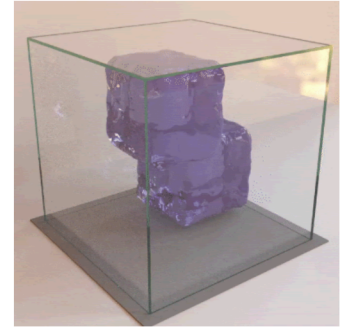
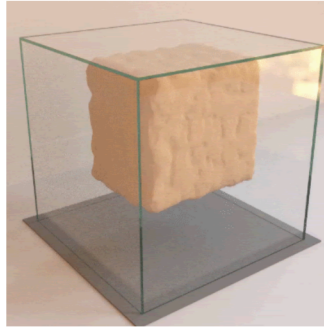
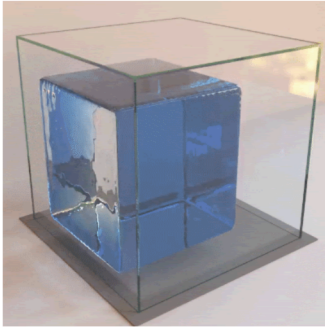


Learning Structured Models of Physics



Peter Battaglia

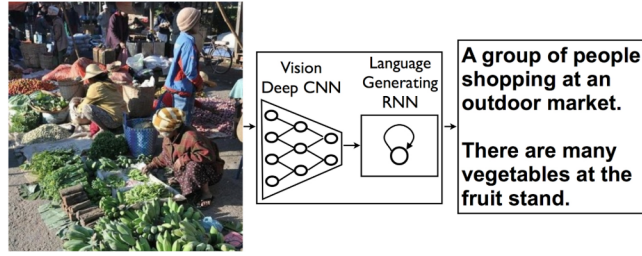


Seminar: Particle Physics Group
University of Birmingham (virtual) - May 6, 2020

What is deep learning good at?

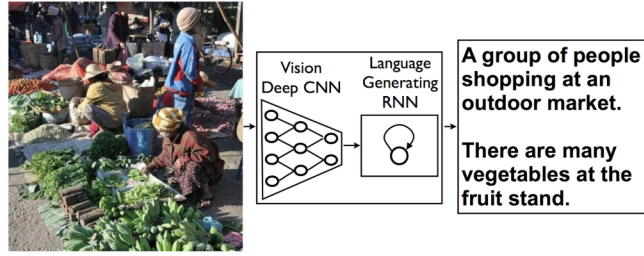
What is deep learning good at?

Image and language processing

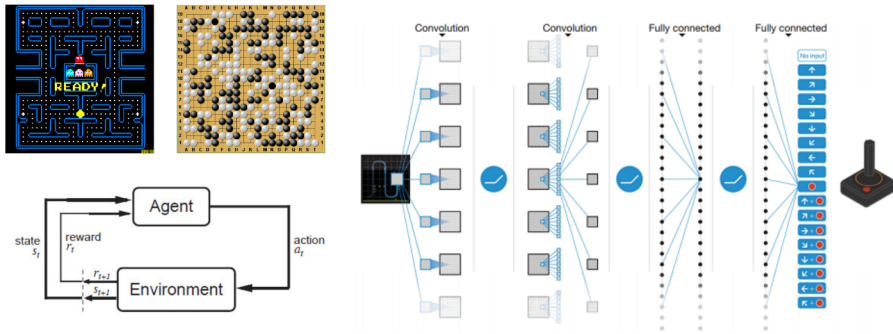


What is deep learning good at?

Image and language processing



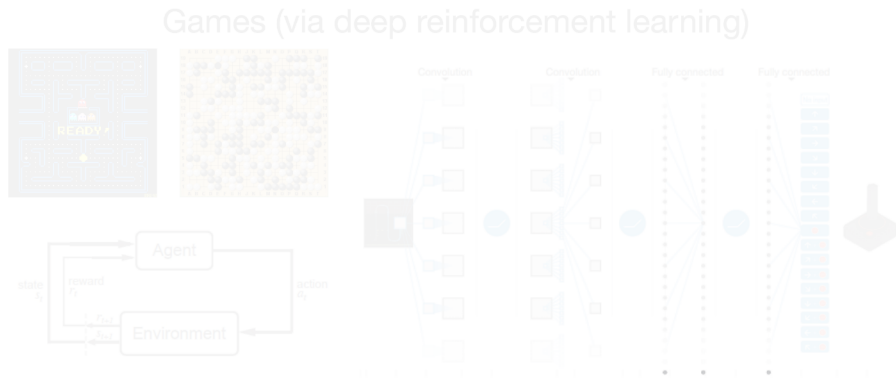
Games (via deep reinforcement learning)



What is deep learning good at?

Image and language processing

What do many of deep learning's successes have in common?



What is deep learning good at?

Image and language processing

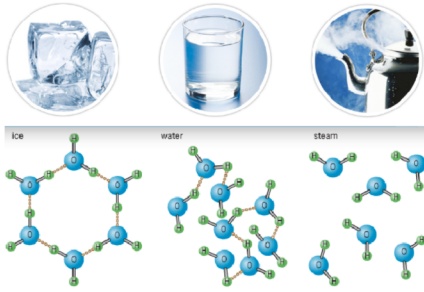
What do many of deep learning's successes have in common?

- * Vectors
- * Grids
- * Sequences

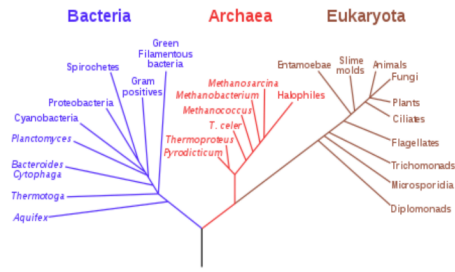


But many important domains are richly structured

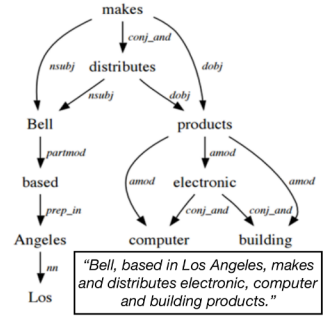
Molecules



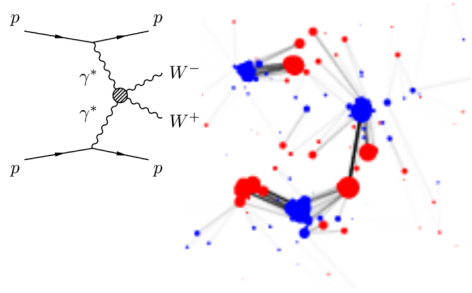
Biological species



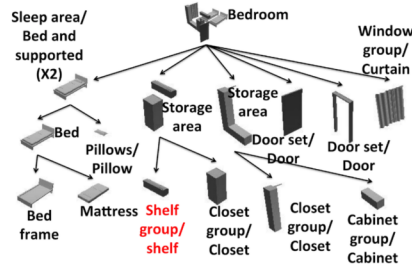
Natural language



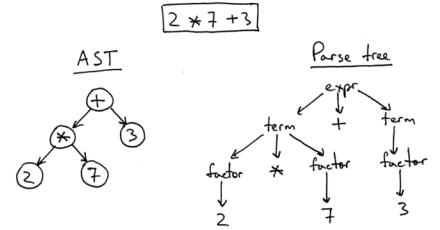
Sub-atomic particles



Everyday scenes



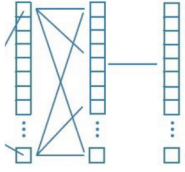
Code



The classic deep learning toolkit...

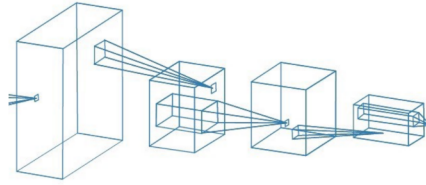
“My data is **vectors**”:

Multi-layer perceptron (MLP)



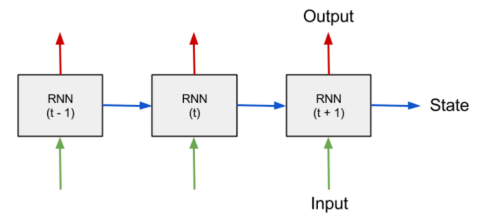
“My data is **grids**”:

Convolutional neural network (CNN)



“My data is **sequences**”:

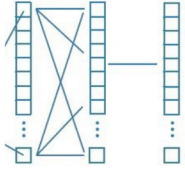
Recurrent neural network (RNN)



The classic deep learning toolkit...

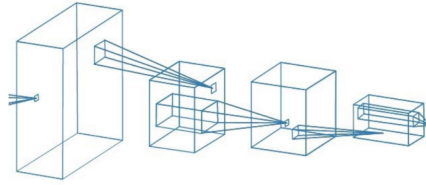
“My data is **vectors**”:

Multi-layer perceptron (MLP)



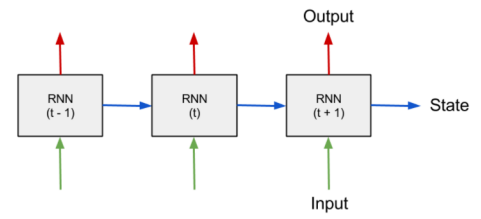
“My data is **grids**”:

Convolutional neural network (CNN)



“My data is **sequences**”:

Recurrent neural network (RNN)

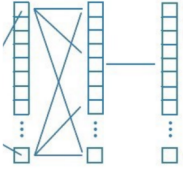


...is not well-suited to reasoning over structured representations.

The classic deep learning toolkit...

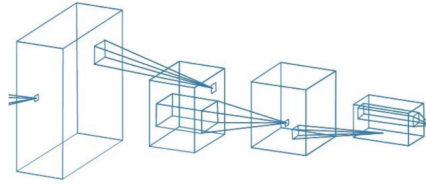
“My data is **vectors**”:

Multi-layer perceptron (MLP)



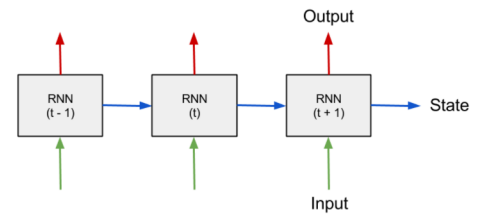
“My data is **grids**”:

Convolutional neural network (CNN)



“My data is **sequences**”:

Recurrent neural network (RNN)



...is not well-suited to reasoning over structured representations.

*But deep networks that operate on **graphs** are.*

Background: Graph Neural Networks

General idea

- Analogous to a convolutional network, but over arbitrary graphs (rather than just grids)
- Can learn to reason about entities and their relations

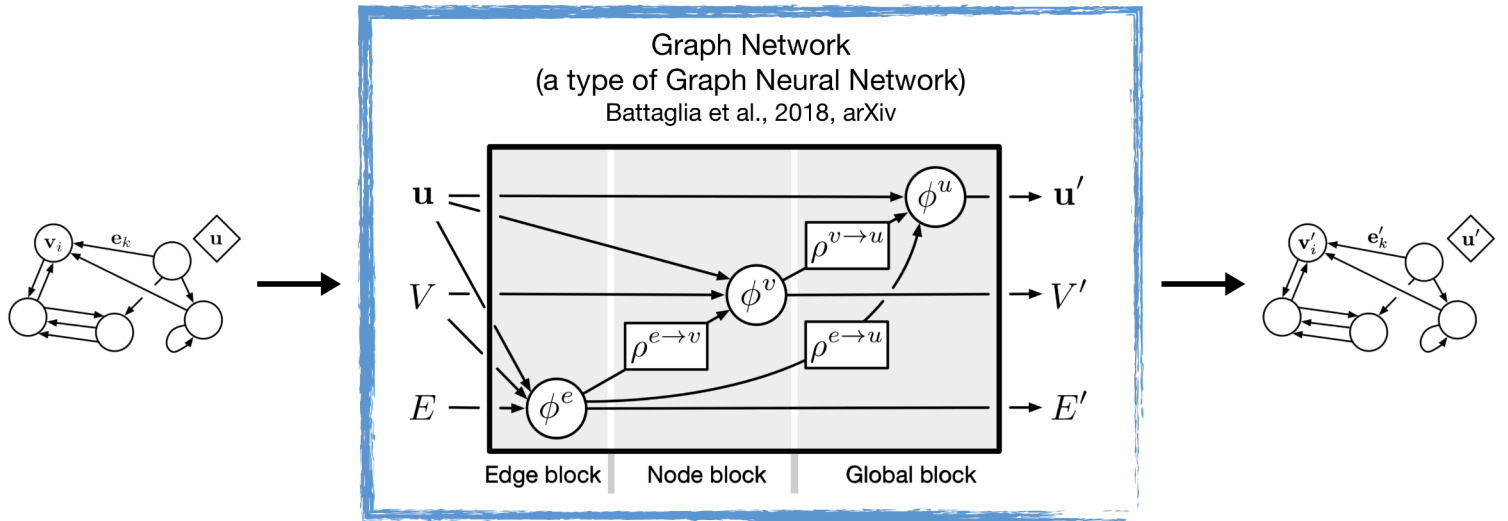
Key literature surveys

- [Scarselli et al. \(2009\) "The Graph Neural Network Model"](#).
Summarizes the initial papers on the topic from ~2005-2009. Original innovation, general formalism.
- [Li et al. \(2015\) "Gated graph sequence neural networks"](#).
Simplified the formalism, trained via backprop, used RNNs for sharing update steps across time.
- [Bronstein et al. \(2016\) "Geometric deep learning: going beyond Euclidean data"](#).
Survey of spectral and spatial approaches for deep learning on graphs.
- [Gilmer et al. \(2017\) "Neural Message Passing for Quantum Chemistry"](#).
Introduced "message-passing neural network" (MPNNs) formalism, unifying various approaches such as graph convolutional networks.
- [Battaglia et al. \(2018\). "Relational inductive biases, deep learning, and graph networks"](#).
Introduced the "graph network" (GN) formalism, extends MPNNs, unifies non-local neural networks/self-attention/Transformer.

Graph Networks (GNs)

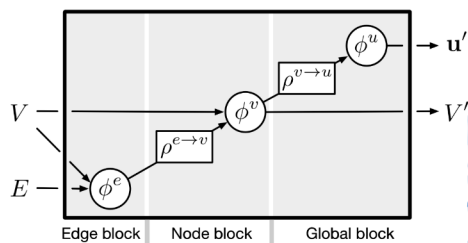
Why do we need another graph neural network variant?

- We designed GNs to be both expressive, and easy to implement
- A GN block is a “graph-to-graph” function approximator
 - The output graph’s structure (number of nodes and edge connectivity) matches the input graph’s
 - The output graph-, node-, and edge-level attributes will be functions of the input graph’s



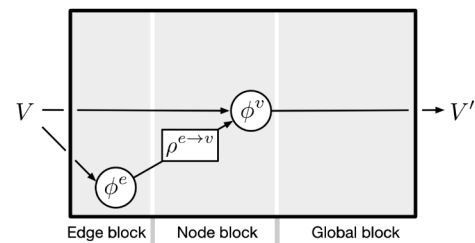
Message-Passing NN (eg. Interaction Net, GCN)

Gilmer et al. 2017



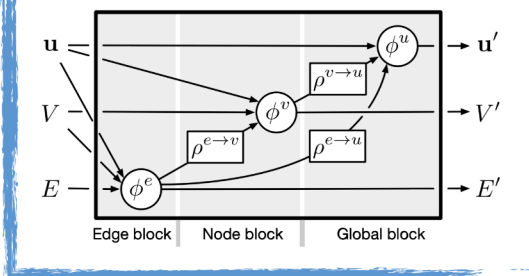
Non-Local NN (eg. Transformer)

Vaswani et al. 2017; Wang et al. 2017



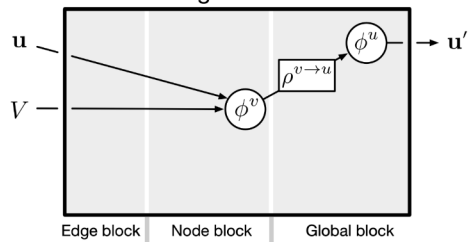
Graph Network (a type of Graph Neural Network)

Battaglia et al. 2018



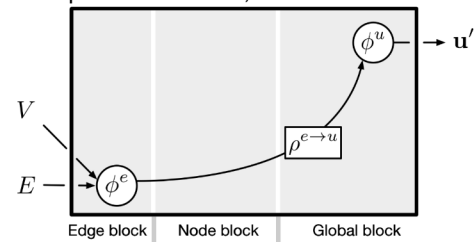
Deep Sets

Zhang et al. 2017



Relation Network

Raposo et al. 2017; Santoro et al. 2017

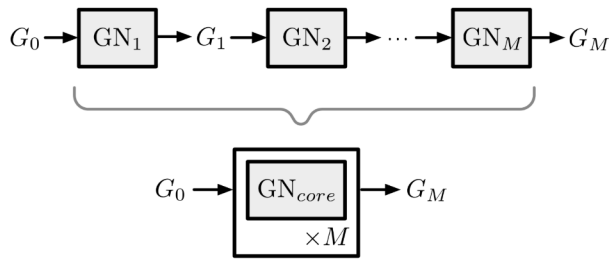


Battaglia et al., 2018, arXiv

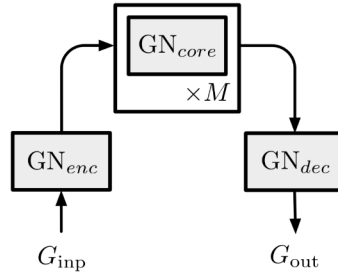
Composing GN blocks

The GN's graph-to-graph interface promotes stacking GN blocks, passing one GN's output to another GN as input

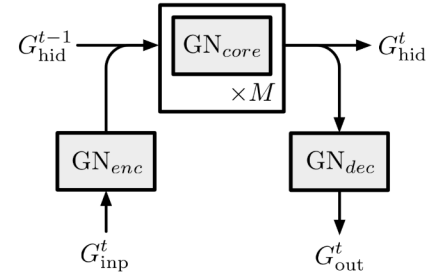
Shared GN core



Encode-process-decode

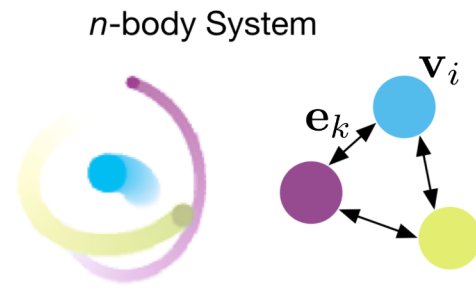


Recurrent GN architecture



Battaglia et al., 2018, arXiv

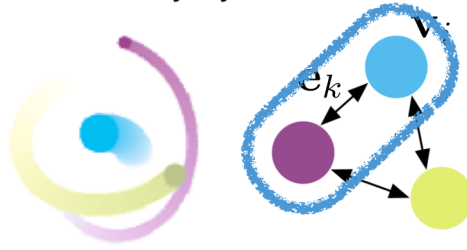
Interaction Network: Learning simulation as message-passing



Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

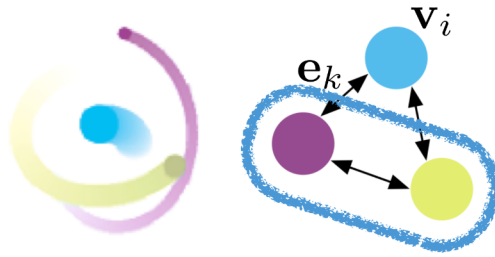
$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

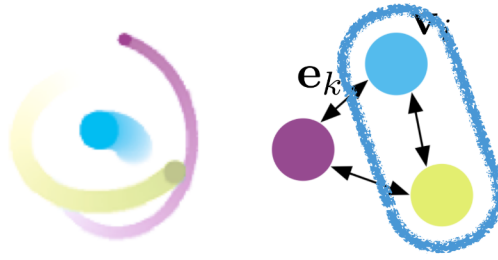
$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

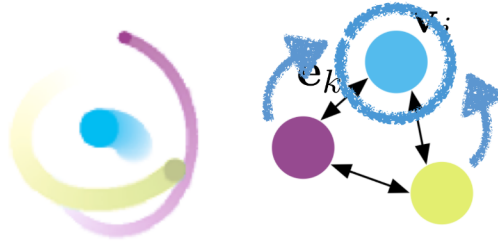
$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Message aggregation

$$\bar{\mathbf{e}}'_i \leftarrow \sum_{r_k=i} \mathbf{e}'_k$$

Node function

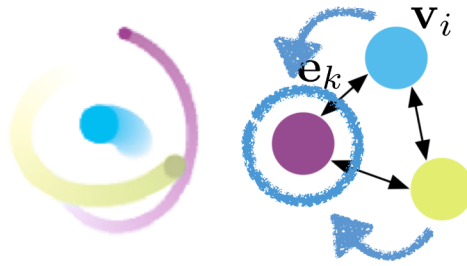
$$\mathbf{v}'_i \leftarrow \phi^v(\bar{\mathbf{e}}'_i, \mathbf{v}_i, \mathbf{u})$$

- Update node info from previous node state and aggregated “messages”

Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Message aggregation

$$\bar{\mathbf{e}}'_i \leftarrow \sum_{r_k=i} \mathbf{e}'_k$$

Node function

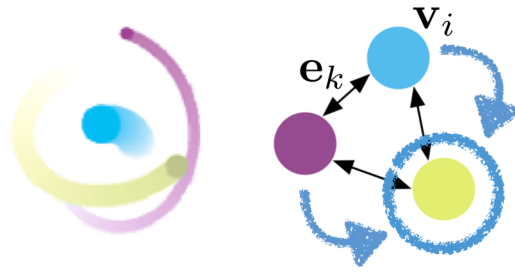
$$\mathbf{v}'_i \leftarrow \phi^v(\bar{\mathbf{e}}'_i, \mathbf{v}_i, \mathbf{u})$$

- Update node info from previous node state and aggregated “messages”

Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Message aggregation

$$\bar{\mathbf{e}}'_i \leftarrow \sum_{r_k=i} \mathbf{e}'_k$$

Node function

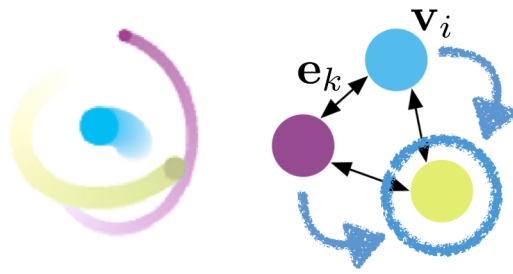
$$\mathbf{v}'_i \leftarrow \phi^v(\bar{\mathbf{e}}'_i, \mathbf{v}_i, \mathbf{u})$$

- Update node info from previous node state and aggregated “messages”

Battaglia et al., 2016, NeurIPS

Interaction Network: Learning simulation as message-passing

n -body System



Edge function

$$\mathbf{e}'_k \leftarrow \phi^e(\mathbf{e}_k, \mathbf{v}_{r_k}, \mathbf{v}_{s_k})$$

- Compute “message” from node and edge attributes associated with an edge

Message aggregation

$$\bar{\mathbf{e}}'_i \leftarrow \sum_{r_k=i} \mathbf{e}'_k$$

Node function

$$\mathbf{v}'_i \leftarrow \phi^v(\bar{\mathbf{e}}'_i, \mathbf{v}_i, \mathbf{u})$$

- Update node info from previous node state and aggregated “messages”

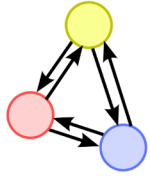
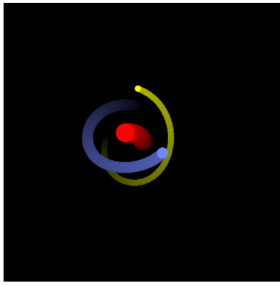
Trained to predict body coordinates



Battaglia et al., 2016, NeurIPS

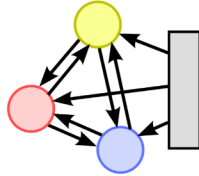
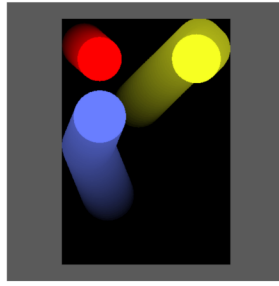
Physical systems as graphs

n-body



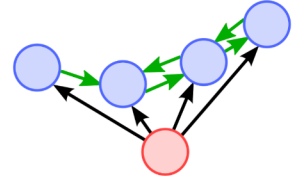
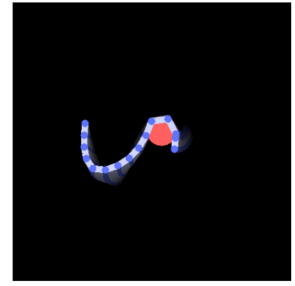
Nodes: bodies
Edges: gravitational forces

Balls



Nodes: balls
Edges: rigid collisions between balls, and walls

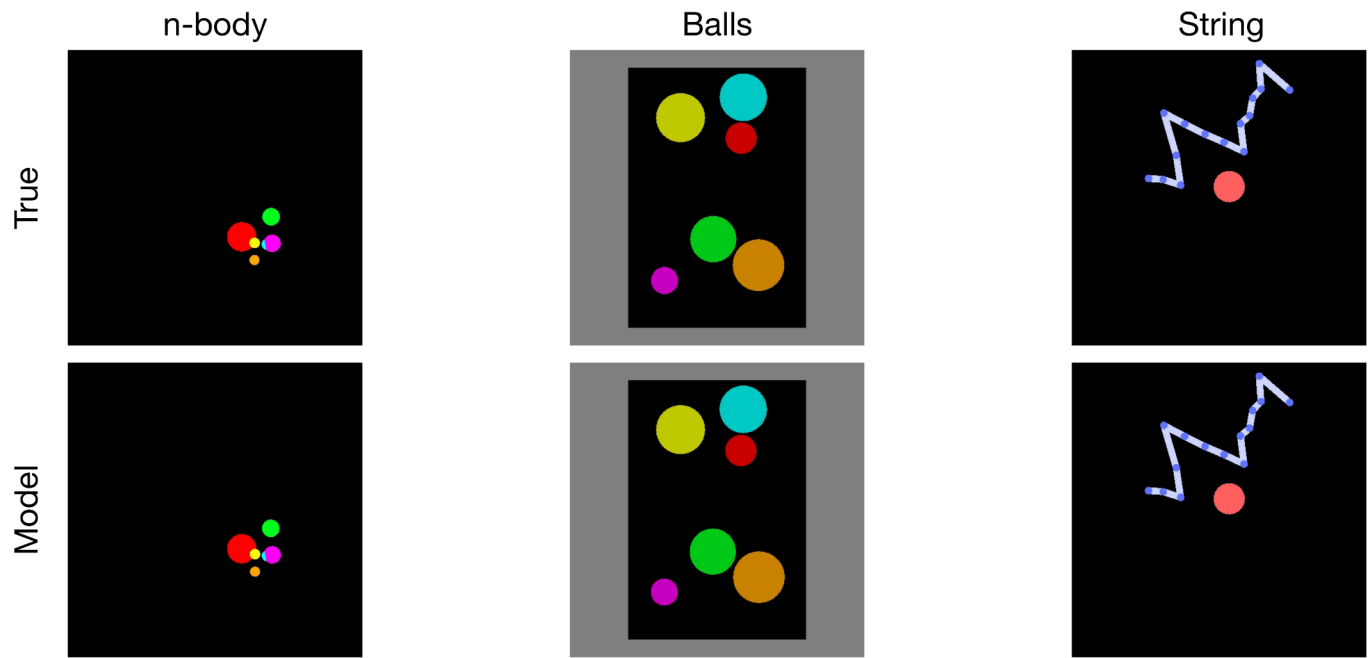
String



Nodes: masses
Edges: springs and rigid collisions

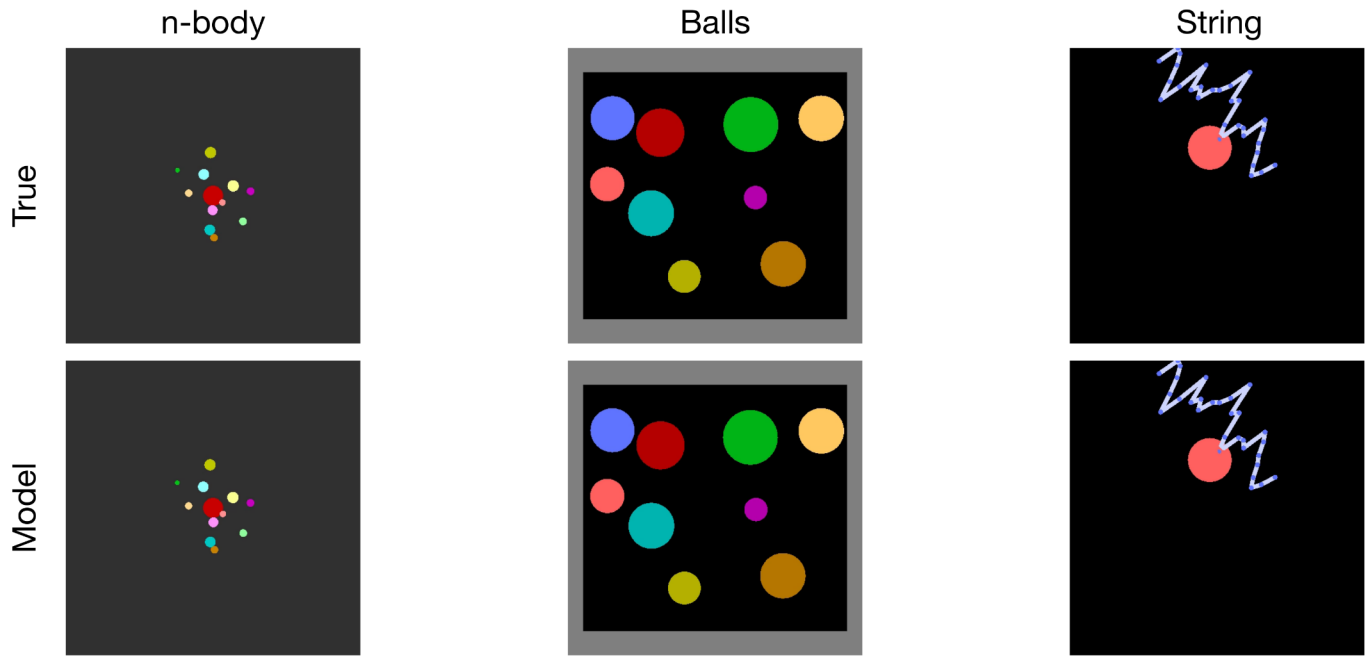
Battaglia et al., 2016, NeurIPS

1000-step rollouts of true (top row) vs predicted (bottom row)



Battaglia et al., 2016, NeurIPS

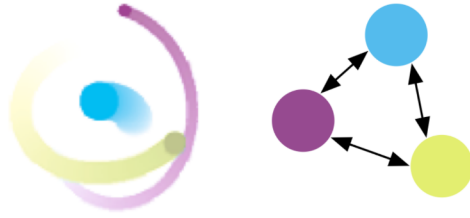
Zero-shot generalisation to larger systems



Battaglia et al., 2016, NeurIPS

Interaction Network: Predicting potential energy

n -body System



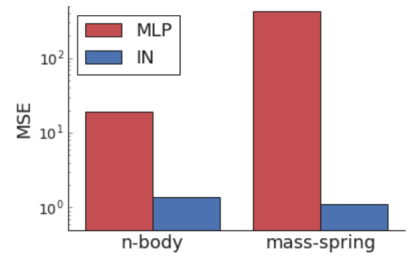
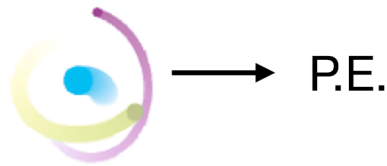
Node aggregation and global function

$$\bar{\mathbf{v}}' \leftarrow \sum_i \mathbf{v}'_i$$

$$\mathbf{u}' \leftarrow \phi^u(\bar{\mathbf{v}}')$$

- Rather than making node-wise predictions, node updates can be used to make global predictions.

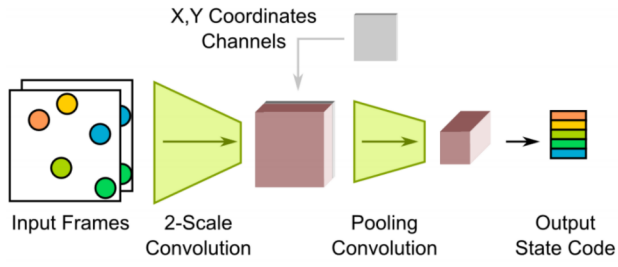
Trained to predict system's potential energy



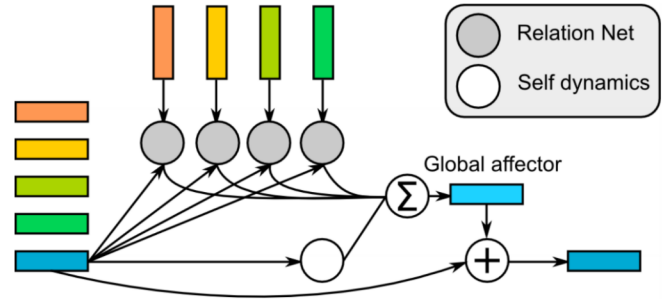
Battaglia et al., 2016, NeurIPS

Visual interaction network: Simulate from input images

Multi-frame encoder (conv net-based)



Interaction network



Watters et al., 2017, NeurIPS

Visual interaction network: Simulate from input images

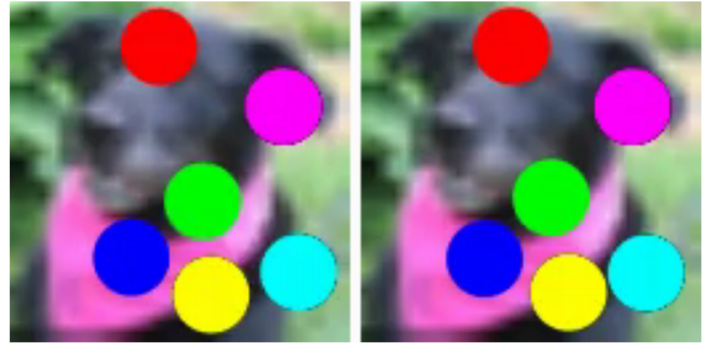
Mass-springs



True

Model

Bouncing balls



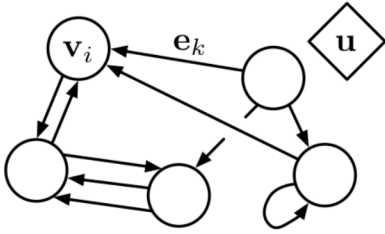
True

Model

Can even predict invisible objects, inferred from how they affect visible ones

Watters et al., 2017, NeurIPS

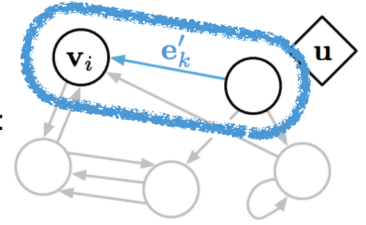
Full "Graph Network" generalizes/extends "Interaction Network"



Edge block

For each edge, e_k, v_{s_k}, v_{r_k}, u , are passed to an "edge-wise function":

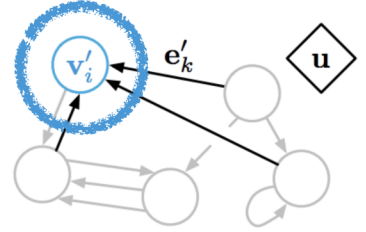
$$e'_k \leftarrow \phi^e(e_k, v_{r_k}, v_{s_k}, u)$$



Node block

For each node, \bar{e}'_i, v_i, u , are passed to a "node-wise function":

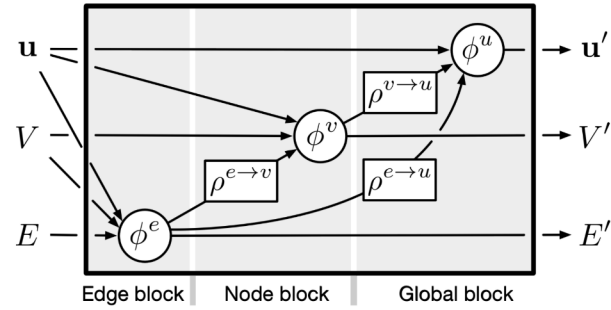
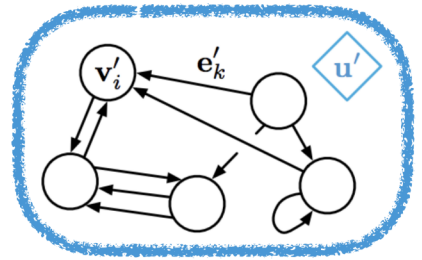
$$v'_i \leftarrow \phi^v(\bar{e}'_i, v_i, u)$$



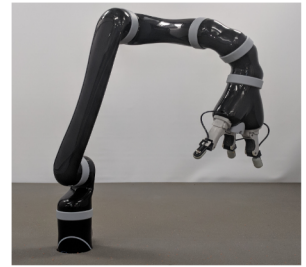
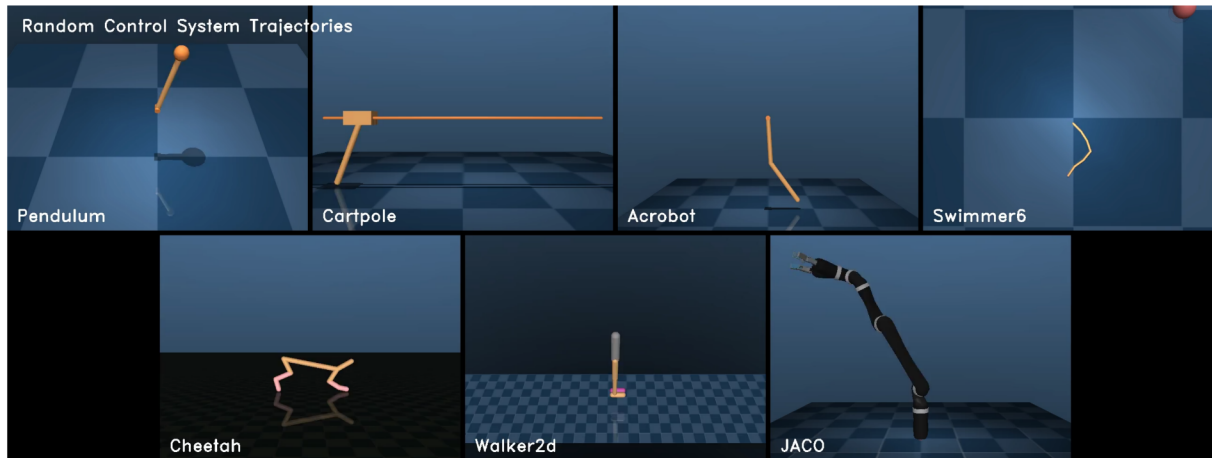
Global block

Across the graph, \bar{e}', \bar{v}', u , are passed to a "global function":

$$u' \leftarrow \phi^u(\bar{e}', \bar{v}', u)$$



Systems: "DeepMind Control Suite" (Mujoco) & real JACO



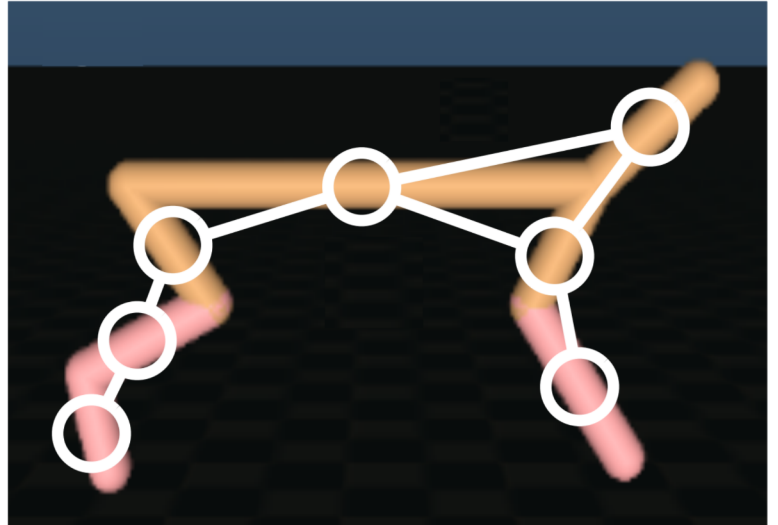
JACO Arm

DeepMind Control Suite (Tassa et al., 2018)

Kinematic tree of the actuated system as a graph

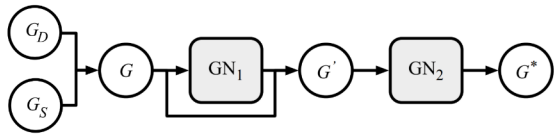
Controllable physical system as a graph:

- Bodies \rightarrow Nodes
- Joints \rightarrow Edges
- Global properties



Sanchez-Gonzalez et al., 2018, ICML

Forward model: Multiple systems & zero-shot generalization

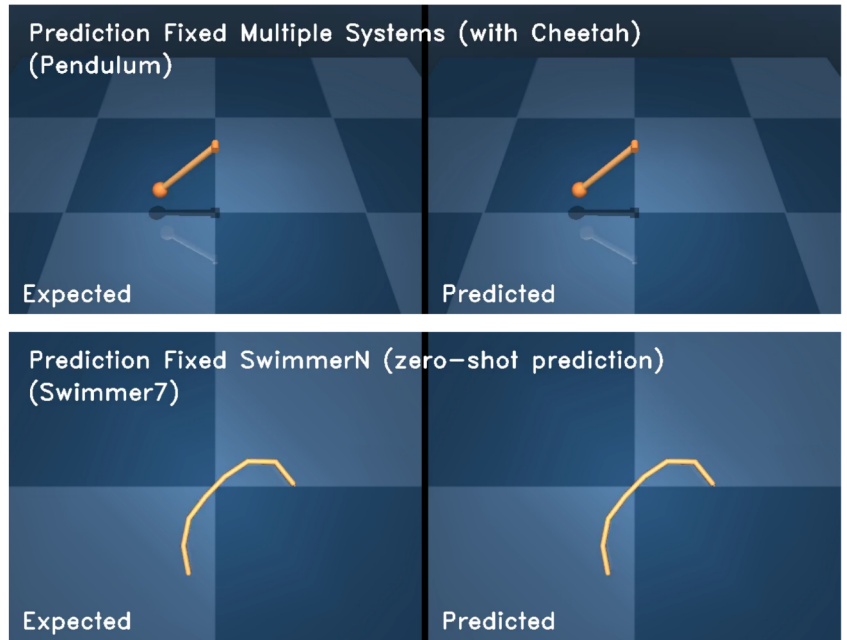


Single model trained:

- Pendulum, Cartpole, Acrobot, Swimmer6 & Cheetah

Zero-shot generalization: Swimmer

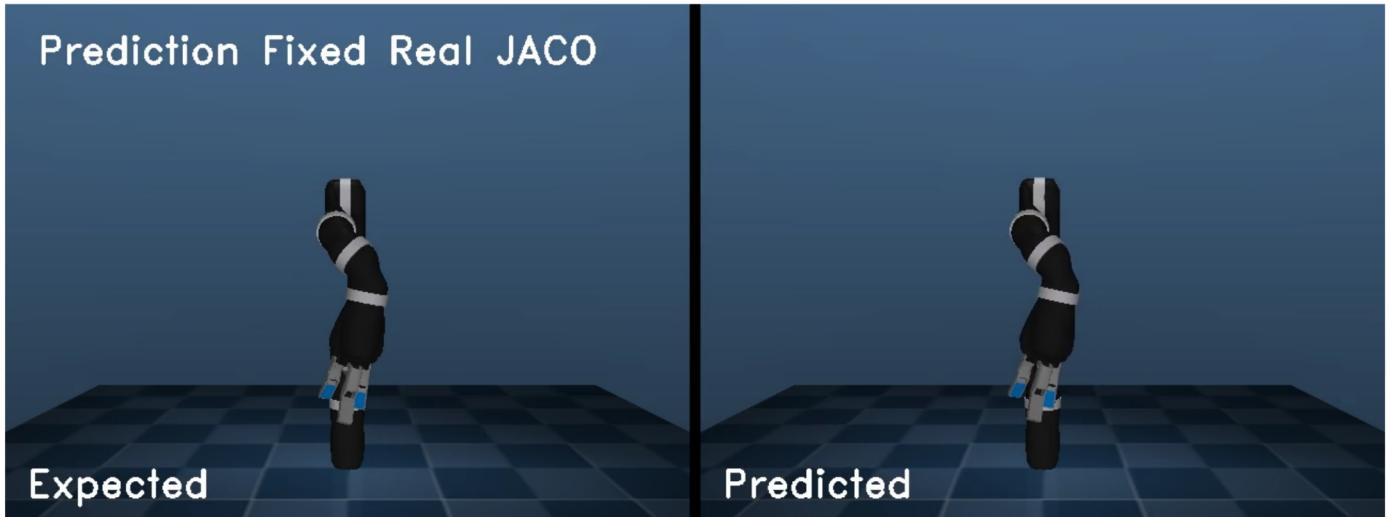
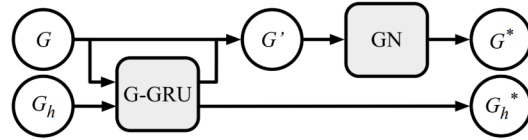
- # training links: {3, 4, 5, 6, -, 8, 9, -, -, ...}
- # testing links: {-, -, -, -, 7, -, -, 10-14}



Sanchez-Gonzalez et al., 2018, ICML

Forward model: Real JACO data

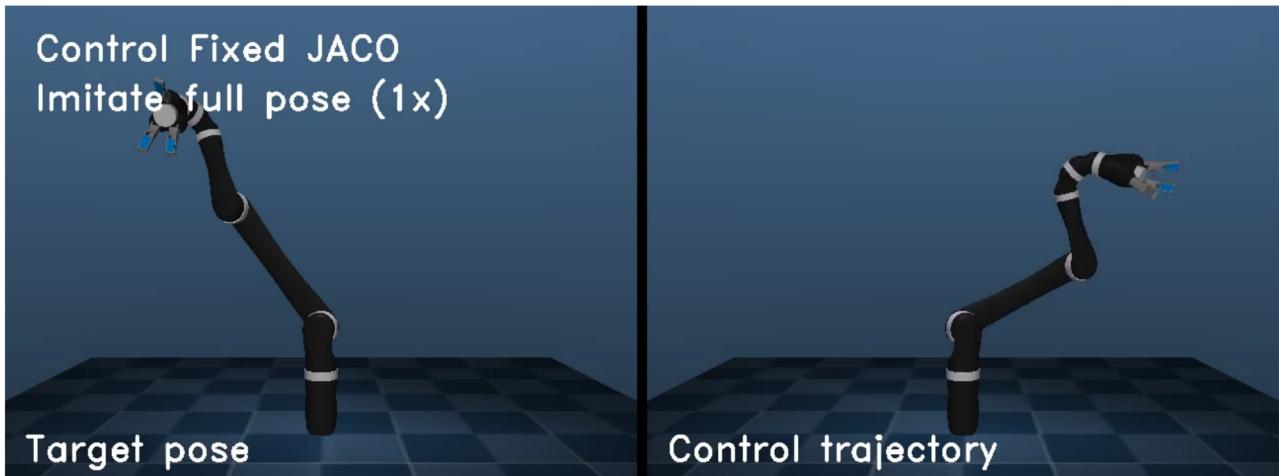
Recurrent GN



Sanchez-Gonzalez et al., 2018, ICML

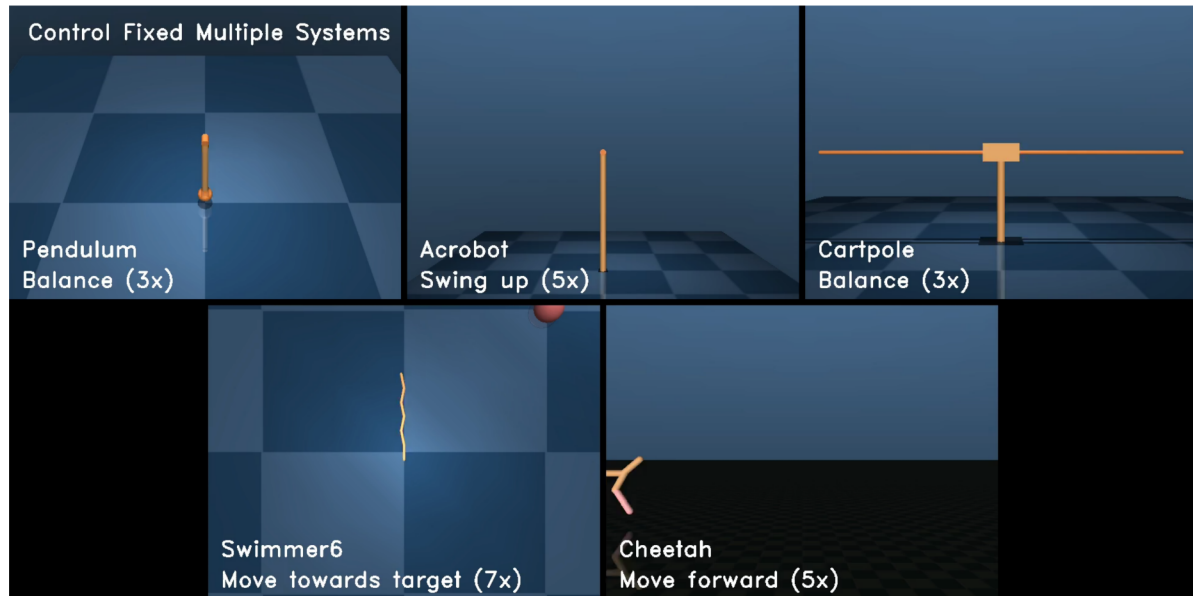
Control: Model-based planning

The GN-based forward model is differentiable, so we can backpropagate through it to search for a sequence of actions that maximize reward.



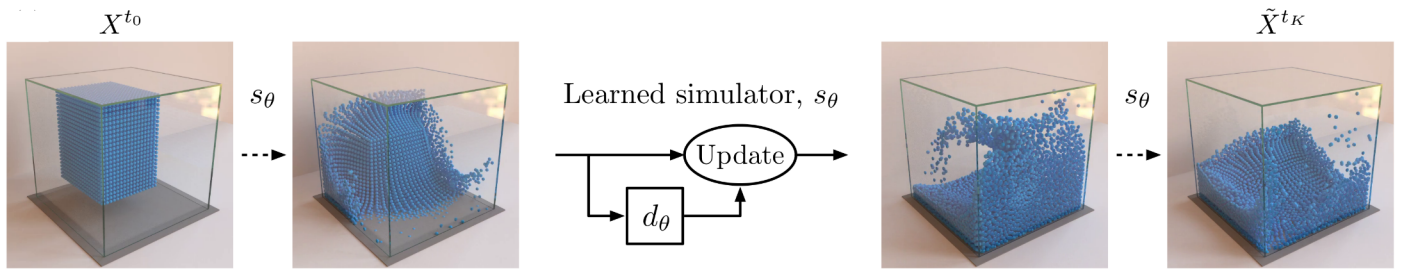
Sanchez-Gonzalez et al., 2018, ICML

Control: Multiple systems via a single model



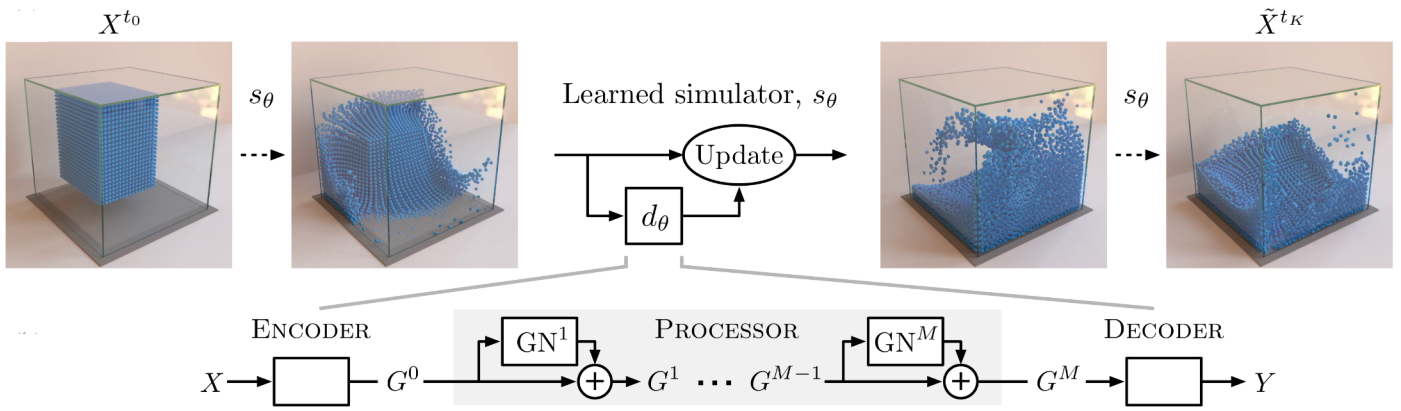
Sanchez-Gonzalez et al., 2018, ICML

Learning to simulate fluids and complex materials



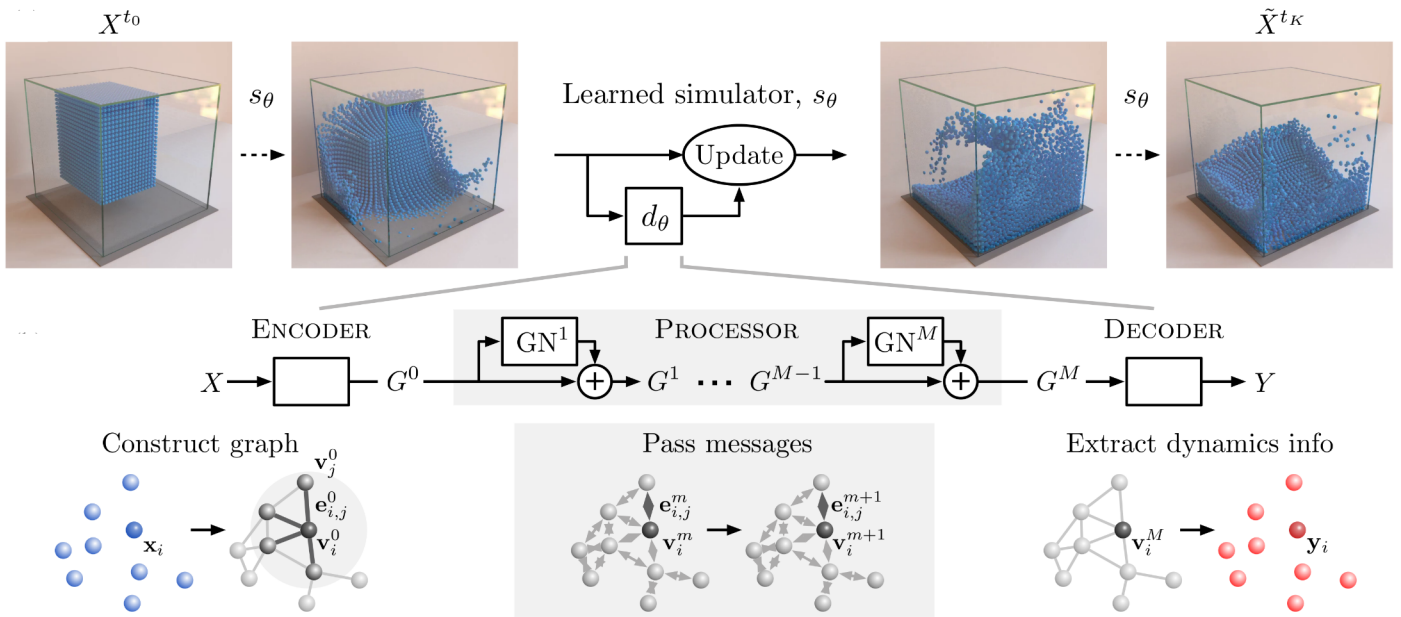
Sanchez-Gonzalez et al., 2020, arXiv/under review

Learning to simulate fluids and complex materials



Sanchez-Gonzalez et al., 2020, arXiv/under review

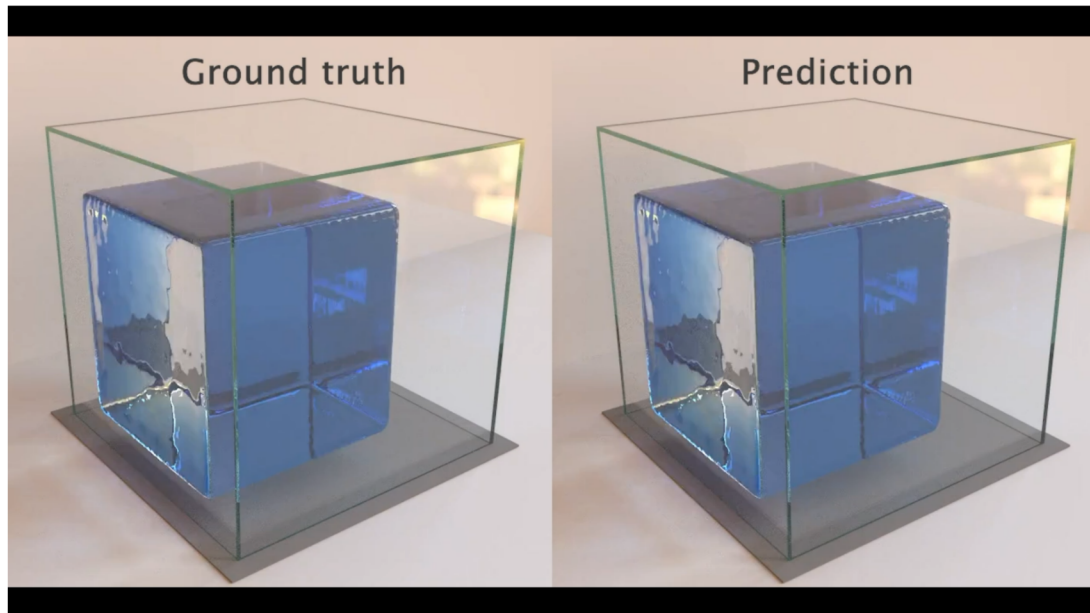
Learning to simulate fluids and complex materials



Sanchez-Gonzalez et al., 2020, arXiv/under review

Learning to simulate fluids and complex materials

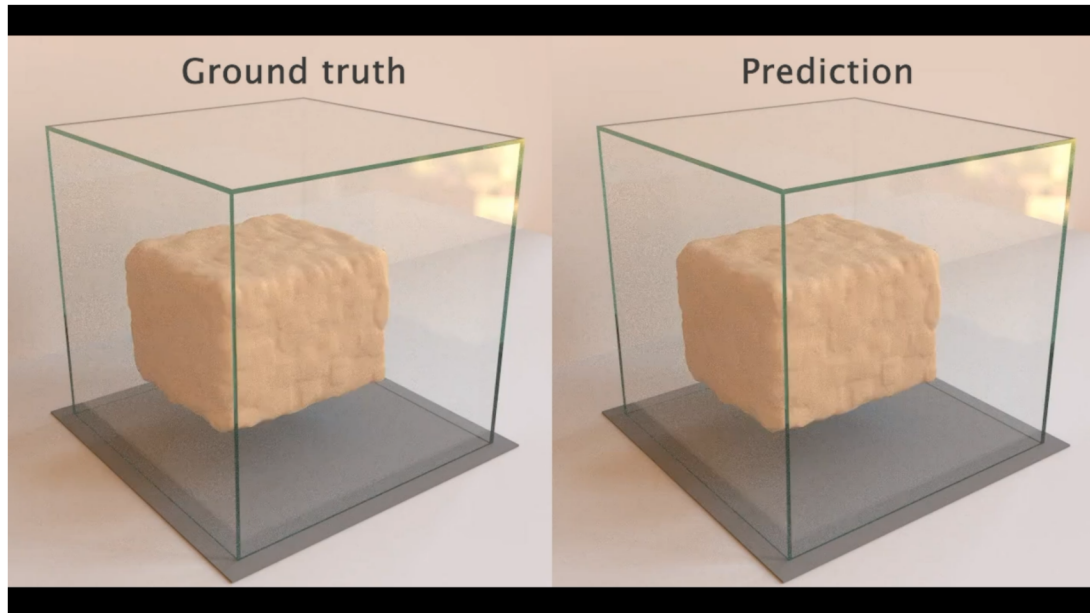
Water-3D (14k particles, SPH)



Sanchez-Gonzalez et al., 2020, arXiv/under review

Learning to simulate fluids and complex materials

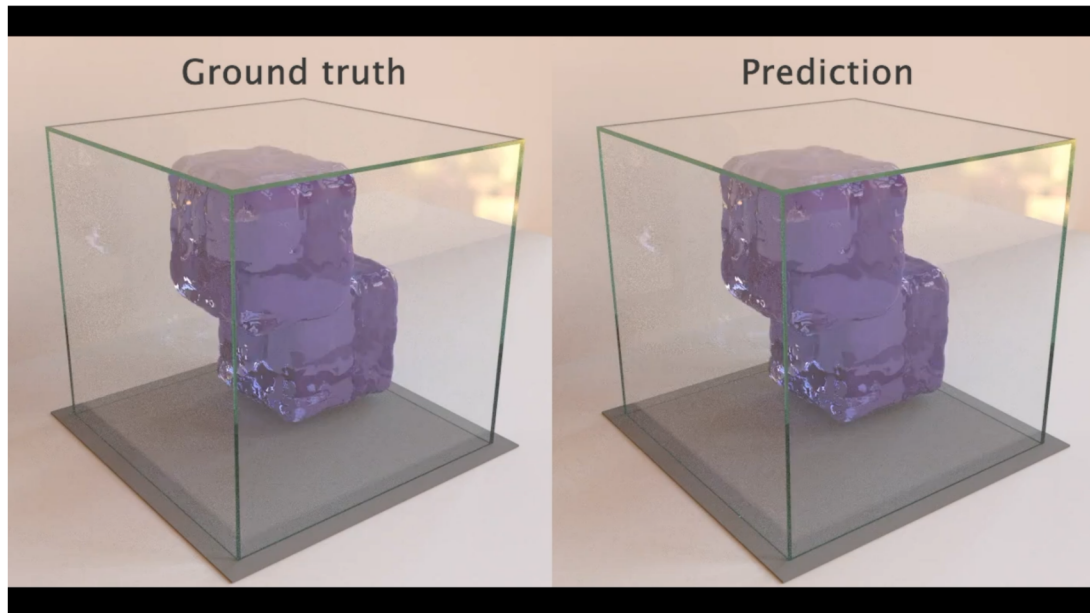
Sand-3D (19k particles, MPM)



Sanchez-Gonzalez et al., 2020, arXiv/under review

Learning to simulate fluids and complex materials

Goop-3D (19k particles, MPM)

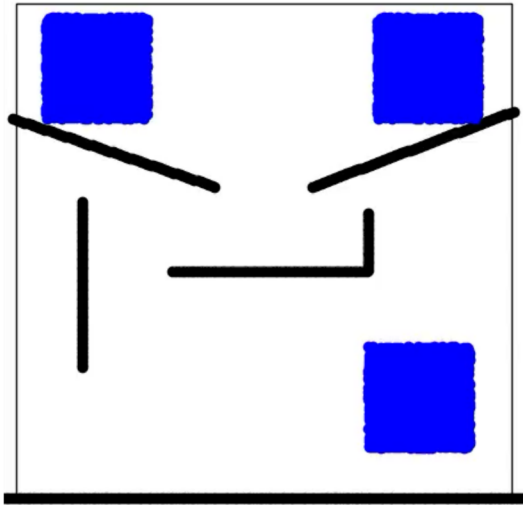


Sanchez-Gonzalez et al., 2020, arXiv/under review

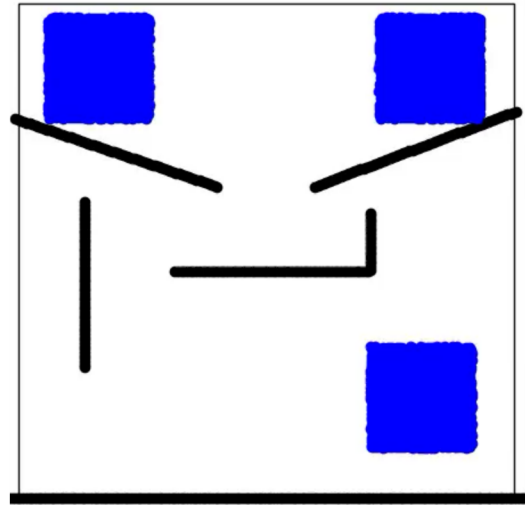
Learning to simulate fluids and complex materials

Water ramps

Ground truth (4943 parts)



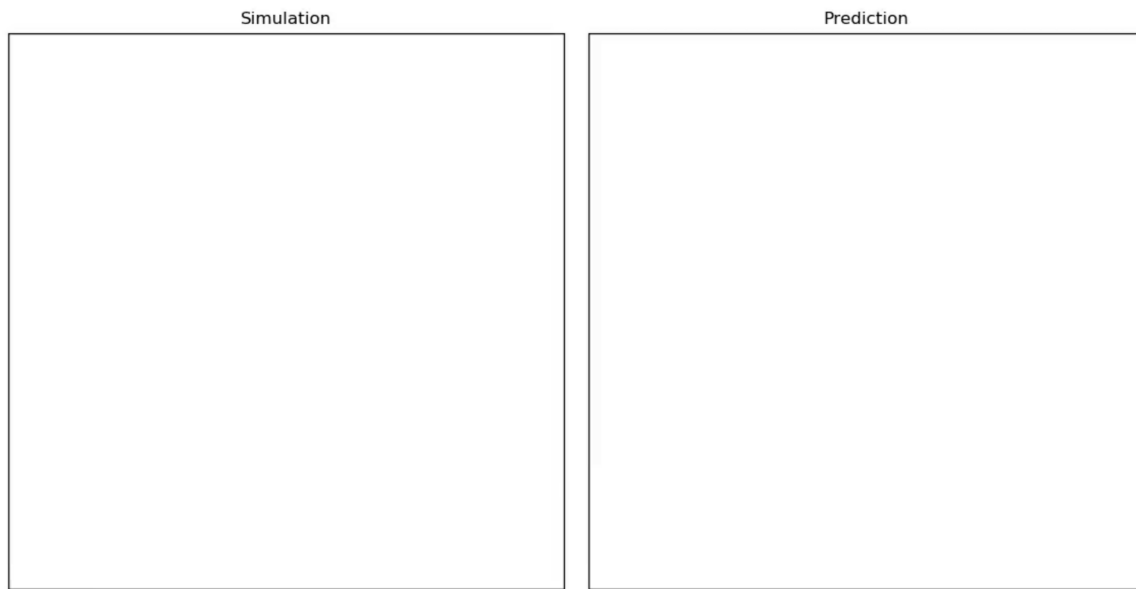
Predictions (4943 parts)



Sanchez-Gonzalez et al., 2020, arXiv/under review

Learning to simulate fluids and complex materials

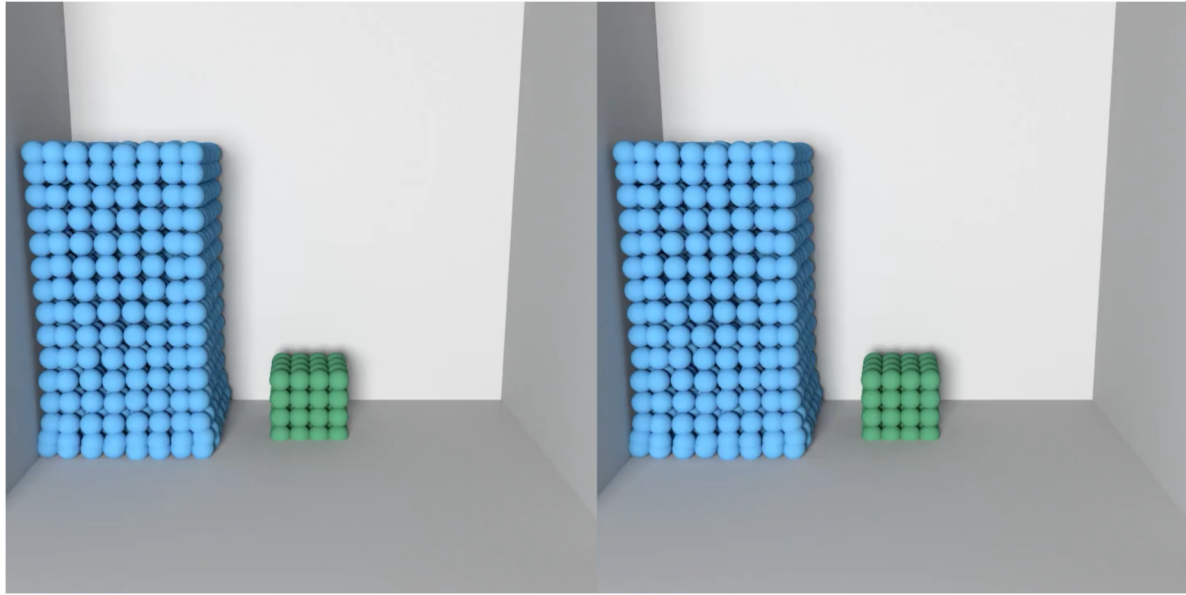
Multiple materials, generalization



Sanchez-Gonzalez et al., 2020, arXiv/under review

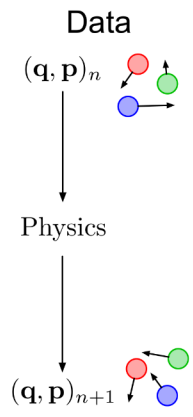
Learning to simulate fluids and complex materials

BoxBath



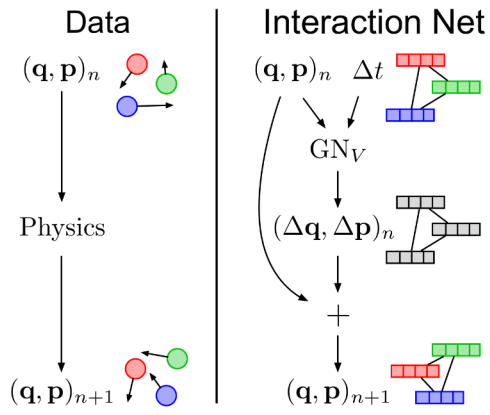
Sanchez-Gonzalez et al., 2020, arXiv/under review

Hamiltonian ODE Graph Network



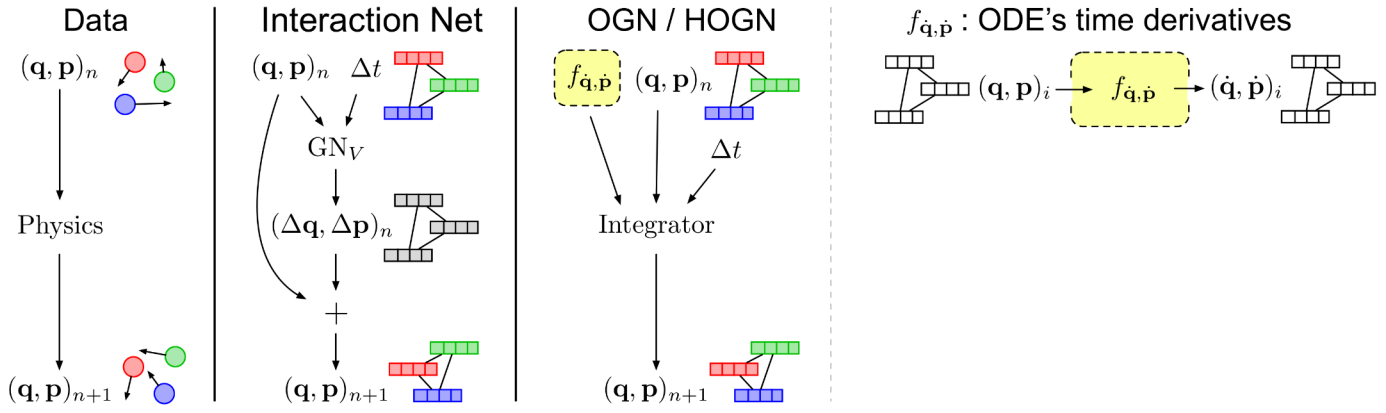
Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

Hamiltonian ODE Graph Network



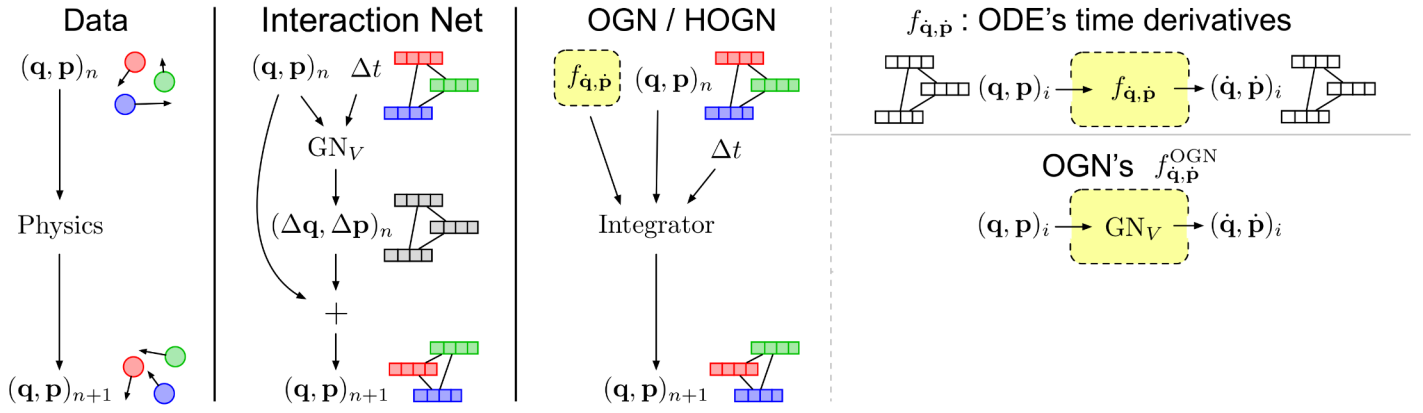
Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

Hamiltonian ODE Graph Network



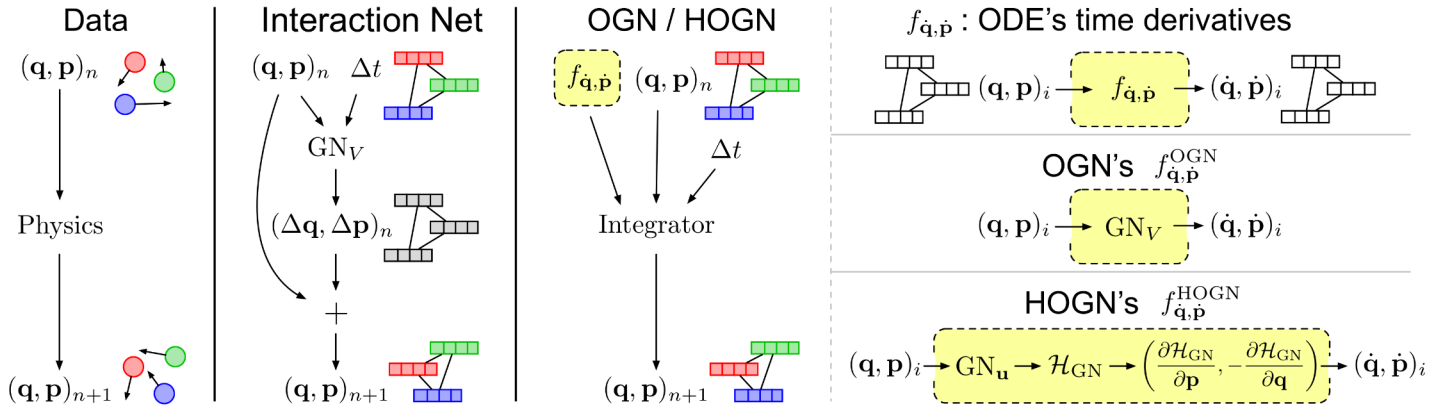
Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

Hamiltonian ODE Graph Network



Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

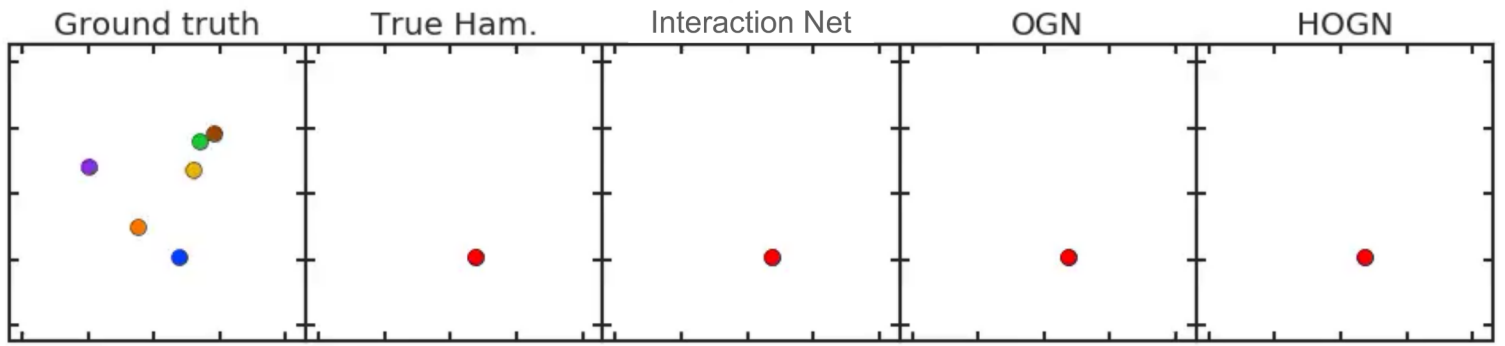
Hamiltonian ODE Graph Network



Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

Hamiltonian ODE Graph Network

t = 0 (Step 0)

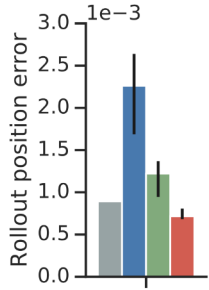


Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

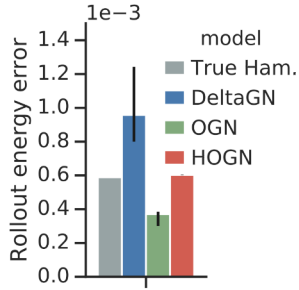
Hamiltonian ODE Graph Network

Performance

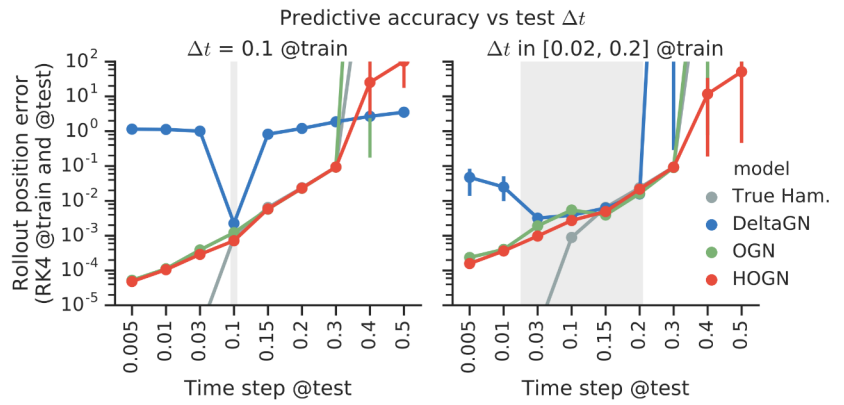
Predictive accuracy per model



Energy accuracy per model



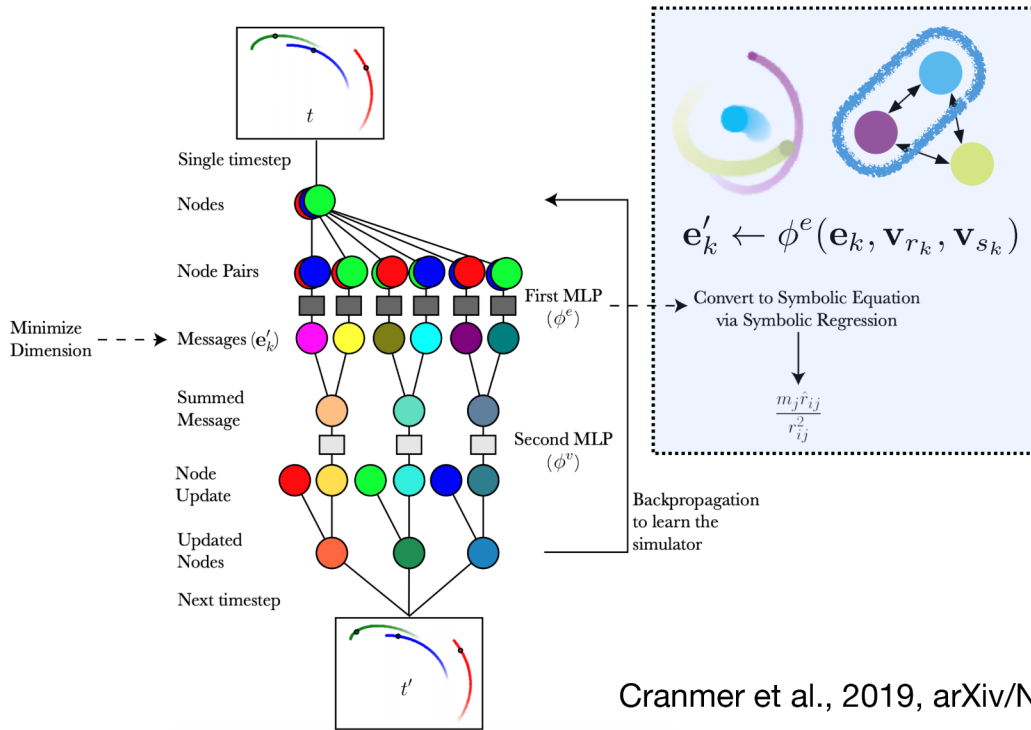
Generalization to untrained time steps



- OGN and HOGN used RK4 integrator (we also tested lower order RK integrators)
- We also tested symplectic integrators, and found HOGN has better energy accuracy/conservation

Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS 2019 workshop

Learning symbolic physics with graph networks



Cranmer et al., 2019, arXiv/NeurIPS 2019 workshop

Learning symbolic physics with graph networks

Experiments

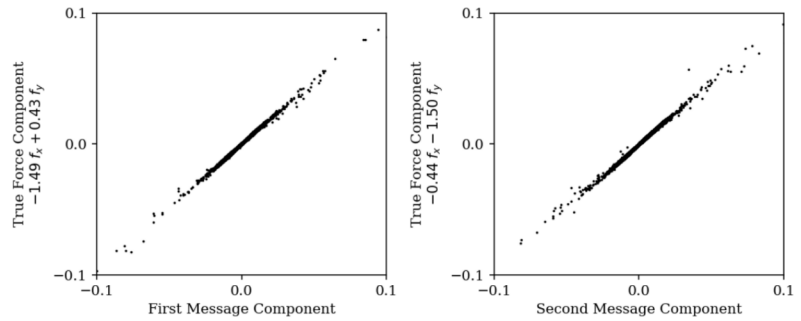
- 2D and 3D n-body ($1/r$ and $1/r^2$ force laws)
- Mass-spring system

Architecture

Interaction network with message vectors constrained to 2 or 3 dimensions

Results

- After training, message vectors are linear transforms of the true forces
- Symbolic regression of the message function's formula reveals the analytical form of the true force laws

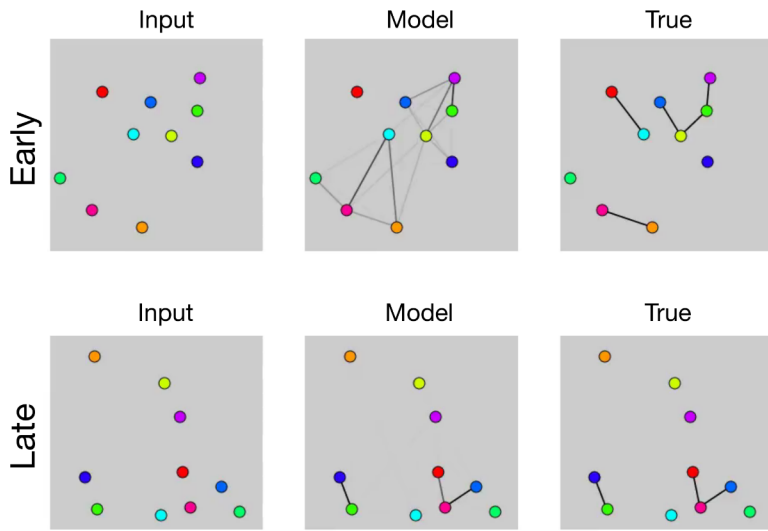


Cranmer et al., 2019, arXiv/NeurIPS 2019 workshop

Inferring relations in dot motion

Model: Relation Network - simple GN with no node update)

Trained on mass-spring systems

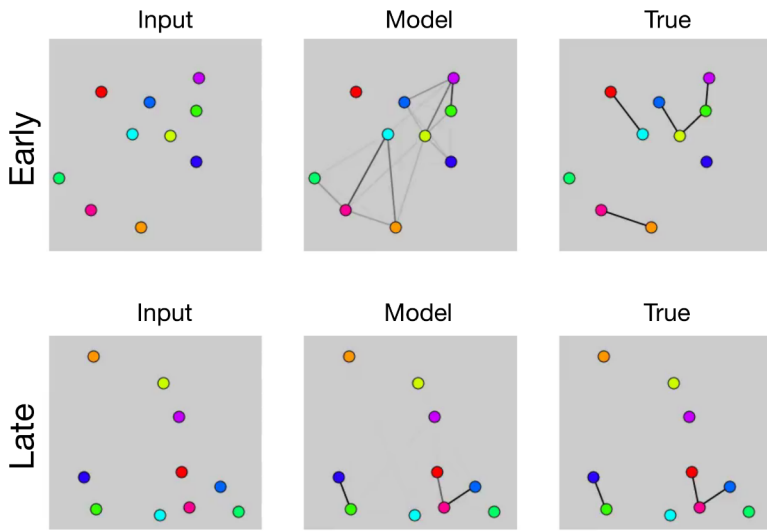


Santoro et al., 2017, NeurIPS

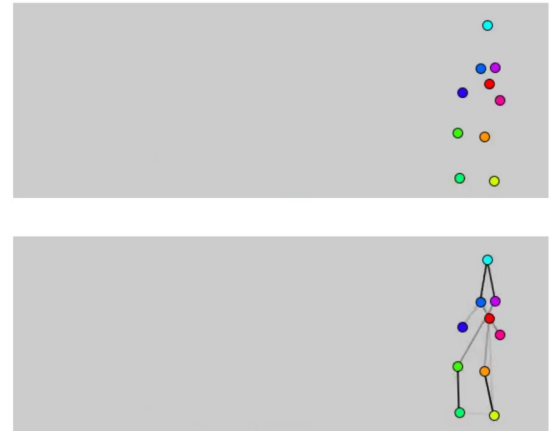
Inferring relations in dot motion

Model: Relation Network - simple GN with no node update)

Trained on mass-spring systems



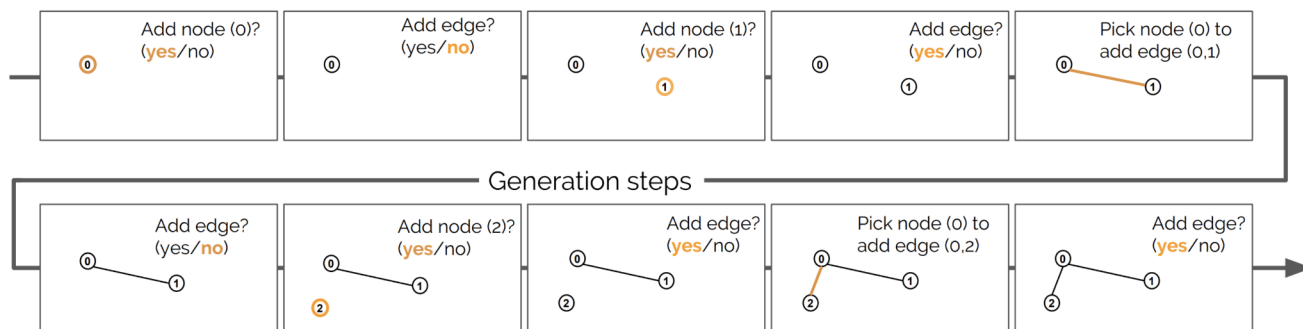
Generalizes to point-light walkers



Santoro et al., 2017, NeurIPS

Learning deep generative models of chemical graphs

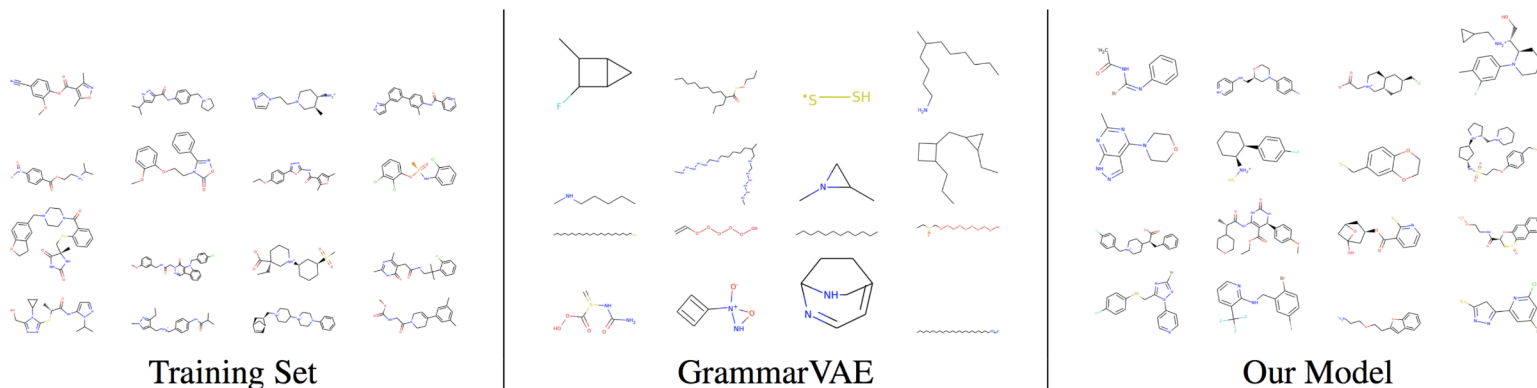
- Generative model defines joint distribution over graph-generating decisions (structure and order).
- Analogous to a decision tree, where decisions are selected by a GNN:
 1. *Add node?* If NO, terminate.
 2. If YES, *Add edge?* If NO, goto (1).
 3. If YES, *Pick node to add edge to.* Goto (2).
- Training optimizes the joint log-likelihood of structure and order, with Monte Carlo integration over permutations.



Li et al., 2018, arXiv

Learning deep generative models of chemical graphs

- GrammarVAE (Kusner et al., 2017) has qualitatively poorer samples from the prior.

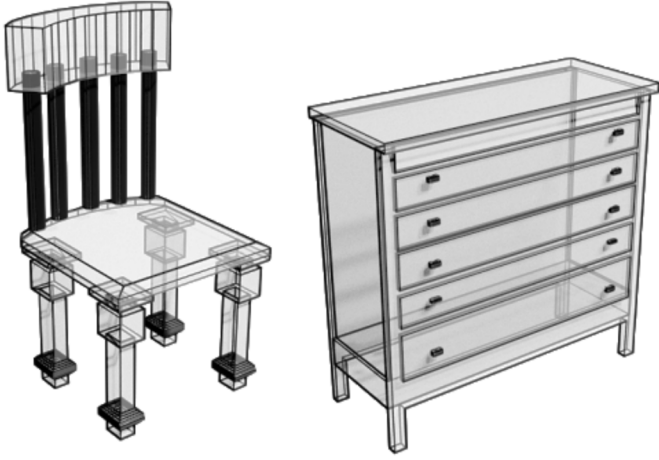


- Our model learns a more accurate model than LSTMs, and can generate more novel molecules.

Arch	Grammar	Ordering	N	NLL	%valid	%novel
LSTM	Graph	Fixed	1	22.06	85.16	80.14
LSTM	Graph	Random	$O(n!)$	63.25	91.44	91.26
Graph	Graph	Fixed	1	20.55	97.52	90.01
Graph	Graph	Random	$O(n!)$	58.36	95.98	95.54

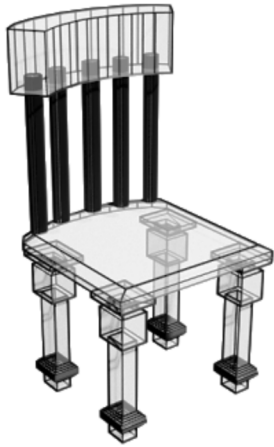
Li et al., 2018, arXiv

PolyGen: Autoregressive generative model of 3D meshes



Nash et al., 2020, arXiv/under review

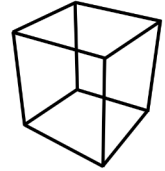
PolyGen: Autoregressive generative model of 3D meshes



.OBJ file: cube

```
v 0.000000 2.000000 2.000000
v 0.000000 0.000000 2.000000
v 2.000000 0.000000 2.000000
v 2.000000 2.000000 2.000000
v 0.000000 2.000000 0.000000
v 0.000000 0.000000 0.000000
v 2.000000 0.000000 0.000000
v 2.000000 2.000000 0.000000
```

```
f 1 2 3 4
f 8 7 6 5
f 4 3 7 8
f 5 1 4 8
f 5 6 2 1
f 2 6 7 3
```



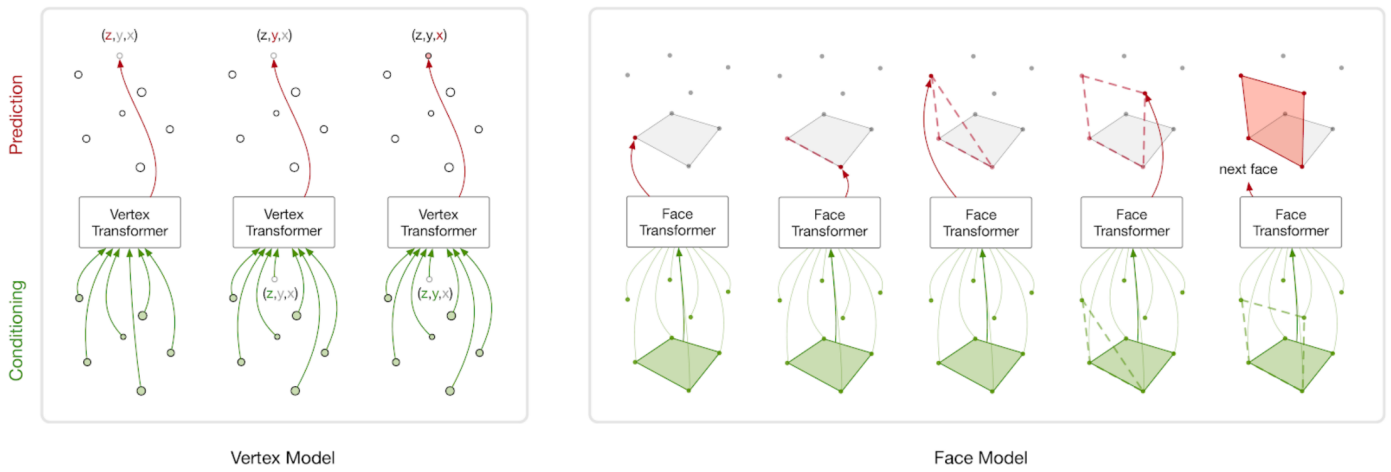
Nash et al., 2020, arXiv/under review

PolyGen: Autoregressive generative model of 3D meshes

Architecture: Transformer-based

Two phases:

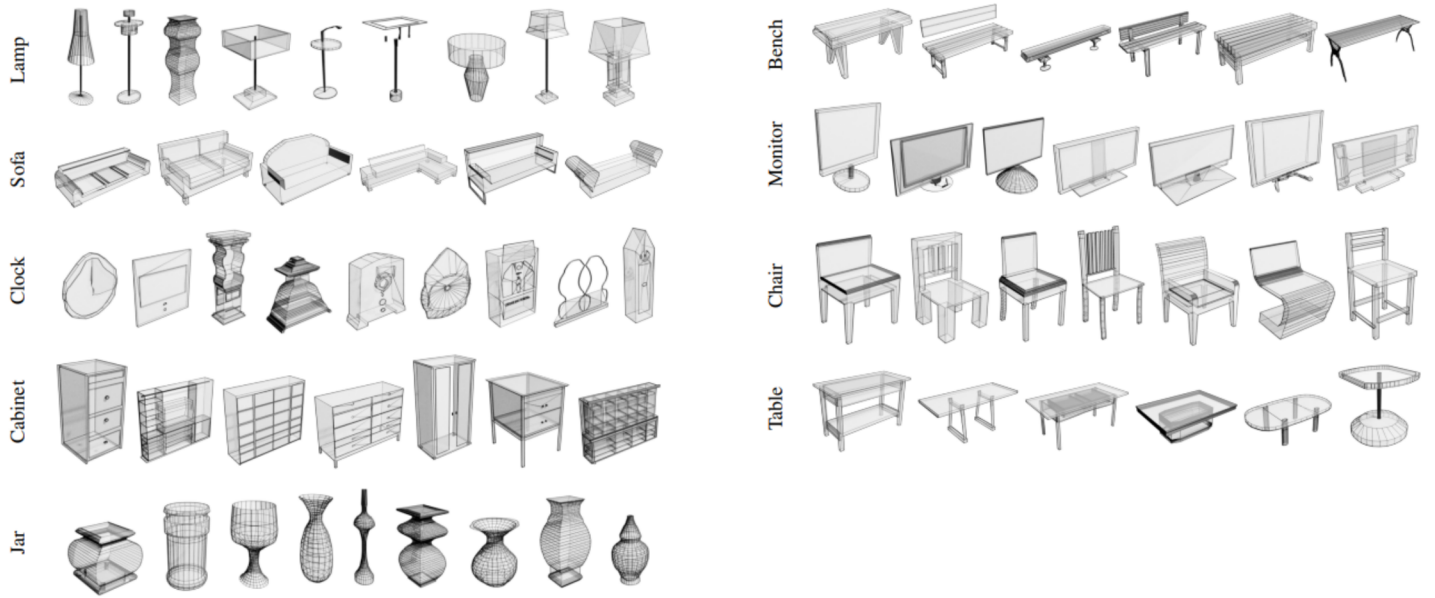
1. Vertex model
2. Face model



Nash et al., 2020, arXiv/under review

PolyGen: Autoregressive generative model of 3D meshes

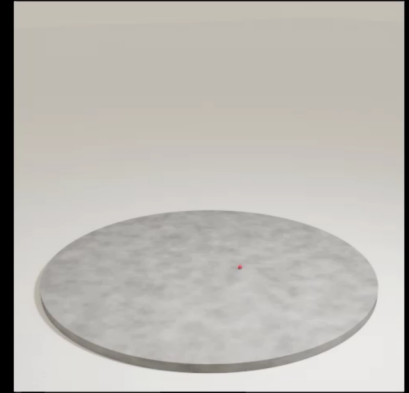
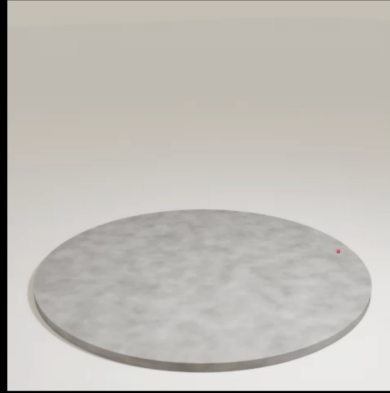
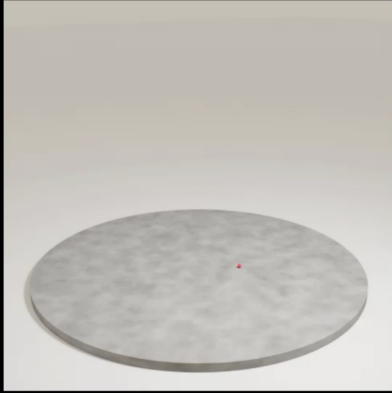
Class-conditional samples



Nash et al., 2020, arXiv/under review

PolyGen

An Autoregressive Generative Model of 3D Meshes



Class conditional samples

Nash et al., 2020, arXiv/under review

Build Graph Nets in Tensorflow

github.com/deepmind/graph_nets

```
# Provide your own functions to generate graph-structured data.
input_graphs = get_graphs()

# Create the graph network.
graph_net_module = gn.modules.GraphNetwork(
    edge_model_fn=lambda: snt.nets.MLP([32, 32]),
    node_model_fn=lambda: snt.nets.MLP([32, 32]),
    global_model_fn=lambda: snt.nets.MLP([32, 32]))

# Pass the input graphs to the graph network, and return the output graphs.
output_graphs = graph_net_module(input_graphs)
```

For GNN libraries in PyTorch, check out:

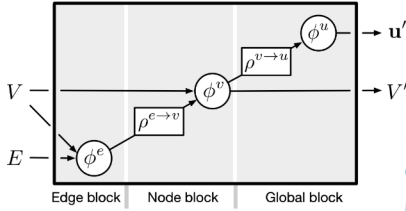
- pytorch_geometric: github.com/rusty1s/pytorch_geometric (for a GN analog, see MetaLayer)
- Deep Graph Library: github.com/dmlc/dgl

Build Graph Nets in Tensorflow

github.com/deepmind/graph_nets

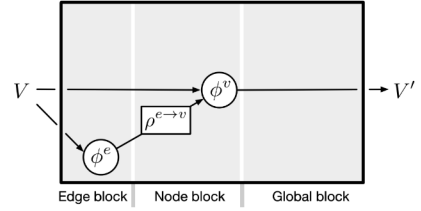
Message-Passing NN (eg. Interaction Net)

Gilmer et al. 2017

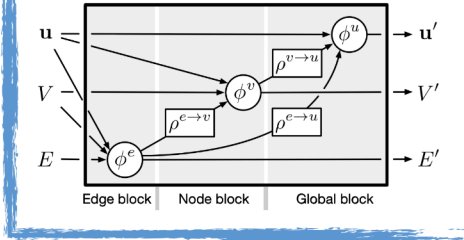


Non-Local NN (eg. Transformer)

Vaswani et al. 2017; Wang et al. 2017

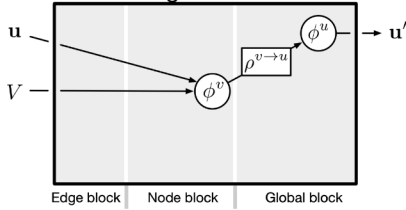


Graph Network
(a type of Graph Neural Network)



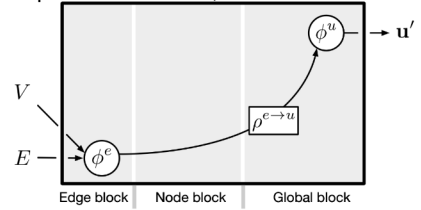
Deep Sets

Zhang et al. 2017



Relation Network

Raposo et al. 2017; Santoro et al. 2017



Build Graph Nets in Tensorflow

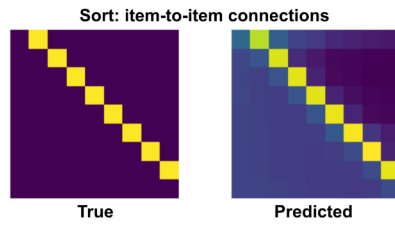
github.com/deepmind/graph_nets

IPython Notebook demos
(All use same architecture)

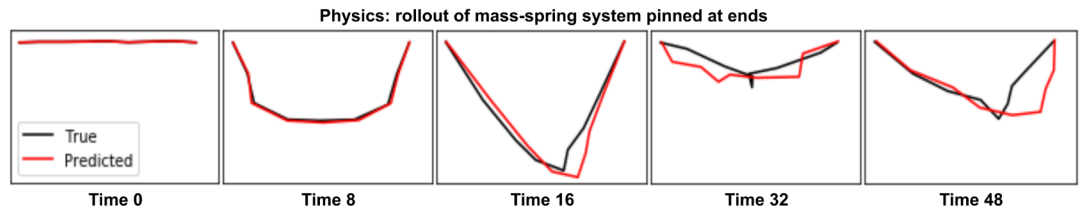
Shortest path:



Sorting:



Predicting physics:



Conclusions

- Graph neural networks: a first-class member of the deep learning toolkit.
- Learned message-passing on graphs can capture complex physical knowledge.
- “Graph Nets” support learning simulation, as well as other forms of structured reasoning and decision-making.
- Build Graph Nets in Tensorflow: github.com/deepmind/graph_nets.

Key collaborators

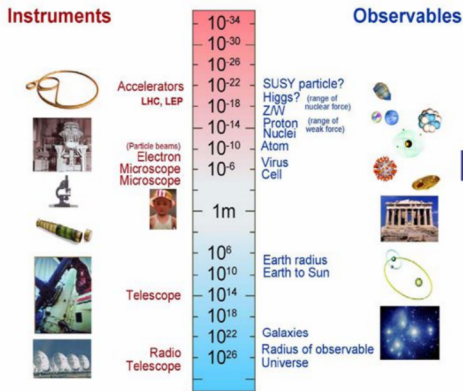
Alvaro Sanchez-Gonzalez	Jess Hamrick
Jonny Godwin	Victor Bapst
Tobi Pfaff	Razvan Pascanu
Rex Ying	Nicholas Heess
Charlie Nash	Ali Eslami
Yaroslav Ganin	Oriol Vinyals
Miles Cranmer	Jure Leskovec
Shirley Ho	

References

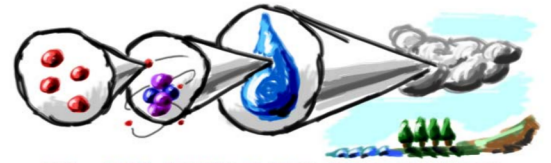
[Battaglia et al. 2018 arXiv](#)
[Battaglia et al., 2016, NeurIPS](#)
[Watters et al., 2017, NeurIPS](#)
[Sanchez-Gonzalez et al., 2018, ICML](#)
[Sanchez-Gonzalez et al., 2020, arXiv/under review](#)
[Cranmer et al., 2019, arXiv/NeurIPS workshop](#)
[Sanchez-Gonzalez et al., 2019, arXiv/NeurIPS workshop](#)
[Li et al., 2018, arXiv](#)
[Nash et al., 2020 arXiv/under review](#)

Discussion: Going beyond everyday scales

Setting the scale



Particle physics
is
Atto-physics



SMALL PARTS COMBINE TO FORM LARGER STRUCTURES

http://www.chem4kids.com/files/atom_intro.html

