angular momentum between final state particles
 - require constrained initial and final states – B decay chain ideal
 - (some exceptions, e.g. $X(3872) \rightarrow J/\psi\gamma$ fixes $C=+1$)

Large, clean samples of B decays at B factories and LHCb

Belle Detector



LHCb detector

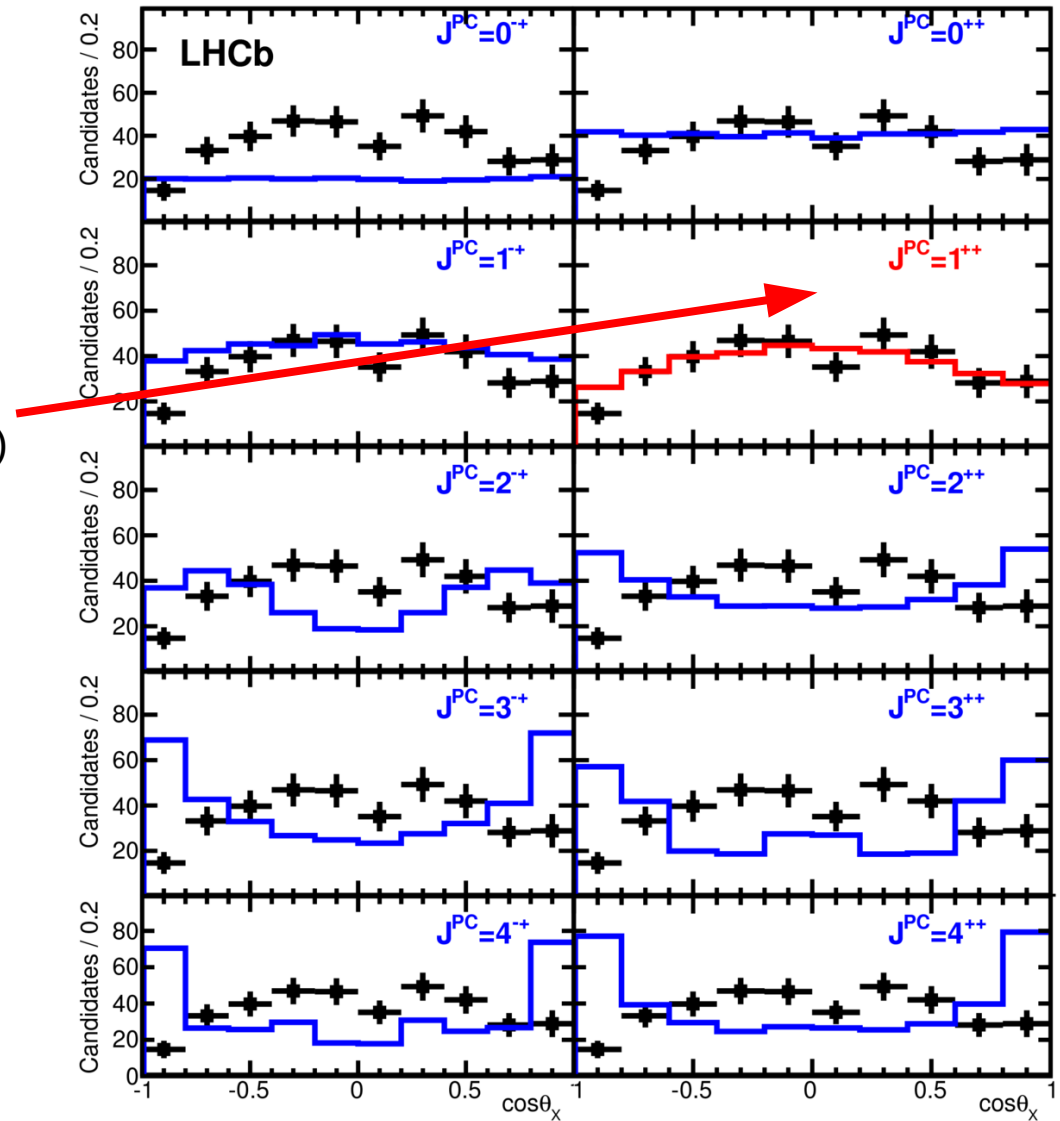
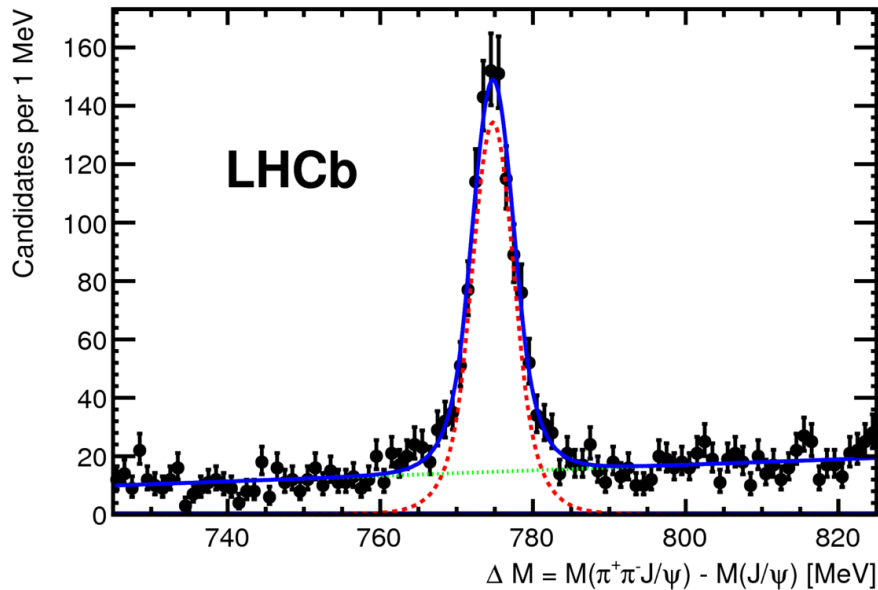


Measuring X(3872) quantum numbers

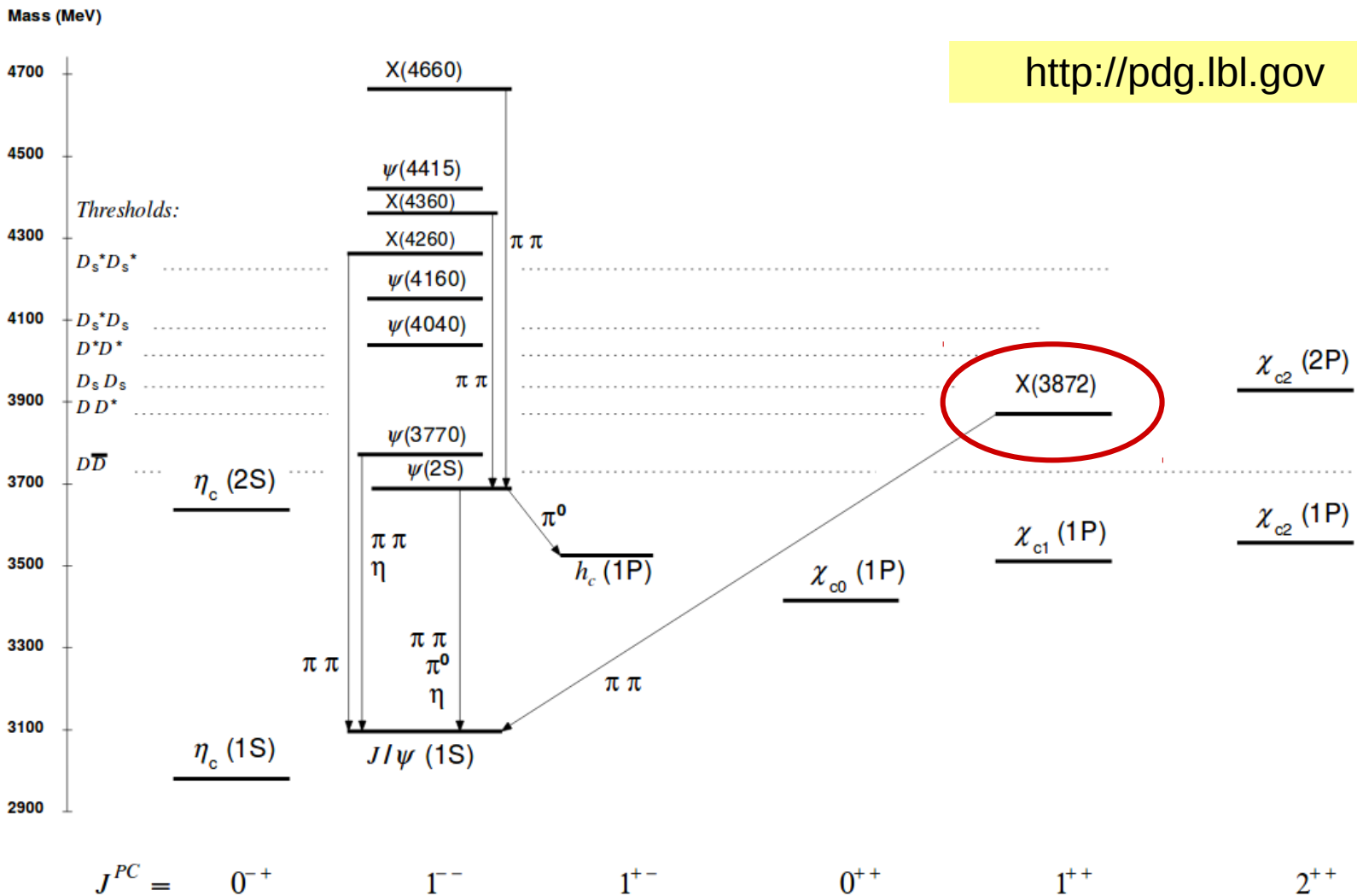
Phys. Rev. D92 (2015) 011102

Example: angular distributions in $B^+ \rightarrow X(3872)K^+$, $X(3872) \rightarrow J/\psi\pi^+\pi^-$

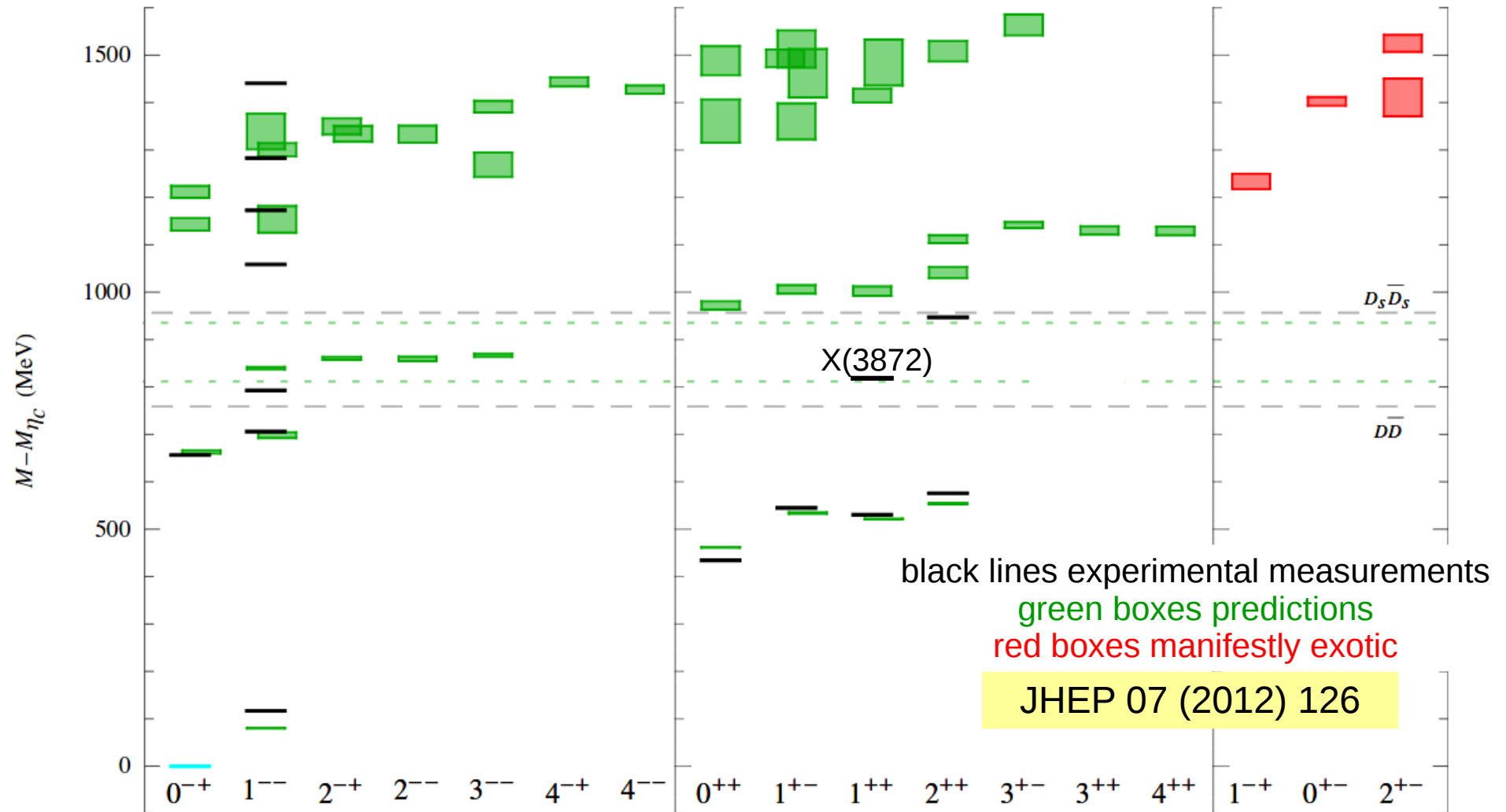
Unambiguously determines $J^{PC} = 1^{++}$
(projections in plots do not carry all information)



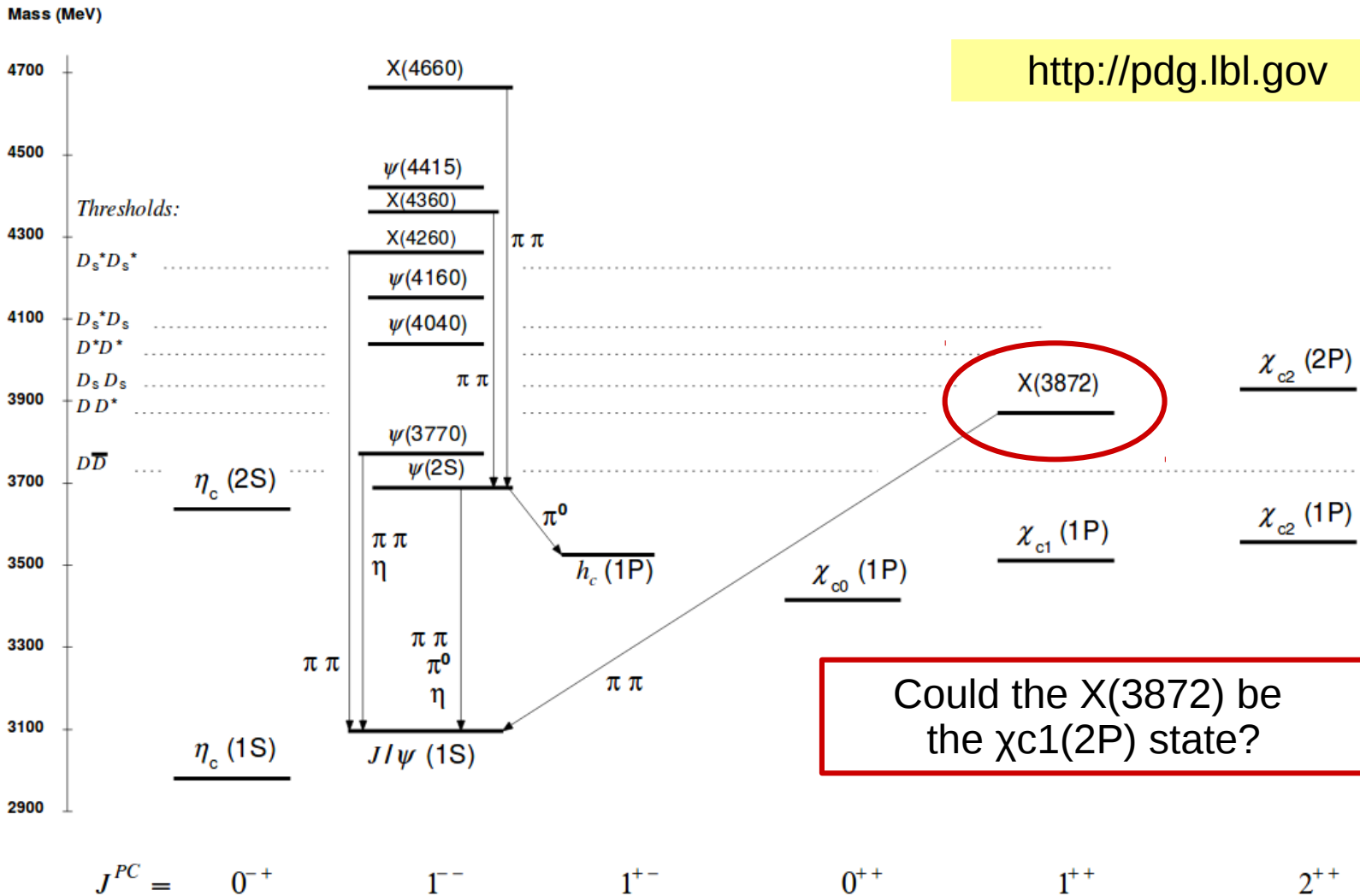
The $c\bar{c}$ spectrum



The $c\bar{c}$ spectrum from lattice QCD



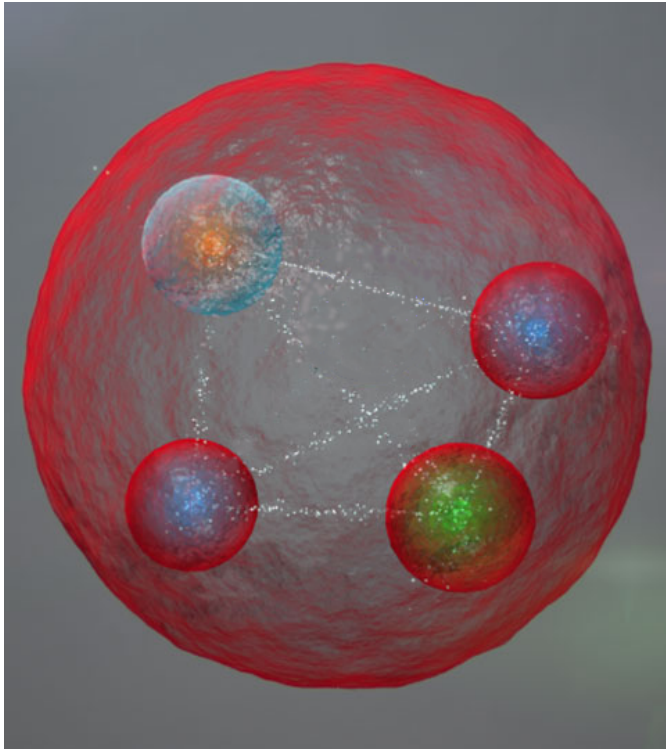
The $c\bar{c}$ spectrum



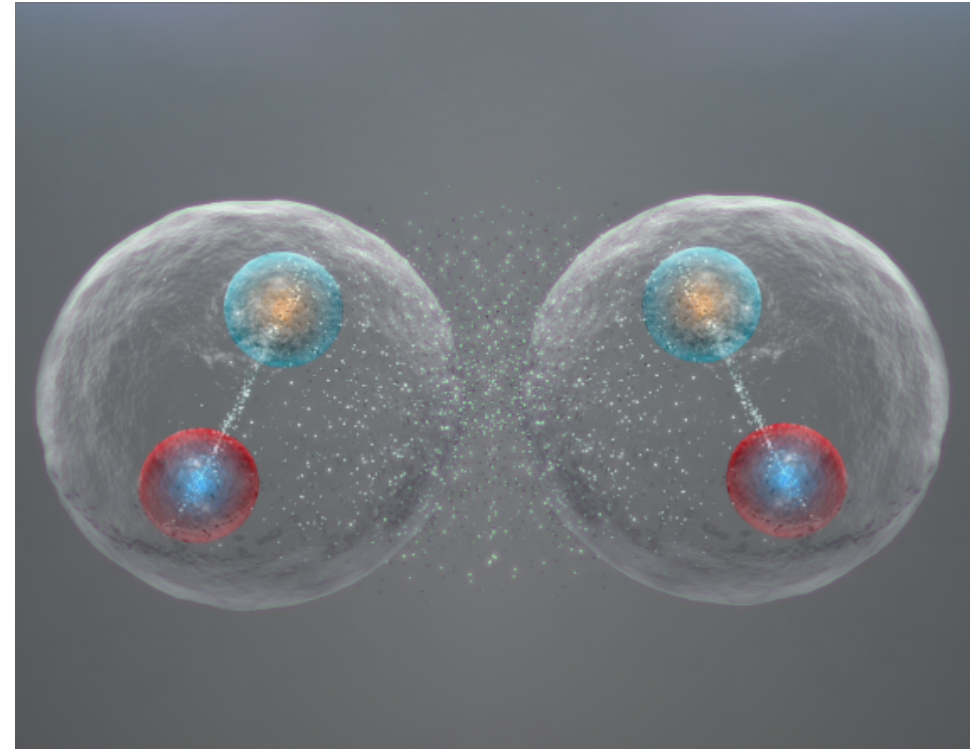
Could the X(3872) be the $\chi_{c1}(2P)$ state?

- Several strong arguments against:
 - isospin violation (decay to $J/\psi\rho$) not expected
 - near equality of branching fractions to $J/\psi\rho$ & $J/\psi\omega$
 - (isospin partners however not observed)
 - above threshold for decay to open charm but not significantly wider than $\chi_{c1}(1P)$
 - only upper limit on X(3872) width measured so far
 - mass splitting relative to $\chi_{c2}(2P)$ state less than expected
 - mass suspiciously close to $D\bar{D}^*$ threshold
- If not, what is it?

Tightly bound tetraquark
(all quarks bound by gluons)



Meson-meson molecule
(bound by pion exchange)



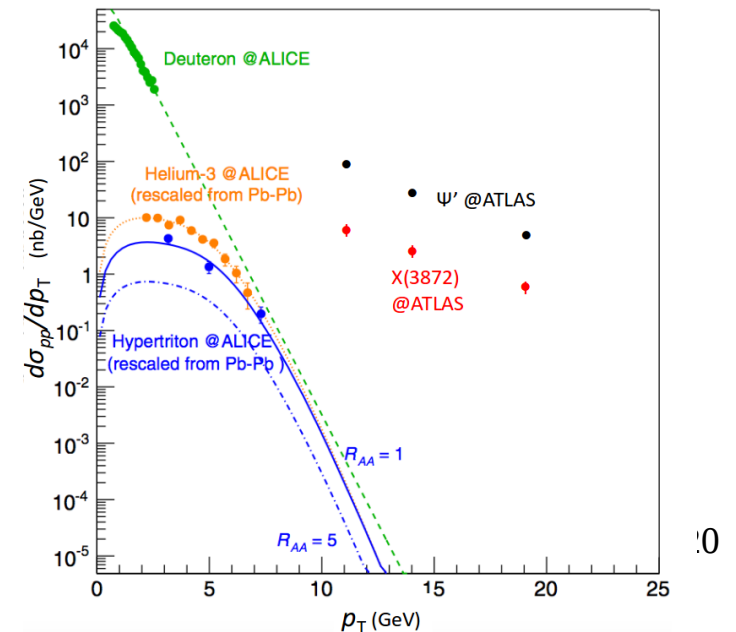
or

or some mixture with $c\bar{c}$,
or something else?

Simplified picture above:
most tightly bound models
involve diquarks

Molecular or tightly-bound?

- Molecular model ($D^0\bar{D}^{*0}$)
 - natural explanation for mass being near threshold
 - natural explanation for isospin violation
 - amplification of $D^{(*)+}-D^{(*)0}$ mass difference
 - production in pp ($p\bar{p}$) not as expected
 - could be explained by admixture with $\chi_{c1}(2P)$
 - lattice QCD calculations support this view (arXiv:1503.03257)



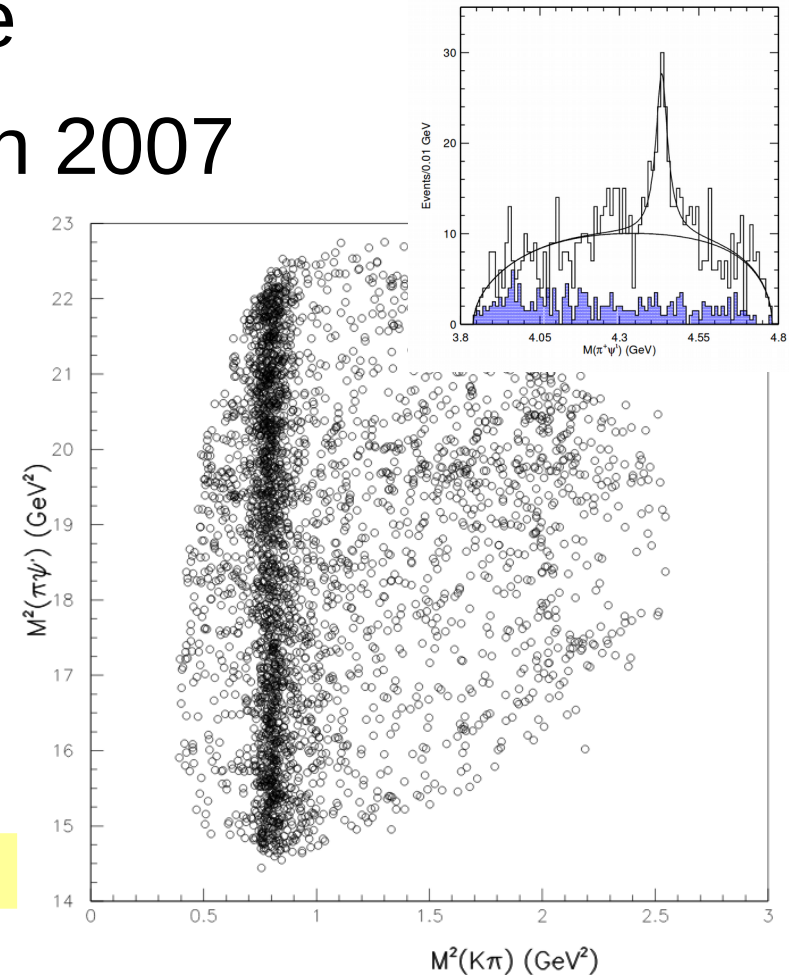
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 - could be explained by admixture with $\chi_{c1}(2P)$
 - lattice QCD calculations support this view (arXiv:1503.03257)
- Tightly bound diquarks ($[cu][\bar{c}\bar{u}]$)
 - can explain isospin violation
 - predicts existence of isospin partners (not seen)

A smoking gun

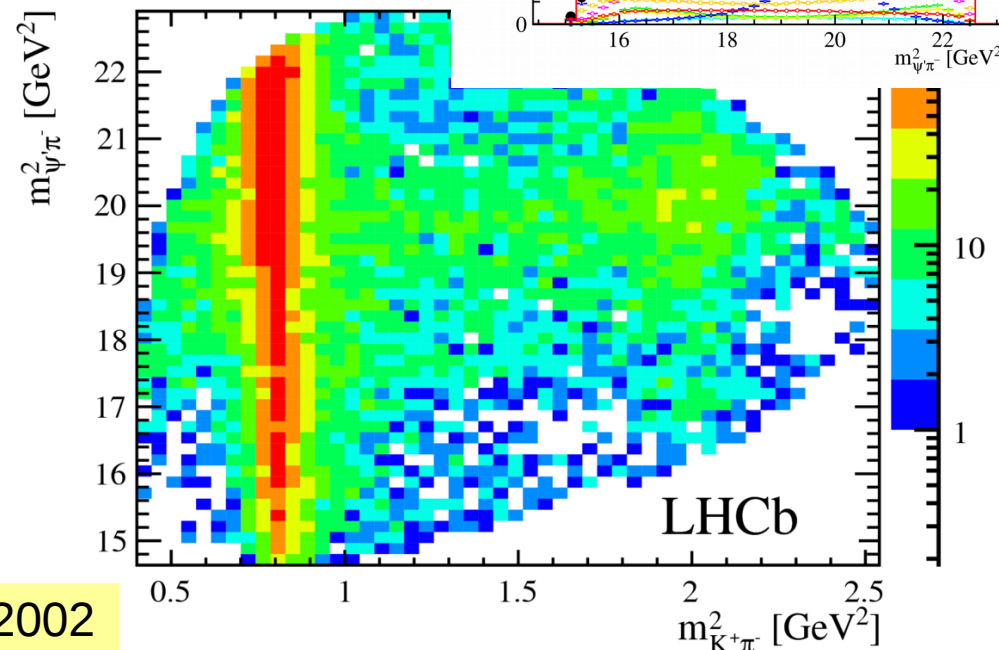
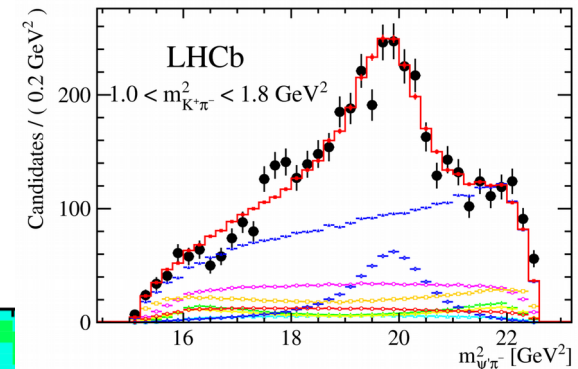
- An unambiguous signal for exotic hadrons is a charged charmonium-like state
- Belle discovered a candidate in 2007
 - $B^0 \rightarrow Z(4430)^- K^+$,
 - $Z(4430)^- \rightarrow \psi(2S) \pi^-$
- Not confirmed by BaBar
 - analysis method too simplistic?

Phys.Rev.Lett. 100 (2008) 142001



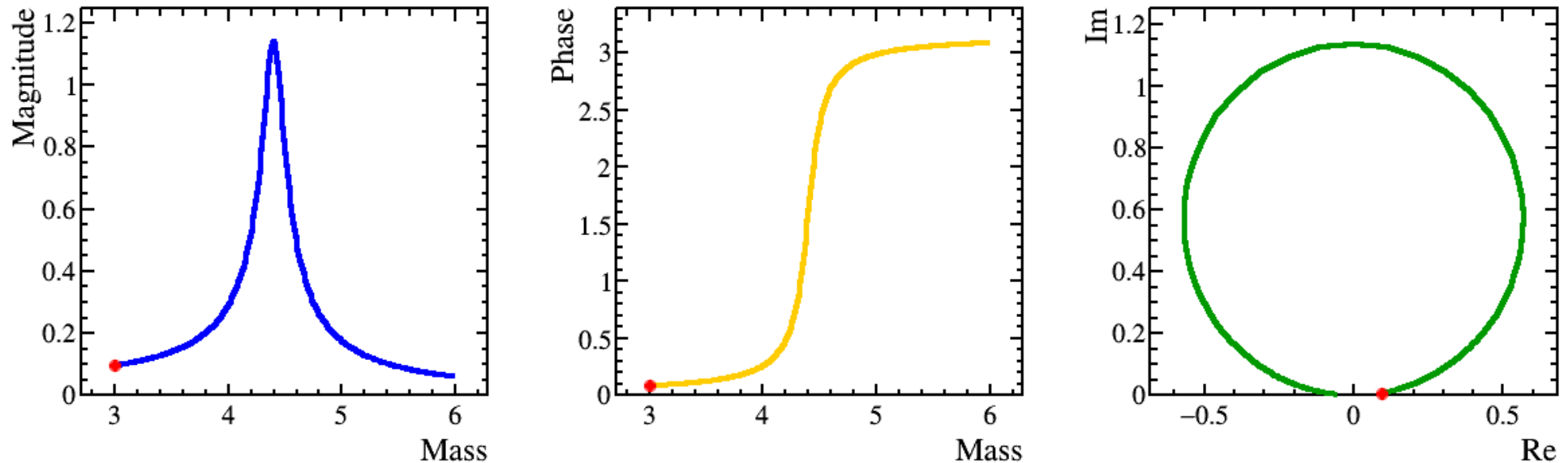
Z(4430) confirmation by LHCb

- An unambiguous signal for exotic hadrons is a charged charmonium-like state
- Belle discovered a candidate in 2007
 - $B^0 \rightarrow Z(4430)^- K^+$,
 - $Z(4430)^- \rightarrow \psi(2S) \pi^-$
- Confirmed by LHCb
 - Full 4D amplitude analysis
 - (necessary to determine parameters correctly)
 - Quantum numbers $J^P = 1^+$



Phys. Rev. Lett. 112 (2014) 222002

Resonant character of the Z(4430)



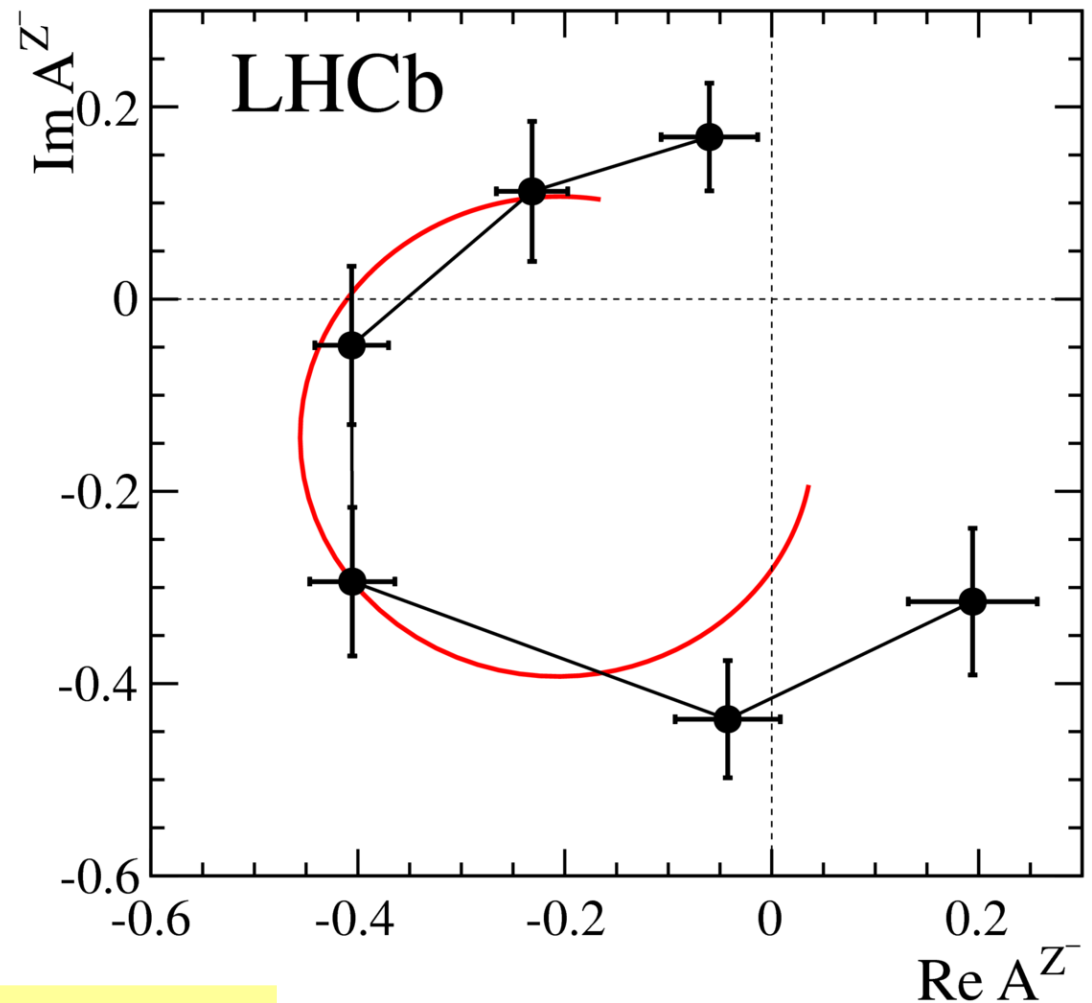
- A Breit-Wigner function has a characteristic rapid change of phase near the resonance peak

$$A(s) \propto \frac{1}{m^2 - s^2 + im\Gamma(s)}$$

- Plotting the amplitude in the Argand plane, the lineshape maps out a circle (anticlockwise, as mass increases)
- **Can be measured in an amplitude analysis**

Resonant character of the Z(4430)

- Complex amplitude measured in 6 bins of $m(\psi(2S)\pi^-)$
- Found to follow expected anticlockwise trajectory in Argand plan
- Rules out models where Z(4430) arises due to kinematic effects

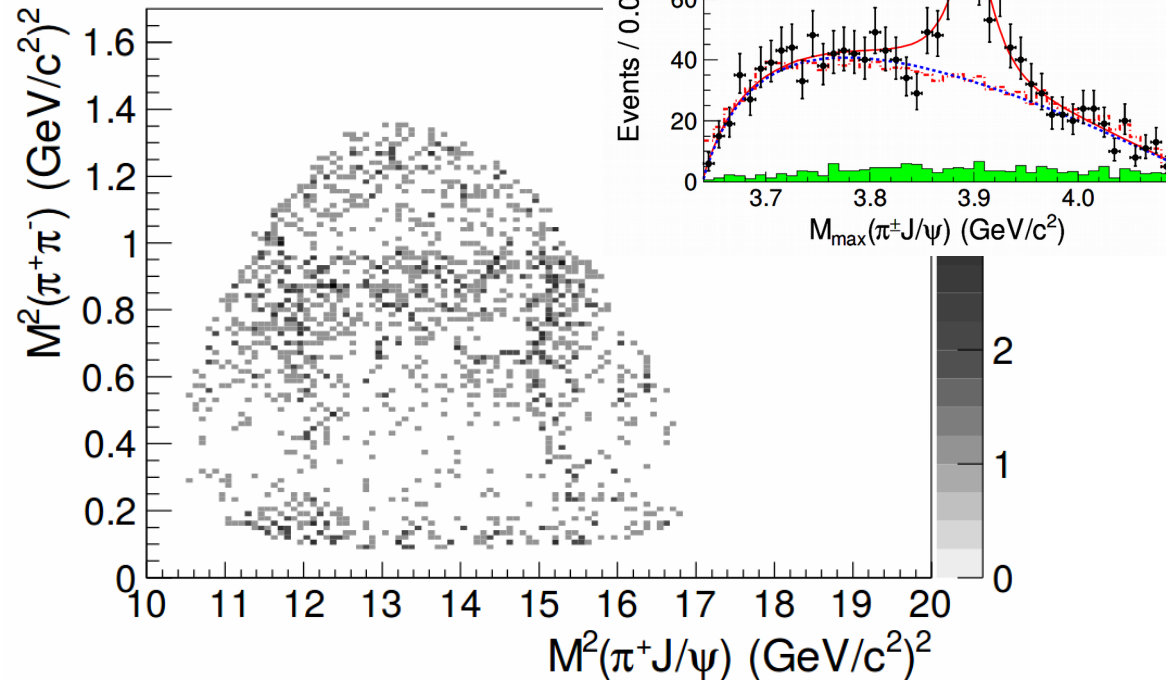
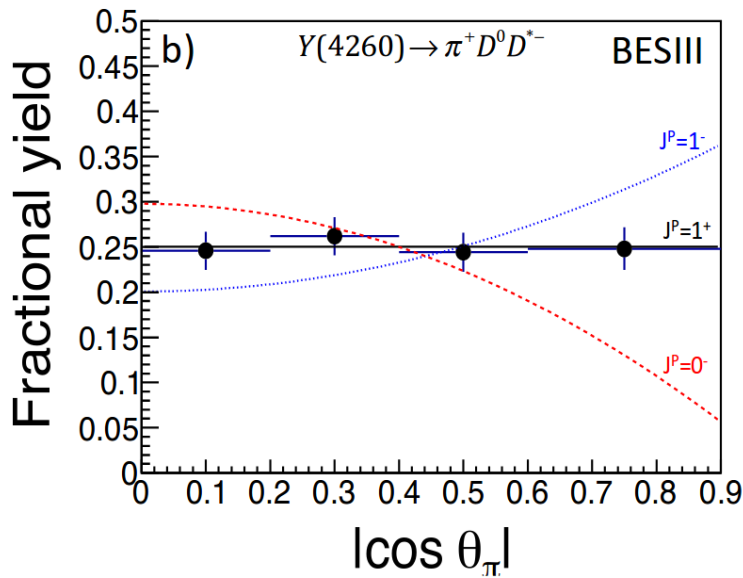


Phys. Rev. Lett. 112 (2014) 222002

More smoking guns

- BESIII and Belle both reported $Y(4260) \rightarrow Z(3900)\pi$, $Z(3900) \rightarrow J/\psi\pi$
- Later seen in DD^* decay mode
- Isospin (neutral) partner observed
 - both $J/\psi\pi$ and DD^* modes
- Quantum numbers $J^P = 1^+$

Phys. Rev. Lett. 110 (2013) 252001
 Phys. Rev. Lett. 110 (2013) 252002

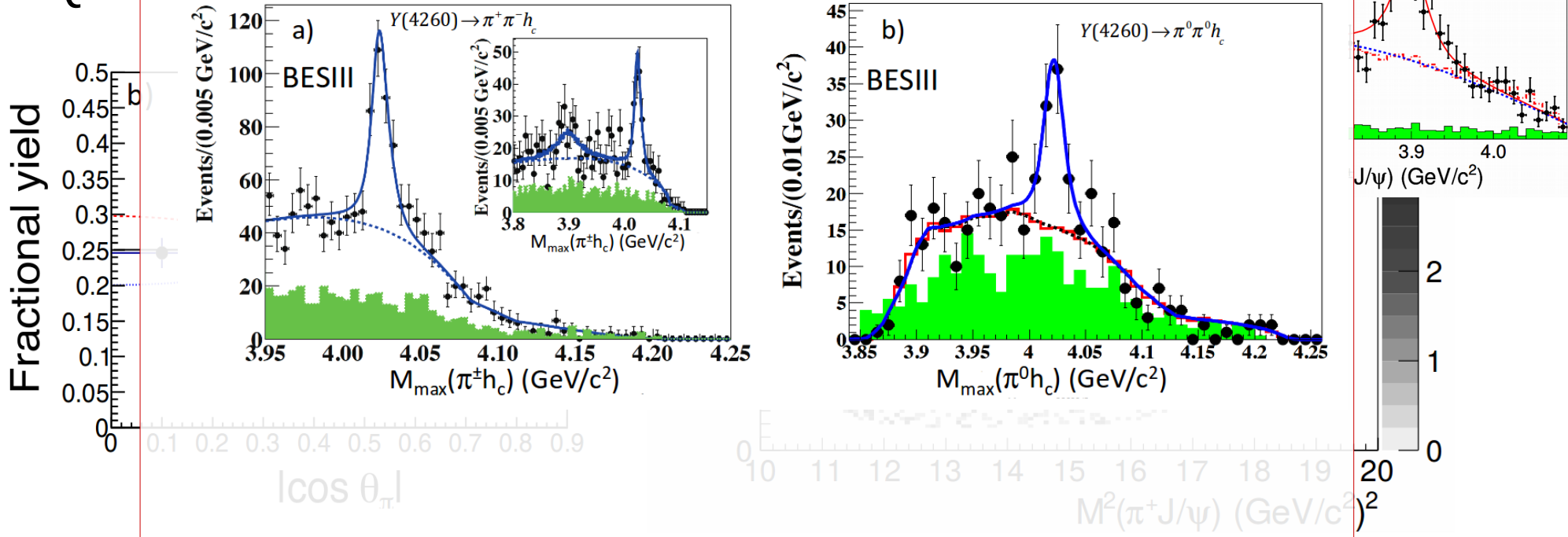


More smoking guns

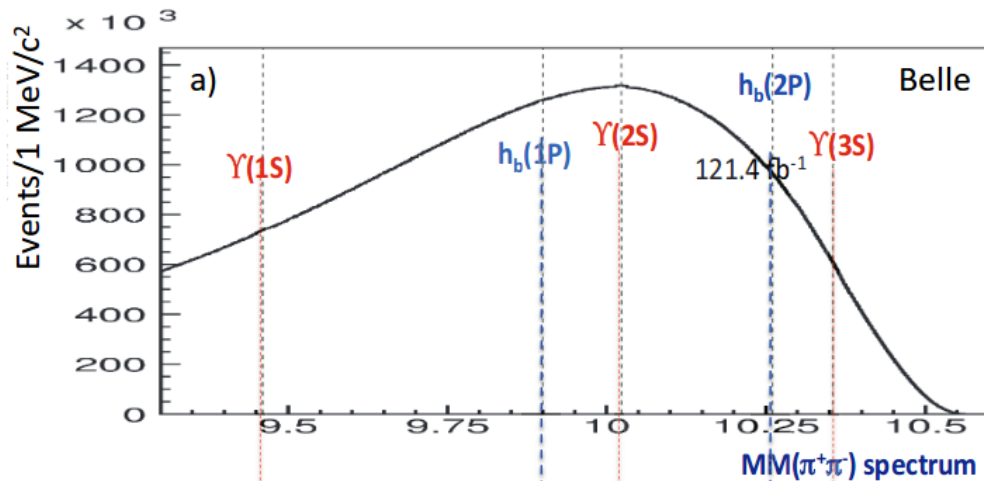
- BESIII and Belle both reported $Y(4260) \rightarrow Z(3900)\pi, Z(3900) \rightarrow J/\psi\pi$
- Later seen in DD^* decay mode
- Isospin (neutral) partner observed
- both $J/\psi\pi$ and DD^* seen decaying to $h_c\pi$ and $D^*\bar{D}^*$
- Quantum numbers $1P - 1+$

Similar isospin triplet $Z(4020)$ seen decaying to $h_c\pi$ and $D^*\bar{D}^*$

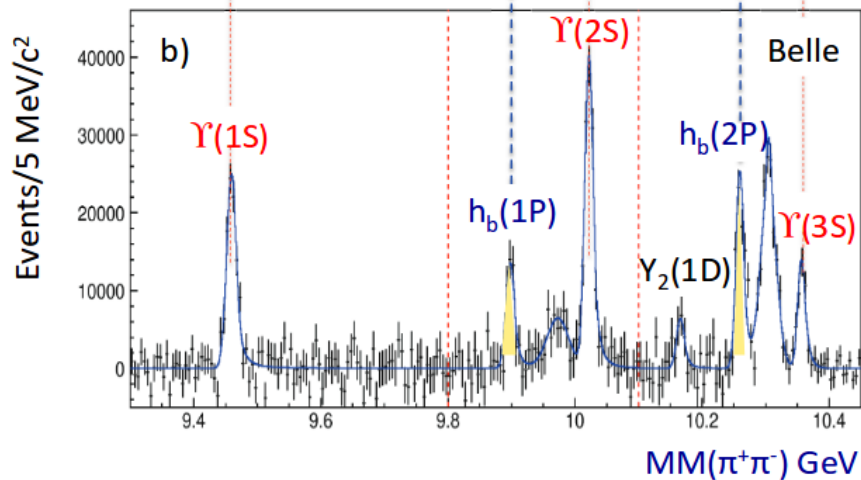
Phys. Rev. Lett. 110 (2013) 252001
 Phys. Rev. Lett. 110 (2013) 252002



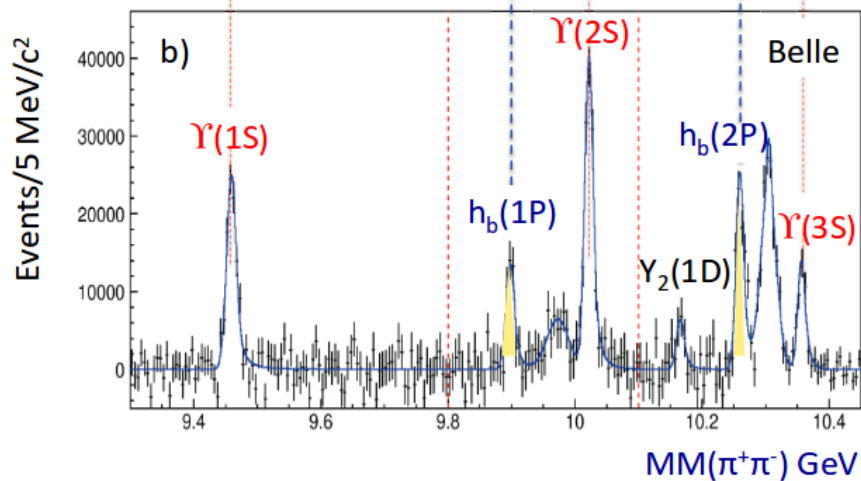
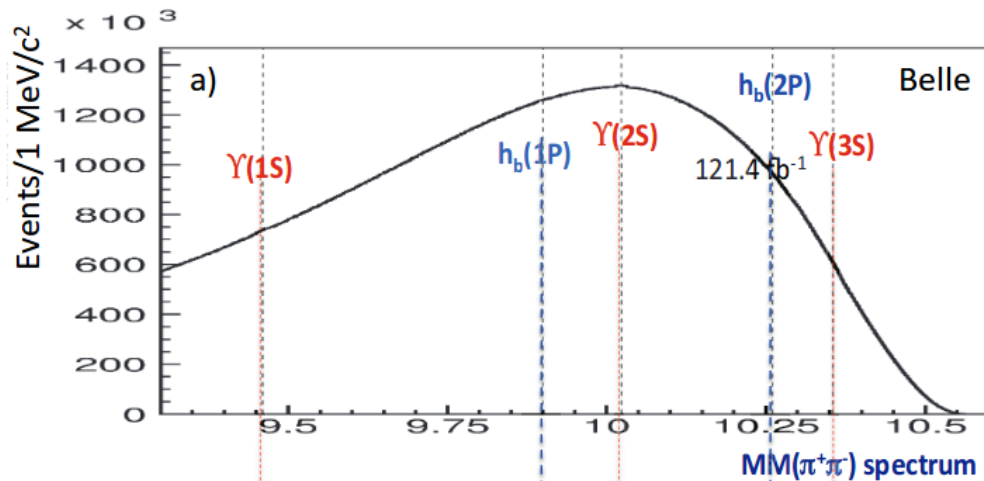
Smoking guns in the $b\bar{b}$ system



- Belle observed anomalously high rate of $e^+e^- \rightarrow \Upsilon(10860) \rightarrow \Upsilon(nS)\pi^+\pi^-$
- Investigation of recoil mass revealed surprising presence of $h_b(1P)$ and $h_b(2P)$ states – first observations!



Smoking guns in the $b\bar{b}$ system

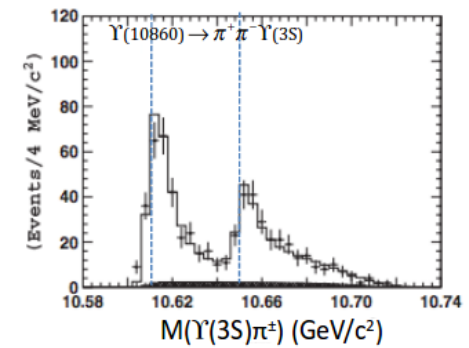
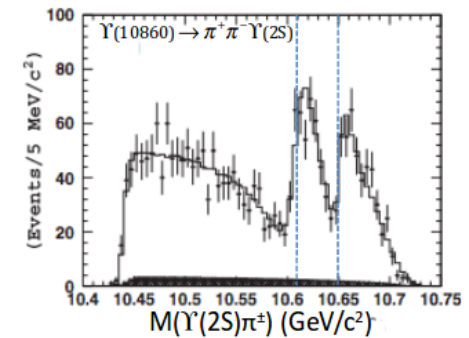
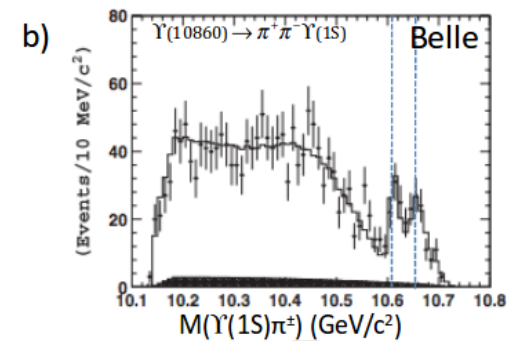
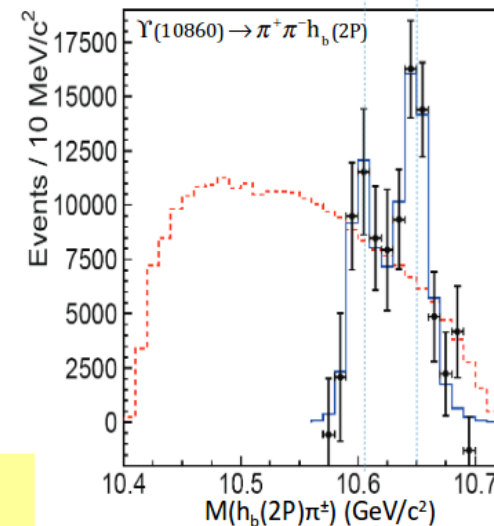
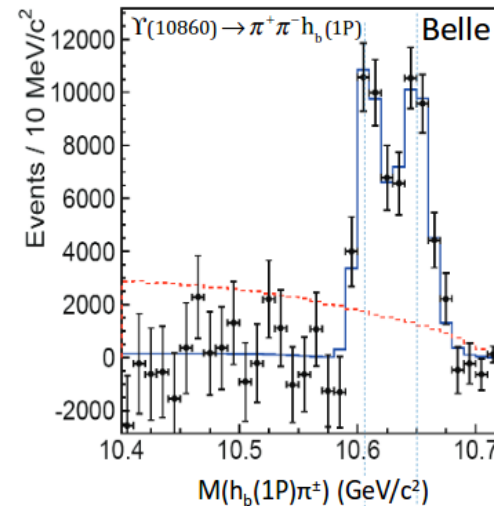


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- Investigation of recoil mass revealed surprising presence of $h_b(1P)$ and $h_b(2P)$ states – first observations!
- Allows study of the $Y(nS)\pi$ and $h_b(nP)\pi$ mass distributions

Phys. Rev. Lett. 100 (2008) 112001
 Phys. Rev. Lett. 108 (2012) 032001

Smoking guns in the $b\bar{b}$ system

- Two peaks, $Z_b(10610)$ and $Z_b(10650)$ seen with consistent properties in five different decay modes!
- Quantum numbers $J^P = 1^+$
- Masses near to $B\bar{B}^*$ and B^*B^* thresholds
 - decays to $B\bar{B}^*$ and B^*B^* also seen
- Isospin partners observed

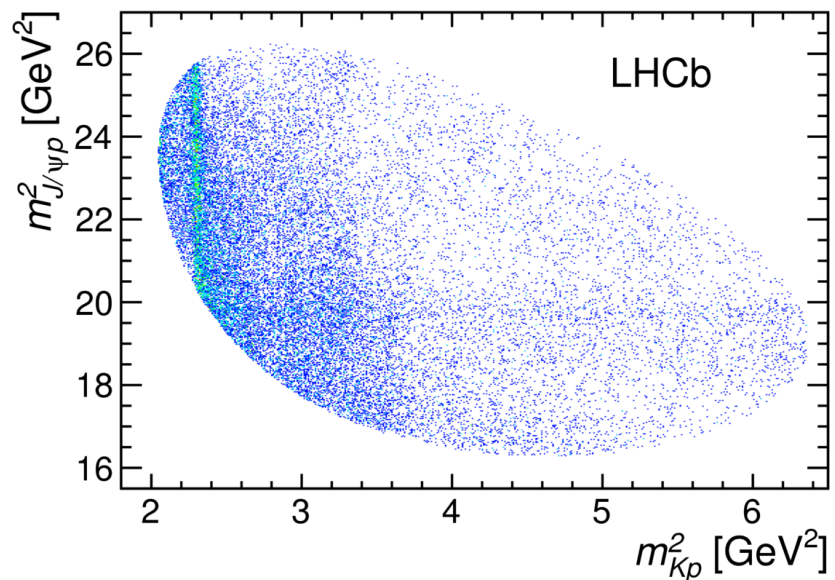
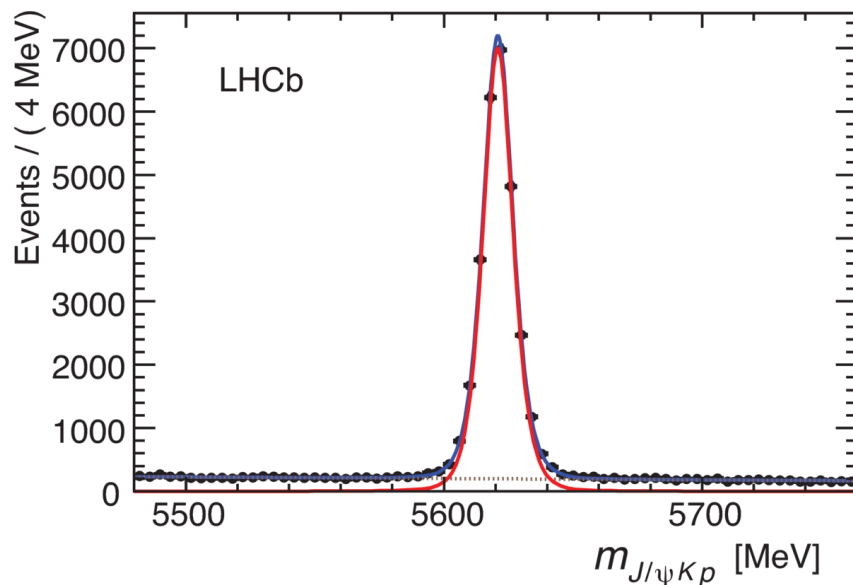


Phys.Rev.Lett. 108 (2012) 122001

Pentaquarks

- Large samples of b baryons produced at LHC
- Ideal to search for pentaquarks containing $c\bar{c}$
 - Particle identification important to reject B meson decay backgrounds
 - Strong advantage of LHCb (but hope ATLAS+CMS can contribute)
- Study of $\Lambda_b \rightarrow J/\psi p K^-$

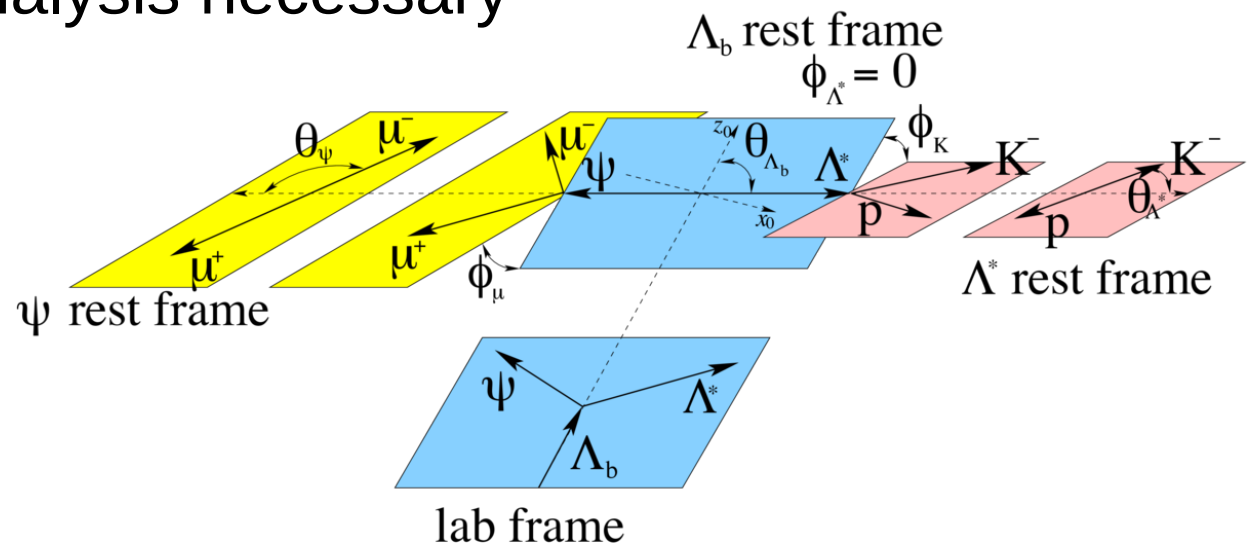
Phys. Rev. Lett. 115 (2015) 072001



Amplitude analysis of baryon decay

Phys. Rev. Lett. 115 (2015) 072001

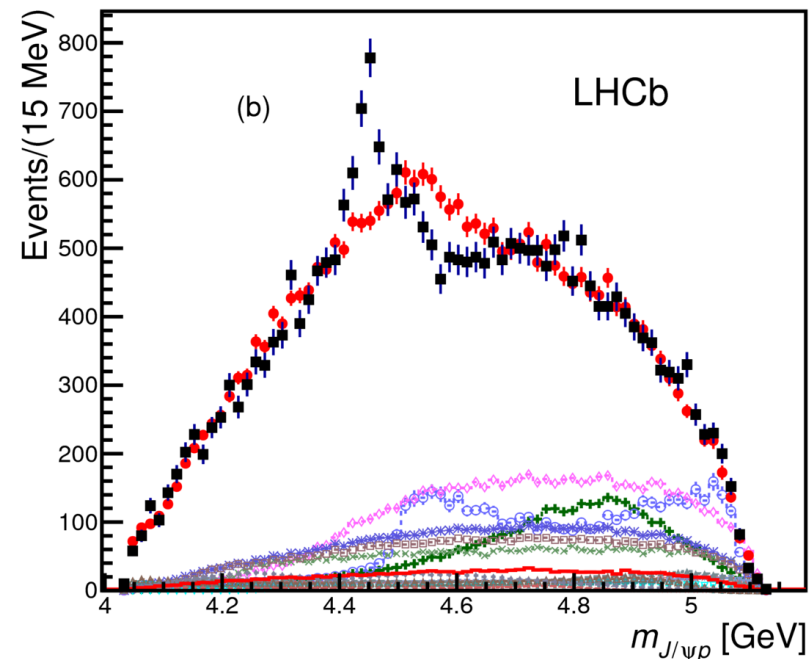
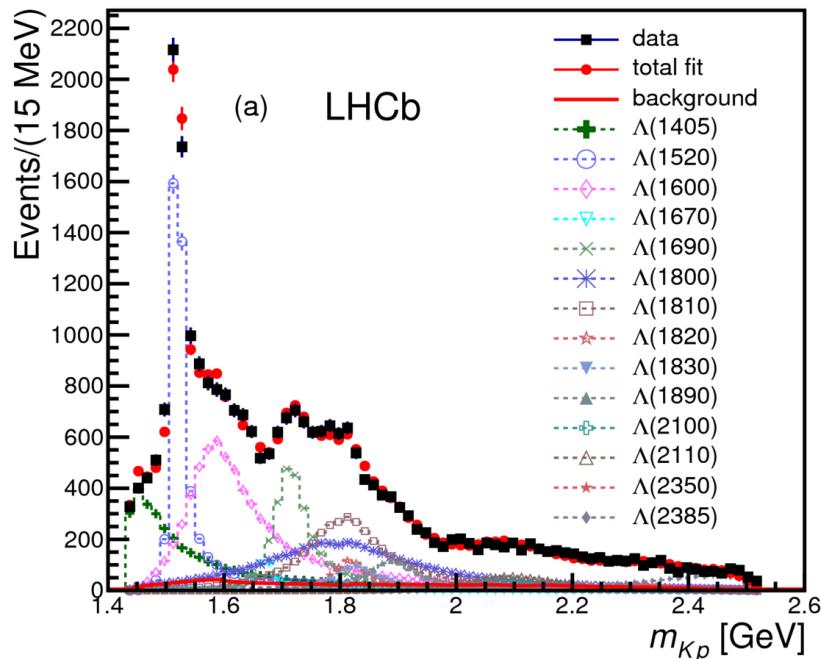
- Lesson from Z(4430)
 - full amplitude analysis is mandatory!
- Additional degrees of freedom for baryons
 - non-zero spin of initial and final state particles
 - 6D amplitude analysis necessary



Amplitude analysis of baryon decay

Phys. Rev. Lett. 115 (2015) 072001

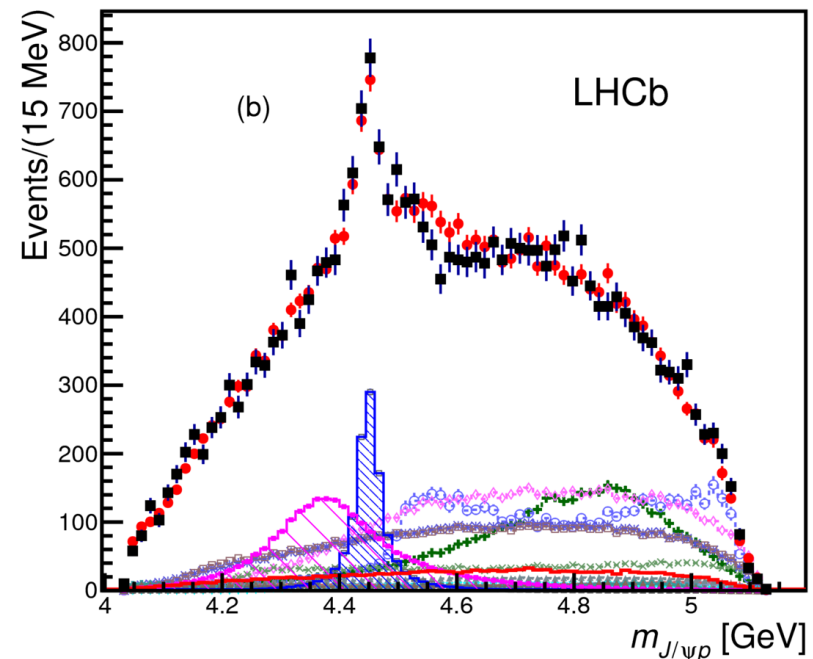
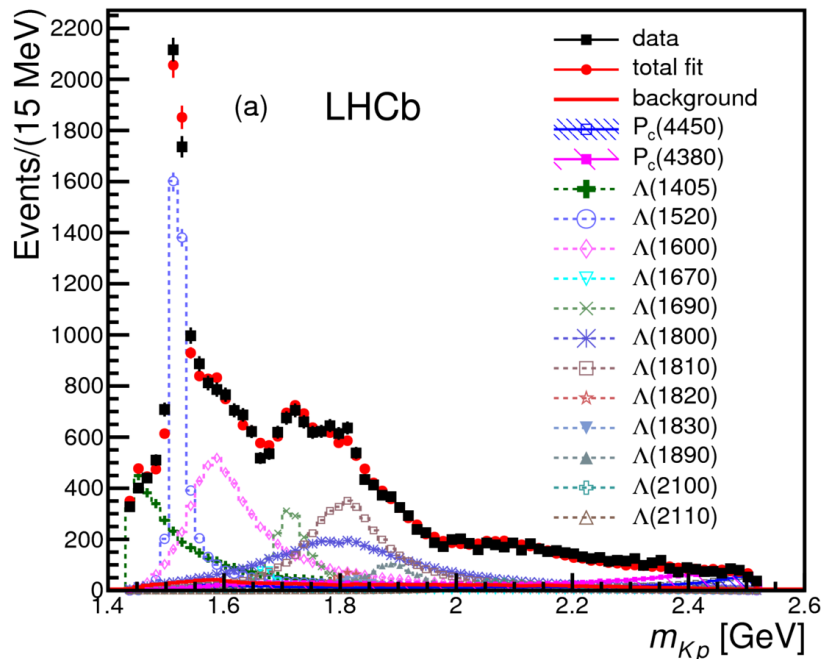
- Not possible to get good description of data including only $\Lambda^* \rightarrow pK$ resonances



Amplitude analysis of baryon decay

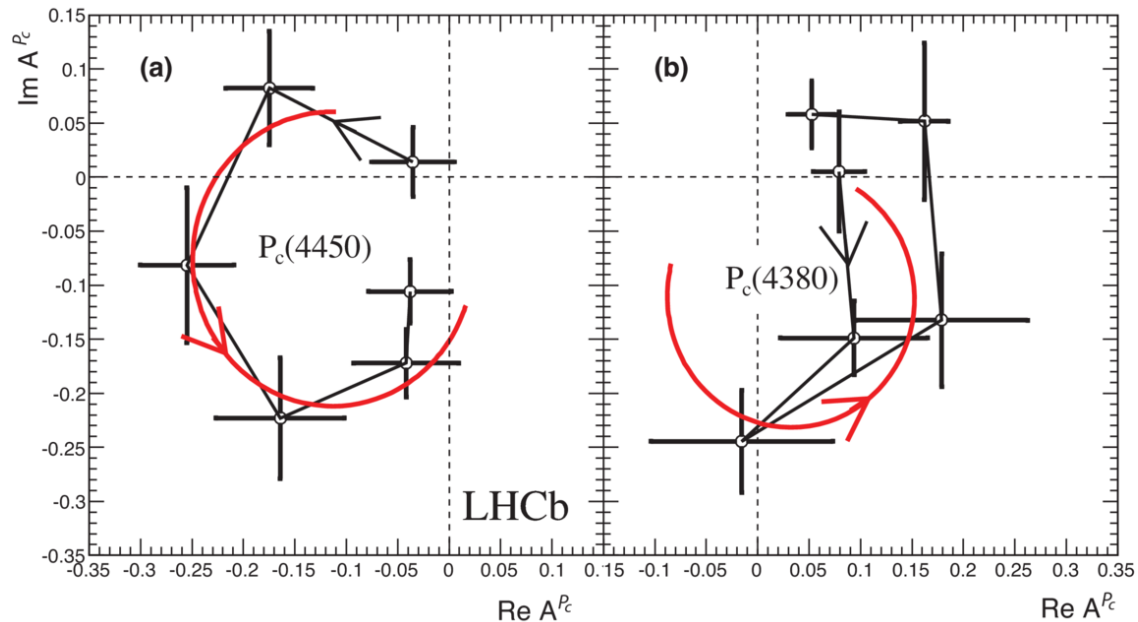
Phys. Rev. Lett. 115 (2015) 072001

- Not possible to get good description of data including only $\Lambda^* \rightarrow pK$ resonances
- Acceptable fit including two $P_c \rightarrow J\psi/p$ states



Resonant nature of the P_c states

Phys. Rev. Lett. 115 (2015) 072001



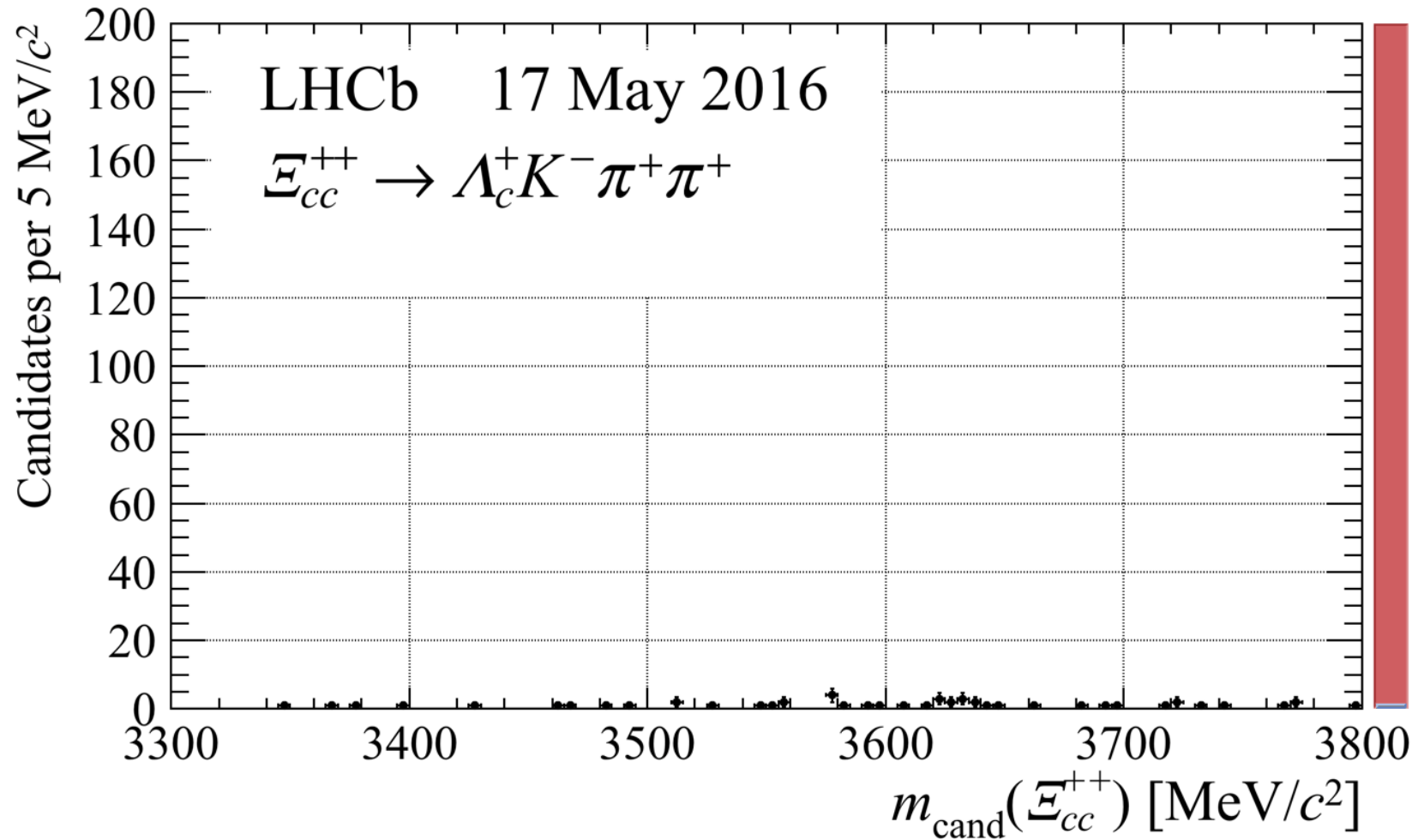
- Phase rotation as expected for $P_c(4450)$
- Situation less clear for $P_c(4380)$ – update with more data needed
- Not possible to unambiguously assign quantum numbers
 - Four possibilities: $J^P (P_c(4450), P_c(4380)) = (3/2^\pm, 5/2^\mp), (5/2^\pm, 3/2^\mp)$

How to make sense of it all?

- We will need
 - better data
 - more measurements inspired by better predictions
 - **excellent prospects with LHCb, Belle II and LHCb upgrades**
 - better predictions
 - can be made by benefitting from better data
 - including results on conventional hadrons
- Excellent example: **doubly heavy baryons**
 - ideal testing ground for QCD potential in diquark models

Observation of the Ξ_{cc}^{++}

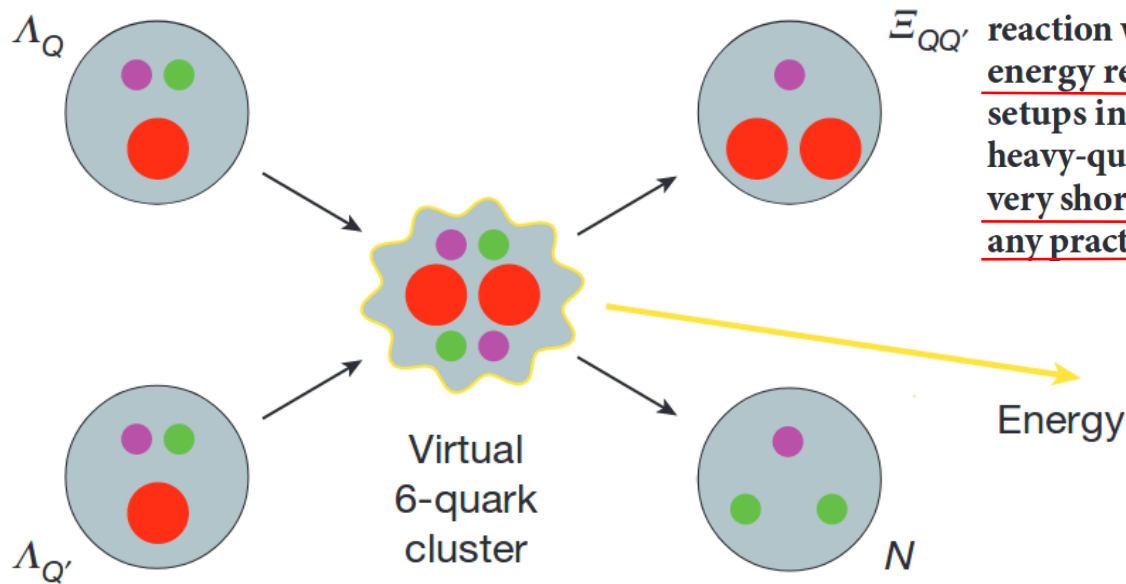
Phys. Rev. Lett. 119 (2017) 112001



Practical applications?

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nuclei. The recent discovery¹ of the first doubly charmed baryon Ξ_{cc}^{++} , which contains two charm quarks (c) and one up quark (u) and has a mass of about 3,621 mega-electronvolts (MeV) (the mass of the proton is 938 MeV) also revealed a large binding energy of about 130 MeV between the two charm quarks. Here we report that this strong binding enables a quark-rearrangement, exothermic reaction in which two heavy baryons (Λ_c) undergo fusion to produce the doubly charmed baryon Ξ_{cc}^{++} and a neutron n ($\Lambda_c \Lambda_c \rightarrow \Xi_{cc}^{++} n$), resulting in an energy release of 12 MeV. This reaction is a quark-level analogue of the deuterium-tritium nuclear fusion reaction ($DT \rightarrow {}^4\text{He } n$). The much larger binding energy (approximately 280 MeV) between two bottom quarks (b) causes the analogous reaction with bottom quarks ($\Lambda_b \Lambda_b \rightarrow \Xi_{bb}^0 n$) to have a much larger energy release of about 138 MeV. We suggest some experimental setups in which the highly exothermic nature of the fusion of two heavy-quark baryons might manifest itself. At present, however, the very short lifetimes of the heavy bottom and charm quarks preclude any practical applications of such reactions.



● Heavy quarks $Q, Q' = b, c$ ● ● Light quarks u and d quarks

Roadmap for double heavies

- The observation of the Ξ_{cc}^{++} (ccu) baryon is the start of a programme
- Crucial to measure properties of isospin partner Ξ_{cc}^+ (ccd) and of their excited states
 - (also lifetime, production rate and other decay modes)
- Studies of Ξ_{bc} states also essential
- Will allow precise predictions of $[bb][\overline{ud}]$, $[bc][\overline{ud}]$, and $[cc][\overline{ud}]$ tetraquarks

Summary

- No longer any doubt that exotic hadrons exist
 - question is now over their binding mechanism
- Situation currently rather cloudy
 - some models explain some of the data well
 - threshold effects, molecules, tightly bound tetraquarks, hadrocharmonium, ...
 - no model explains all of the data by itself
 - more than one effect contributing?
- Good reasons for optimism about progress in coming years
 - quite likely that major discoveries are waiting to be made

Bibliography

- Several excellent recent review articles
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