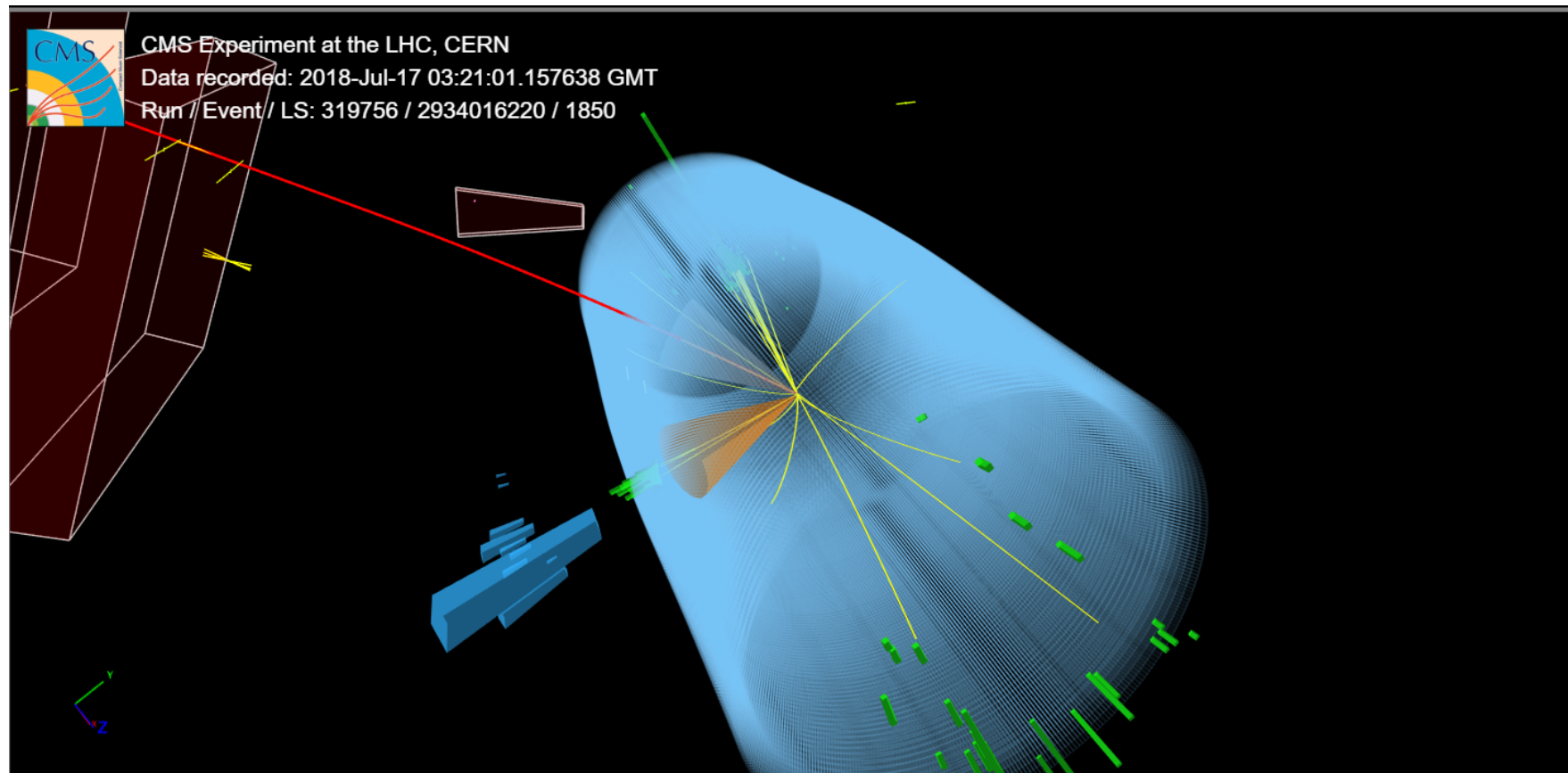




Measuring Higgs couplings and properties in the $H \rightarrow \tau\tau$ decay channel



University of Birmingham Particle Physics group seminar 09/06/21

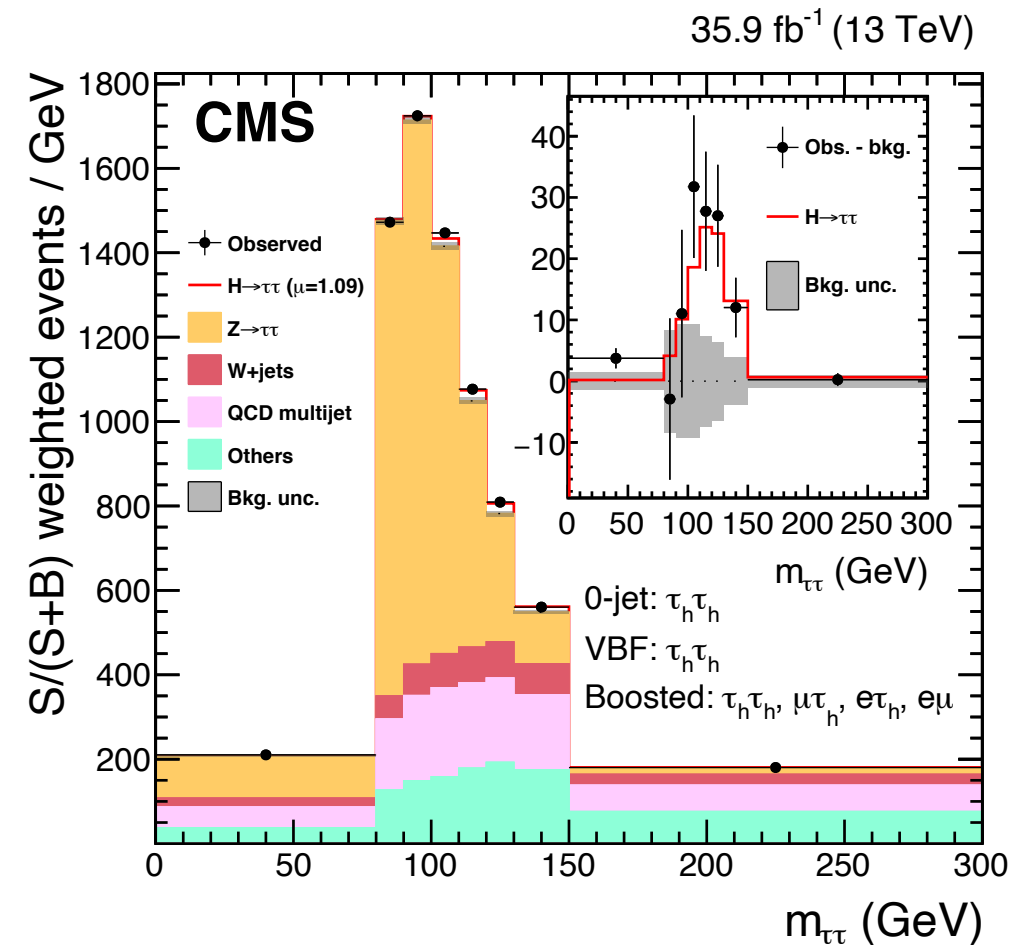
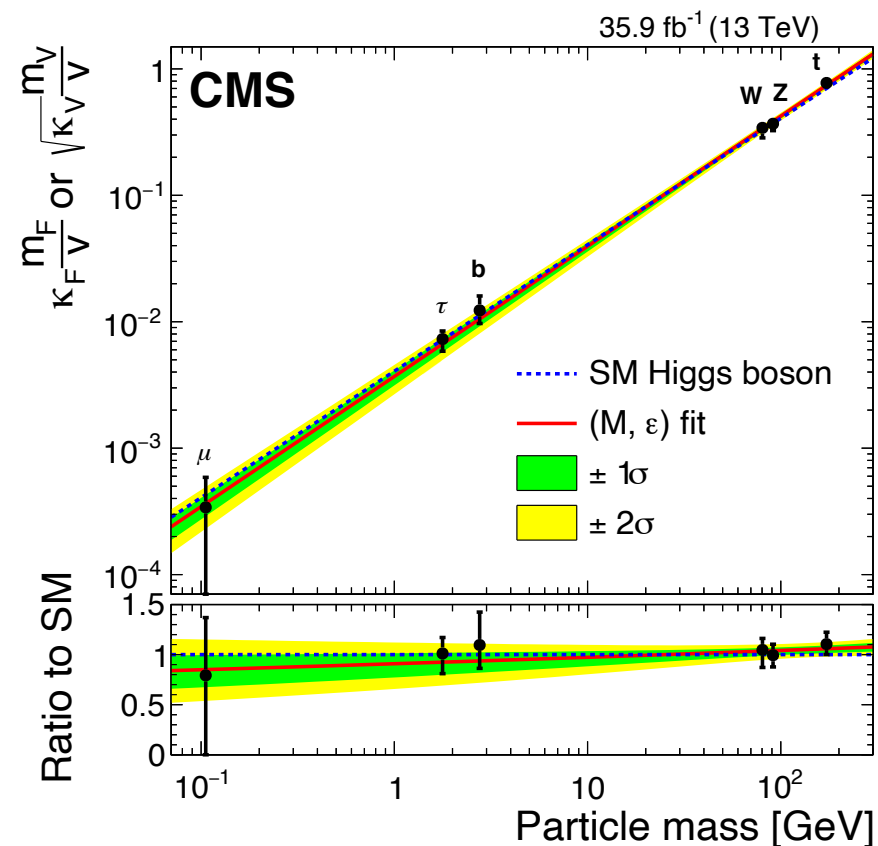
Daniel Winterbottom

d.winterbottom15@imperial.ac.uk

- A brief history of $H \rightarrow \tau\tau$ + motivations
- Common components to $H \rightarrow \tau\tau$ analyses
- Measurements of cross sections and couplings
- Measurement of the Higgs CP properties
- Conclusions

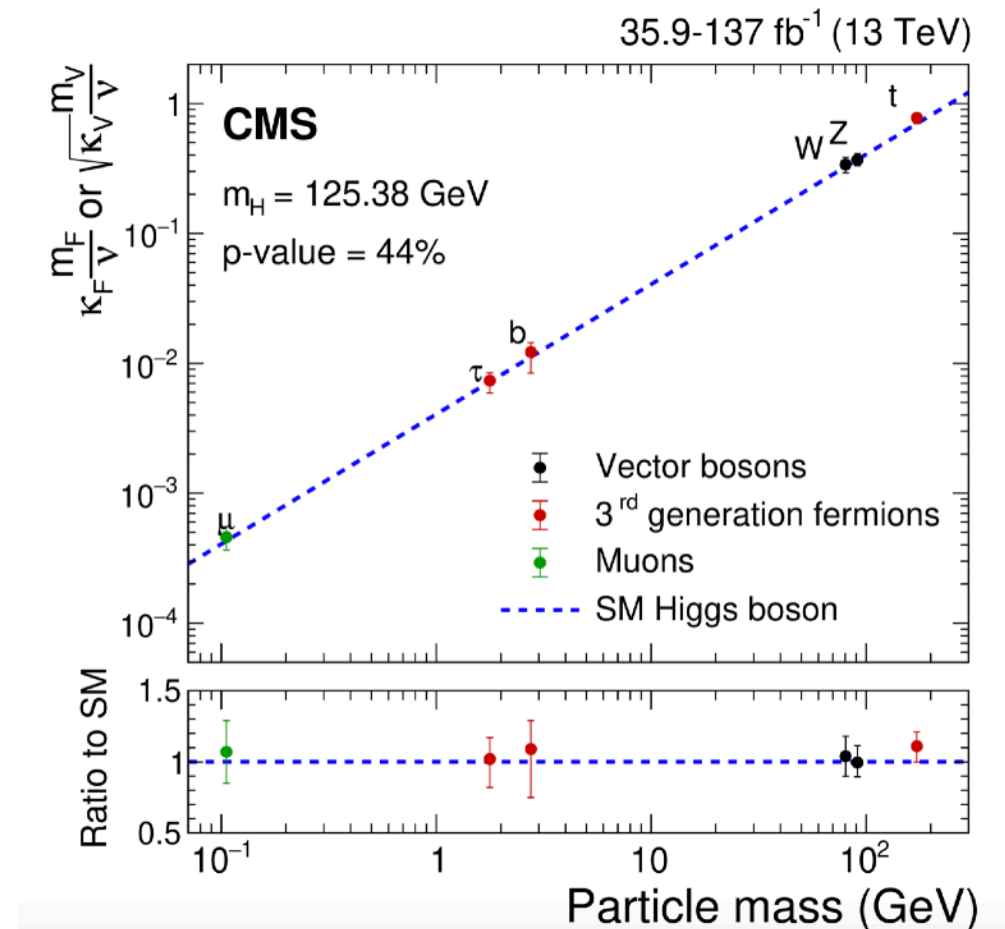
A brief history of $H \rightarrow \tau\tau$ in CMS

- 2012: Discovery of the Higgs Boson
- 2016: Observation of the $H \rightarrow \tau\tau$ process
- 2018: Combined CMS coupling measurement extracting y_τ coupling



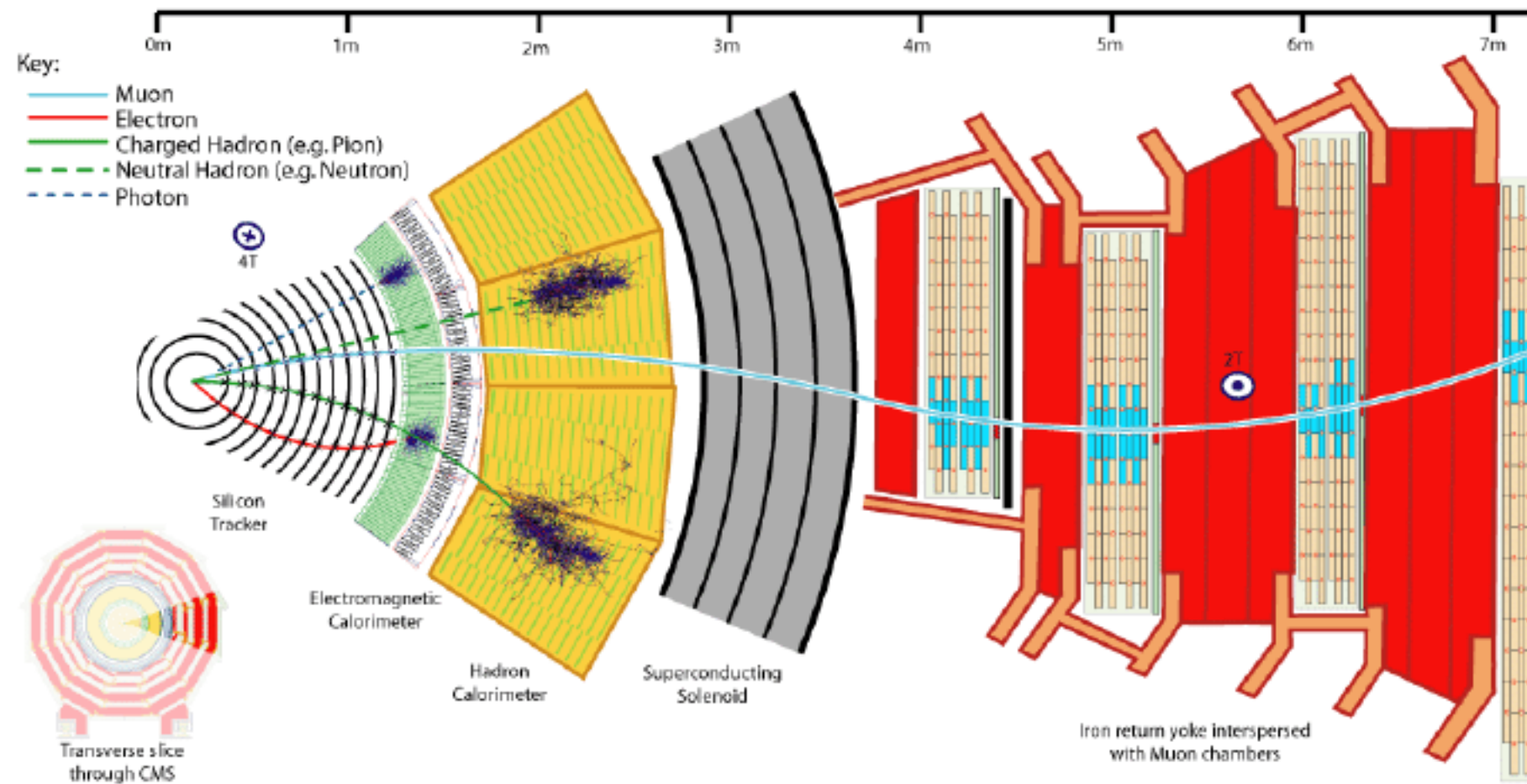
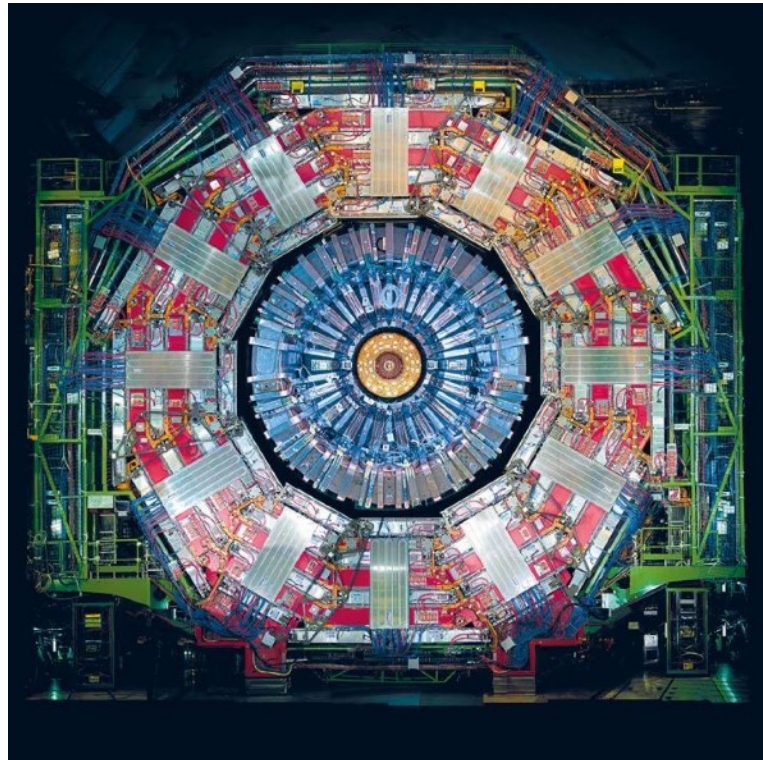
Motivations for $H \rightarrow \tau\tau$ measurements

- Since observation real shift in focus from “search-mode” to “precision-mode”
- We want to measure cross-sections, couplings, and properties precisely
- We have also started to perform differential measurements
 - Highly motivated as we can expect BSM effects to show up predominantly in certain regions of the phase space - e.g boosted events
- For property measurements $H \rightarrow \tau\tau$ decays can be used to determine Higgs CP state



The CMS experiment

- LHC delivered proton-proton collisions at C.O.M energy = 13 TeV between 2015-2018
- CMS recorded 137/fb of collision data between 2016-2018 (so called Run 2)



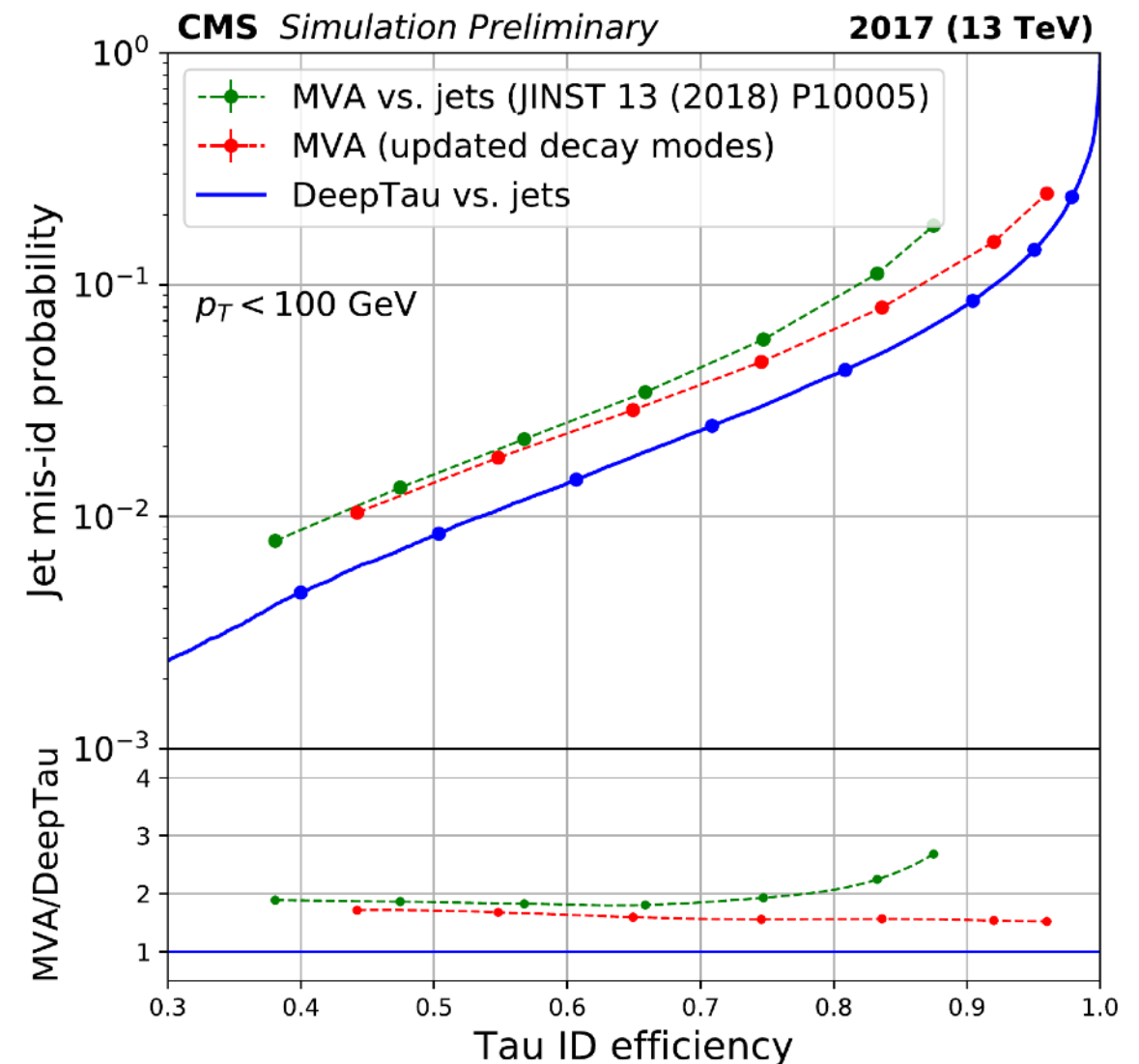
Common components to $H \rightarrow \tau\tau$ analyses

Challenges with the $H \rightarrow \tau\tau$ channel

- Tau leptons are unstable, they decay very close to the primary interaction point in the beam pipe to leptons or hadrons + neutrinos
 - $\tau \rightarrow \mu\nu\nu / e\nu\nu \sim 35\%$
 - $\tau \rightarrow N \times h^- + M \times \pi^0 + \nu$ [$N = 1, 3, \dots$; $M \geq 0$] $\sim 65\%$
 - Neutrinos are undetectable but can partially reconstruct them due to transverse momentum imbalance (MET)
 - In order to maximise selection efficiencies we need to consider as many tau decay modes as possible - both leptonic and hadronic decays!
 - Hadronic decays (τ_h) are not as distinct as electrons/muons, we need to avoid being overwhelmed with $j \rightarrow \tau_h$ fakes from multijet QCD events
- Significant backgrounds due to several processes: e.g Drell-Yan, QCD
 - Shapes are complicated so require template fitting
 - Associated systematic uncertainties with MC simulations can be large - need to reduce these
 - Statistical populations of templates can be problematic
- Due to MET we cannot reconstruct H system fully \rightarrow need to improve mass resolution

Tau reconstruction and identification

- Leptonically decaying taus reconstructed with standard CMS electron / muon identification
- Hadronic tau reconstruction based on hadron plus strips algorithm (HPS)
 - Charged PF candidates = hadrons
 - Strips = rectangular clusters of e/ γ 's aiming to reconstruct π^0 's
- After reconstruction we want to perform tau identification to reduce background from jet and lepton fakes
- State of the art tau ID in CMS uses deep neural networks including a mix of low level information (PF candidates), and high level variables sensitive to properties such as tau lifetimes, isolation, intermediate resonances etc
- Significant improvement over previous tau ID using BDTs
- More details on Deeptau in [CMS-DP-2019-033](#)

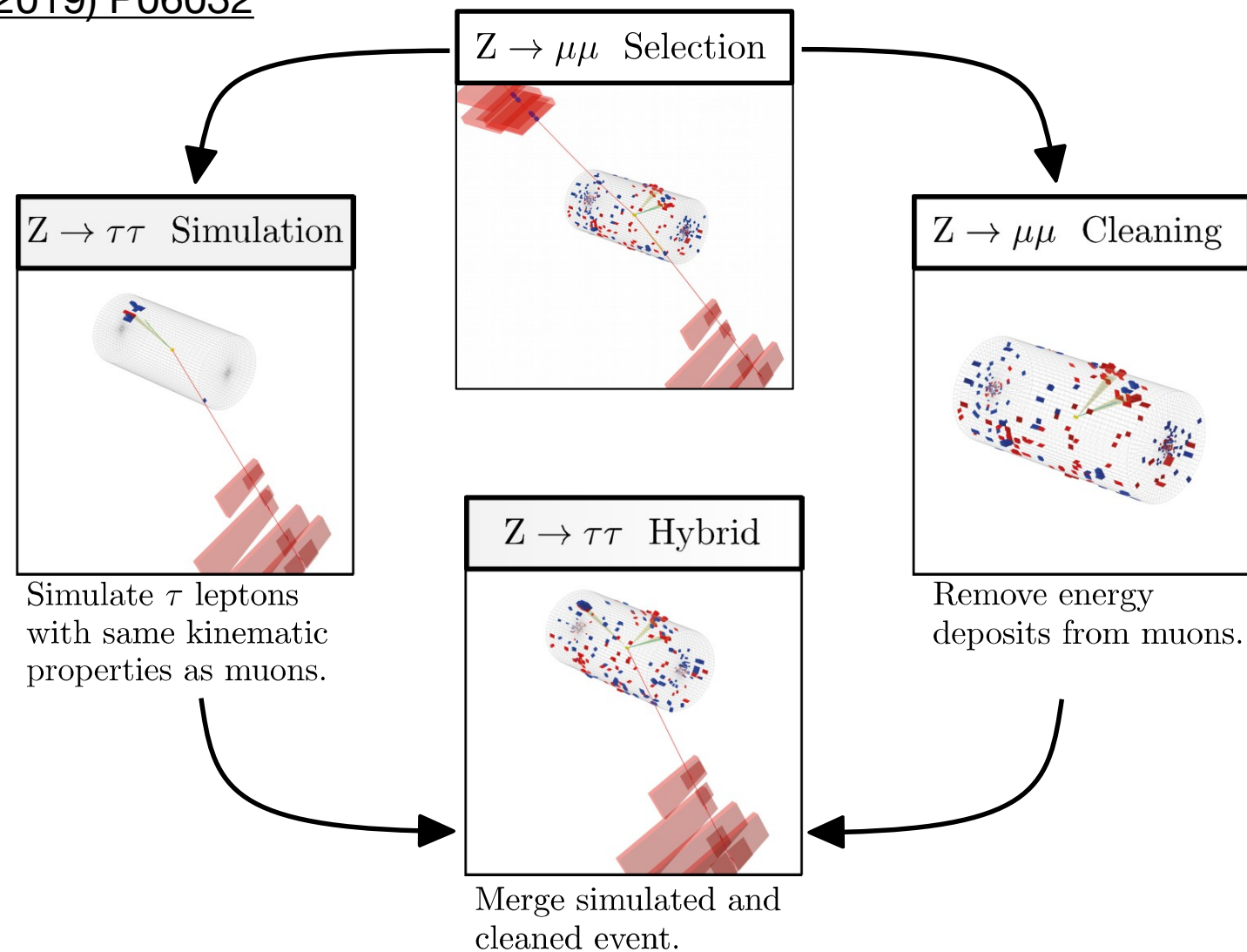


Background modelling

- Two largest contributions to background are $Z \rightarrow \tau\tau$ and jets faking hadronic taus ($j \rightarrow \tau_h$)
- We use data-driven method to estimate these processes
- This has advantaged such as reduced systematic uncertainties
 - For example objects such as jets can come directly from data so we aren't sensitive to data vs simulation differences in jet energy scale / resolution
- Statistics can be very large compared to MC simulations so help reduce statistical uncertainties considerably

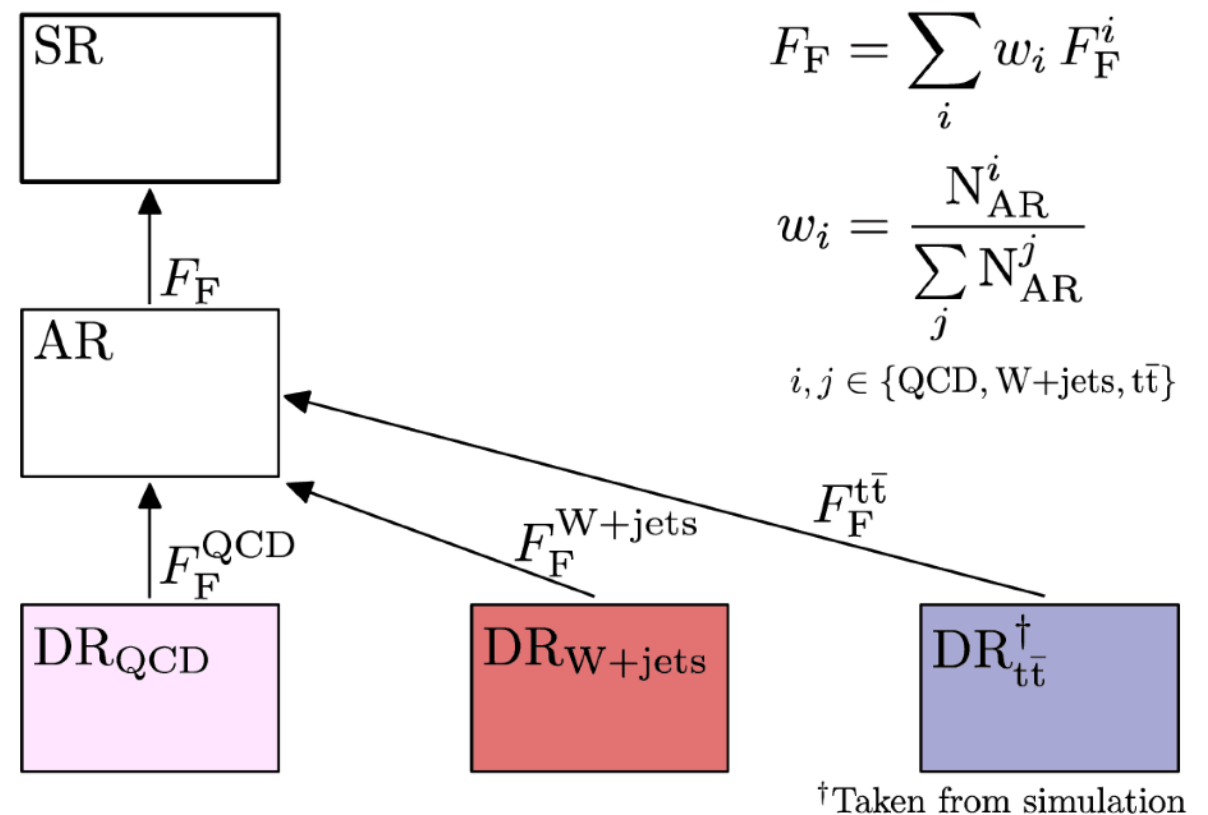
The embedding method

- Used to estimate backgrounds with real di-tau pairs - mainly $Z \rightarrow \tau\tau$
- Method exploits lepton universality in Z decays
- Replace muons selected in data with simulated tau leptons
- Bulk of events content (e.g jets, PU, UE, ...) comes directly from data so described perfectly
- Full details in [JINST 14 \(2019\) P06032](#)



The fake factor method

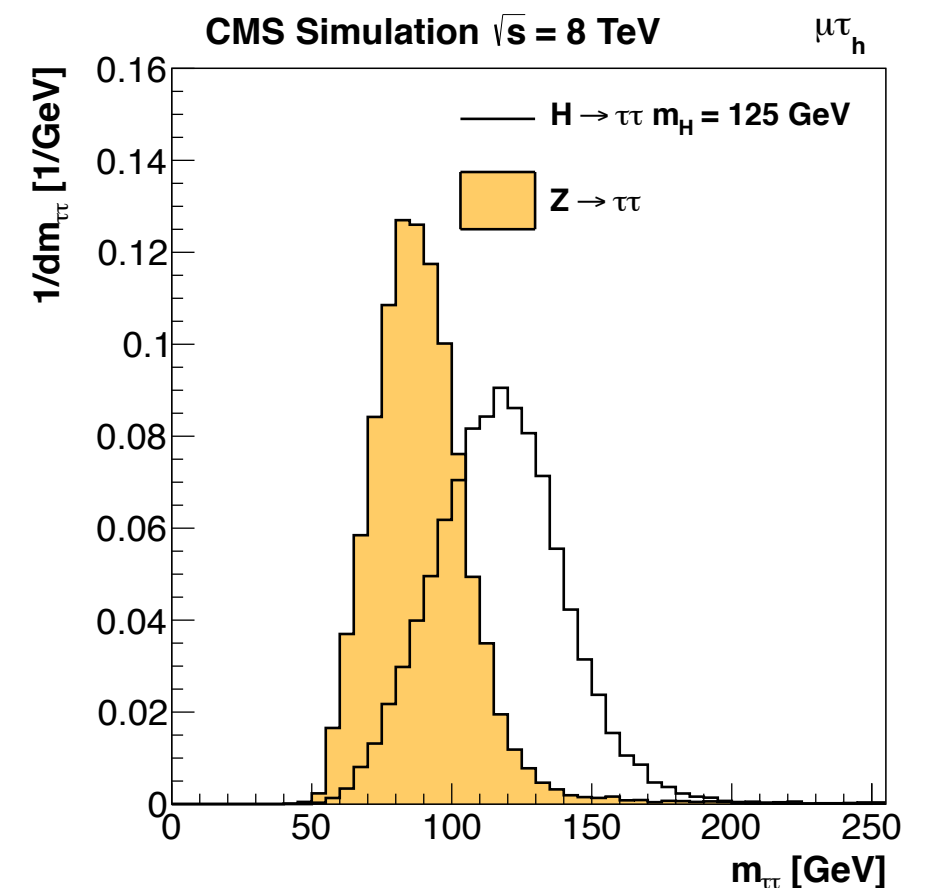
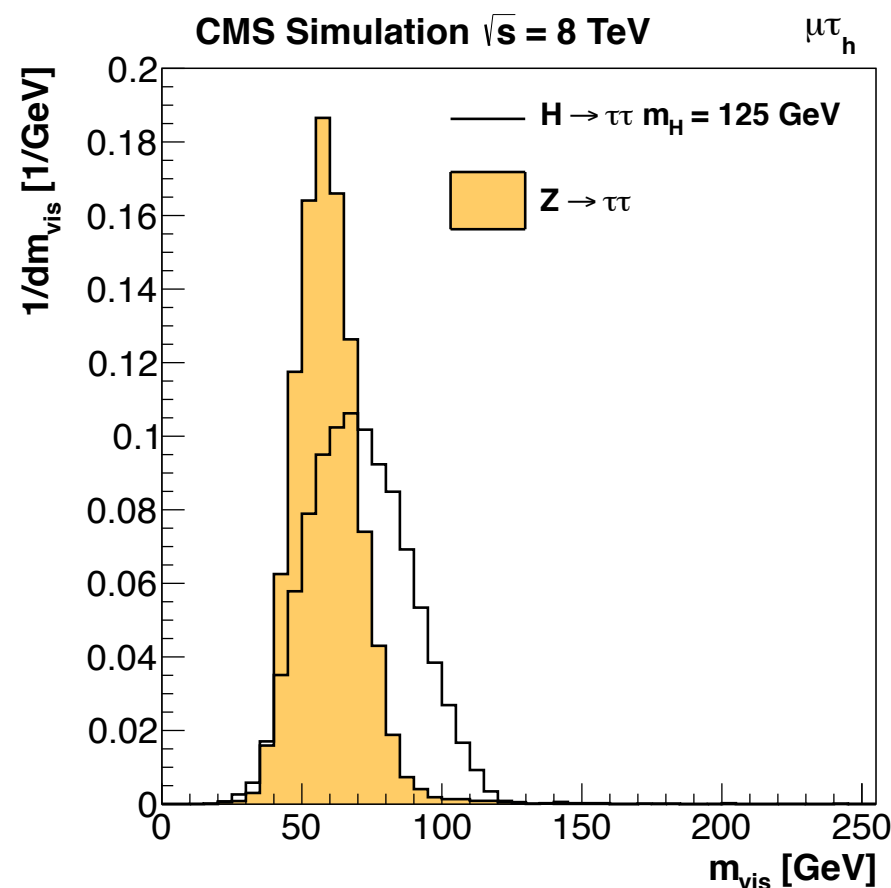
- The “fake factor” method is used to estimate all background with jets faking hadronic taus ($j \rightarrow \tau_h$)
- We select events in a sideband region failing nominal tau ID requirements but passing a relaxed selection
- Scale events by ratios:
 $FF = (\text{nominal ID}) / (\text{relaxed ID})$
 which we call fake factors
- Dominant processes are:
 QCD and W+jets



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Mass estimates: the SVFit algorithm

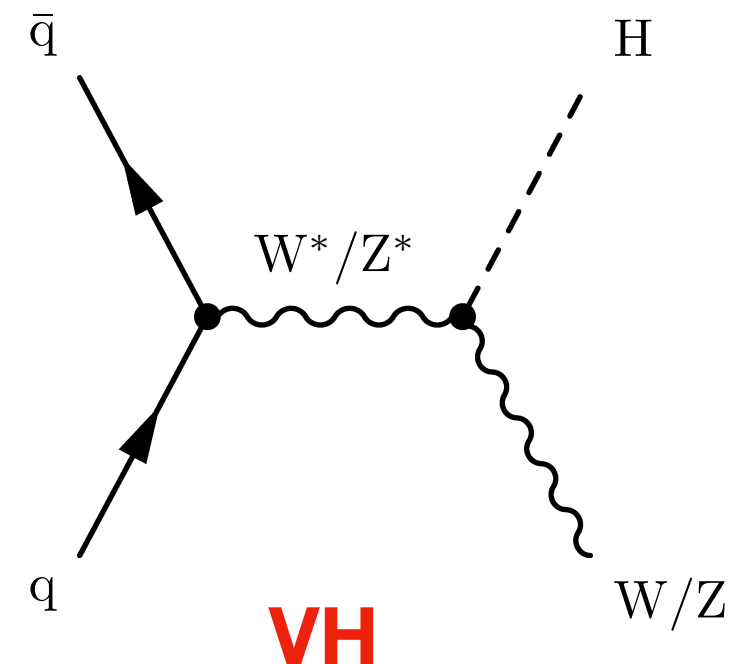
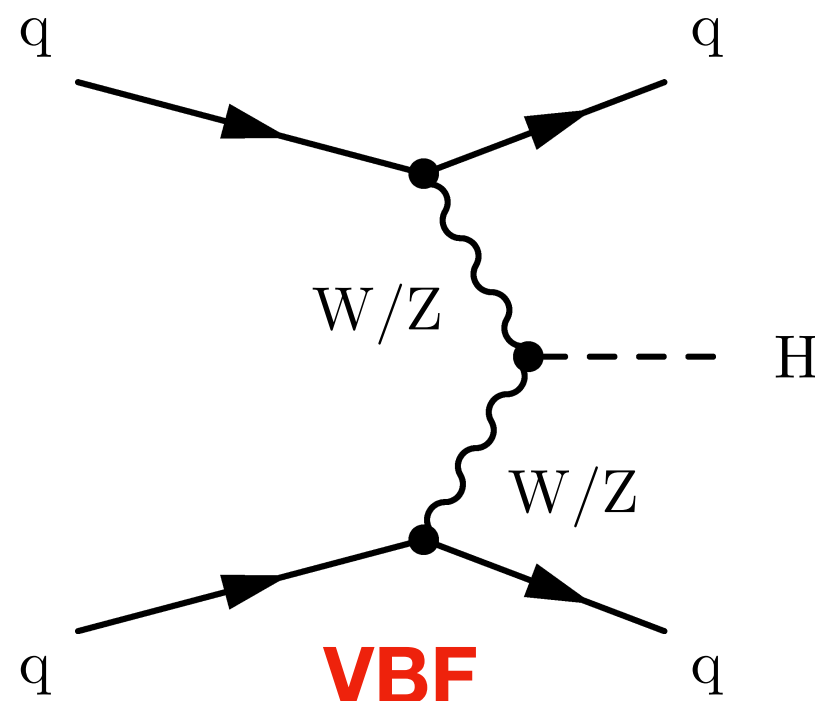
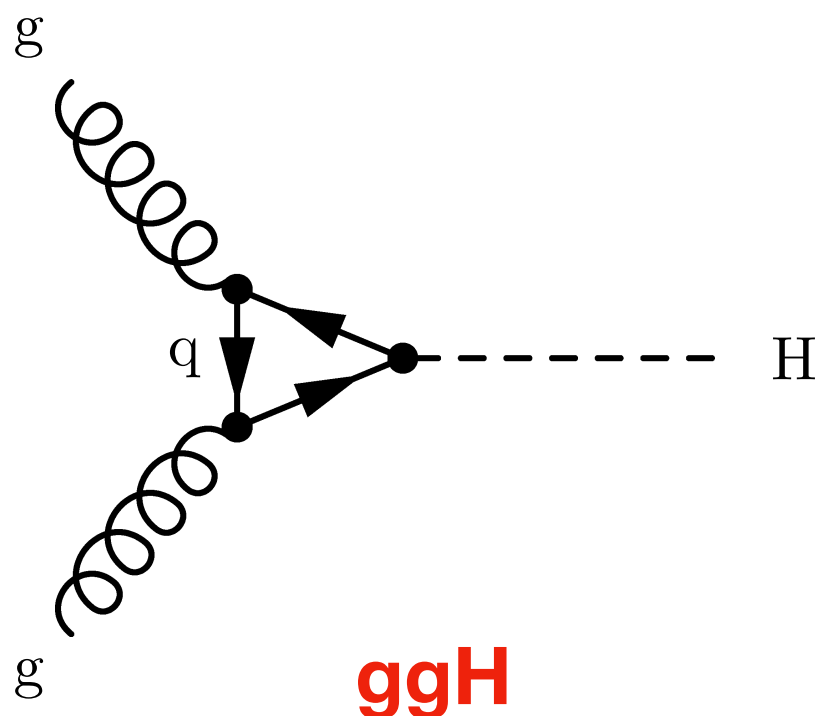
- The SV-Fit algorithm is a simplified matrix element method that combines the missing transverse momentum vector + corresponding uncertainties with the 4-vectors of the visible decay products to calculate the parent boson mass,
- Gives a significant improvement over using only the visible 4-vectors (m_{vis})



Cross section and STXS measurements

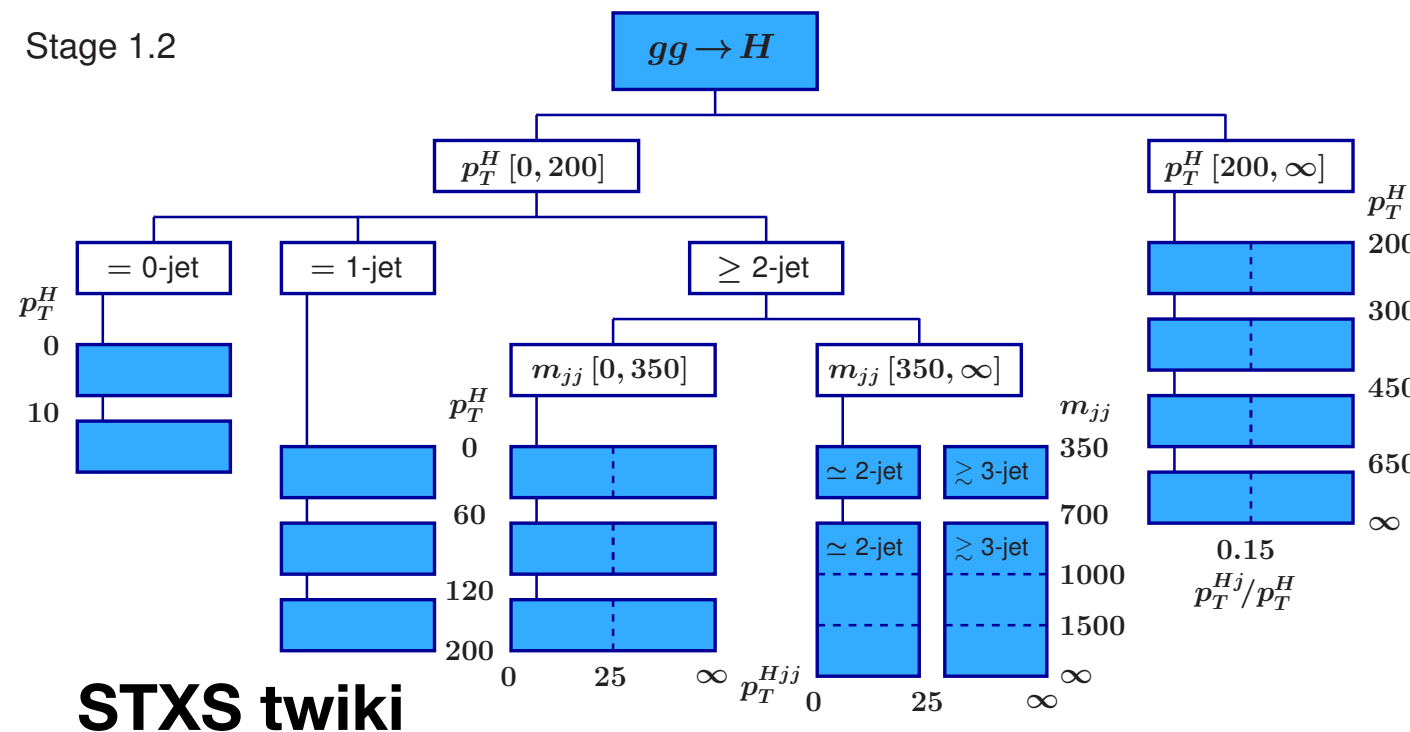
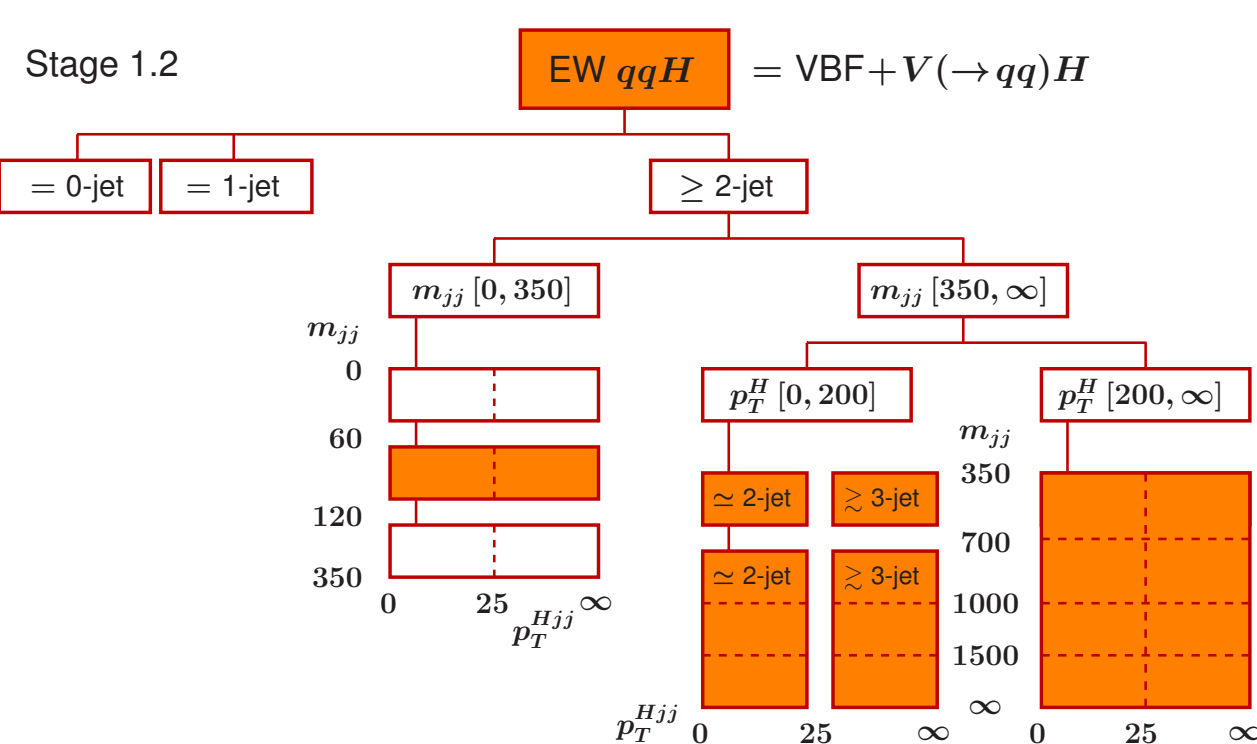
Considered signal productions

- The analysis targets mainly the gluon fusion (ggH) and vector boson fusion (VBF) processes, and pick up a smaller amount of the VH production with $V \rightarrow \text{hadron}$ decays
- We have separate dedicated analyses to target other production modes: ttH and VH ($V \rightarrow \text{leptons}$)
- Largest cross section ggH (48 pb), then VBF (4 pb), then VH (2 pb)
- Although ggH is largest other production modes have additional jet topologies that make them more distinct from backgrounds
 - e.g VBF we get 2 additional jets in the forward detector regions, tend to be well separated in η and have large invariant mass
 - The result is $H \rightarrow \tau\tau$ tends to be \sim equally sensitive to ggH and VBF production



STXS overview

- In Run 2 there has been a move towards differential Higgs measurements
- The Simplified Template Cross Section (STXS) scheme is an example of framework for such measurements, its aims are to :
 - Provide granular measurements for individual Higgs production modes
 - Reduce theoretical uncertainties that are directly folded into the measurements



Event selections

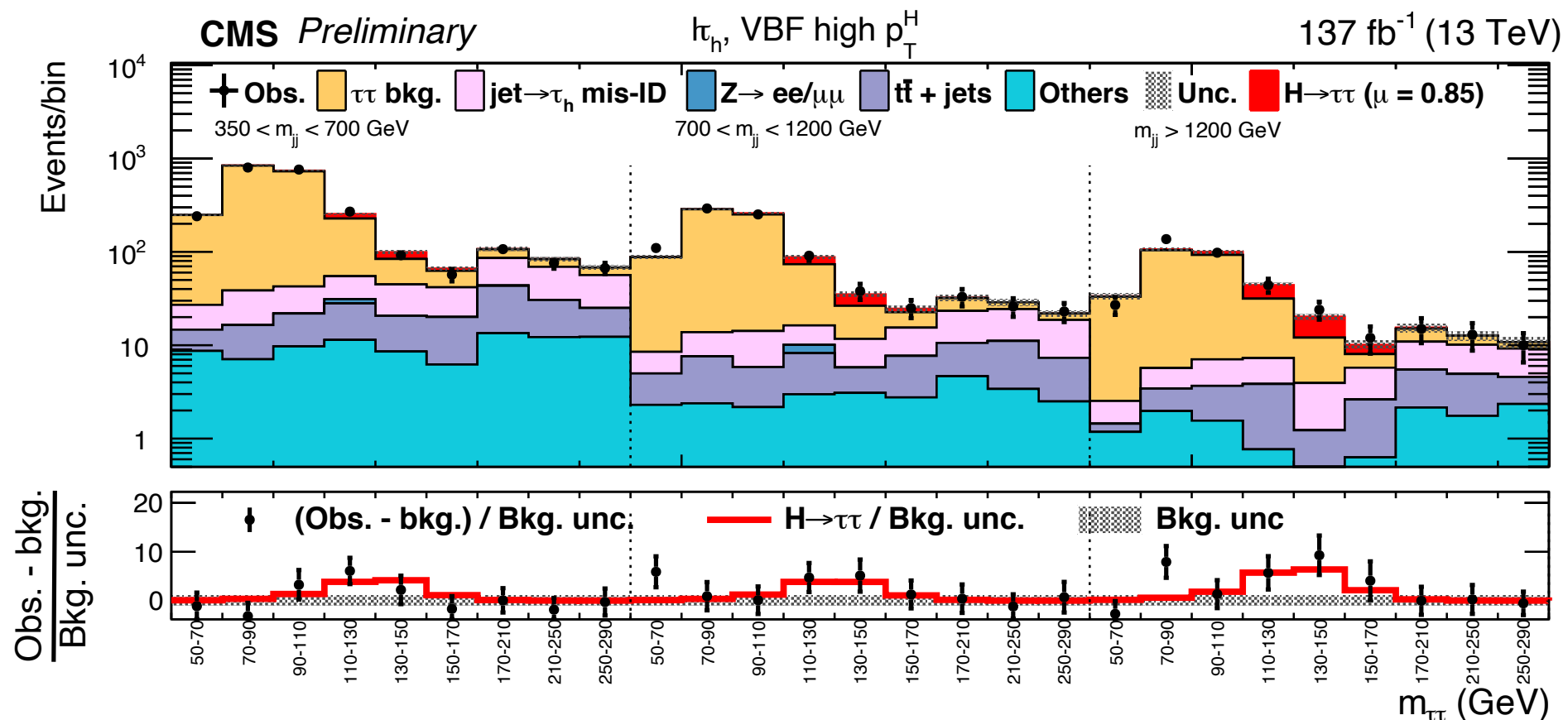
- We select oppositely charged pairs of hadronic taus (τ_h), electrons (e), and muons (μ)
- Events grouped into channels depending on pairs
 - We use only the 4 most sensitive channels: $\tau_h\tau_h$, $e\tau_h$, $\mu\tau_h$, and $e\mu$
- Electron, muons, and taus are required to pass ID discriminants and be isolated
- We apply additional vetos on events with additional leptons and bjets to reduce background such a Drell-Yan and $t\bar{t}$
- In the semi-leptonic channels we also require the transverse mass of the lepton+MET system to be < 50 GeV to reduce the W +jets background

Event categorisation

- We first split events into 3 categories to target different production processes:
 - 0-jet: No jets with $p_T > 30$ GeV - targets mainly ggH
 - VBF: 2 or more jets with $m_{jj} > 300$ GeV ($|\Delta\eta|_{jj} > 2.5$ and $p_T^H > 100$ GeV) for the $e\tau_h$, $\mu\tau_h$, and $e\mu$ ($\tau_h\tau_h$) channels - targets VBF events
 - Boosted: 1-jets events or 2+ jets events failing VBF cuts - selects boosted ggH+j events, VH, and some VBF
- We then further categorise events based on p_T^H and N_{jets} and to align with STXS bin boundaries
 - VBF: split into two categories with $p_T^H > 200$ GeV and $p_T^H < 200$ GeV
 - Boosted: split into two categories with $N_{\text{jets}}=1$ and $N_{\text{jets}}>1$
- Gives 5 categories in total

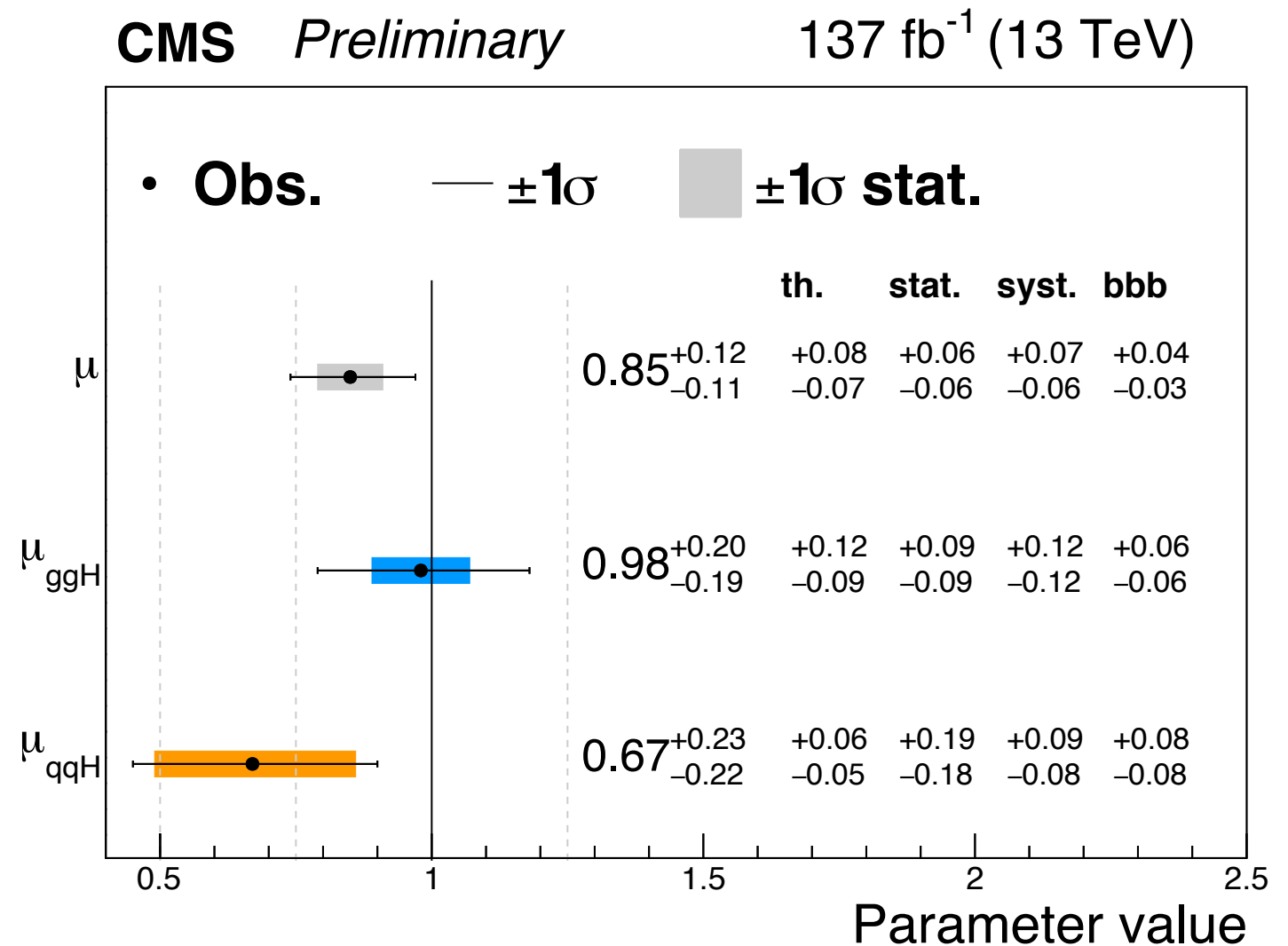
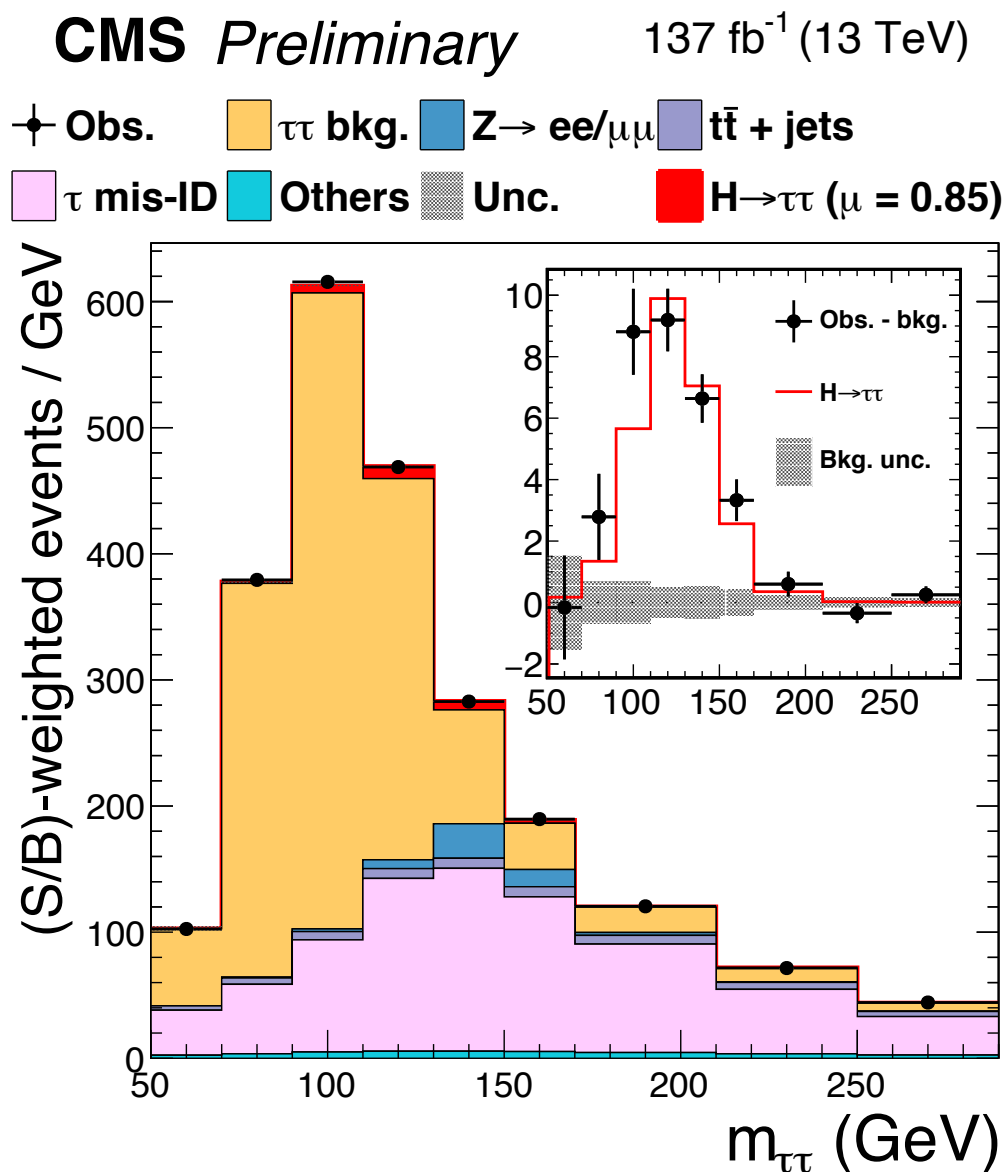
Signal extraction

- In each category a 2D (or 1D) distributions is built:
 - 0-jet: $m_{\tau\tau}$ vs p_T (2D) for $e\tau_h$, $\mu\tau_h$; $m_{\tau\tau}$ for $\tau_h\tau_h$ and $e\mu$ (1D)
 - Boosted: $m_{\tau\tau}$ vs p_T^H
 - VBF : $m_{\tau\tau}$ vs m_{jj}
- We perform a binned maximum likelihood fit combining all channels and categories to extract the results



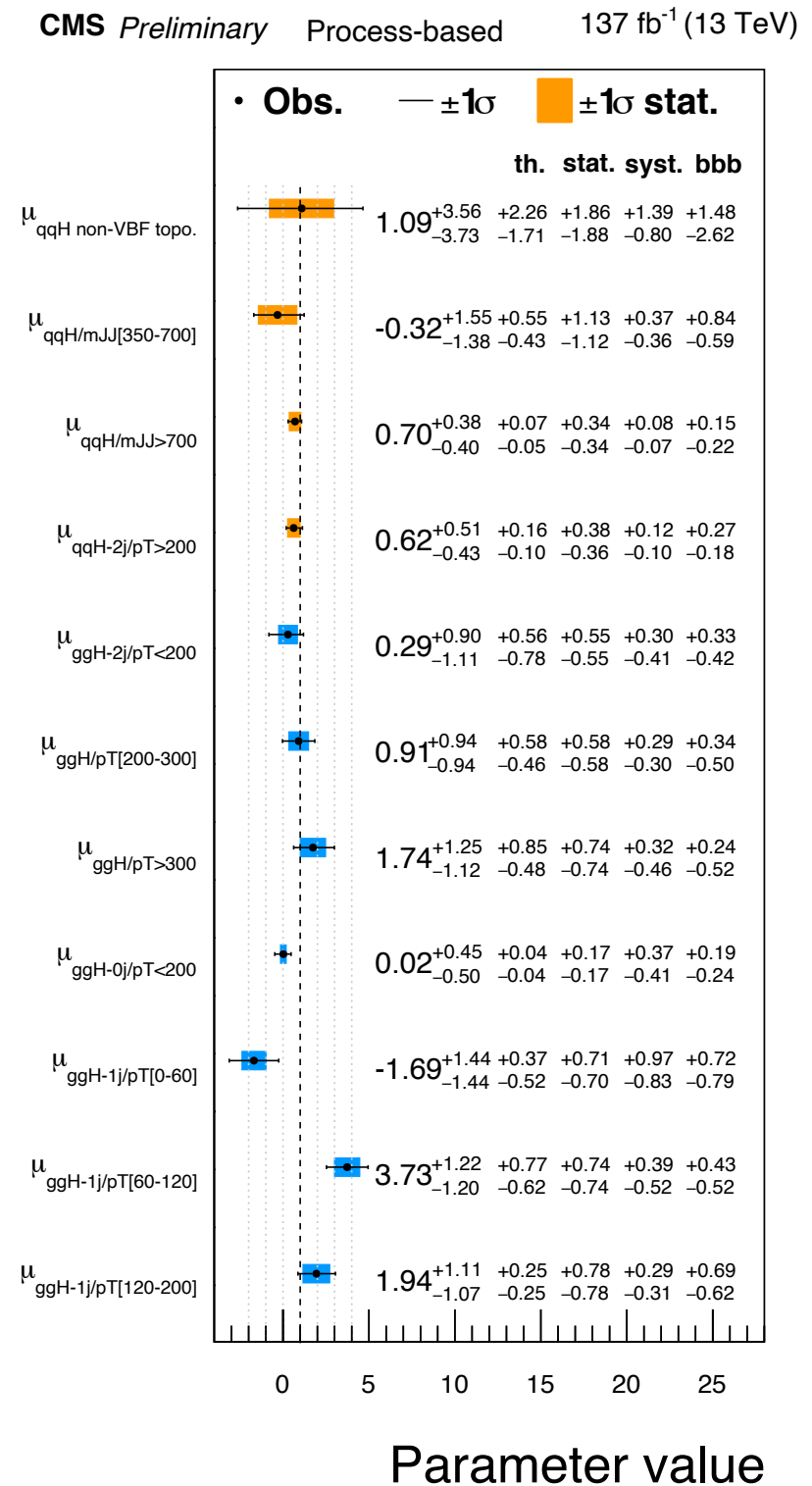
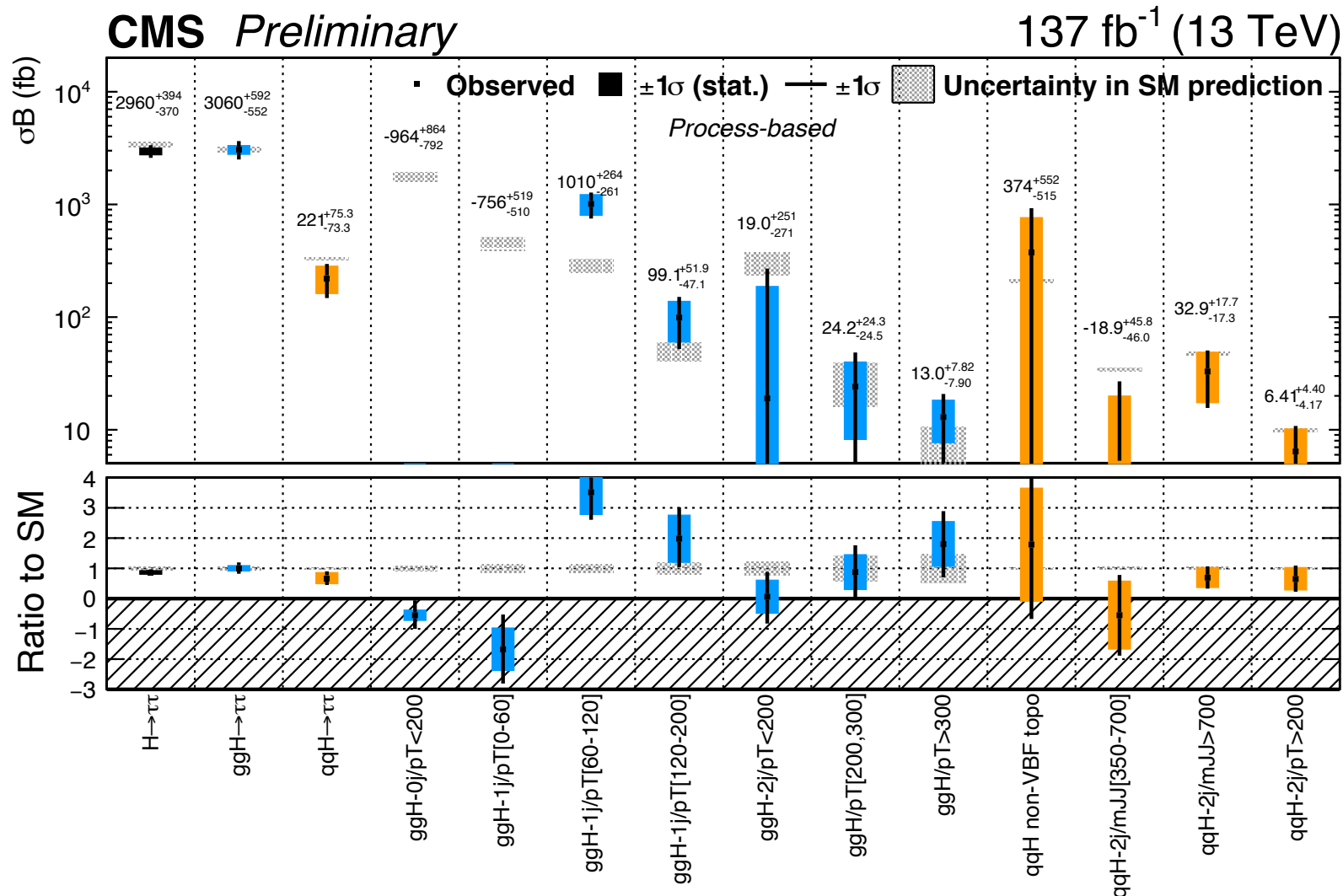
Results: inclusive cross sections

- Inclusive Higgs cross section measured (all production modes collectively)
- ggH and qqH (VBF+VH) cross sections also measured separately



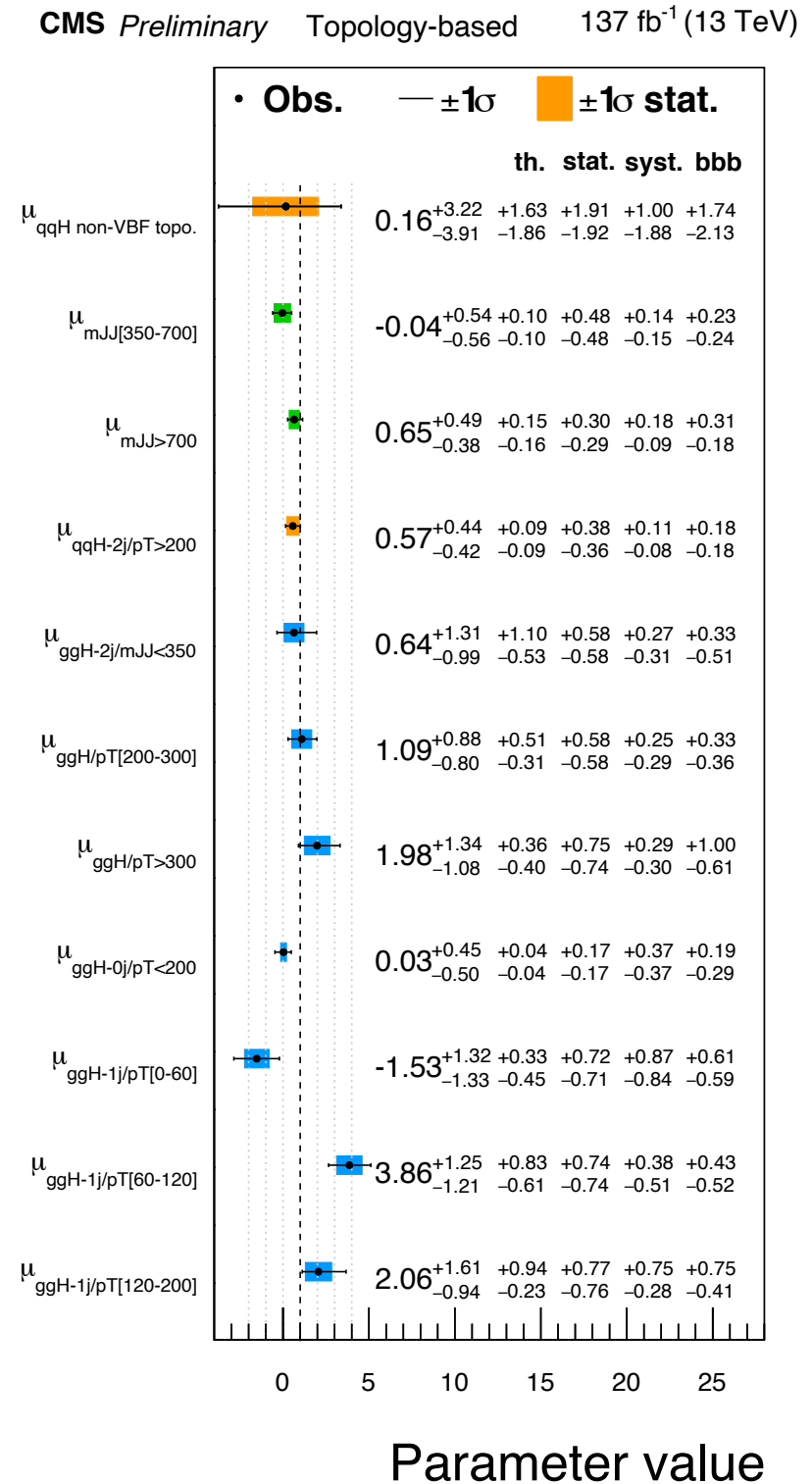
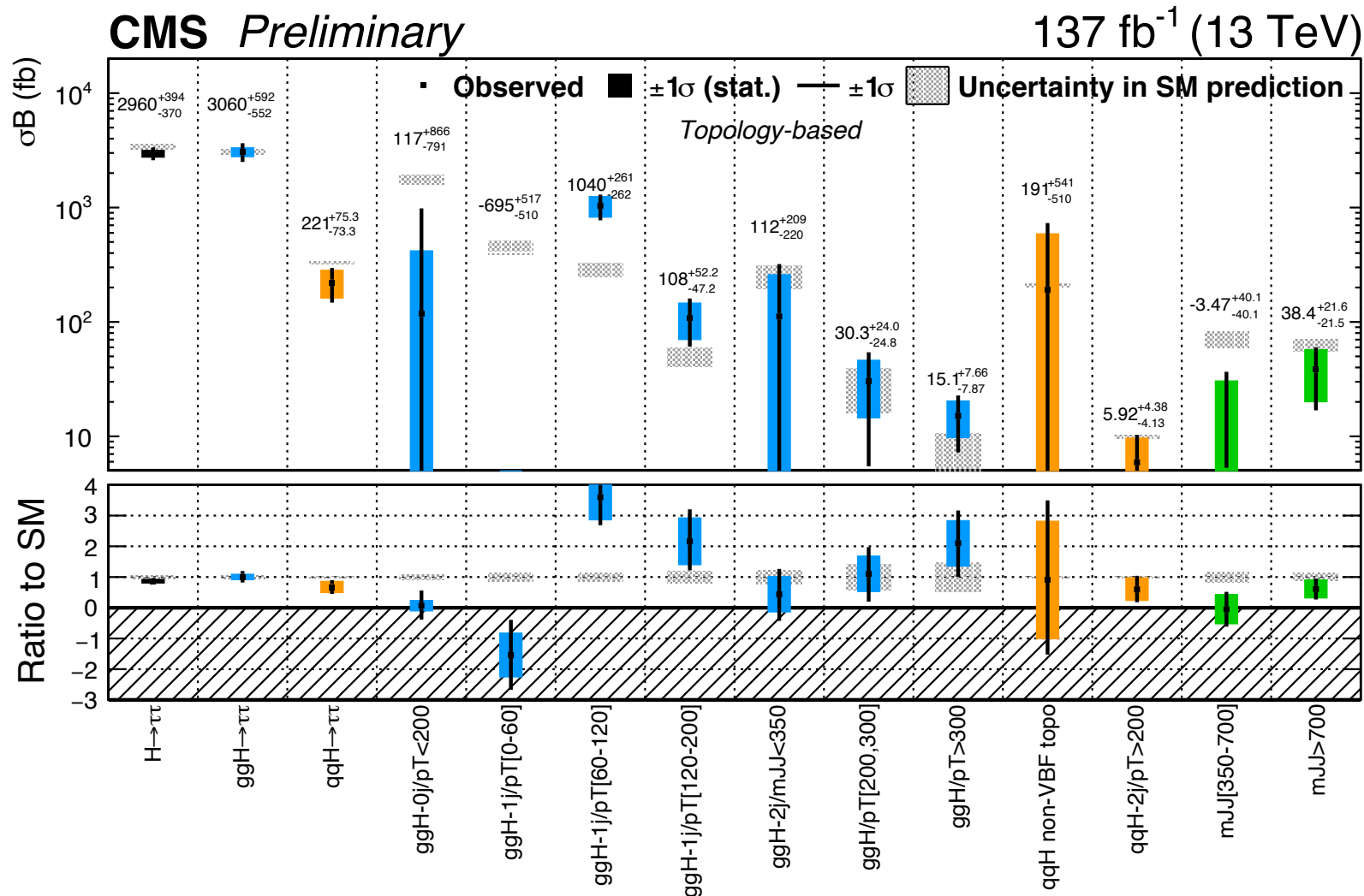
Results: STXS measurements (process based)

- The STXS results for **process based** merging scheme
- Some small tensions in low p_T bins but altogether compatible with the expectation



Results: STXS measurements (topology-based)

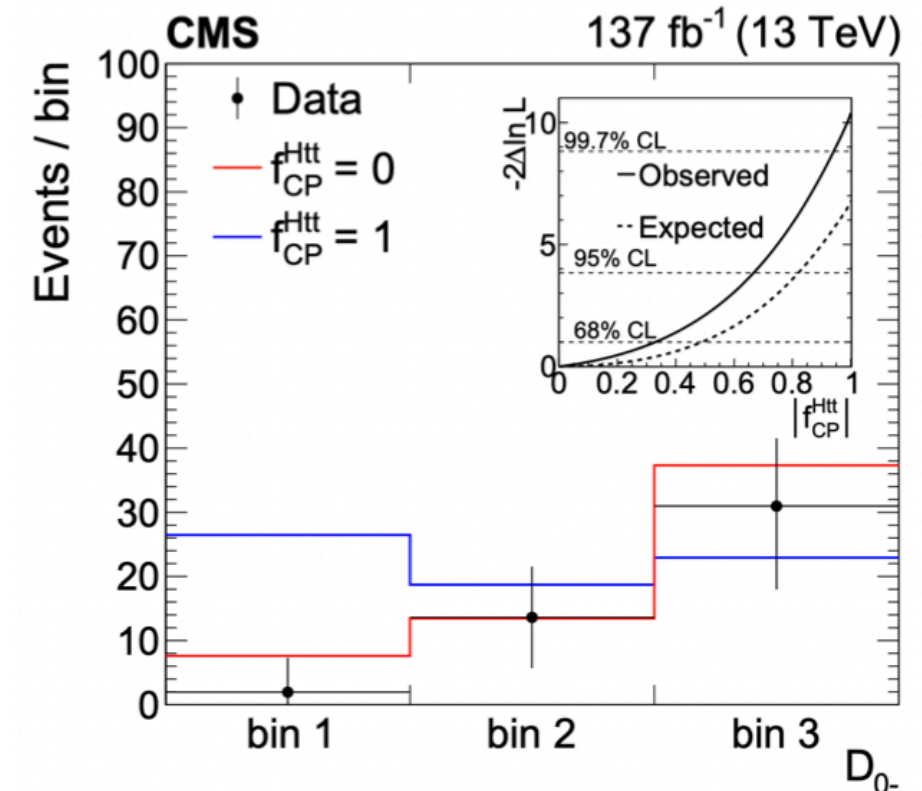
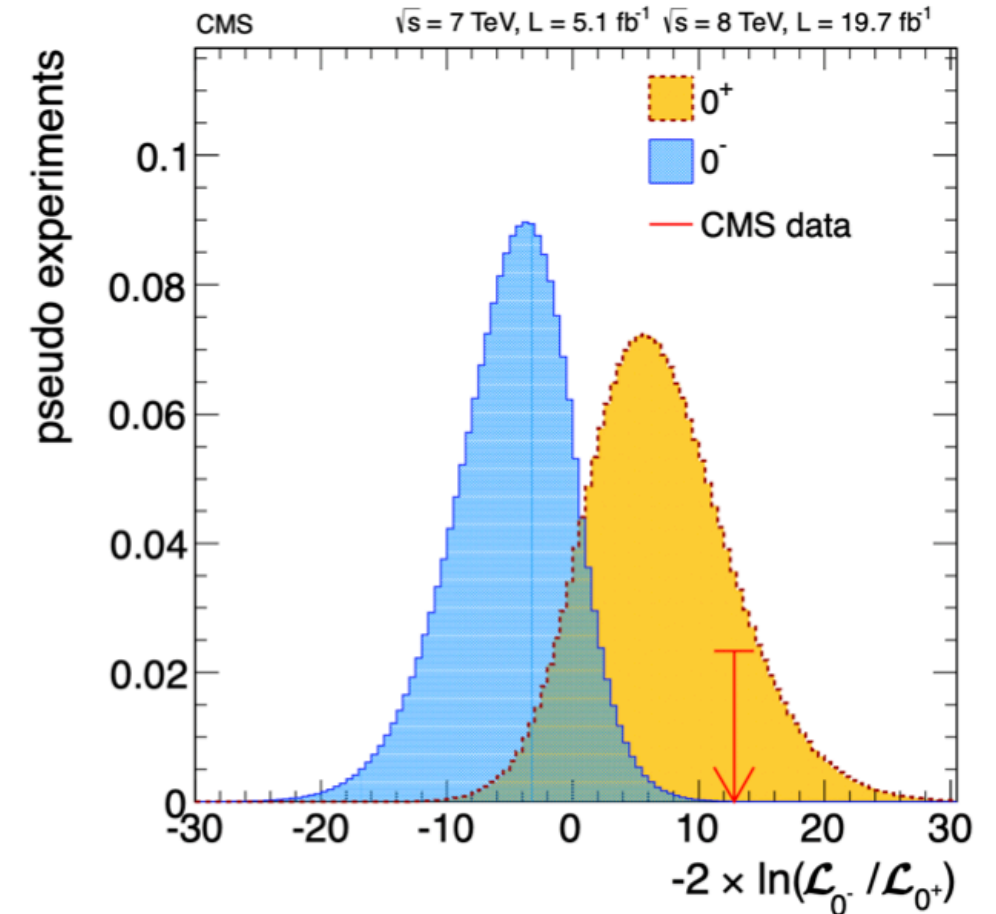
- The STXS results for **topology based** merging scheme
- Some small tensions in low p_T bins but altogether compatible with the expectation



CP measurements

Motivations for CP measurements

- In the SM Higgs sector Higgs bosons is a CP-even state (0^+)
- Extended Higgs sectors predict modified properties of the 125 GeV Higgs boson and/or new observable states in scalar sector
- Discovery of such a extended Higgs sector would be evidence for new physics beyond the standard model (BSM)
- One such class of extensions include additional CP phases in the Higgs sector
- Such models can help explain observed matter-antimatter asymmetry in the universe
- Higgs CP properties well measured in HVV couplings **but** CP-odd HVV coupling typically suppressed (no tree level coupling) \rightarrow current bounds actually quite weak
- $H \rightarrow ff$ couplings well motivated because CP-odd coupling at tree-level \rightarrow not suppressed like HVV!
- Measurements of H_{tt} CP-properties by CMS ([arXiv:2003.10866](https://arxiv.org/abs/2003.10866)) and ATLAS ([arXiv:2004.04545](https://arxiv.org/abs/2004.04545))
- In this talk: first measurement of $H \rightarrow \tau\tau$ CP-properties: results presented at ICHEP 2020 conference ([CMS-PAS-HIG-20-006](https://arxiv.org/abs/2006.00066))



- Parameterise Lagrangian in terms of **CP-even** and **CP-odd** Yukawa couplings:

$$\mathcal{L}_Y = -\frac{m_\tau}{v} (\kappa_\tau \bar{\tau}\tau + \tilde{\kappa}_\tau \bar{\tau} i \gamma_5 \tau) h \quad \kappa_i = y_i / y_i^{SM}$$

- Define mixing angle as:

$$\tan \phi_{\tau\tau} = \frac{\tilde{\kappa}_\tau}{\kappa_\tau}$$

- CP-even:** $\phi_{\tau\tau} = 0^\circ$, **CP-odd:** $\phi_{\tau\tau} = 90^\circ$, **CP-mixed:** $0^\circ < |\phi_{\tau\tau}| < 90^\circ$

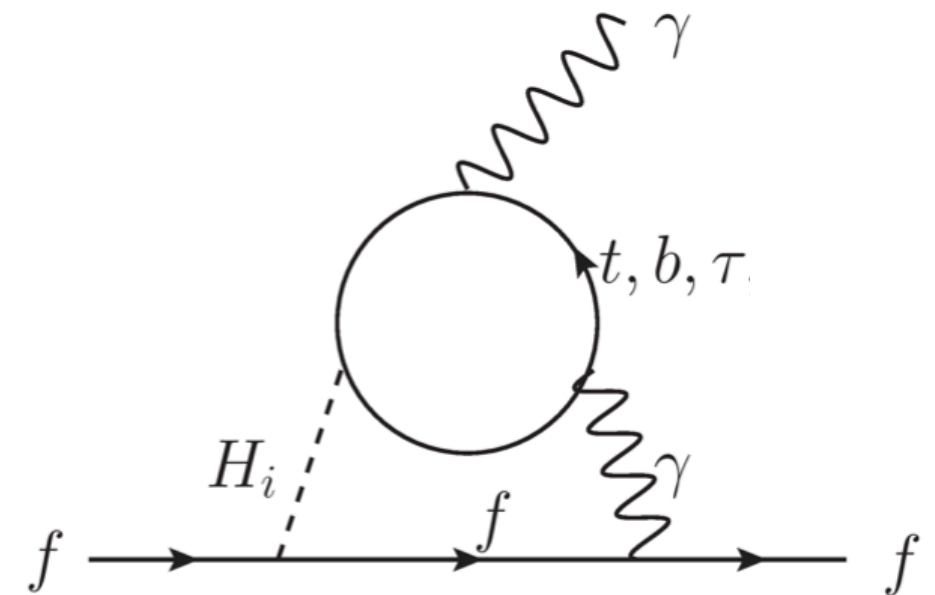
- Can write partial decay width as:

$$d\Gamma \sim 1 - s_z^- s_z^+ + \cos(2\phi_{\tau\tau}) (\mathbf{s}_T^- \cdot \mathbf{s}_T^+) + \sin(2\phi_{\tau\tau}) \left[(\mathbf{s}_T^- \times \mathbf{s}_T^+) \cdot \hat{k}^- \right]$$

- \mathbf{s} =spin \rightarrow transverse spin correlations sensitive to $\phi_{\tau\tau}$ S. Berge, et al.

Indirect measurements EDMs

- CP-violating Higgs couplings can lead to the generation of electric dipole moment (EDMs) from diagrams such as those shown right



- Measurements of EDMs can therefore allow indirect constraints to be set on $H \rightarrow \tau\tau$ CP properties

- Tightest bound come from electron EDM measurements:

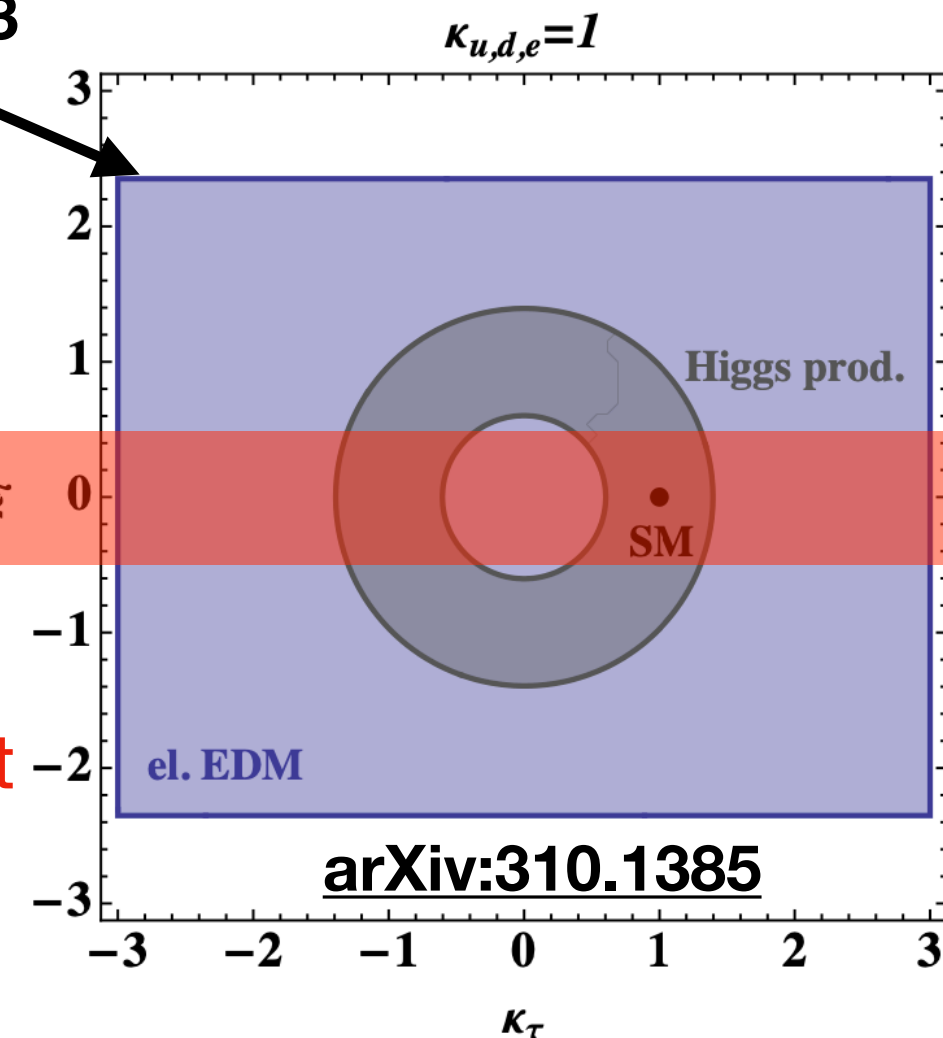
ACME, 2013

- $\sim 10^{-28}$ e cm (ACME Coll., 2013)

- $\sim 10^{-29}$ e cm (ACME Coll., 2018)

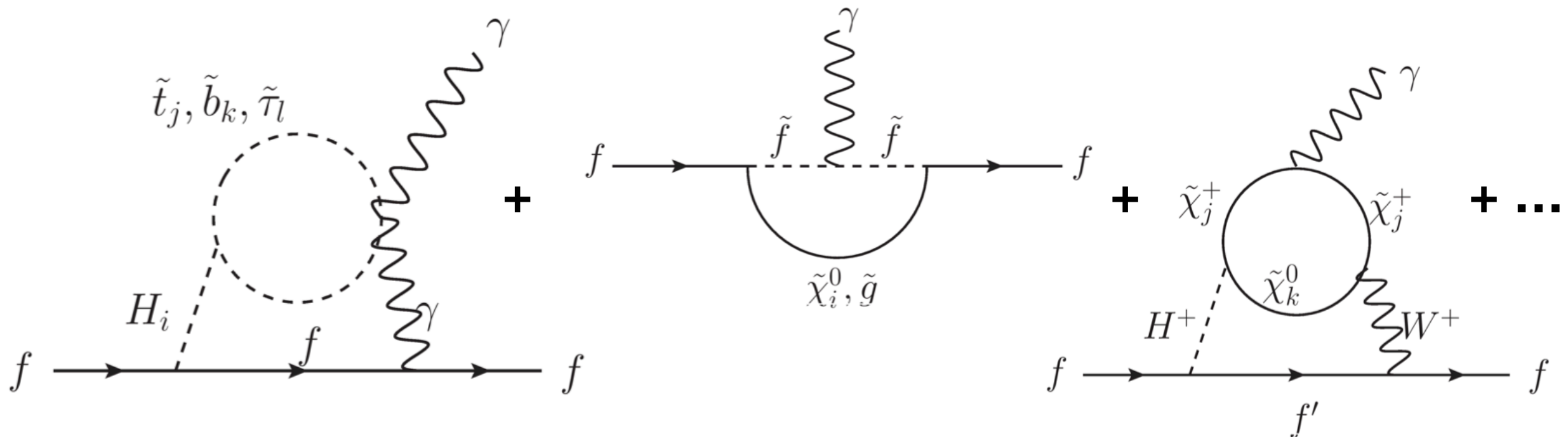
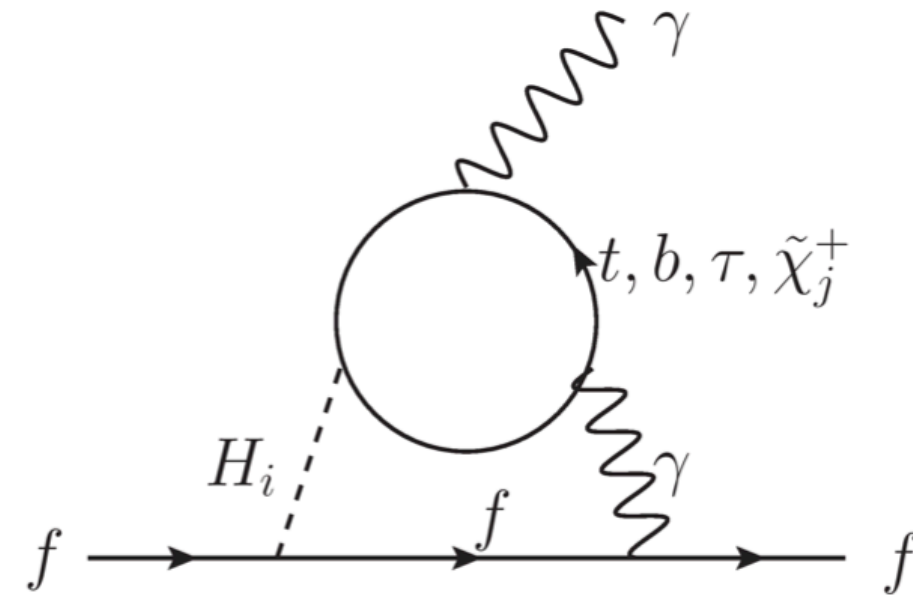
\sim ACME, 2018

- Note model dependent bounds show in the next slides use 2013 measurement so are actually tighter than what is shown



Indirect measurements EDMs

- **But** such constraints are model-dependent
 - Have to assume something about coupling of other particles to Higgs e.g $H \rightarrow ee$ coupling
 - For some models e.g SUSY get additional diagrams contributing - can change EDMs



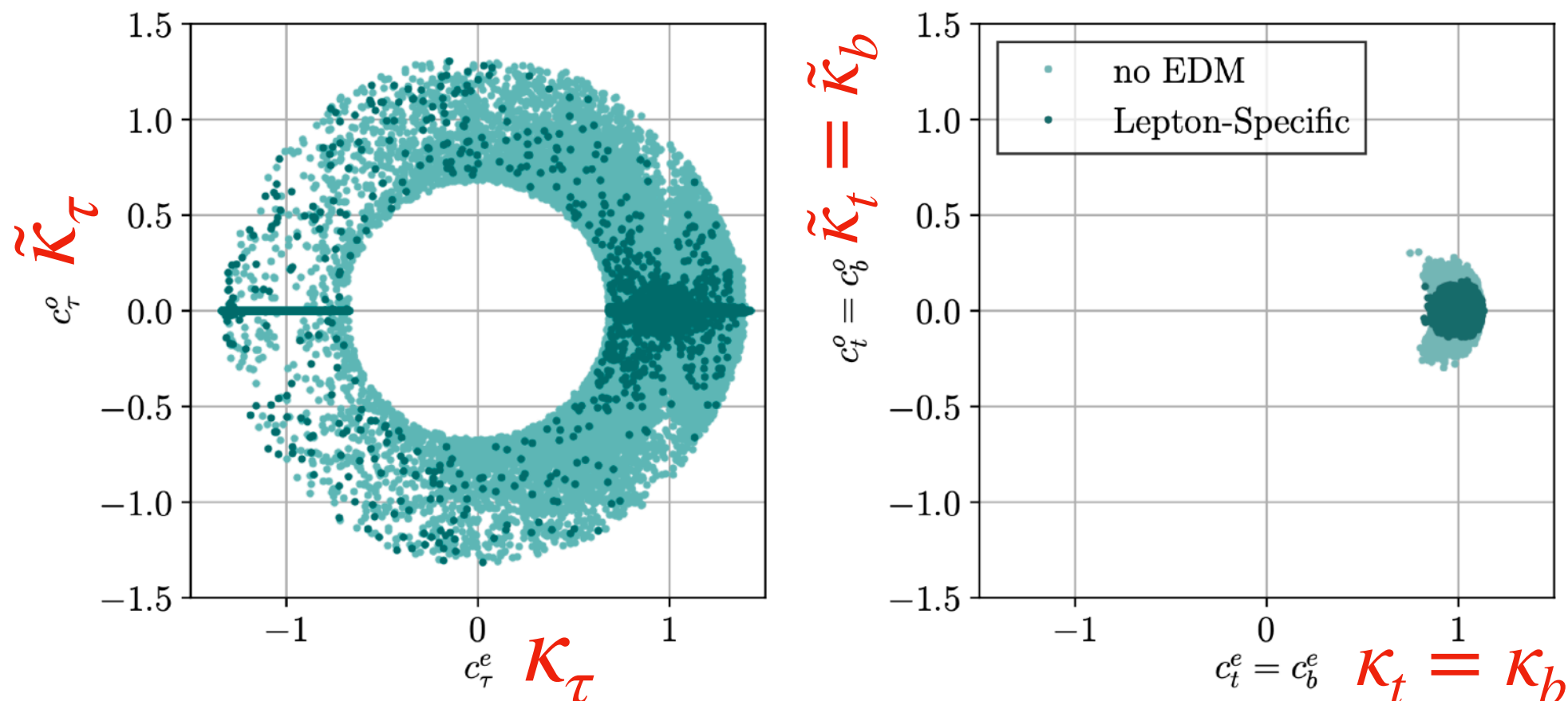
Two Higgs doublet models

- SM Higgs sector has one Higgs doublet
- Two Higgs doublet models (2HDM) introduce an additional Higgs doublet
- Results in 4 additional Higgs bosons: in CP-conserving case $h, H, A, H^\pm \rightarrow$ one of h, H is the 125 GeV boson
- Several different types of 2HDM possible depending on which doublet the fermions couple to, including (not not limited to):

	u-type	d-type	Leptons
Type 1	ϕ_2	ϕ_2	ϕ_2
Type 2	ϕ_2	ϕ_1	ϕ_1
Lepton-specific	ϕ_2	ϕ_2	ϕ_1
Flipped	ϕ_2	ϕ_1	ϕ_2
Type 3	ϕ_1, ϕ_2	ϕ_1, ϕ_2	ϕ_1, ϕ_2

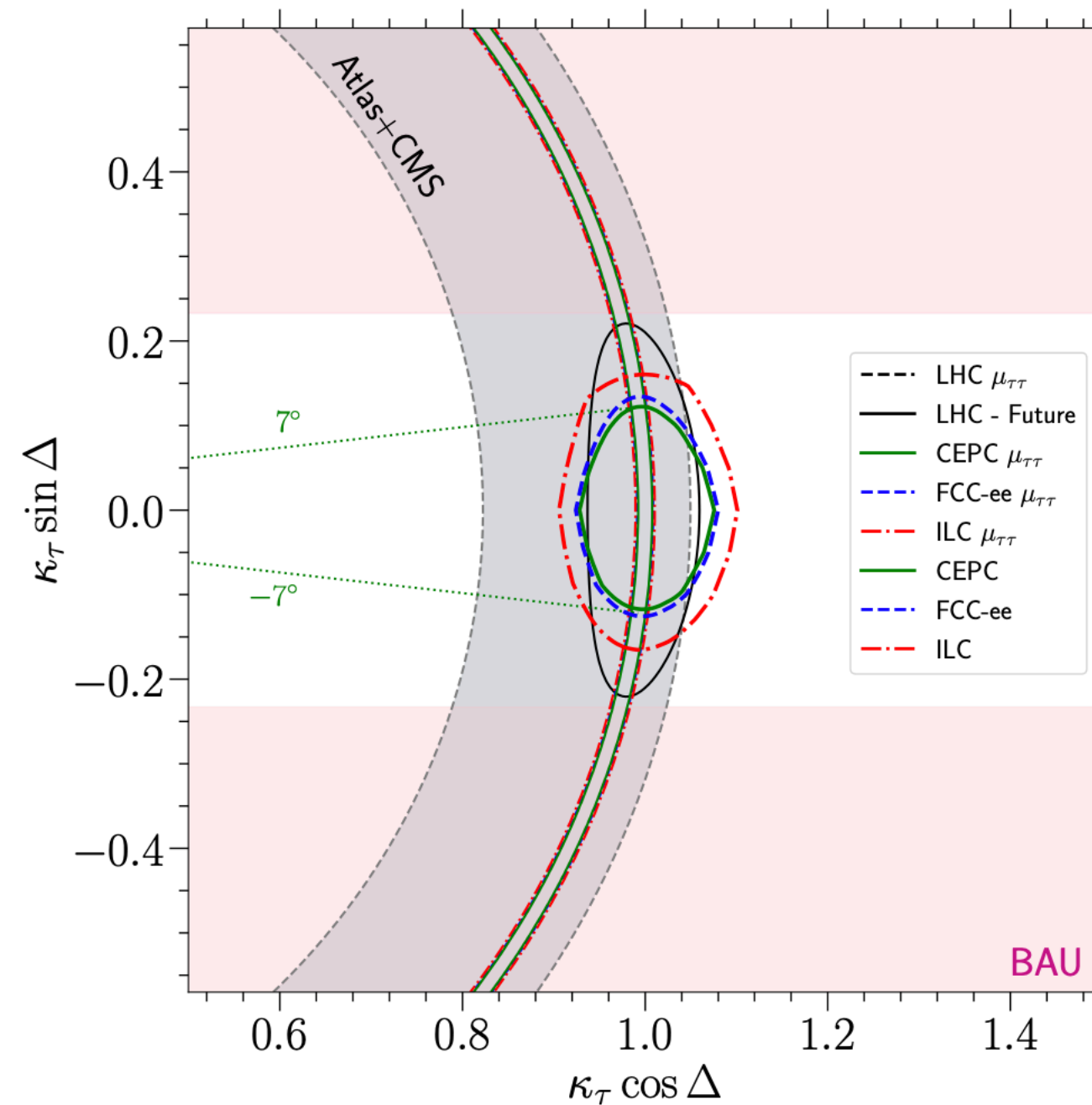
C2HDM

- 2HDM simplest extension that allows for CP-violation in Higgs sector - complex 2HDM (C2HDM)
- 4 additional Higgs bosons $H_1, H_2, H_3, H^\pm \rightarrow$ one of H_i is the 125 GeV boson
- In [JHEP 02 \(2018\)073](#) they show allowed points for various 2HDM scenarios - light points allowed by all constraints except EDMs, dark points show points also passing EDM constraints
- Lots of points even for large scenarios $\bar{\kappa}_\tau$ for lepton-specific 2HDM - similar situation for Type 2
- More constrained for Type I and flipped scenarios

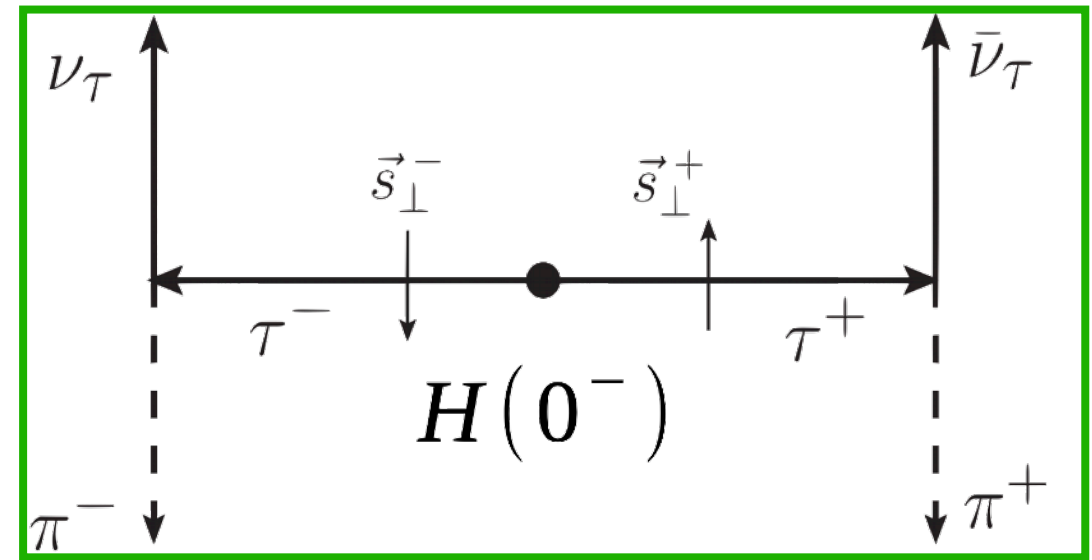
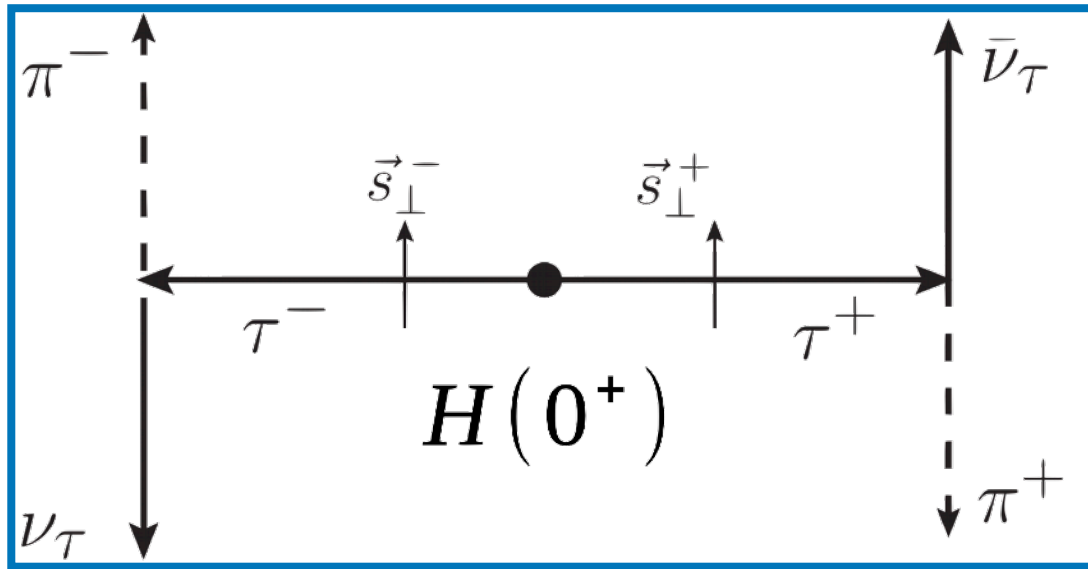


Matter-Antimatter asymmetry

- Models with CP violation in the Higgs sector that can explain matter-antimatter asymmetry can predict a measurable value of $\phi_{\tau\tau}$
- For example [Phys. Rev. D 103, 095021](#) they compare the expected precision of various colliders with the minimum value of $\phi_{\tau\tau}$ (13°) in a Type III 2HDM model that can explain the matter antimatter asymmetry
- This means that measurements of $\phi_{\tau\tau}$ to within a precision of \sim a few degrees could establish evidence for or even an observation of such models



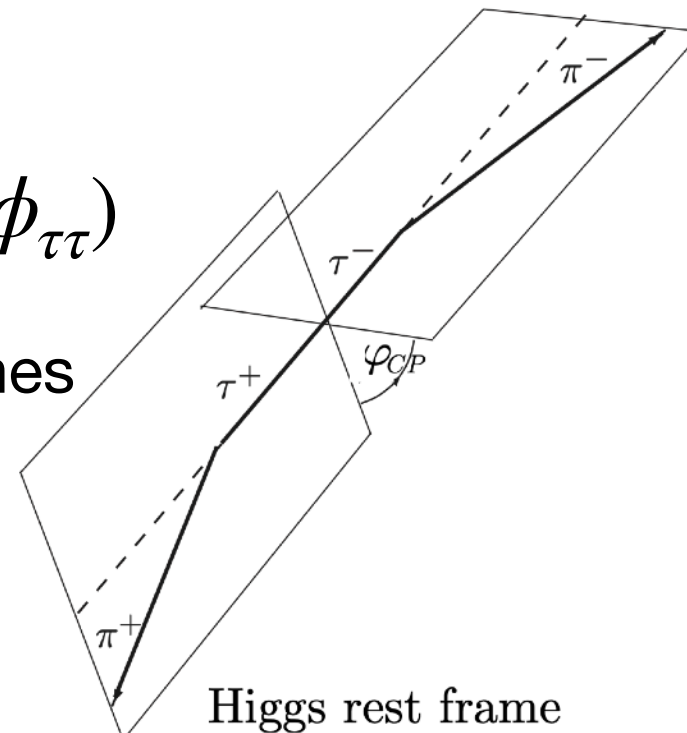
Observables sensitive to $\phi_{\tau\tau}$



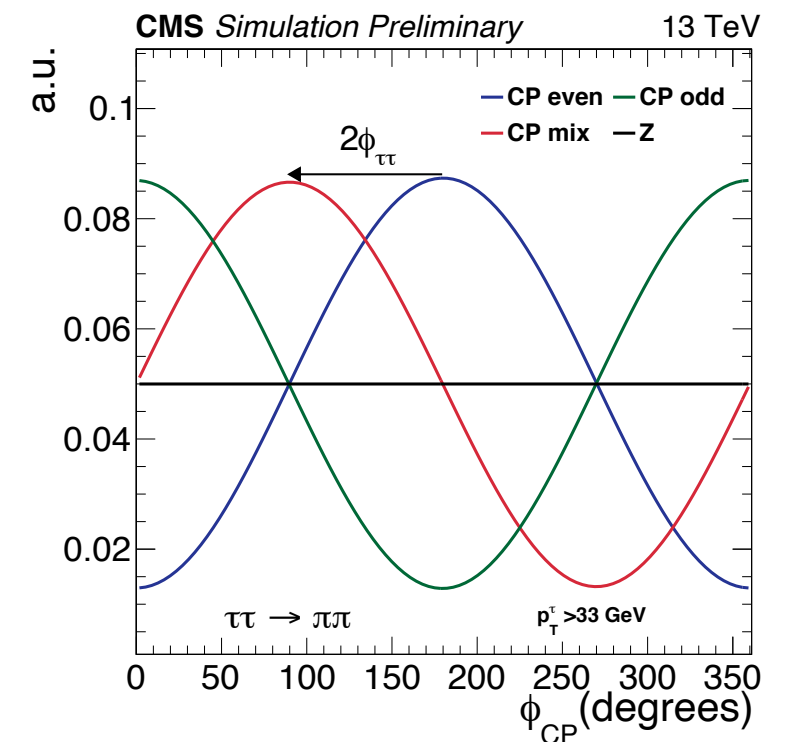
- Transverse spin correlations manifest as angular correlations of τ decay products
- Most simple 2-body decay: $\tau \rightarrow \pi \nu$
- Partial decay width looks like:

$$d\Gamma = \alpha 1 - C \cdot \cos(\phi_{CP} - 2\phi_{\tau\tau})$$

ϕ_{CP} is angle between τ decay planes in Higgs rest frame

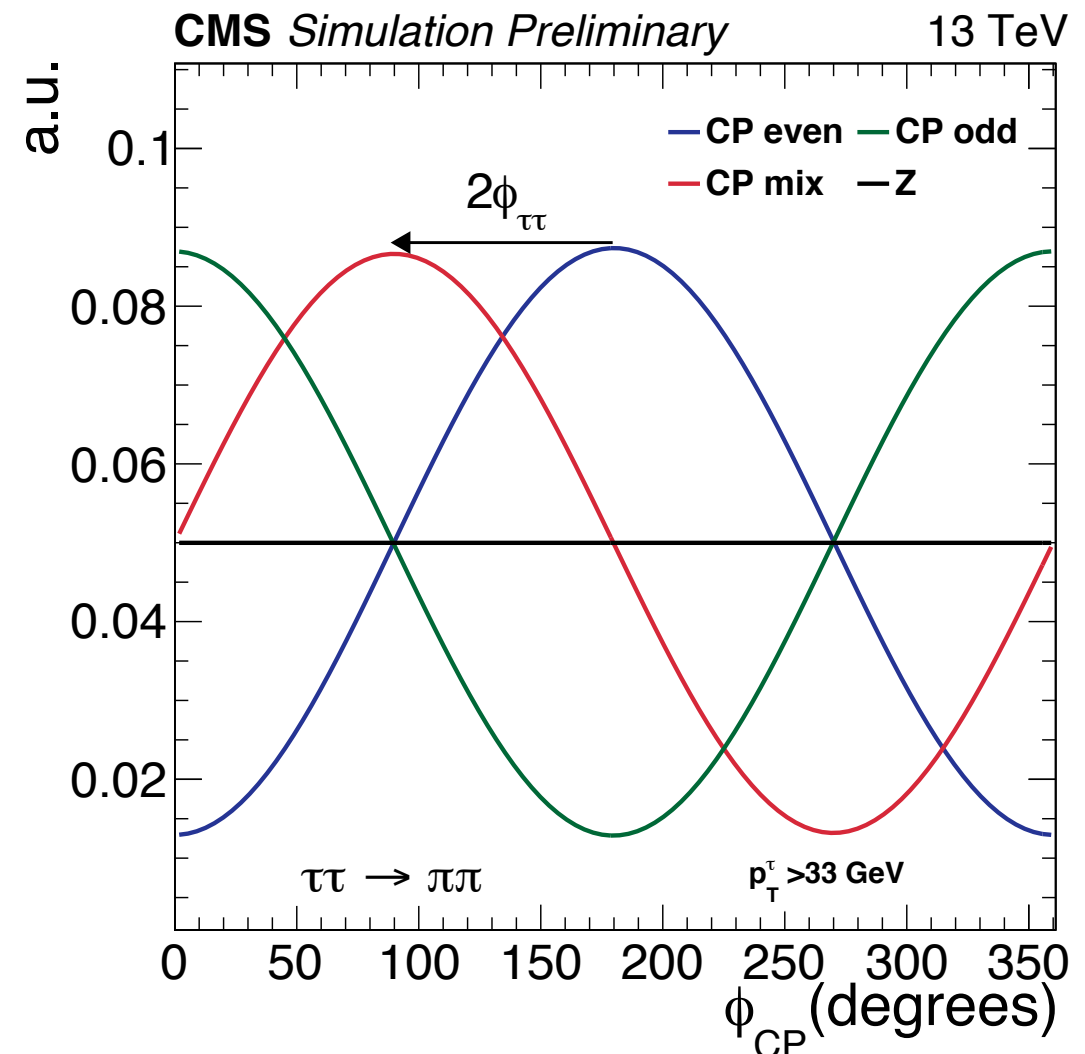
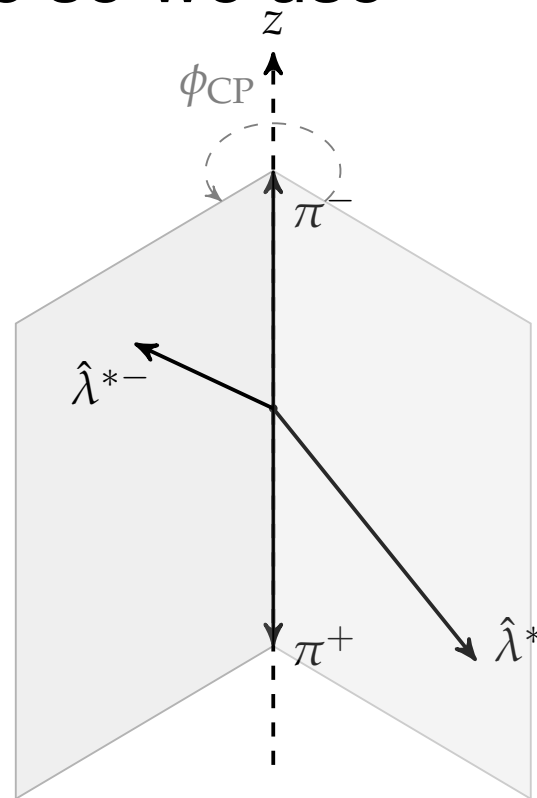
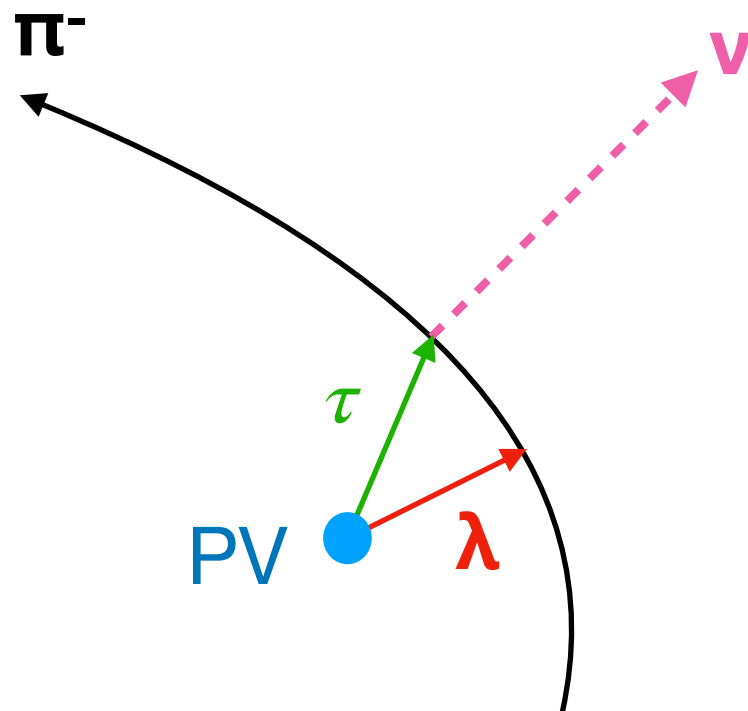


Plots courtesy of S. Berge



The IP method

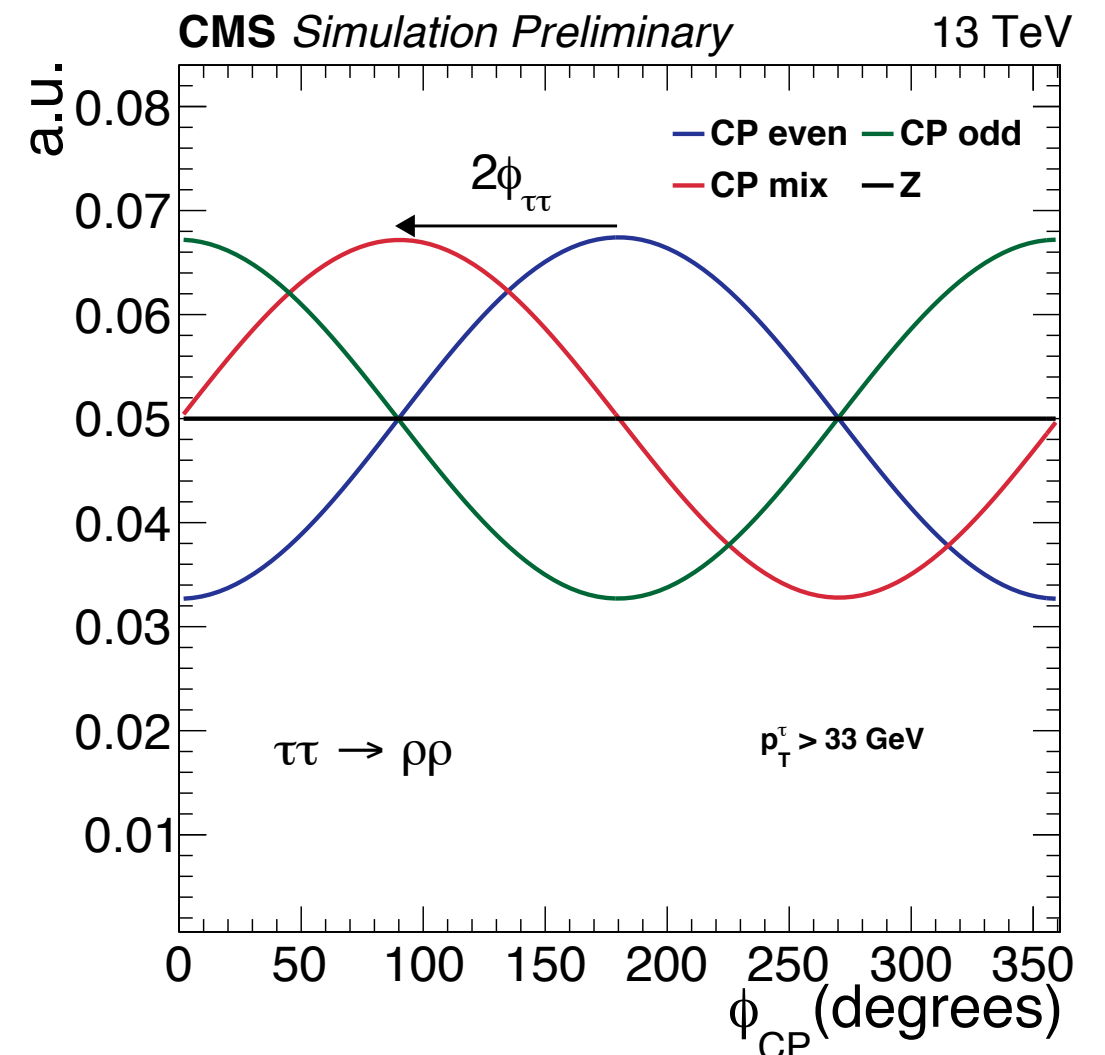
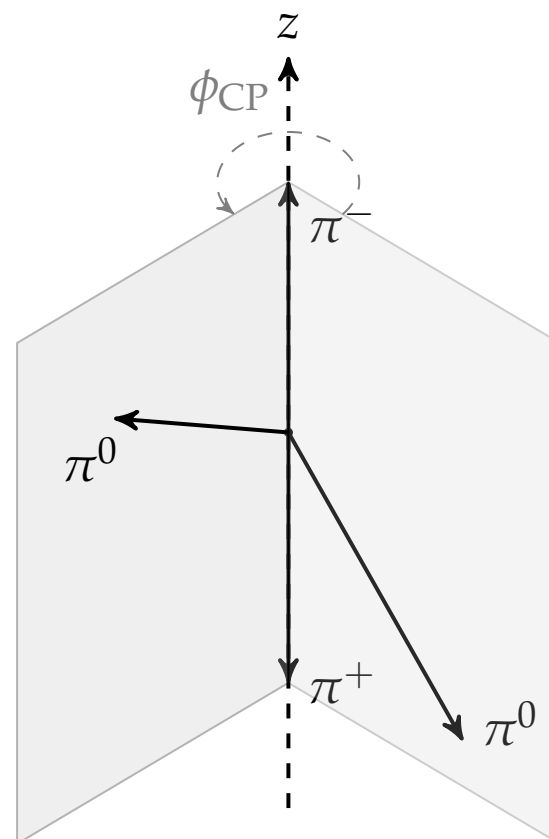
- In practise the ϕ_{CP} defined on the previous slide cannot be well measured at a hadron collider due to the neutrinos
- But we can measure the impact parameter (IP) λ of the charged particle
 - IP is the vector that points from the primary vertex (PV) to the point of closest approach to the charged particle track
- Cannot use Higgs rest frame so we use $\pi^+\pi^-$ rest frame



The π^0 method

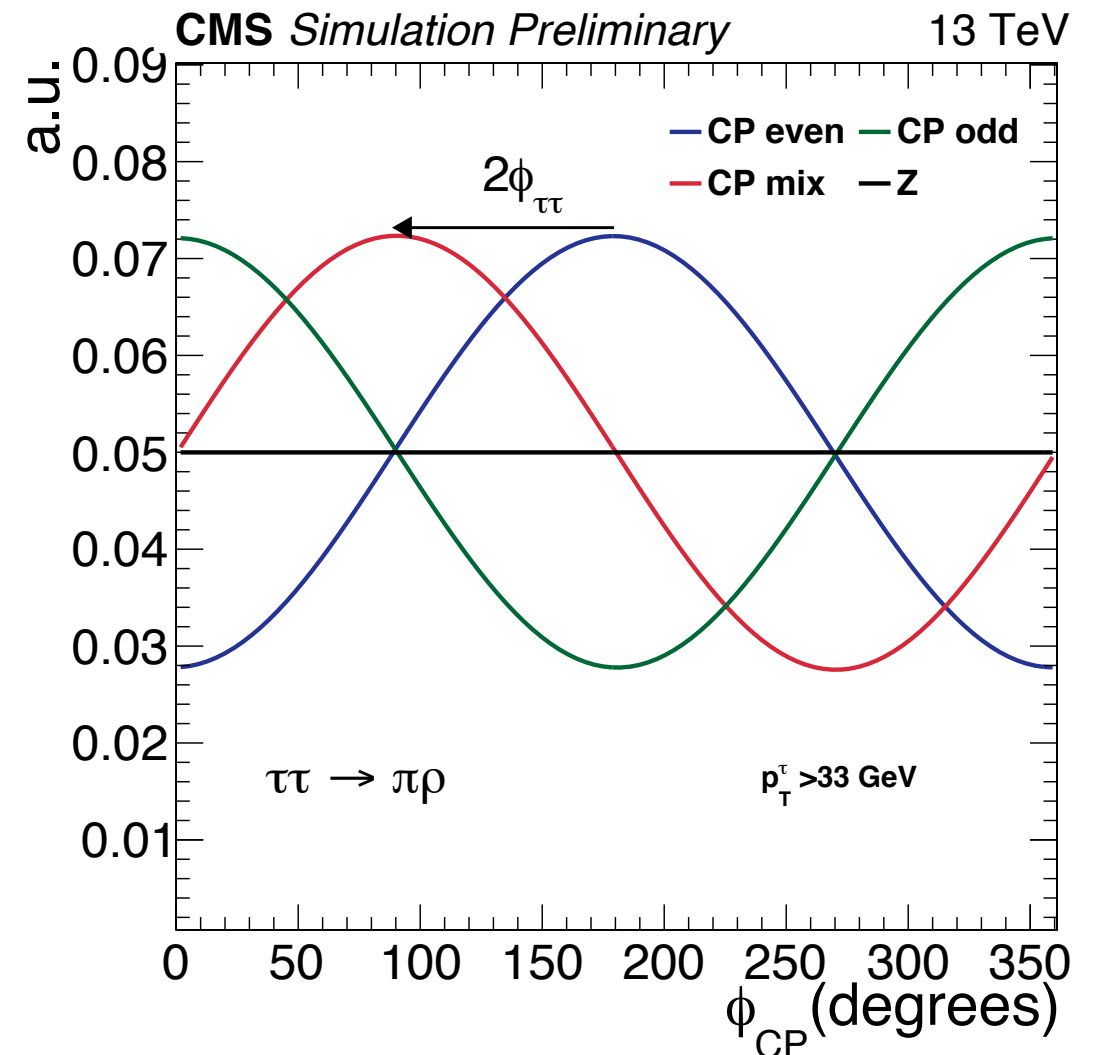
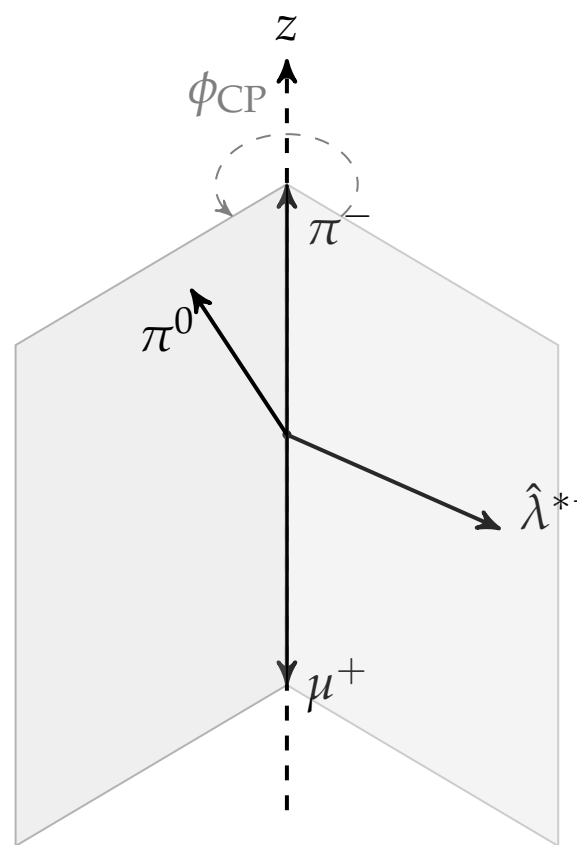
- For events with an intermediate resonances we can define a variable using only visible decay products
 - e.g $\tau\tau \rightarrow \rho^+\nu\rho^-\nu \rightarrow \pi^+ \pi^0\nu \pi^- \pi^0\nu$
- This avoids using the IP which is quite short compared to tracker resolution so is imprecisely reconstructed

- In this case we define ϕ_{CP} similar to previous but use π^0 vector instead of IP



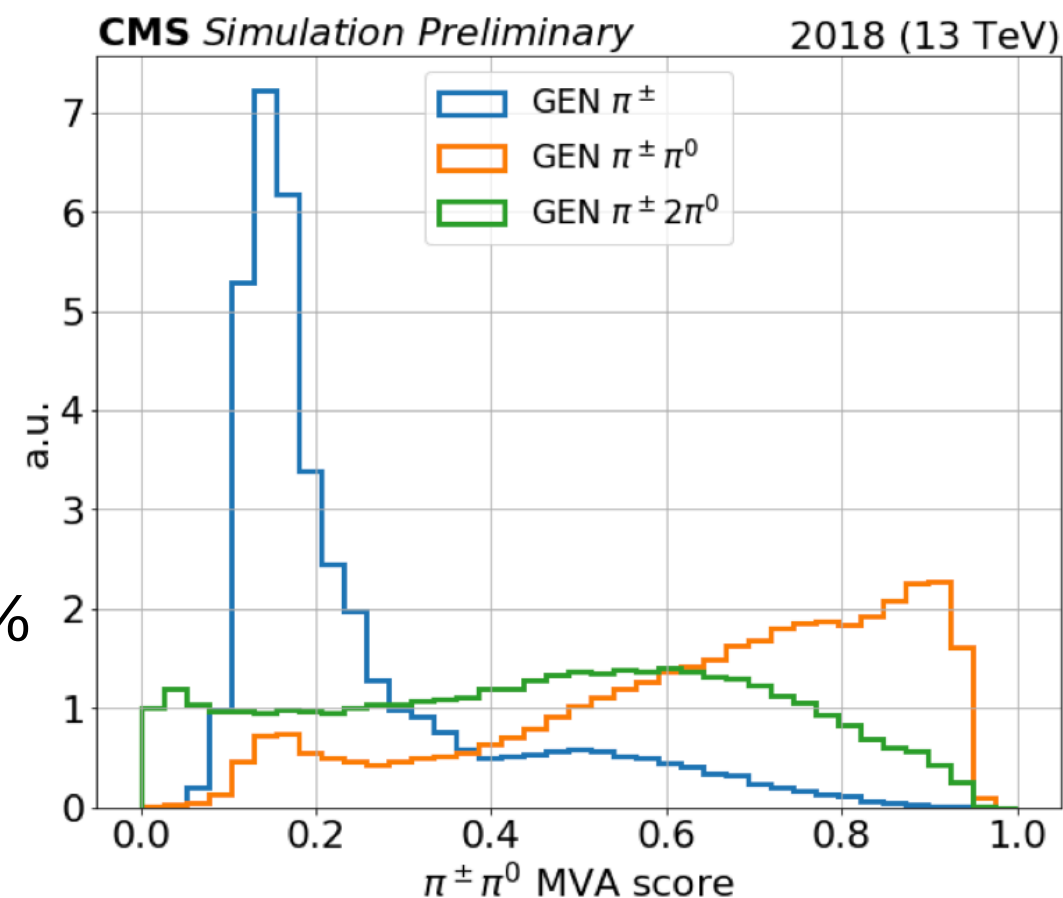
The “mixed” method

- Can also define ϕ_{CP} using a so-called “mixed” method when we have a neutral pion from 1 tau decay only
- E.g for a $H \rightarrow \tau\tau \rightarrow \rho^+\nu\mu^-\nu \rightarrow \pi^+ \pi^0\nu \mu^-\nu\nu$



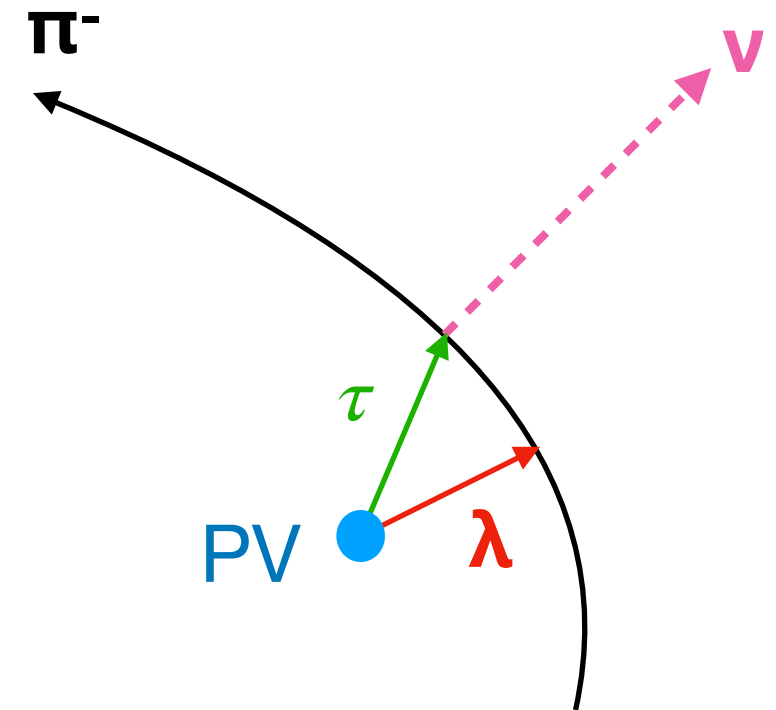
Tau decay mode selection

- The analysis is very sensitive to proper identification of the various hadronic decay modes
- For example a $\tau \rightarrow \rho \rightarrow \pi \pi^0$ looks a lot like a $a_1 \rightarrow \pi 2\pi^0$ as two π^0 tend to be merged by π^0 reconstruction algorithm
- But the CP separation (i.e the amplitude of the ϕ_{CP} distribution) is very different for these two cases
- We improve the separation between modes using a dedicated BDT
- Variables include kinematic variables such as masses, γ pT; angular observables; variables sensitive to γ density such as N_γ
- Improvement to final sensitivity using this BDT is $\sim 25\%$
- CMS released a DPS with more details:
[CMS-DP-2020-041](#)



Primary vertex and impact parameters

- Charged tracks from tau decays do not originate exactly from PV
 - We exclude these tracks and refit the vertex
- We also include an additional constraint from the LHC luminous region (so-called beam spot)
- To find IP we minimise distance between PV and track in 3D
- Our IP method also allows us to propagate uncertainties on the track and PV to define a significance $\delta_{IP} = |\boldsymbol{\lambda}|/\sigma_{IP}$
- We reject events with $\delta_{IP} < 1.5 \rightarrow$ gives about a 15% improvement in the final sensitivity



Event selections

- We select di-tau events in the fully hadronic final state ($\tau_h\tau_h$) and one semi-leptonic final state ($\tau_\mu\tau_h$)
 - collectively these channel include $\sim 55\%$ of all di-tau decay, and include all the most sensitive channels
- For $\tau_h\tau_h$ we require:
 - Two opposite-sign τ_h candidates passing HPS and deepTau ID
 - Taus should be separated by $\Delta R > 0.5$ and have $p_T > 40$ GeV
 - Pass the double-tau trigger (with p_T threshold of 35 GeV)
 - Veto events with additional light leptons
- For $\tau_\mu\tau_h$ we require:
 - A τ_h candidate with $p_T > 20$ GeV passing HPS and deepTau ID
 - A isolated μ passing identification and with $p_T > 23$ (25) GeV for 2016 (2017 and 2018)
 - The τ_h and μ should have opposite sign charges and be separated by $\Delta R > 0.5$
 - Event should pass either a single muon trigger (p_T threshold between 23-27 GeV) or muon+tau trigger
 - Veto events with additional light leptons, b-jets, or with transverse mass $m_T > 50$ GeV

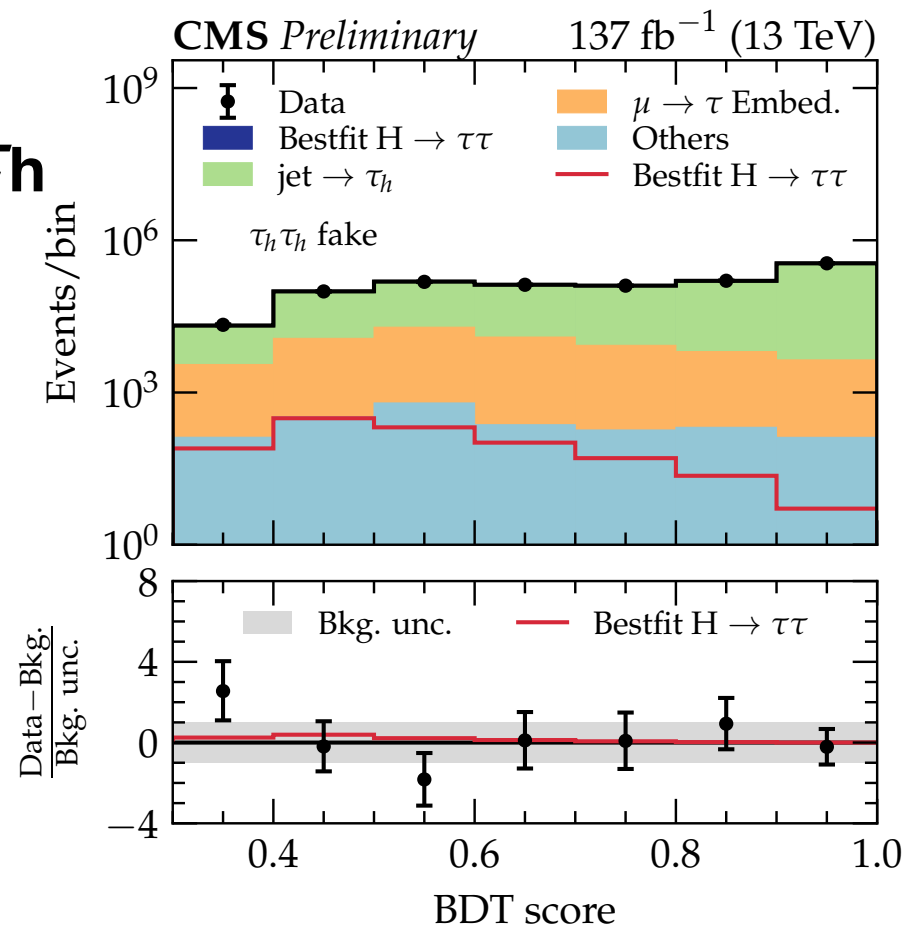
MVA signal vs background

- Event after apply previous event selections the background is significantly larger than the signal (S/B \sim 0.006)
- We use multi-class MVAs to improve separation between the backgrounds
 - 2 background classes: genuine- τ_h and fake- τ_h , + 1 inclusive Higgs signal class
- For $\tau_h\tau_h$ ($\tau_\mu\tau_h$) channel we use BDT (NN)
 - Includes several variables such as: p_T 's, $m_{\tau\tau}$, N_{jets} , m_{jj} , ..
 - $m_{\tau\tau}$ most important variable - because of neutrinos we estimate using SV-fit algorithm ([J. Phys. Conf. Ser. 513 022035](#))

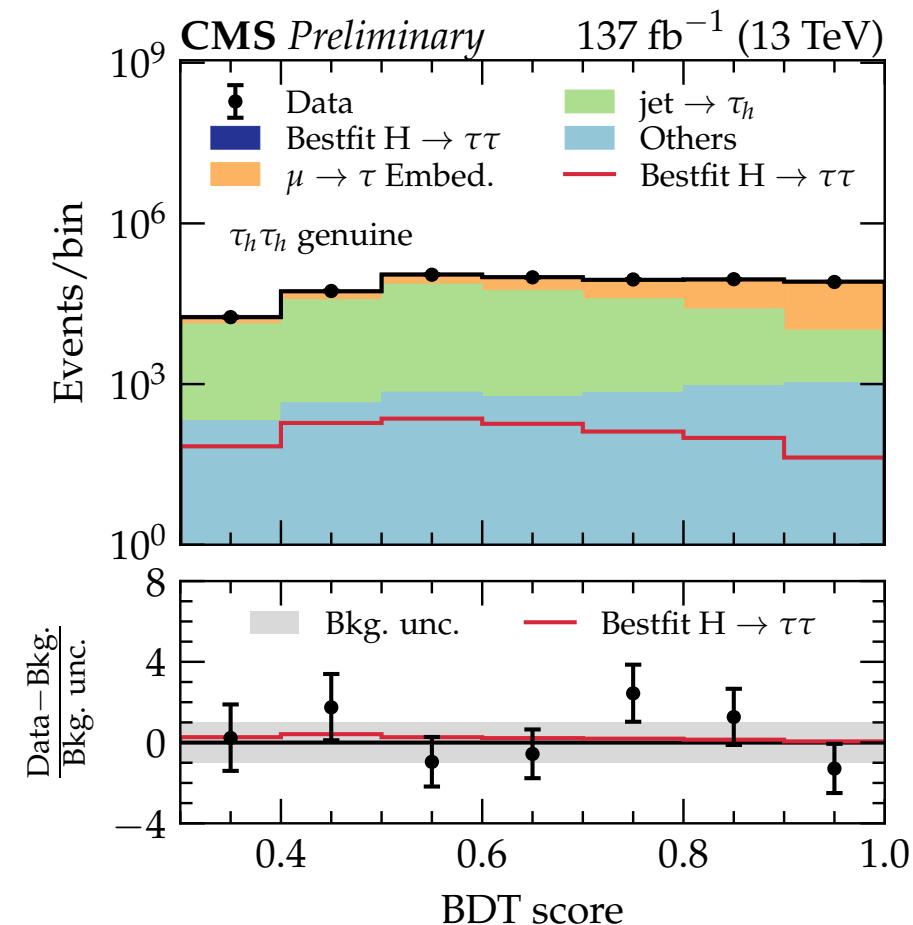
Background categories

- Output of MVAs are three scores (or “probabilities”) that sum to 1, 1 score per class
- We sort events into signal and background categories based on which score is the largest
- In each category we then fit the corresponding score as a discriminating variable

fake- τ_h



genuine- τ_h

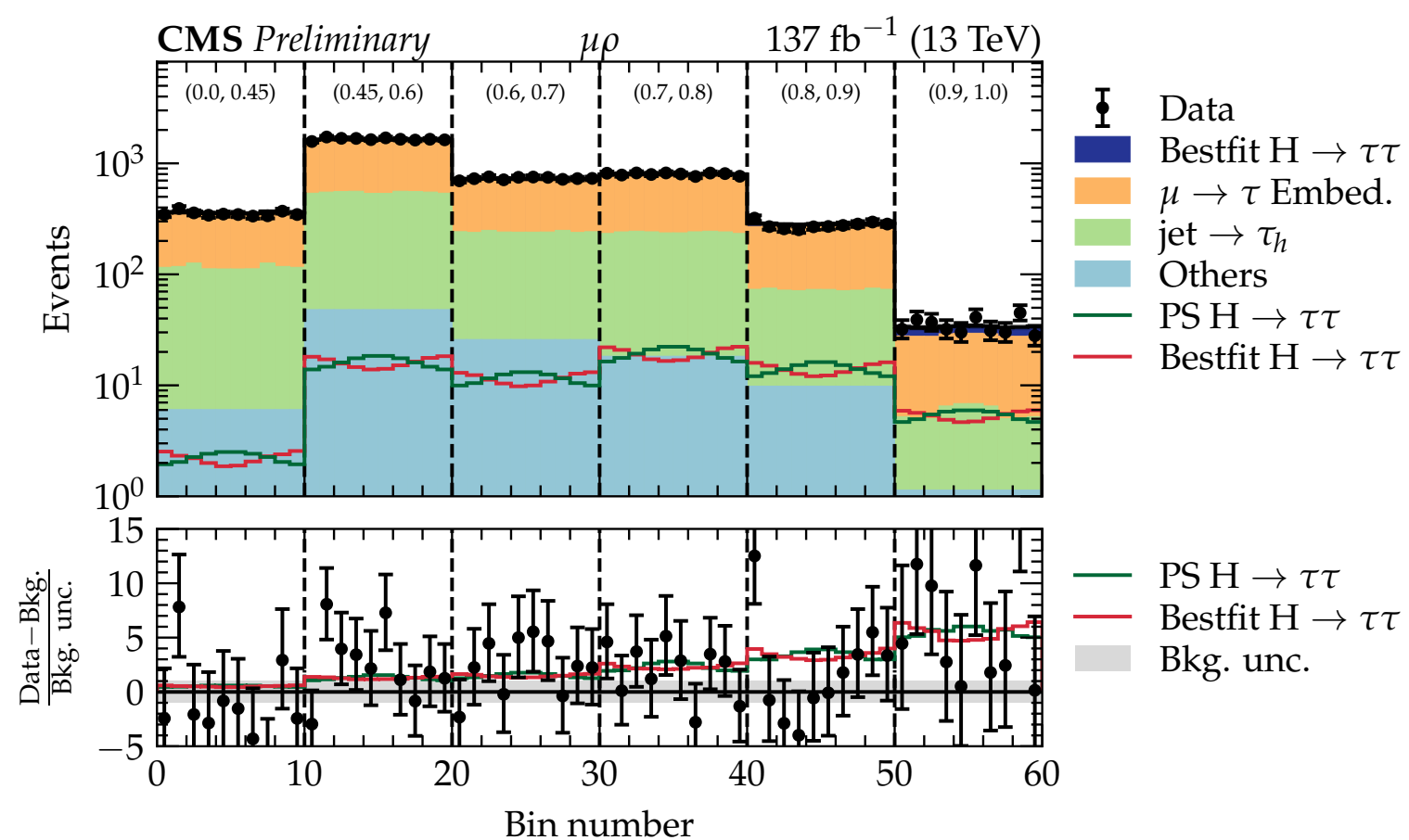
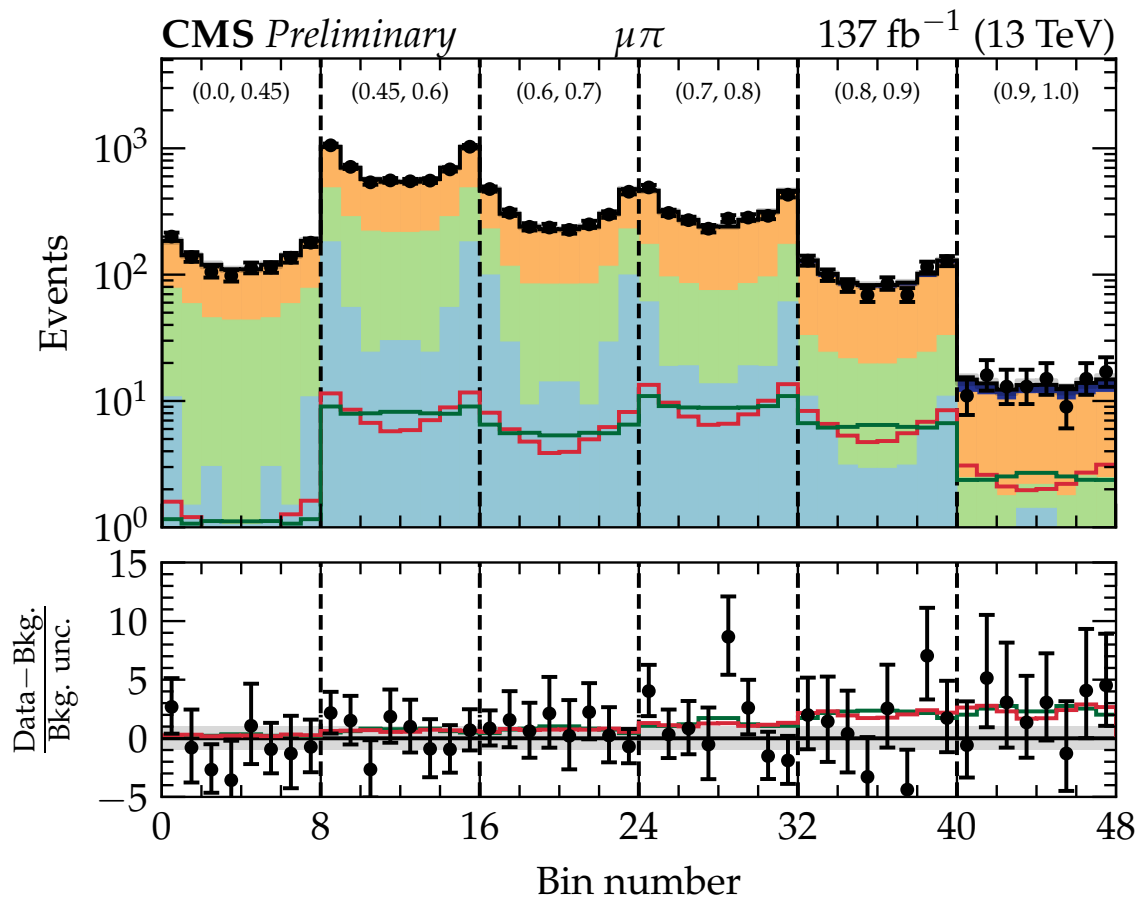


Signal categories

- For the Higgs signal category we further divide events depending on the τ_h decay mode
- We fit 2D variables: 1 variable is the MVA score, the second is ϕ_{CP}

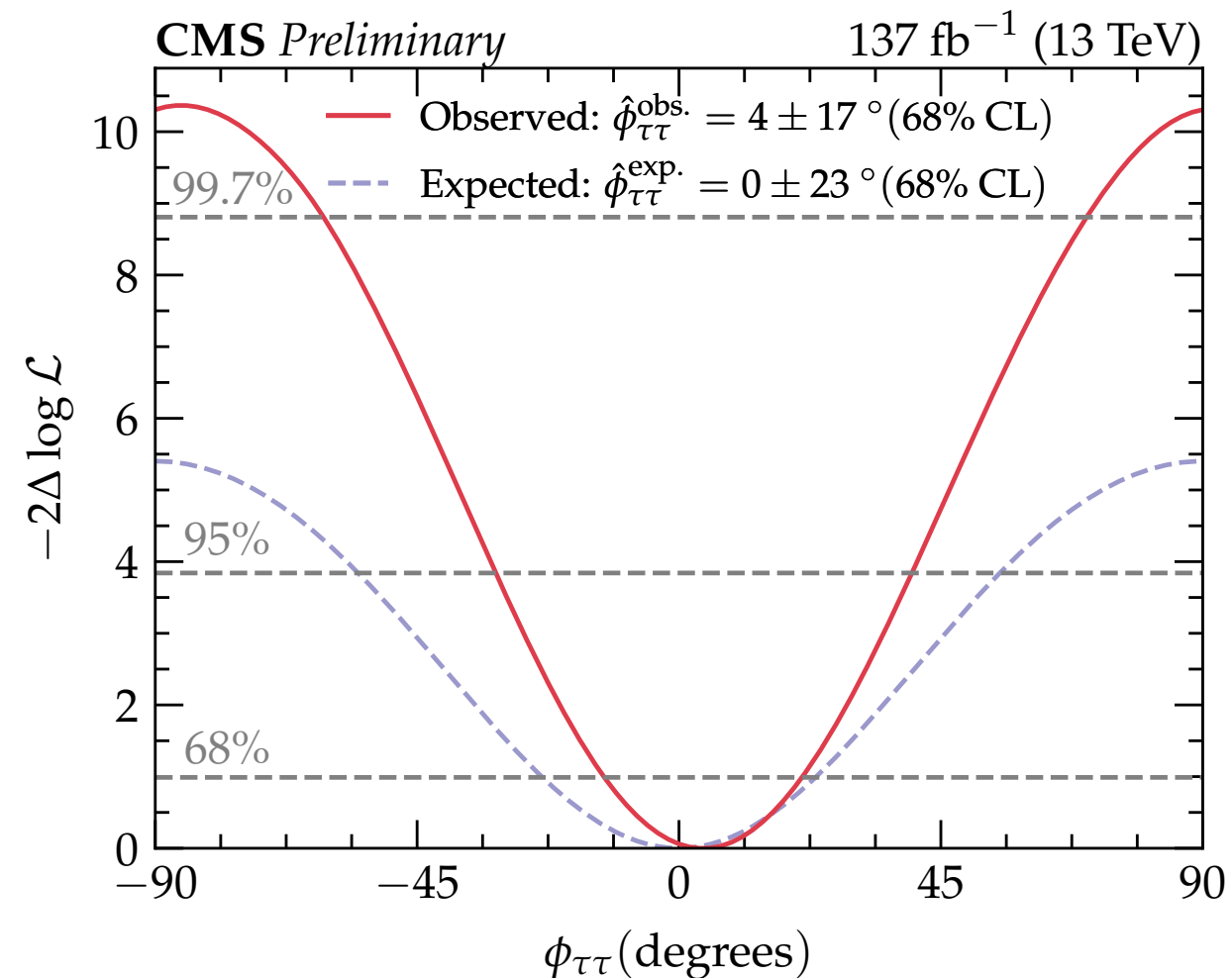
$$\tau_\mu \tau_h, \tau_h \rightarrow \pi^- V$$

$$\tau_\mu \tau_h, \tau_h \rightarrow \rho^- V$$



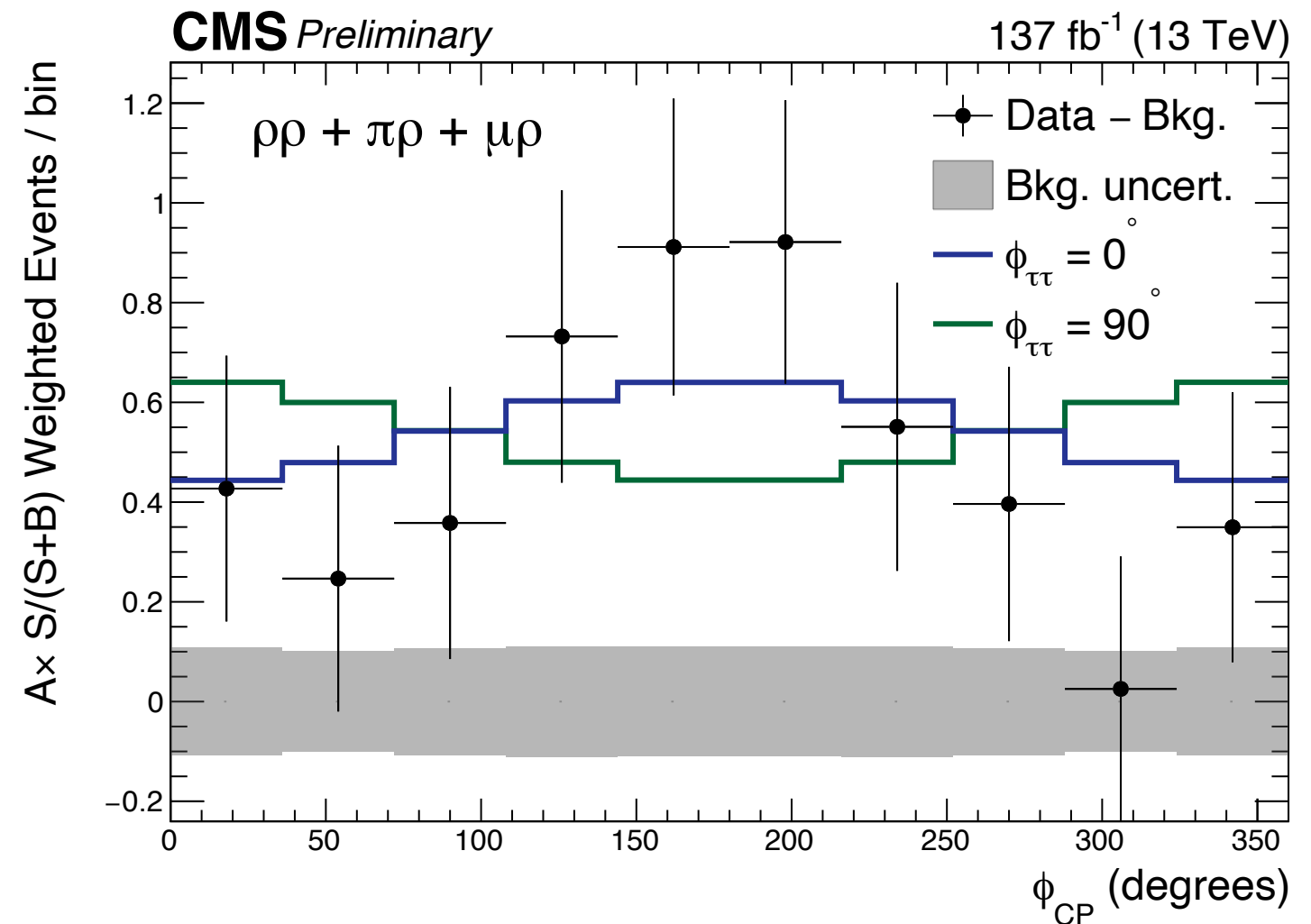
Results

- We extract our results by means of a binned maximum likelihood fit combining all channels and categories
- The observed (red) and expected (blue) $-2\Delta\log(L)$ scan is shown below
- The best fit value and uncertainty is $4 \pm 17^\circ$ compared to an expected value of $0 \pm 23^\circ$
- Results are therefore in agreement with the SM although uncertainties are large so there is still lots of room for new physics
- Due to a slight upwards fluctuation we are able to exclude the pure CP-odd hypothesis at the 3σ level



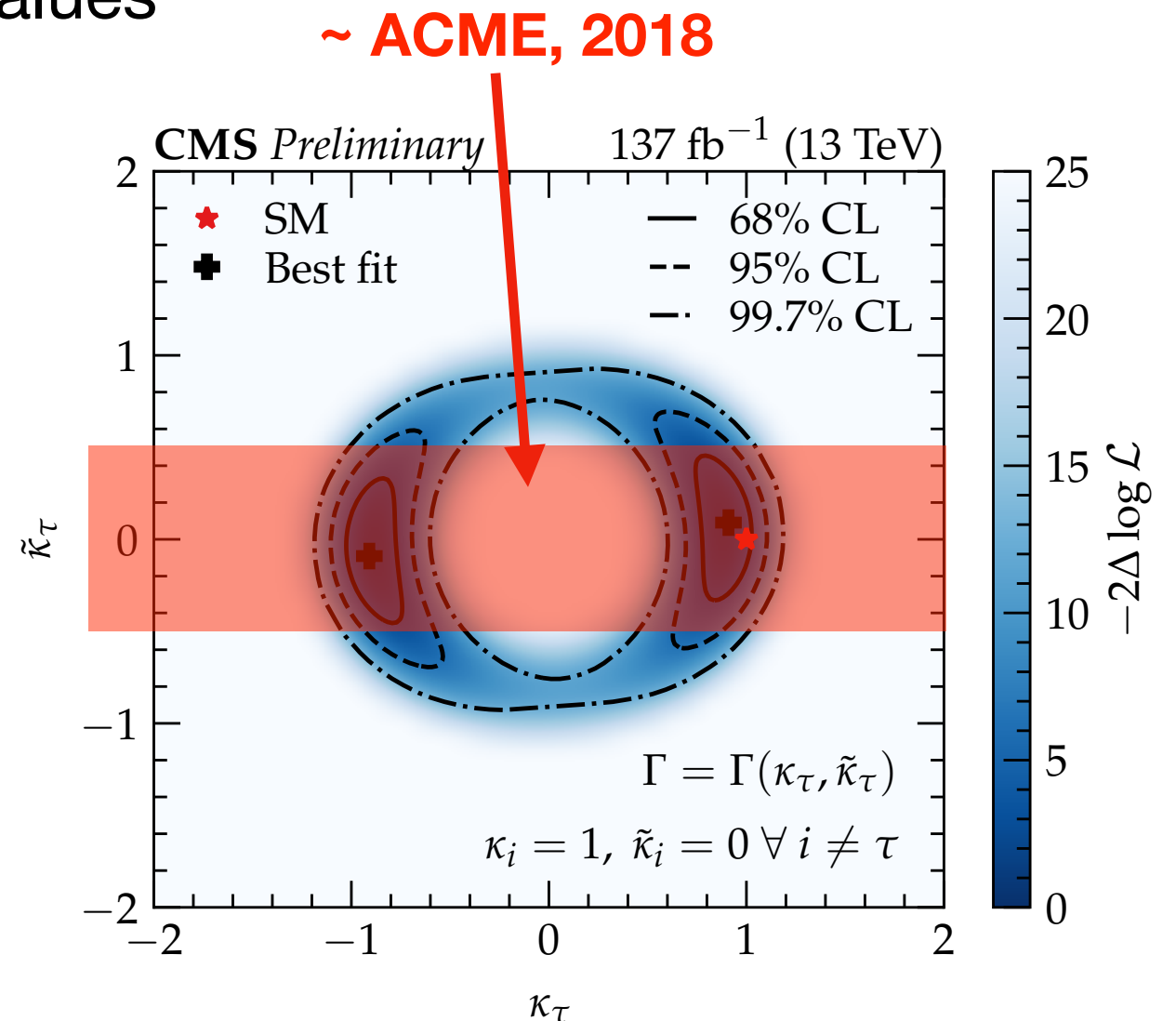
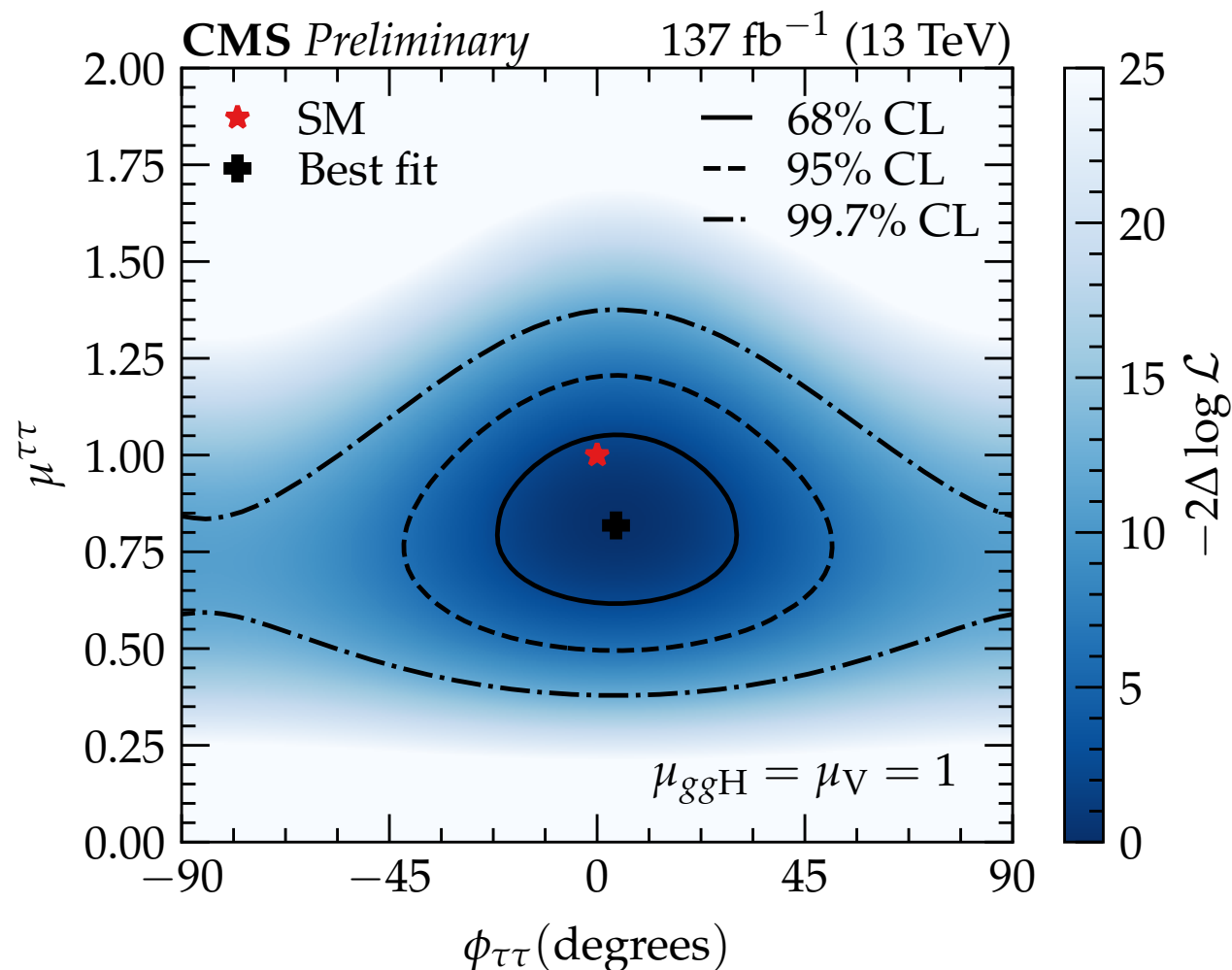
Results: ϕ_{CP} distribution

- For a visual representation of the measurement we produce a double weighted distribution of the muon sensitive categories
- Weight by $S/(S+B)$ and the parameter A
- A is the “average asymmetry” = sum of absolute differences between CP-even and CP-odd for all bins / N_{bins}



2D scans and coupling measurements

- Plot 2D scan of branching ratio modified $\mu_{\tau\tau}$ vs $\phi_{\tau\tau}$ (left)
- Also interpret results in terms of couplings: κ_τ and $\bar{\kappa}_\tau$ (right)
- Assume all other couplings = SM values



Future measurements: LHC

- Even shorter term (~ spring/summer 2021):
 - Add more channels e.g $e\mu$ $e\pi$ $e a_1$
 - Likely bring ~ 10-15% improvement in sensitivity
- Medium term (LHC Run 3 ~ 2025):
 - Take into account more information/variables to constrain the $\tau\tau$ system e.g missing energy, secondary vertices, impacts parameters (where not already used e.g pp channel)
 - Improvements in signal vs background separation can help as well
 - Should improve sensitivity compared to current analysis but by how much remains to be seen
- Long term (end of HL-LHC data taking ~ 2037)
 - Breakdown of expected statistical and systematic uncertainties
 $\phi_{\tau\tau} = 0 \pm 23$ (stat.) + 2 (syst.)^o
 - Very naive prediction for HL-LHC (3/ab): scale statistical error by $1/(3000/137)^{0.5}$:
 $\phi_{\tau\tau} = 0 \pm 5$ (stat.) + 2 (syst.)^o - remains stats. Limited with total error ~ 5^o

Conclusions

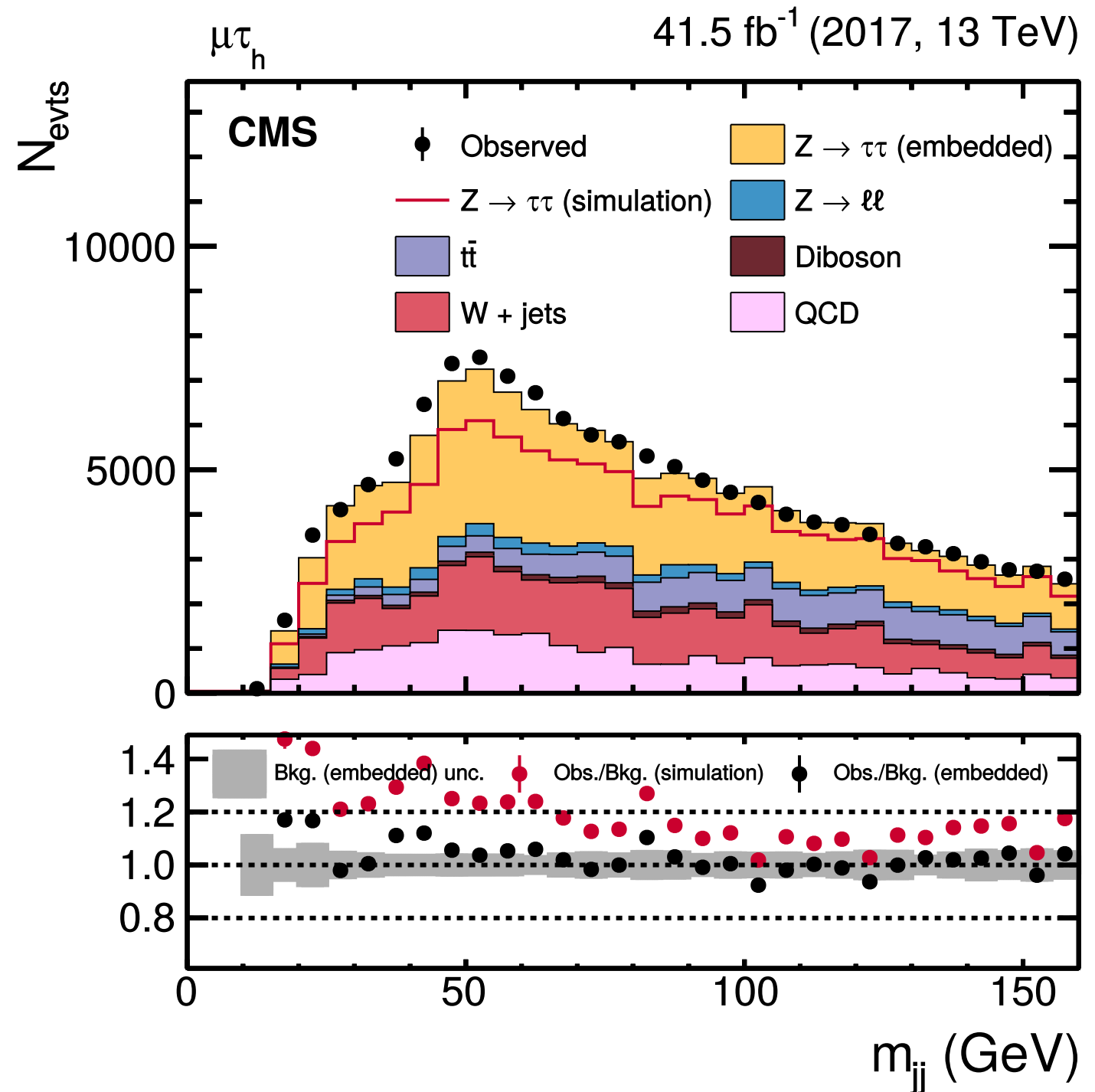
- The latest Higgs cross section and coupling measurements by the CMS experiment have been presented
- Current best fit value of Higgs production cross section is 0.85 ± 0.12 times the SM expectation
- Presented the first CP property results from the CMS collaboration using Run 2 data (2016-2018)
 - Current best measurement: $\phi_{\tau\tau} = 4 \pm 17^\circ$
 - Pure CP-odd hypothesis excluded at 3σ level

Thanks for your attention!

Backup

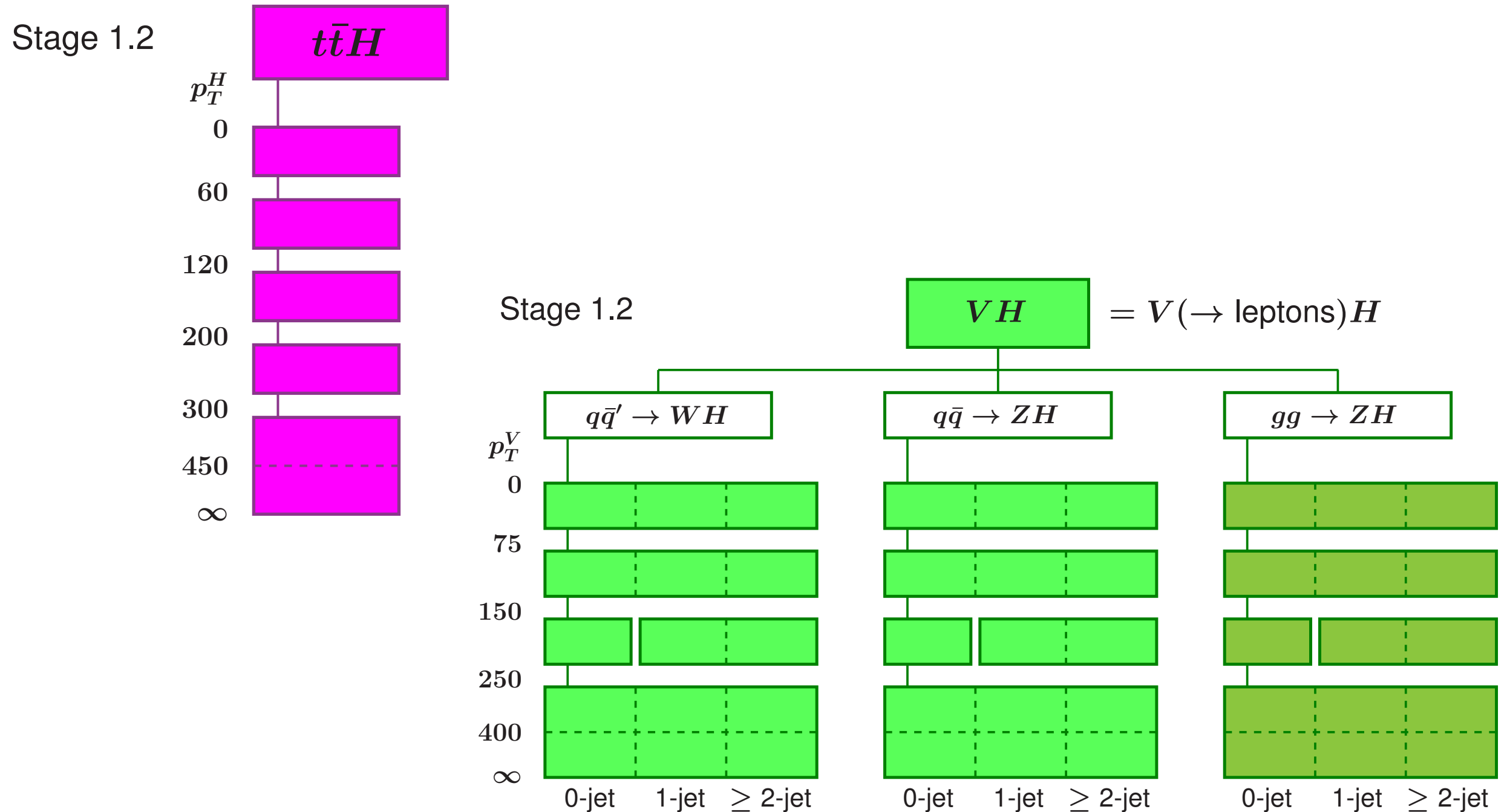
Embedding method vs pure MC simulations

- Embedding method brings improvements in description of the data
- All objects except simulated tau leptons come from real data events so are described perfectly (e.g jets)
- For example the di-jet invariant mass distribution (right) is described much better for embedding (black points) vs pure MC simulations (red points)



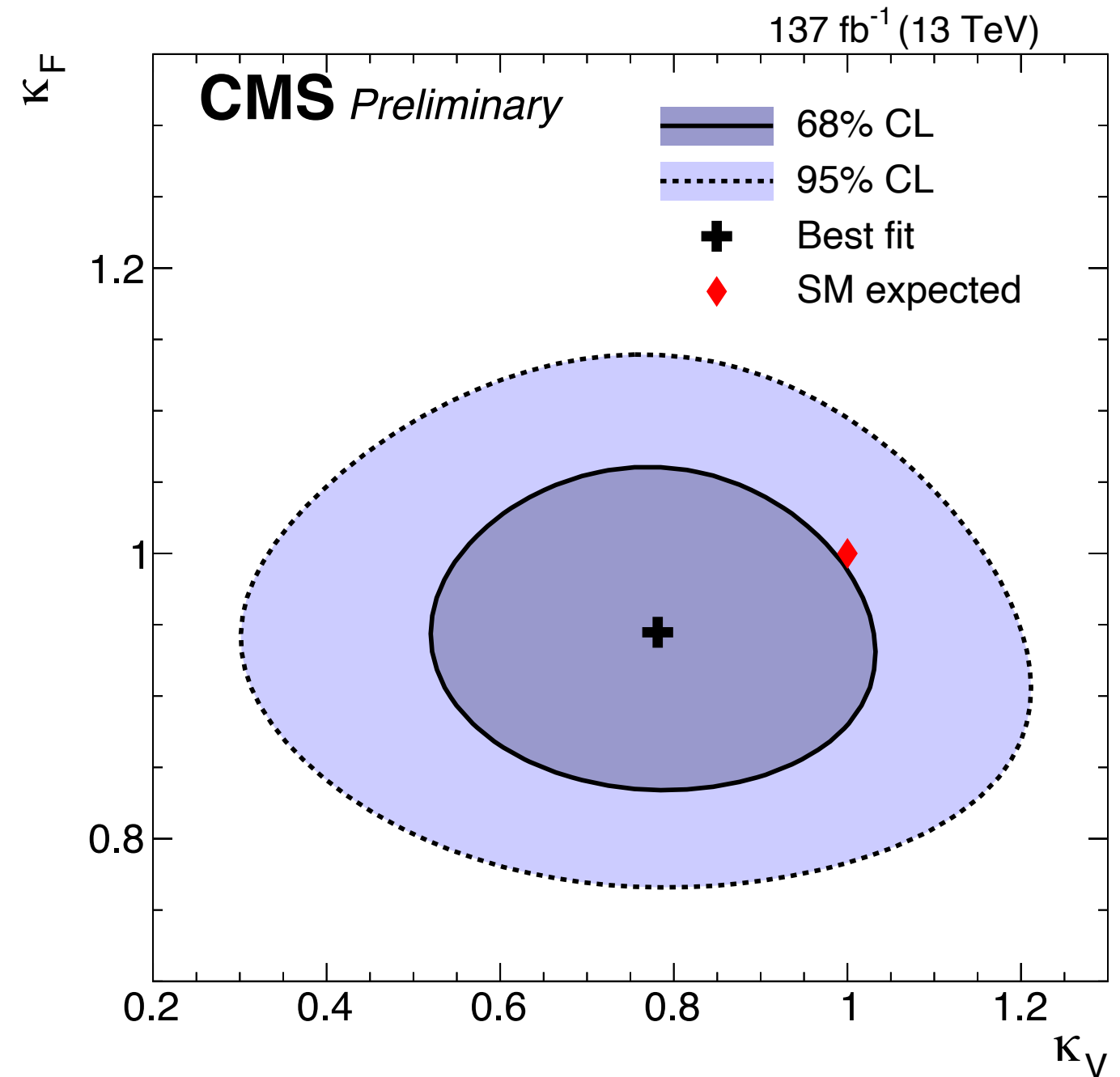
STXS: ttH and VH

- Also STXS bins defined for VH ($V \rightarrow \text{leptons}$), and ttH

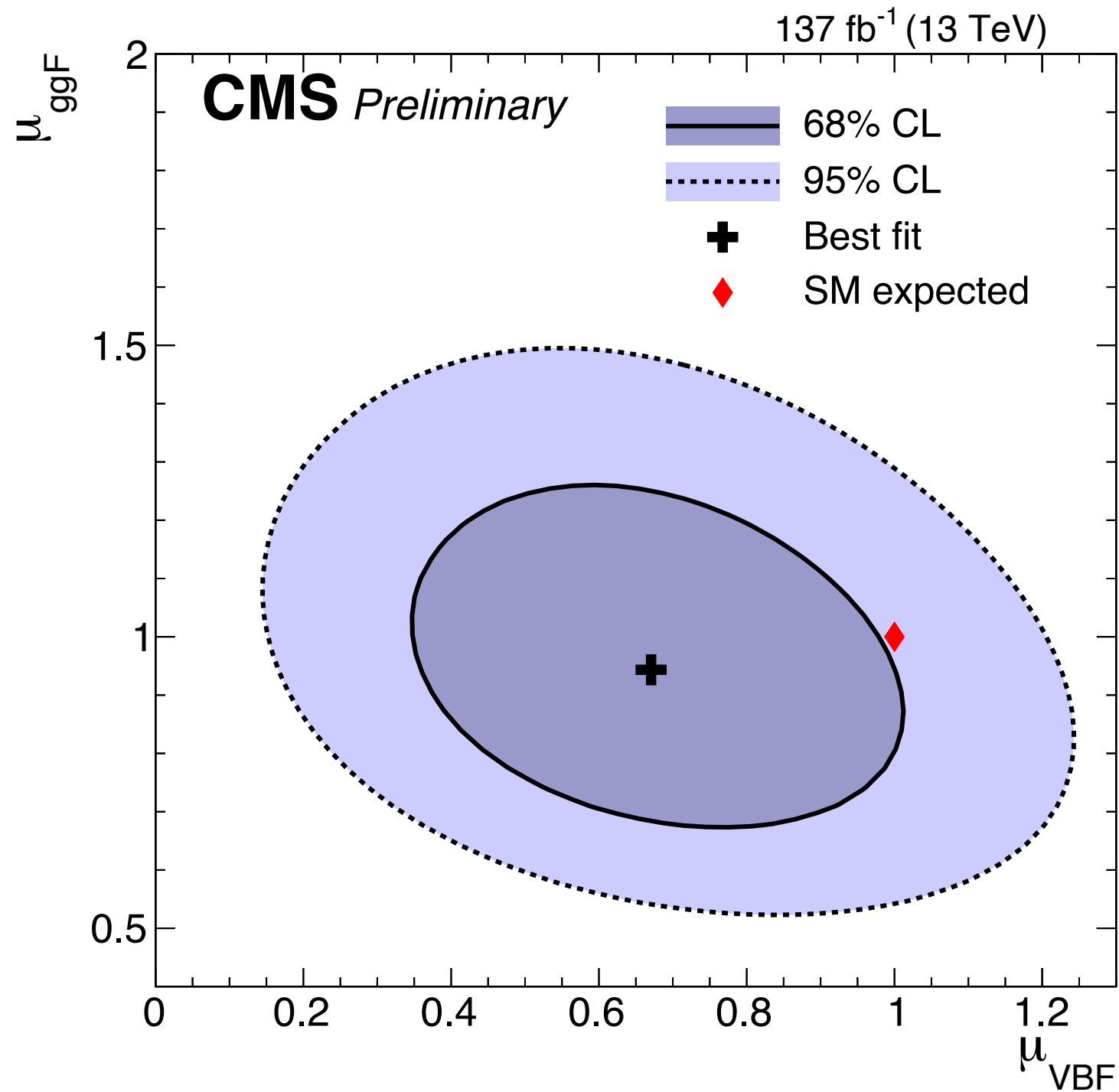


Results: coupling measurements

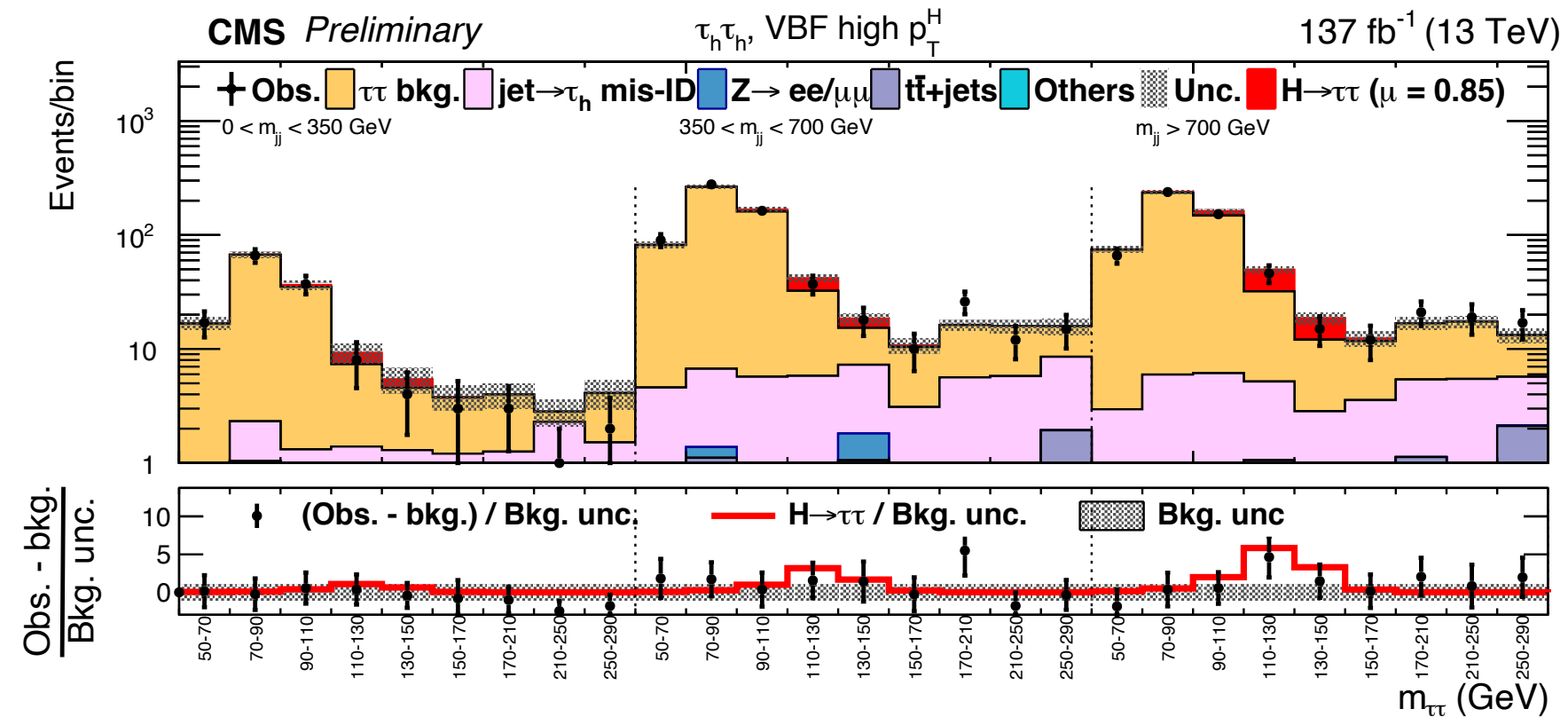
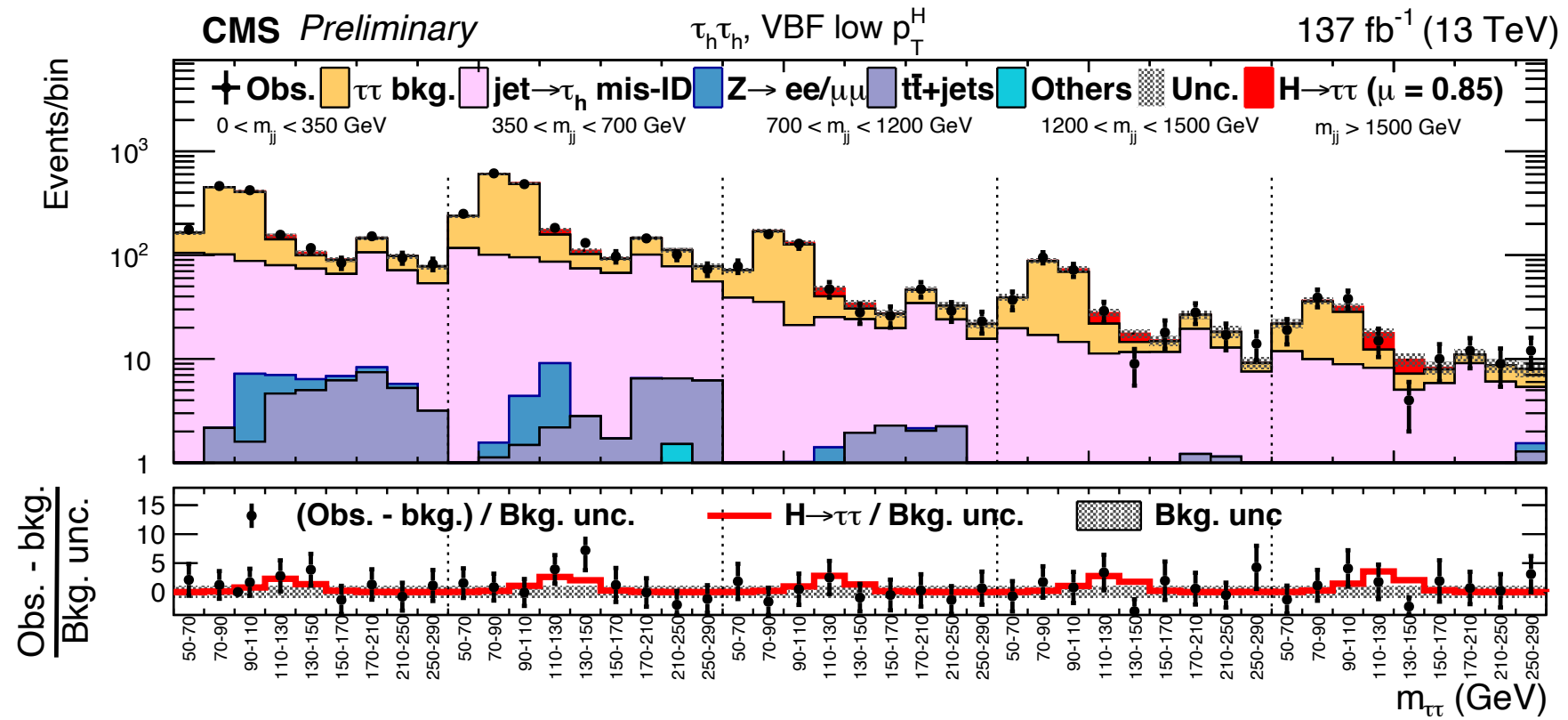
- The results are also interpreted in terms of coupling strength modifiers
- Here we assume common coupling modifiers for fermions (κ_f) and bosons (κ_V)
- Coupling strength modifiers = coupling relative to the SM expectation e.g $\kappa_\tau = y_\tau / y_\tau^{\text{SM}}$



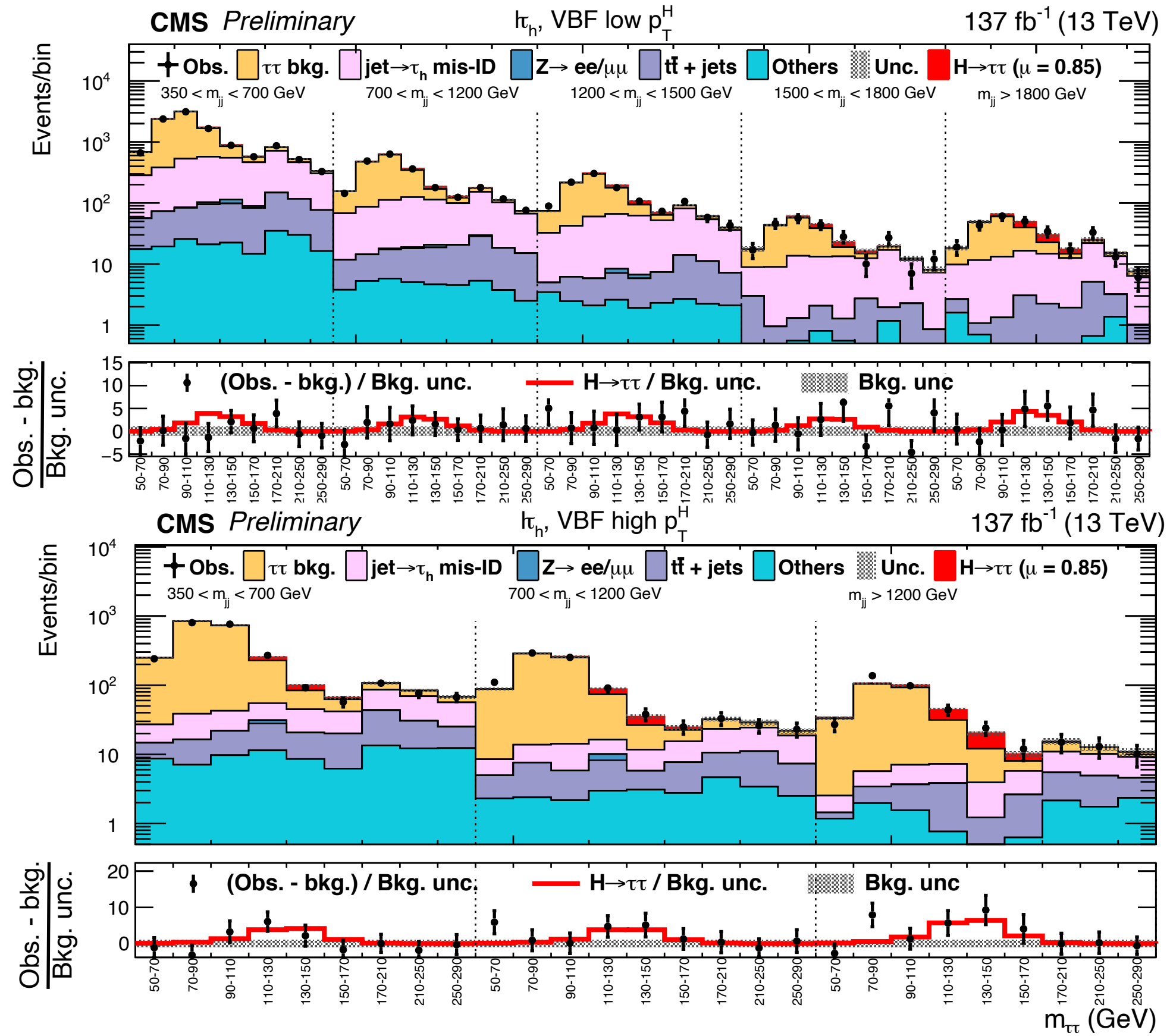
2D scans of ggH and VBF cross sections



Signal extraction: additional examples of fitted distributions



Signal extraction: additional examples of fitted distributions



C2HDM: overview

- Compared to SM Higgs sector has one additional doublet
- 4 allowed types depending on which doublet the Higgs couples to:

	u-type	d-type	Leptons
Type 1	ϕ_2	ϕ_2	ϕ_2
Type 2	ϕ_2	ϕ_1	ϕ_1
Lepton-specific	ϕ_2	ϕ_2	ϕ_1
Flipped	ϕ_2	ϕ_1	ϕ_2

- Potential looks like:

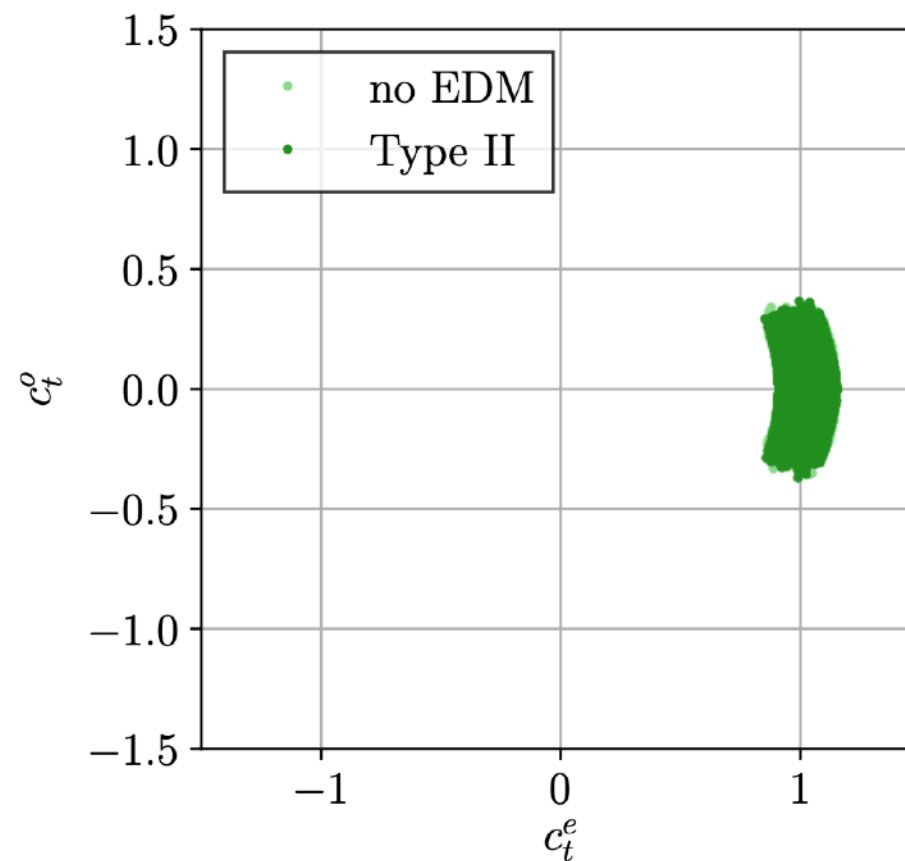
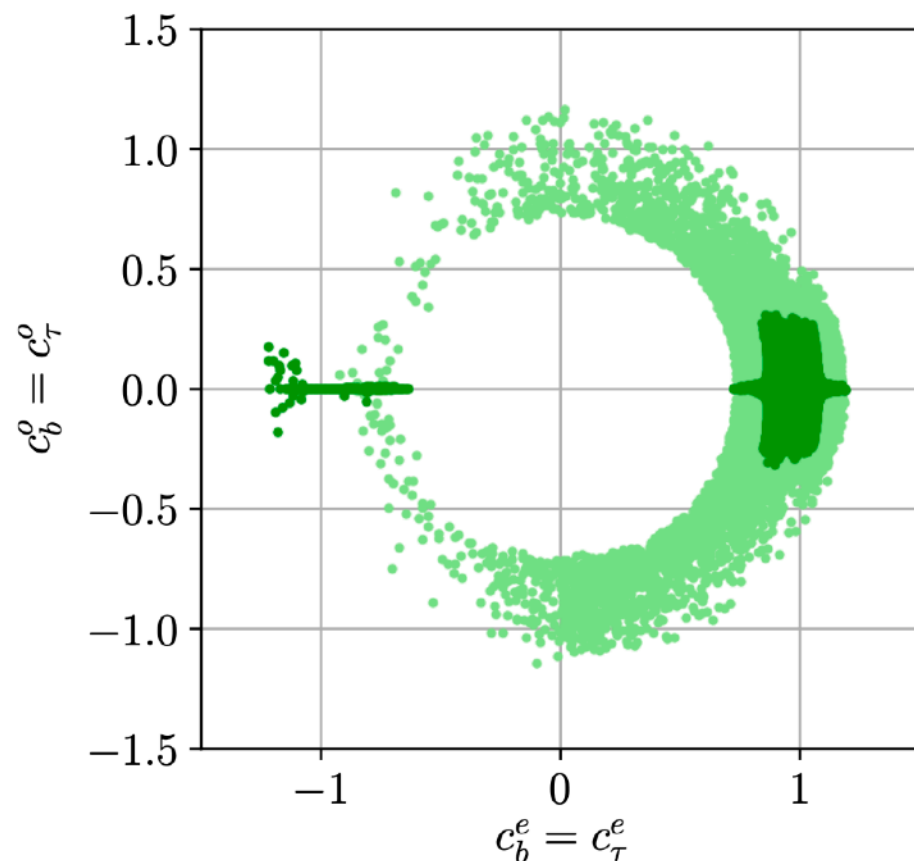
$$\begin{aligned}
 V = & m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - \left(m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\
 & + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left[\frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \text{h.c.} \right].
 \end{aligned}$$

- Complex parameters m_{12}^2 and λ_5 allow CP-violation

- In [JHEP 02 \(2018\)073](#) they show allowed points for various 2HDM scenarios considering several bounds:
 - Electron EDMs (ACME 2013)
 - Theoretical bounds: boundless from below and perturbative unitarity
 - Electroweak precision data
 - Flavour physics
 - Higgs 125 GeV coupling constraints
 - HiggsBounds (searches for additional bosons)

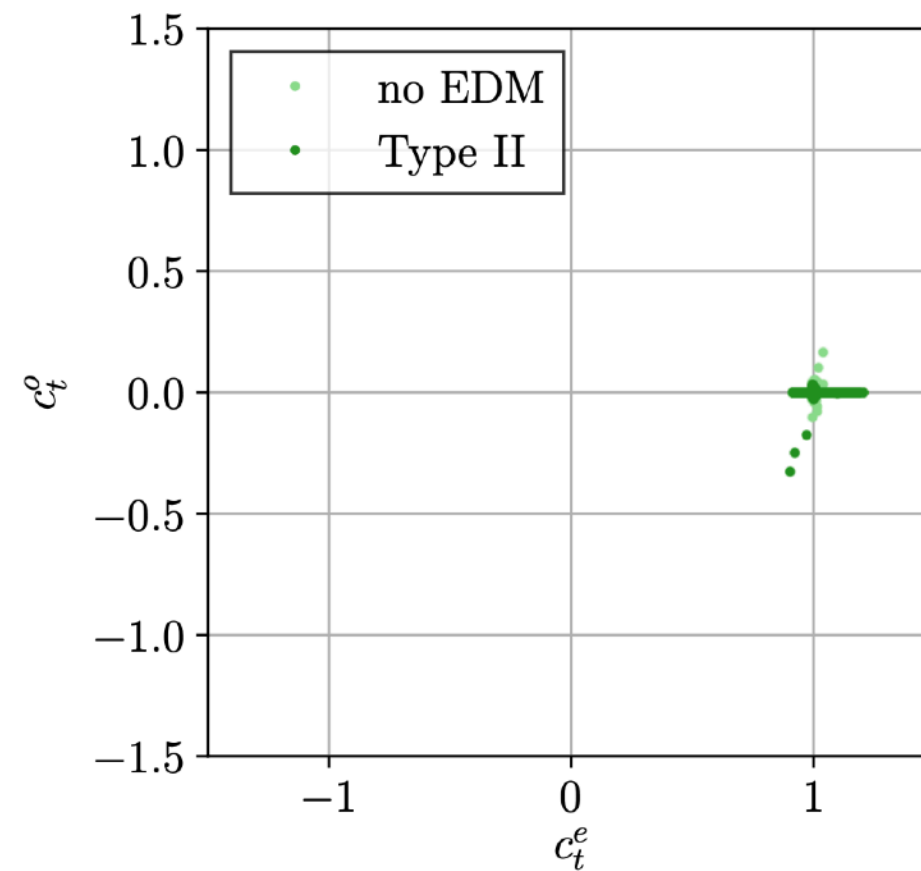
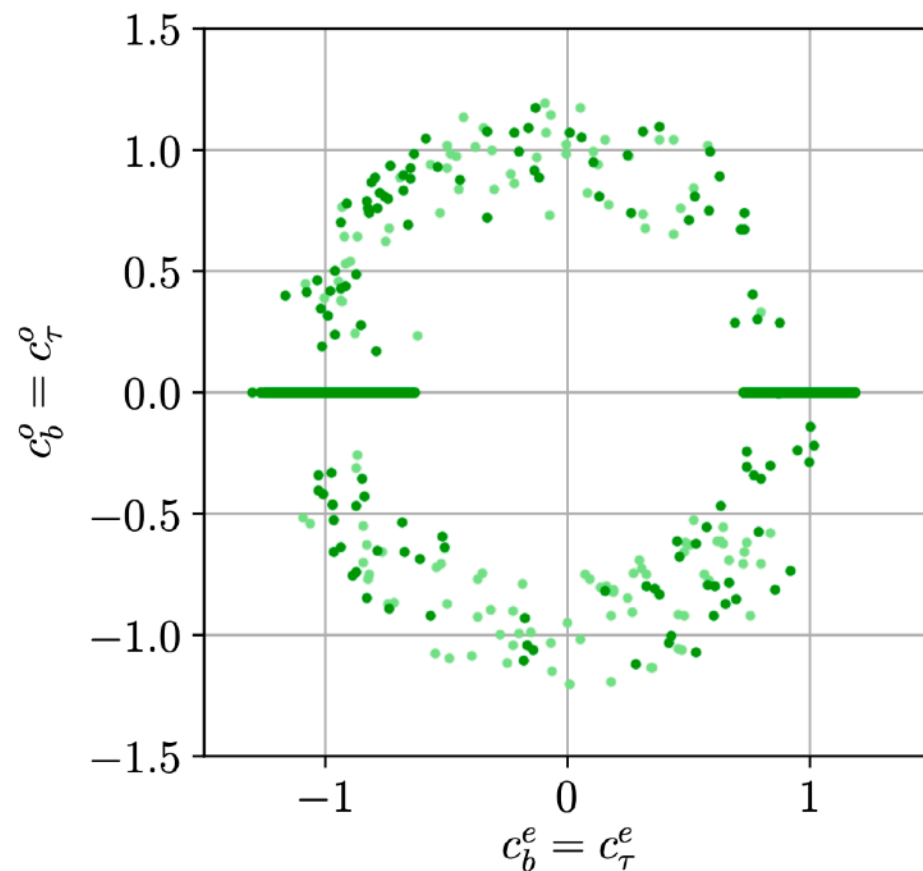
C2HDM: Type 2

- In [JHEP 02 \(2018\)073](#) they show allowed points for various 2HDM scenarios
- In Type 2 2HDM where $H_1 = 125$ GeV boson
- EDMs constrain scenarios with large-iso $\bar{\kappa}_\tau$ quite alot



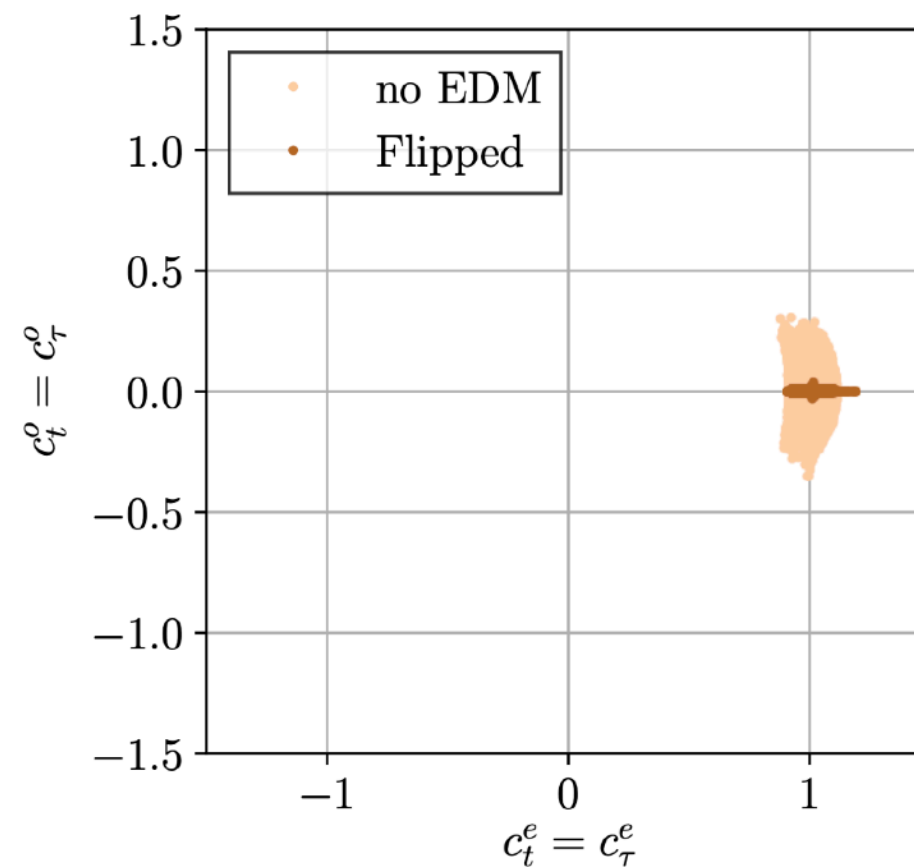
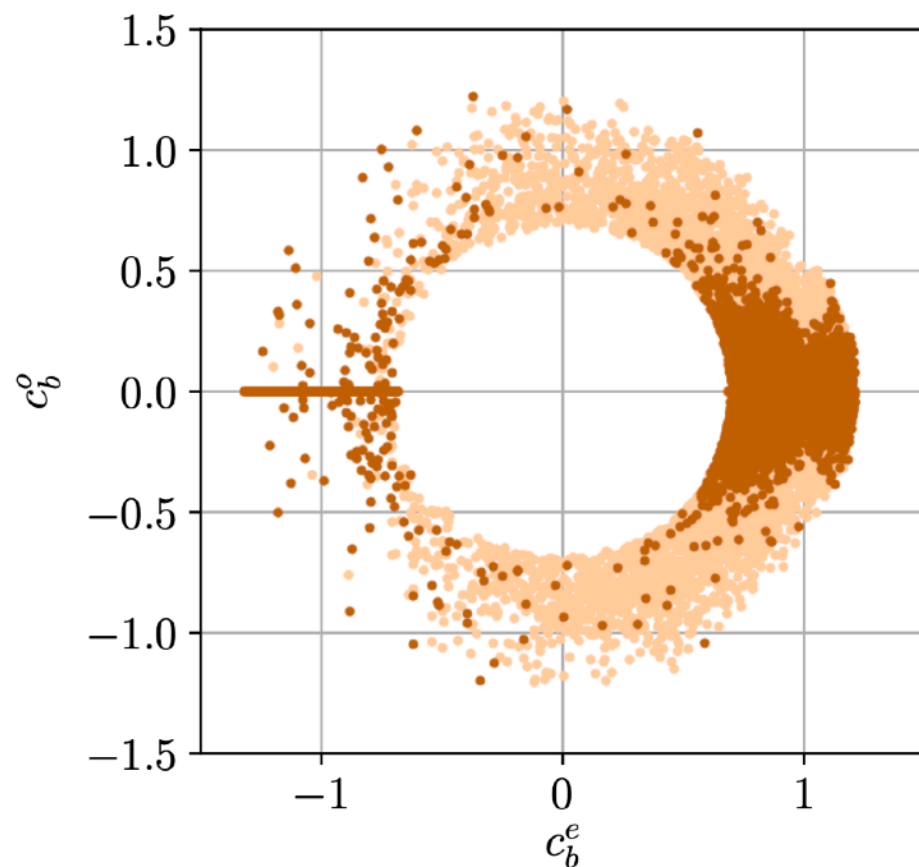
C2HDM: Type 2

- In [JHEP 02 \(2018\)073](#) they show allowed points for various 2HDM scenarios
- In Type 2 2HDM can also get points with larger $\bar{\kappa}_\tau$ not excluded for cases where $H_2 = 125$ GeV boson



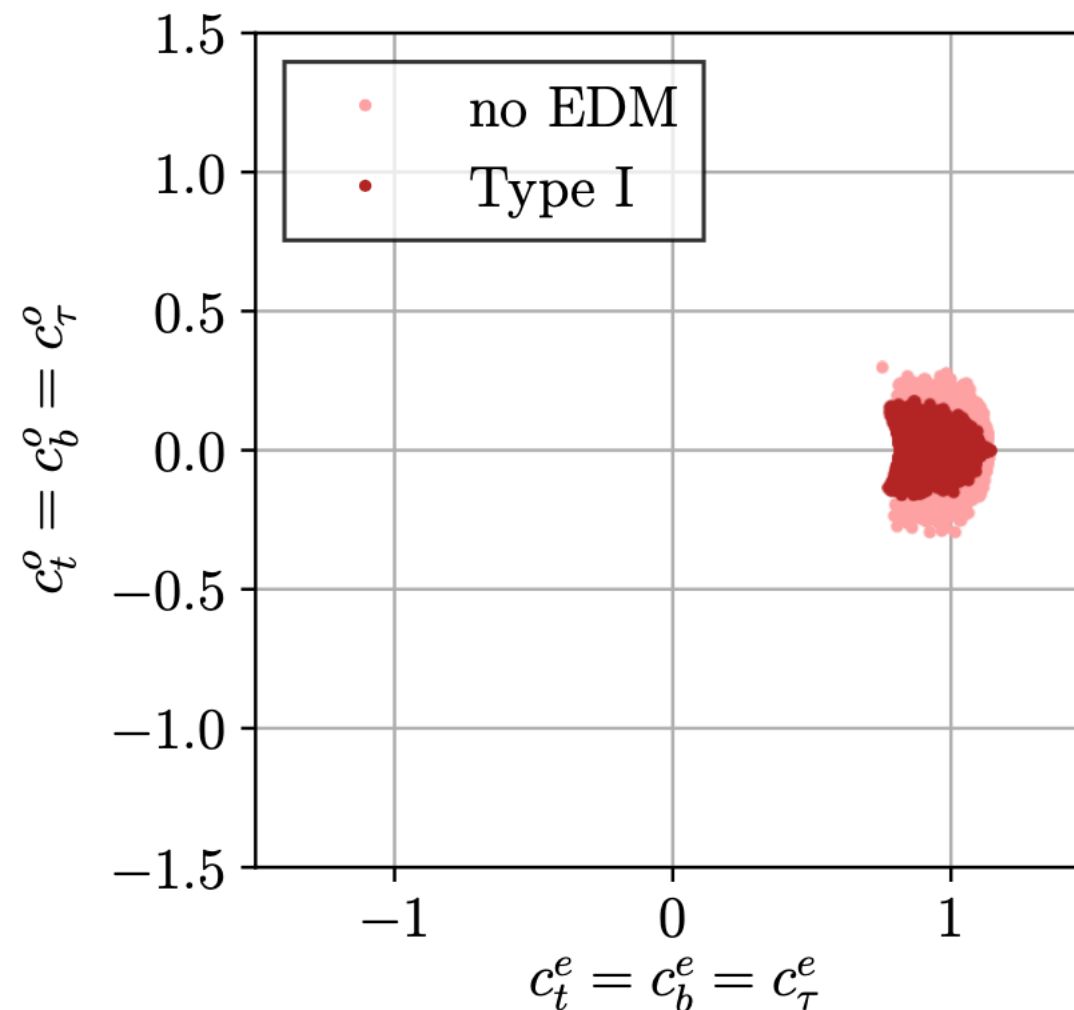
C2HDM: Type-Y

- In [JHEP 02 \(2018\)073](#) they show allowed points for various 2HDM scenarios
- In Type-Y (flipped) 2HDM where $H_1 = 125$ GeV boson
- EDMs constrain scenarios with large $\bar{\kappa}_\tau$ significantly
- But lots of points still unexplored if we could measure $\bar{\kappa}_b$



C2HDM: Type 1

- In [JHEP 02 \(2018\)073](#) they show allowed points for various 2HDM scenarios
- In Type 1 2HDM where $H_1 = 125$ GeV boson
- Most tightly constrained



NMSSM: the μ -problem

- The Higgsino mass parameter, μ , is constrained to be of order the weak scale (~ 200 GeV) by the SM phenomenology
- But naturally μ is expected to be of order the Planck scale (10^{19} GeV)
→ why is μ so small?

- The NMSSM solves the μ -problem by introducing an additional complex singlet, S

$$W_{MSSM} = \mu \hat{H}_u \hat{H}_d$$

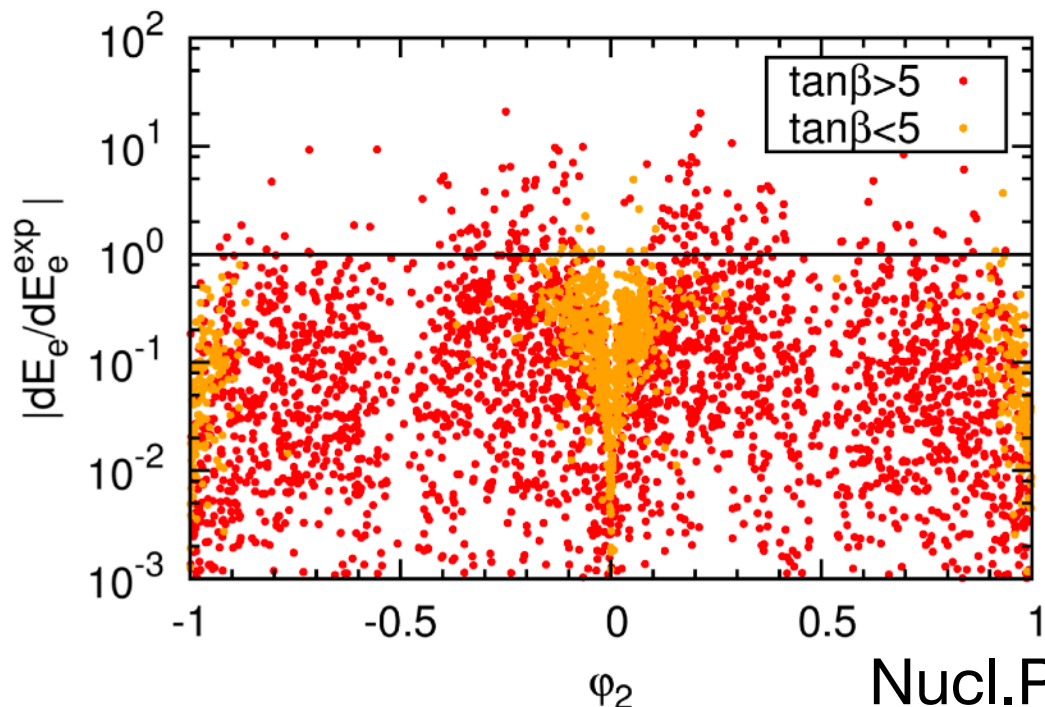
$$W_{NMSSM} = \lambda \hat{S} \hat{H}_u \hat{H}_d + \kappa \hat{S}^3$$

- In NMSSM the μ parameter is generated as the vacuum expectation value of S

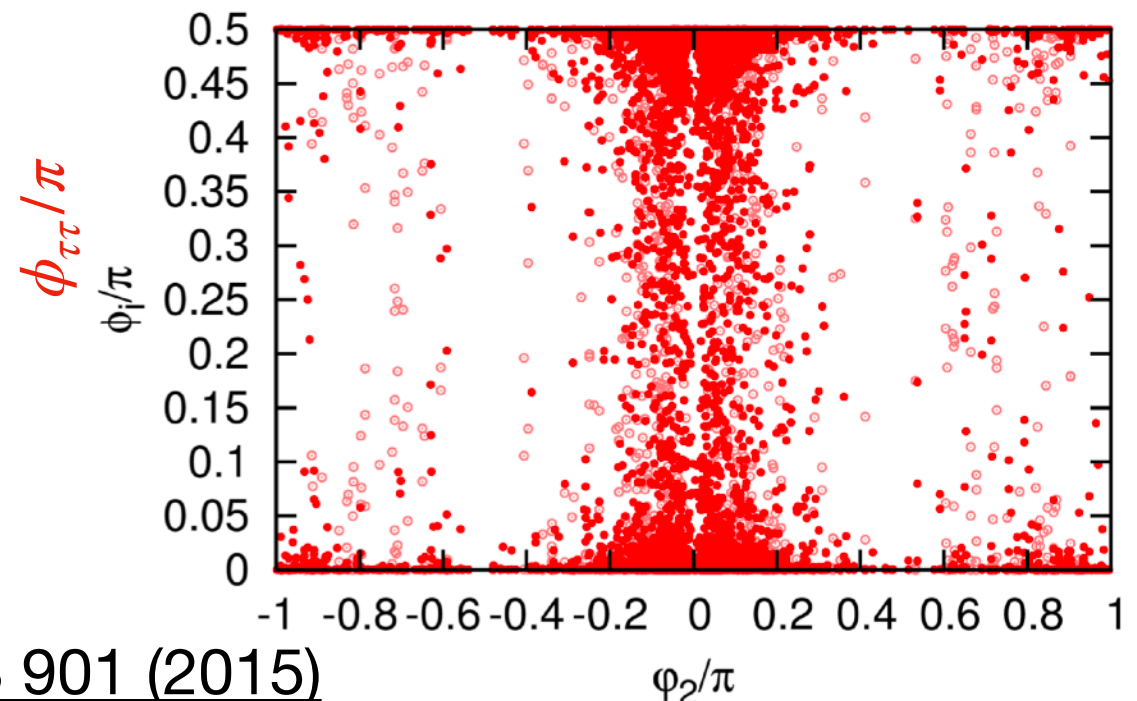
$$\mu = \lambda \langle \hat{S} \rangle$$

NMSSM

- Higgs sector in MSSM is a type 2 2HDM
 - But additional constraints on parameters means there is no CP-violation at tree level (can get CP violation at higher orders but suppressed)
 - CP-violation in MSSM probably not observable from H125 measurements
- In NMSSM Higgs sector is extended with additional complex singlet
- 7 Higgs bosons: 5 neutral + 2 charged
- Two CP-phases φ_1 (“MSSM-like” - tightly constrained) and φ_2 (“NMSSM-like” largely unconstrained)
- In examples below solid points not excluded by theory/experiment including EDMs, open points = conflict with EDMs
 - Lots of points still allowed up to $\phi_{\tau\tau} \sim 27^\circ$ - using older ACME 2013 EDM constraints

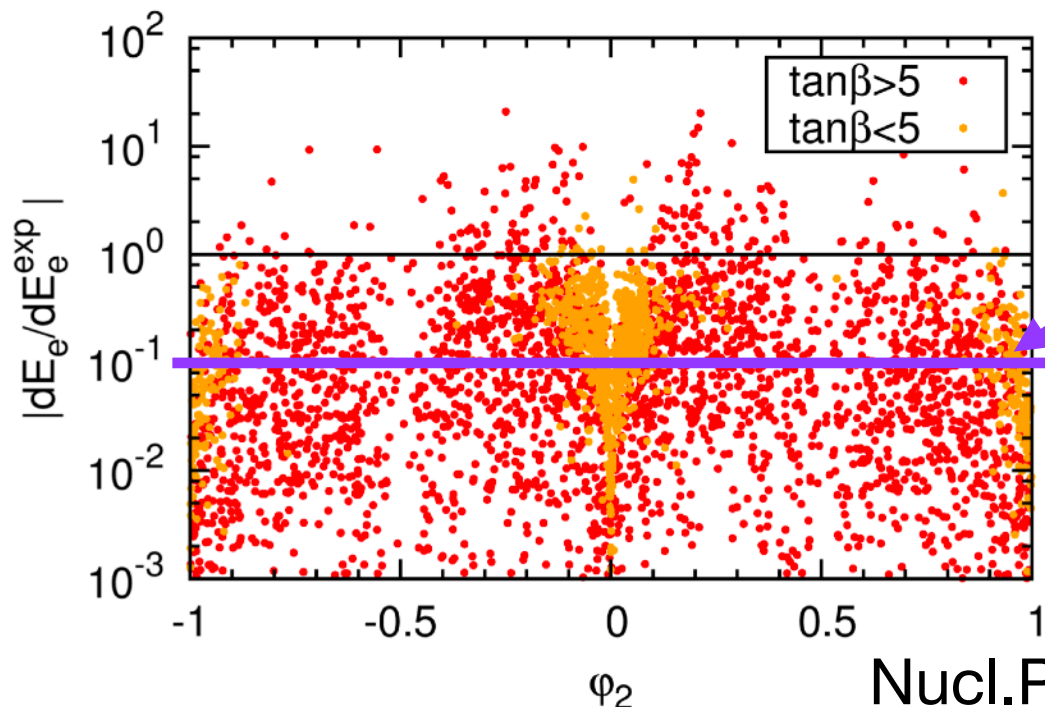


Nucl.Phys.B 901 (2015)



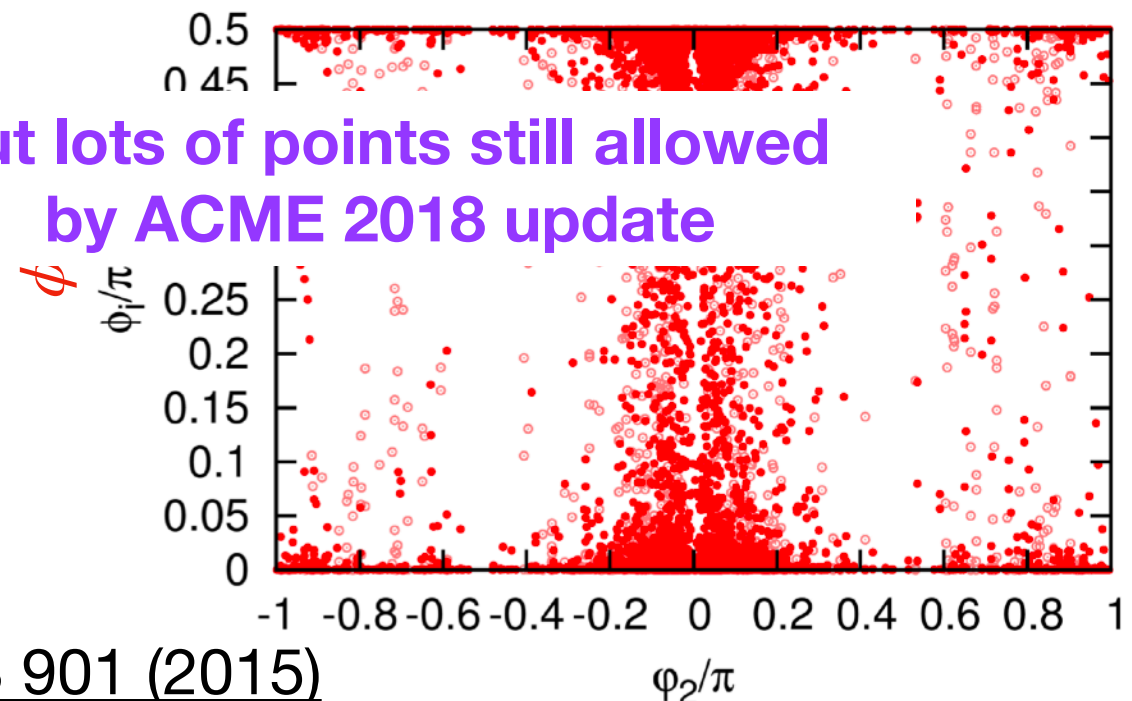
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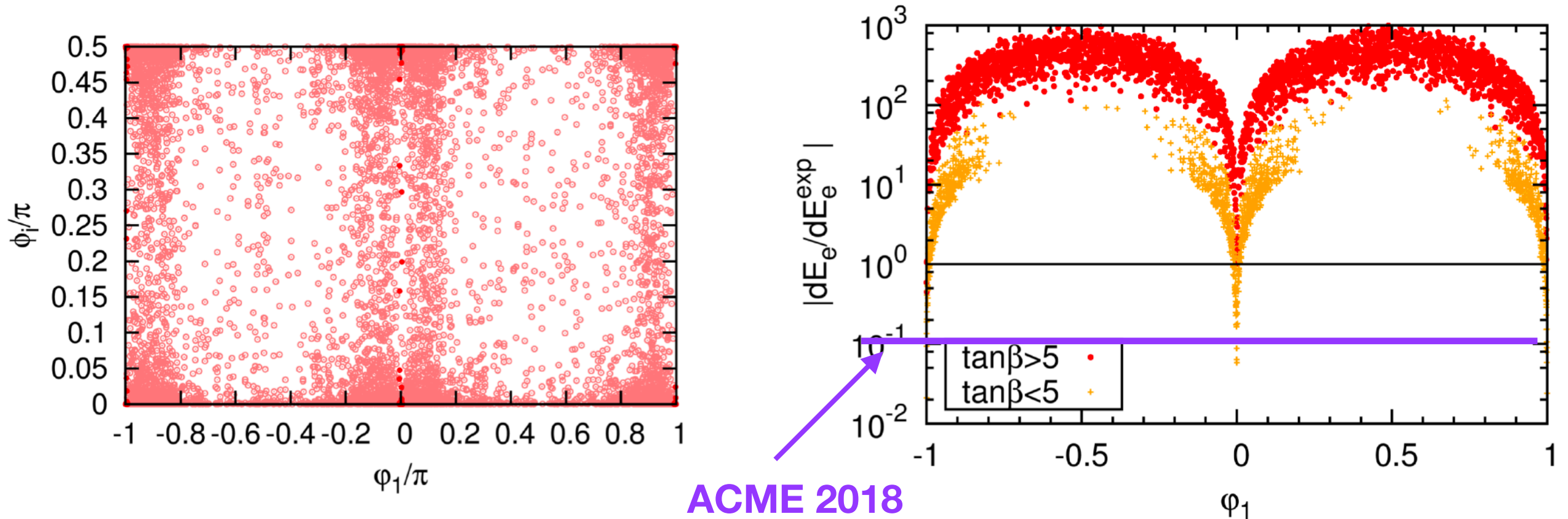
Nucl.Phys.B 901 (2015)

But lots of points still allowed
by ACME 2018 update



NMSSM: MSSM-type

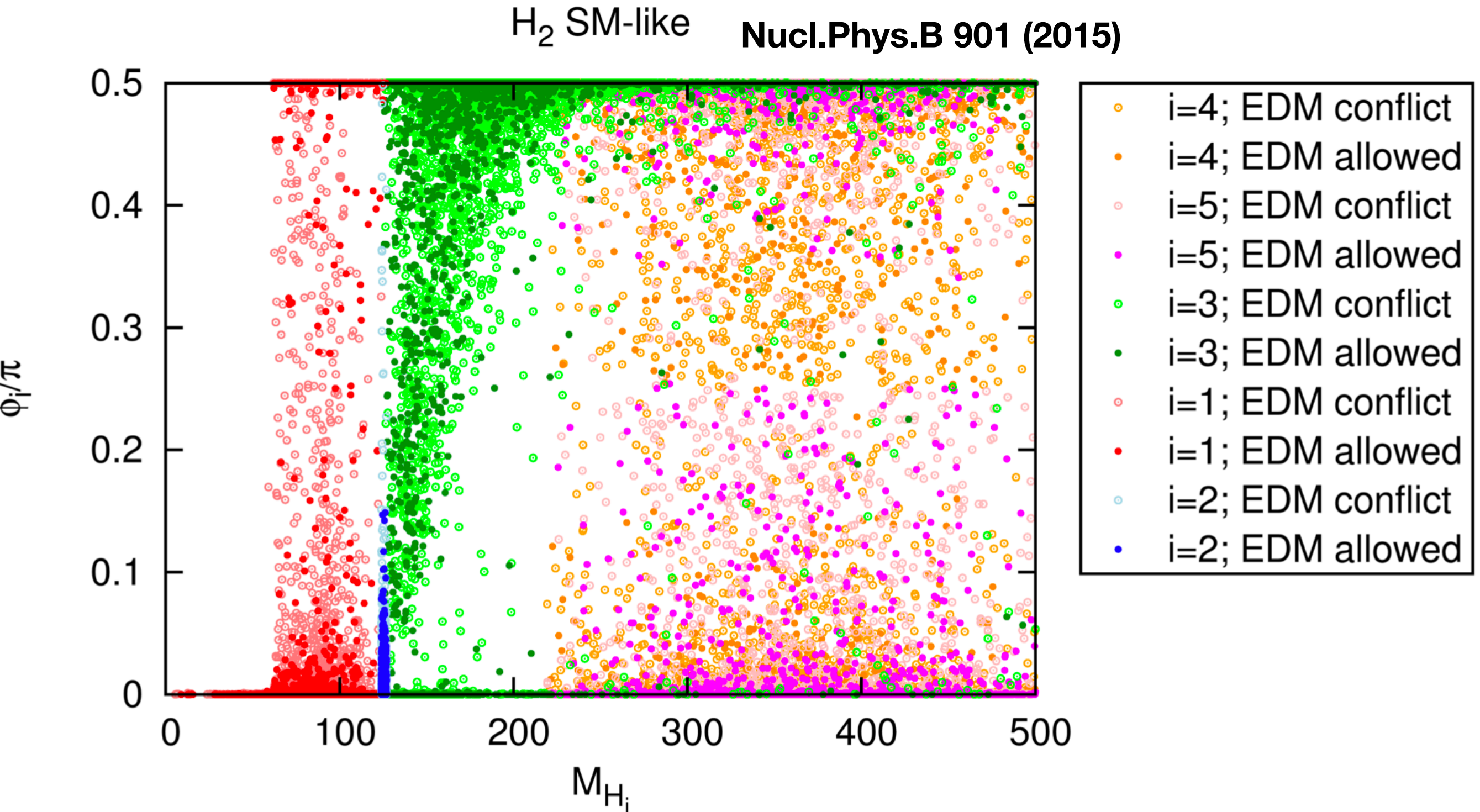
- MSSM-type CP-violation tightly constrained by EDMs
 - not many open points in left plot
 - Most points below EDM limit in right plot



Nucl.Phys.B 901 (2015)

NMSSM: Allowed H_i masses

- Allowed H_i masses



- Formulas for IP-IP method:

$$\phi^* = \arccos(\hat{\lambda}_{\perp}^{+*} \cdot \hat{\lambda}_{\perp}^{-*})$$

$$O^* = \hat{q}^{-*} \cdot (\hat{\lambda}_{\perp}^{+*} \times \hat{\lambda}_{\perp}^{-*})$$

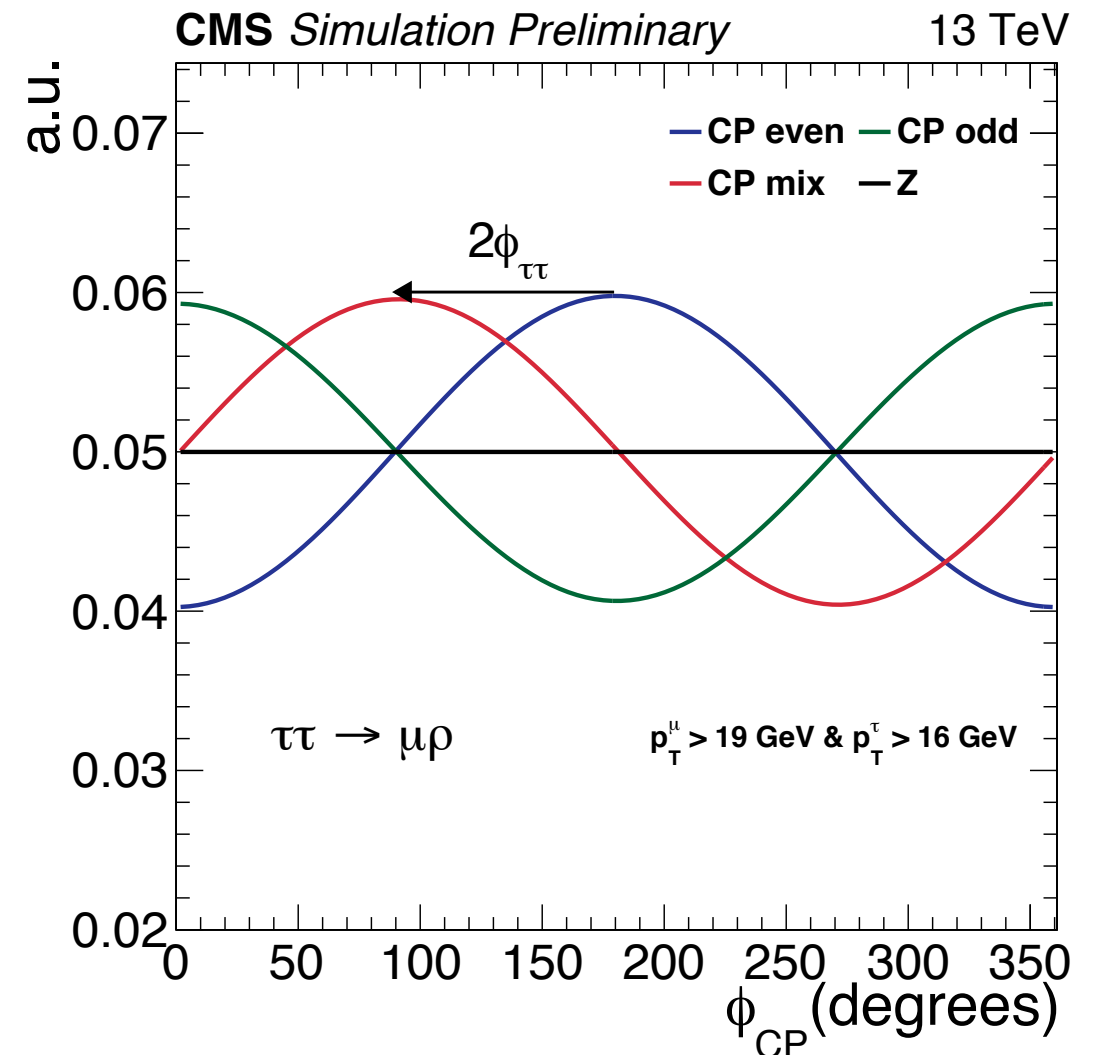
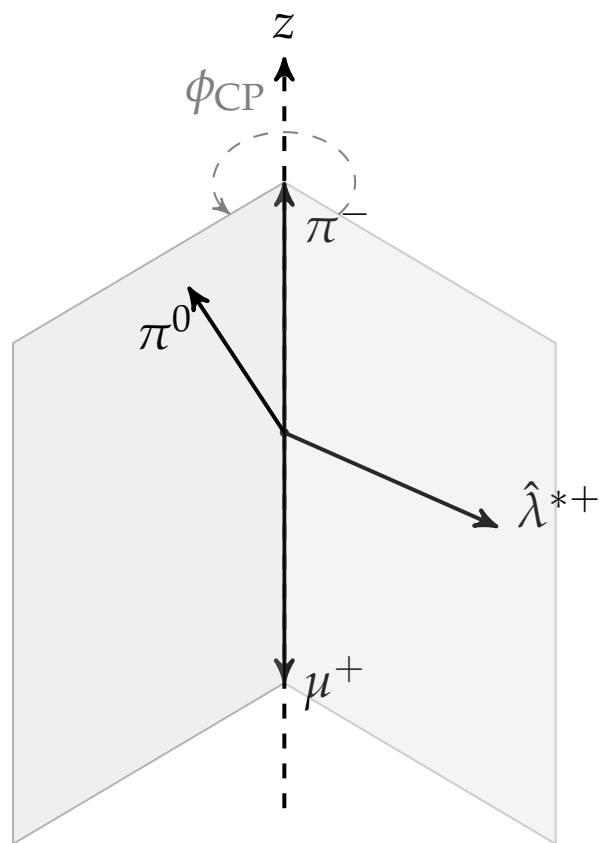
$$\phi_{CP} = \phi^*, \text{ if } O^* \geq 0$$

$$\phi_{CP} = 360^\circ - \phi^*, \text{ if } O^* < 0$$

- λ are IP vectors perpendicular to π^\pm , q is π^\pm direction vector
- “*” means we are boosted into the charged pion rest frame
- For π^0 -method and mixed-method the same formulas are used except λ is substituted with π^0 4-vectors

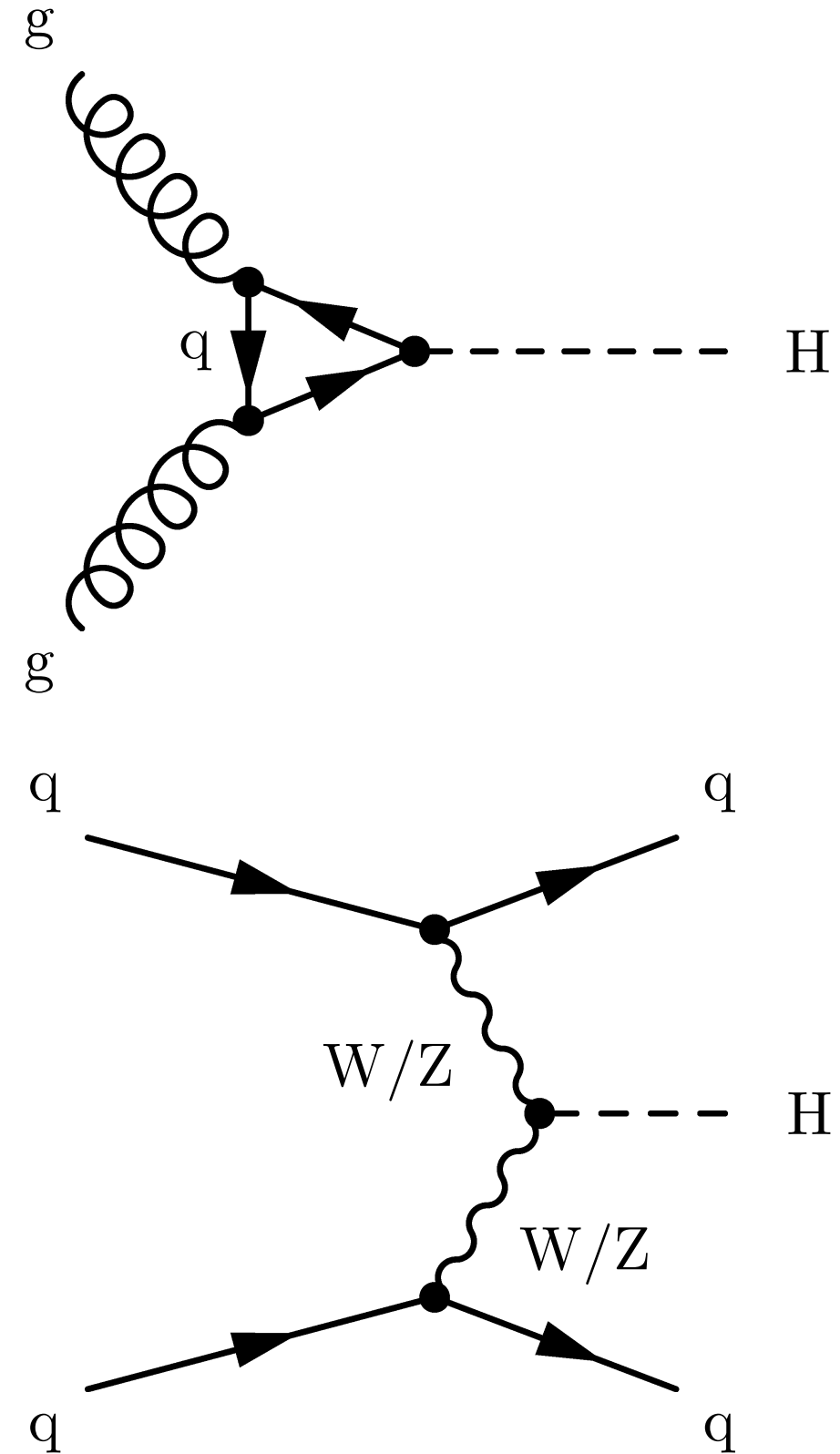
CP sensitive variables for $\tau_\mu\tau_h$ events

- Replacing $\tau \rightarrow \pi\nu$ with $\tau \rightarrow \mu\nu$ we can define equivalent CP sensitive variables for $\tau_\mu\tau_h$ channel



Signal modelling

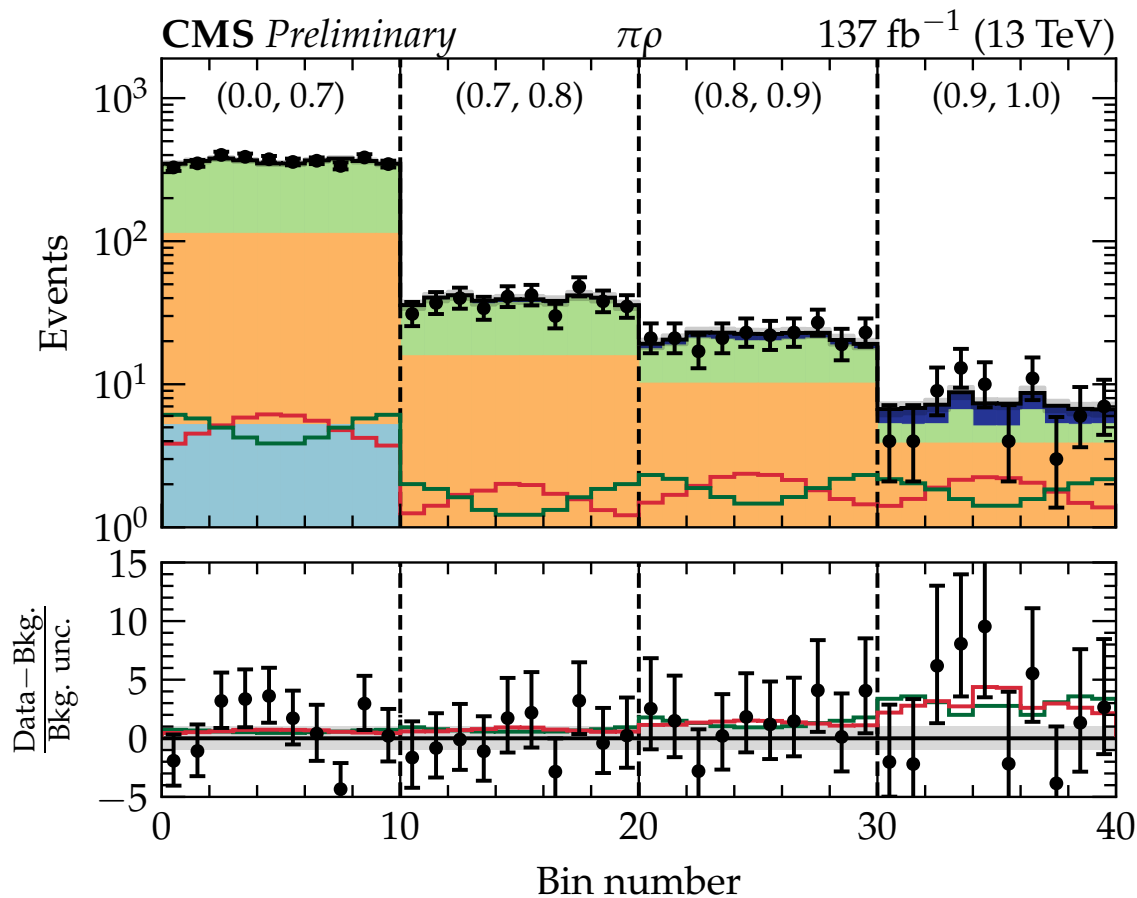
- $H \rightarrow \tau\tau$ has relatively sizeable branching ratio and is relatively clean
- Most sensitive production modes are ggH and VBF
 - ggH has larger cross section but VBF has additional jet topology to tag events
 - When we put both together we get about same sensitivity to both processes
- We assume production kinematics are SM-like and produce scalar H bosons with POWHEG-BOX-V2
- $H \rightarrow \tau\tau$ decays handled by Pythia 8.2
 - We force taus to decay without spin correlations
 - Spin effects then added back using weights computed with TauSpinner ([arXiv:1802.05459](https://arxiv.org/abs/1802.05459))
 - This has advantage that we can use a single MC sample to model any generic CP scenario



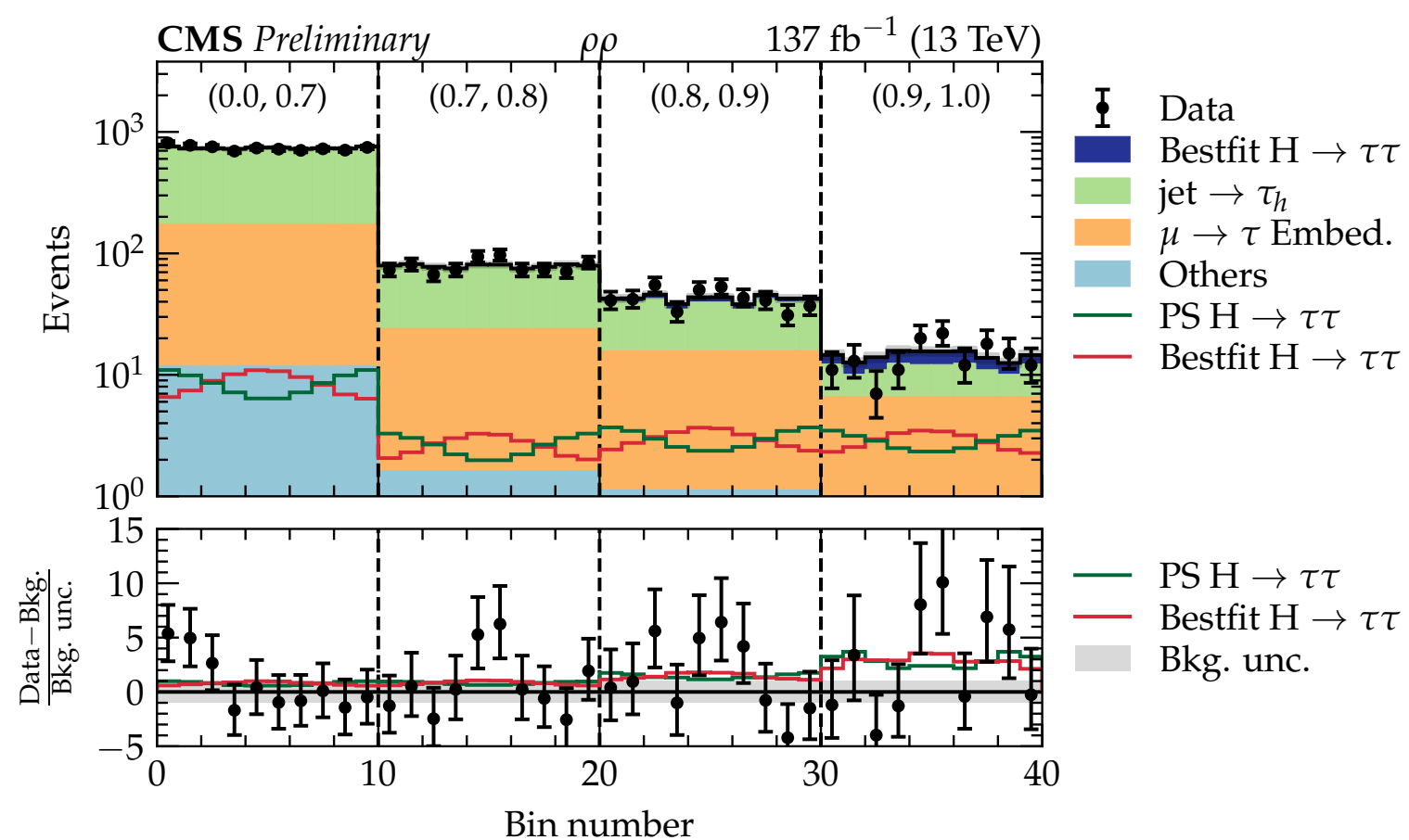
More examples of signal categories

- Two more examples of signal categories for $\tau_h\tau_h$ final states

$$\tau_h\tau_h \rightarrow \pi^- \nu \rho^+ \nu$$

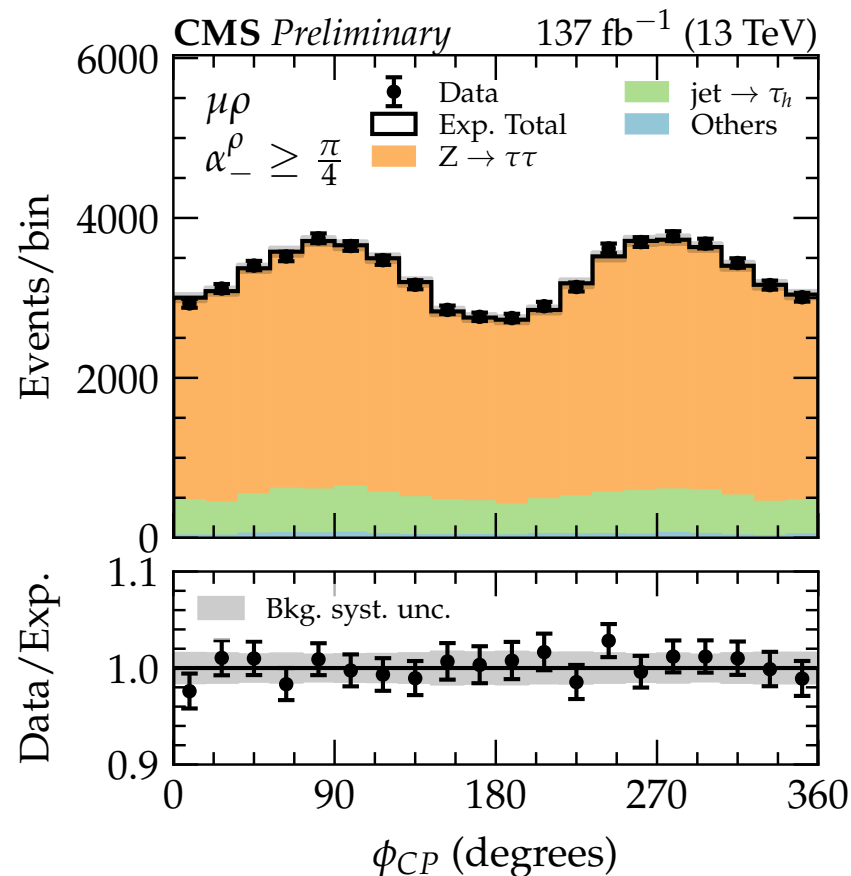
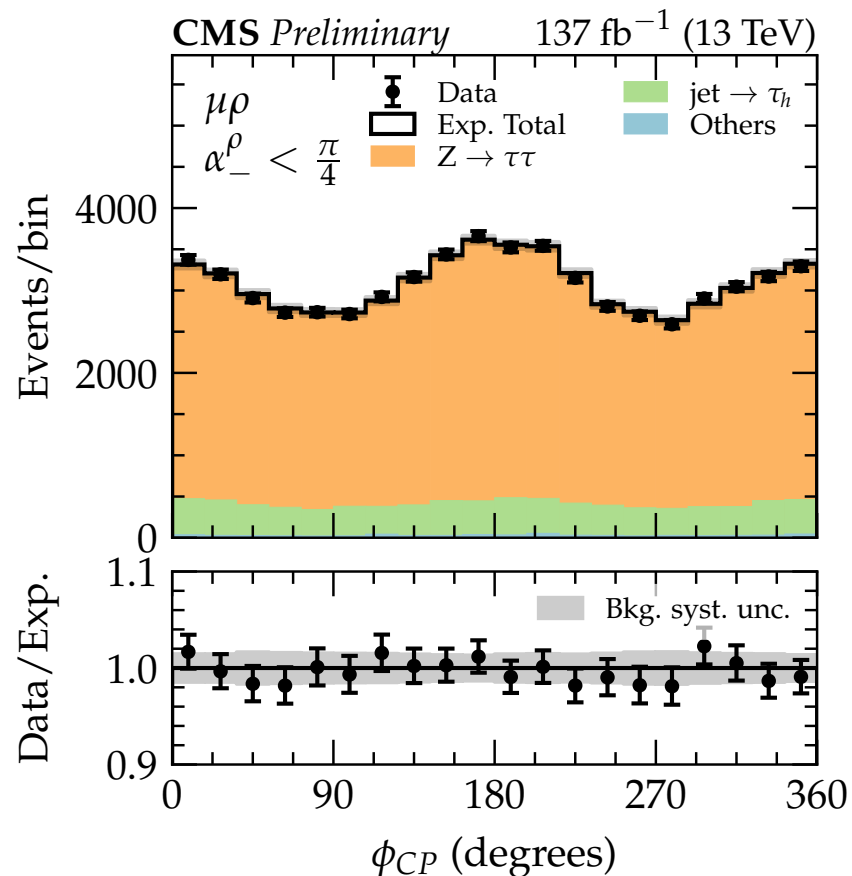


$$\tau_h\tau_h \rightarrow \rho^- \nu \rho^+ \nu$$



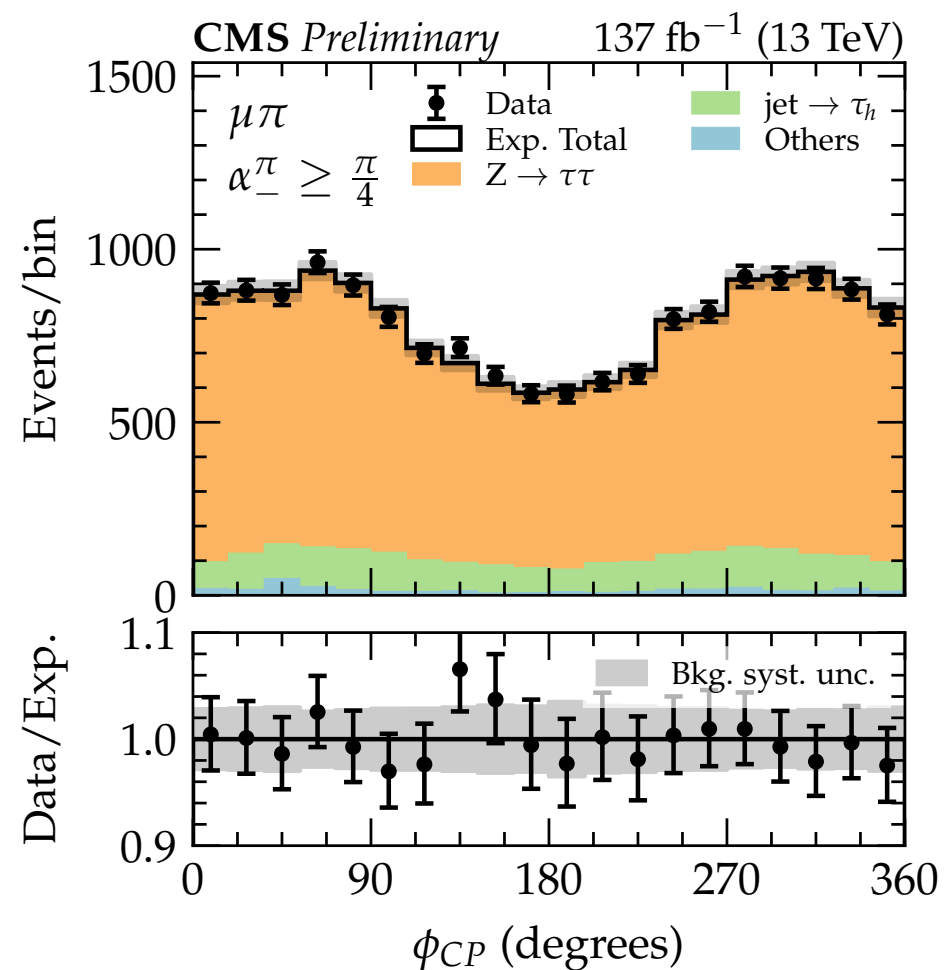
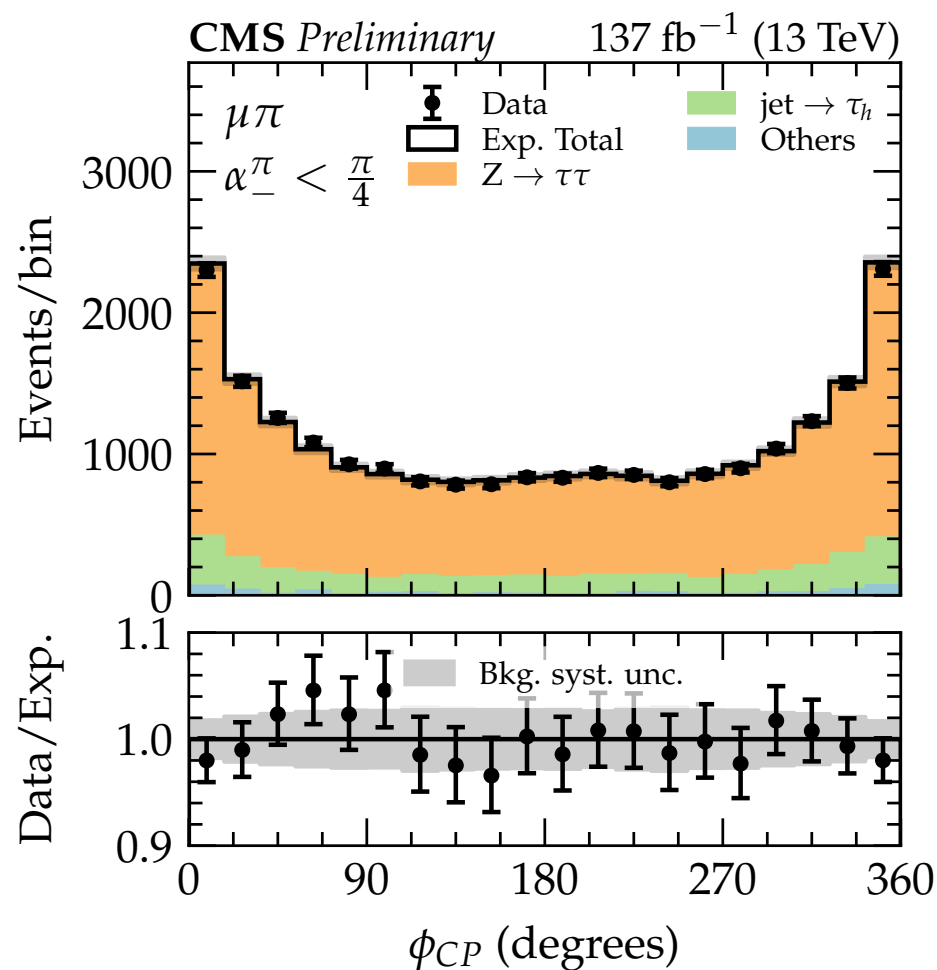
Checks using $Z \rightarrow \tau\tau$

- All $H \rightarrow \tau\tau$ analyses use $q\bar{q} \rightarrow Z \rightarrow \tau\tau$ events as “standard candle” to validate MC description of data
- Same for the CP-analysis except as $Z \rightarrow \tau\tau$ has \sim flat distribution of $\phi_{\tau\tau}$
- But we can split into two sinusoidal contributions using α - variable
 - Separates events into those “nearly coplanar” ($\alpha < \pi/4$) and “nearly perpendicular” ($\alpha > \pi/4$) to $q\tau$ plane in lab frame
- Definition in paper by Stefan Berge et al.



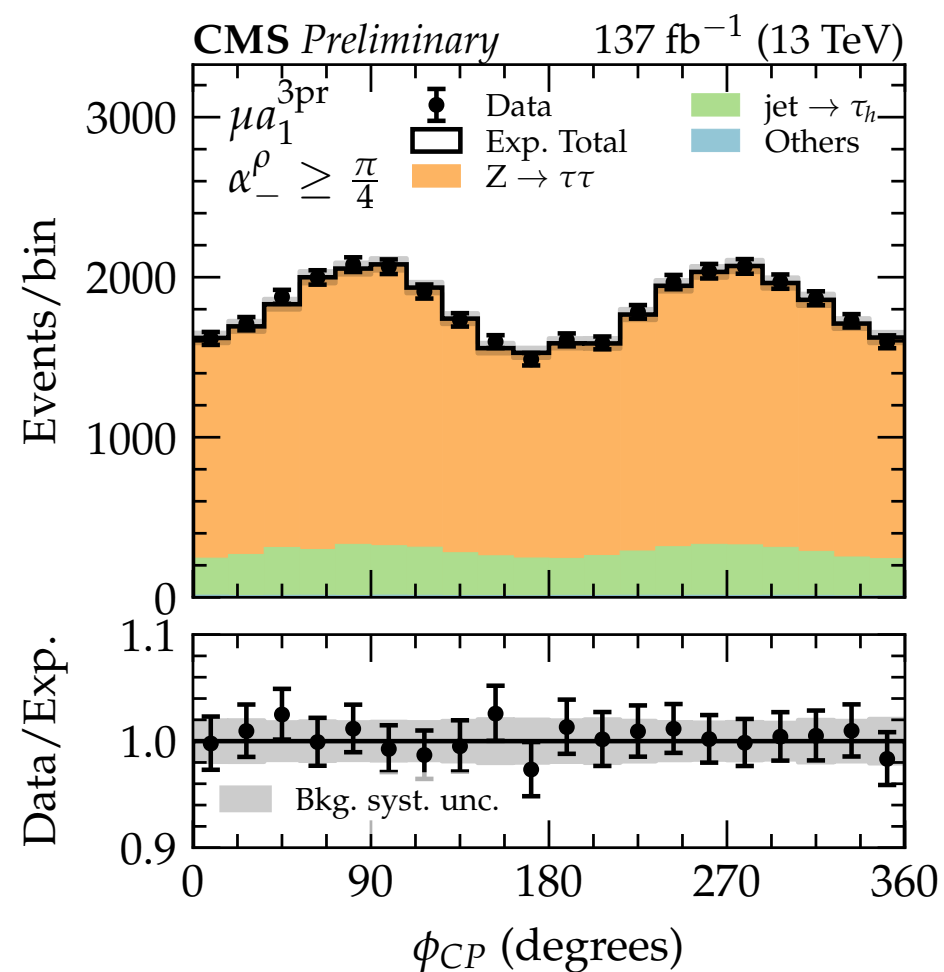
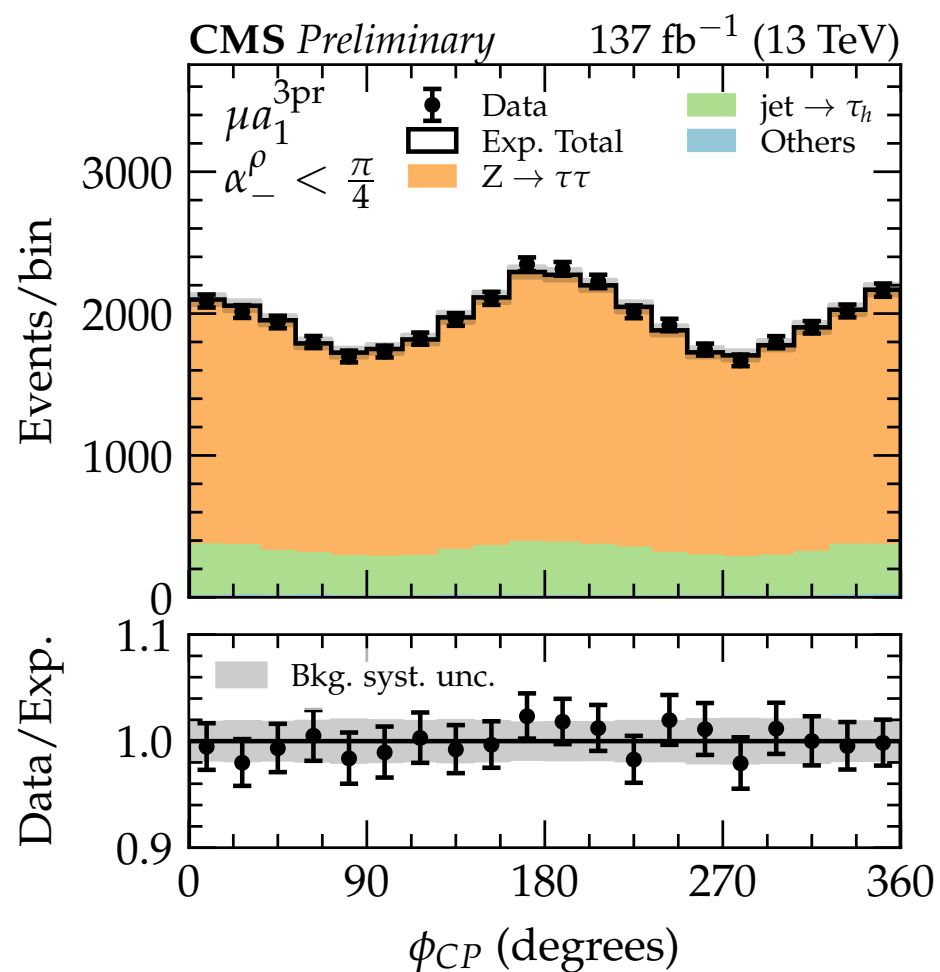
Checks using $Z \rightarrow \tau\tau$: $\tau_h \rightarrow \pi\nu$

- Check of $Z \rightarrow \tau\tau$ using α -splitting for $\tau_h \rightarrow \pi\nu$
- Definition in paper by [Stefan Berge et al.](#)



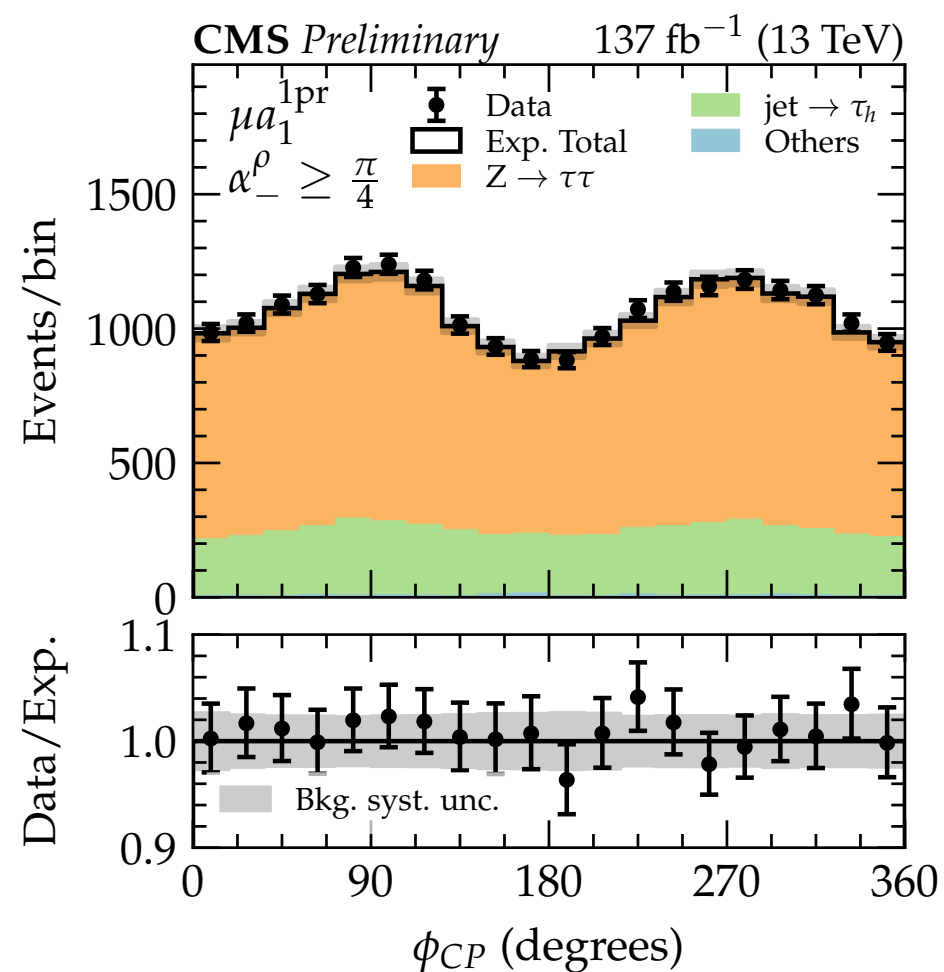
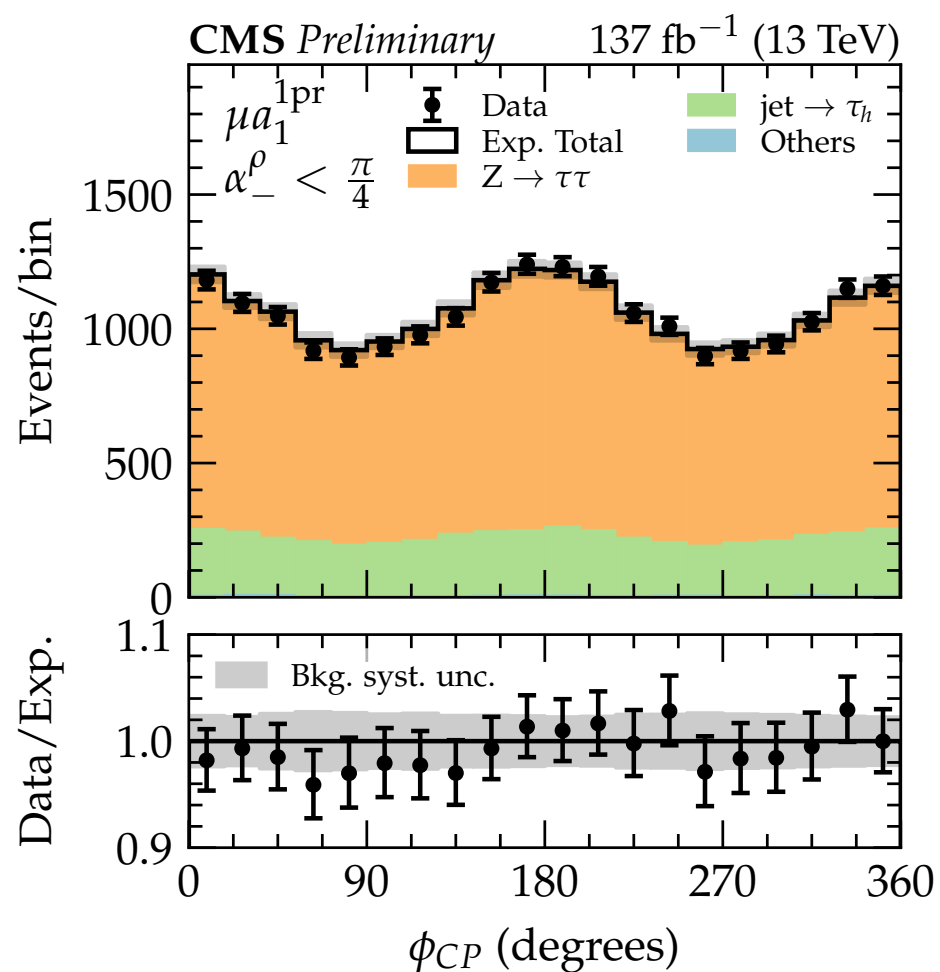
Checks using $Z \rightarrow \tau\tau$: $\tau_h \rightarrow a_1 v \rightarrow \pi^- \pi^+ \pi^+ v$

- Check of $Z \rightarrow \tau\tau$ using α -splitting for $\tau_h \rightarrow a_1 v \rightarrow \pi^- \pi^+ \pi^+ v$
- Definition in paper by [Stefan Berge et al.](#)

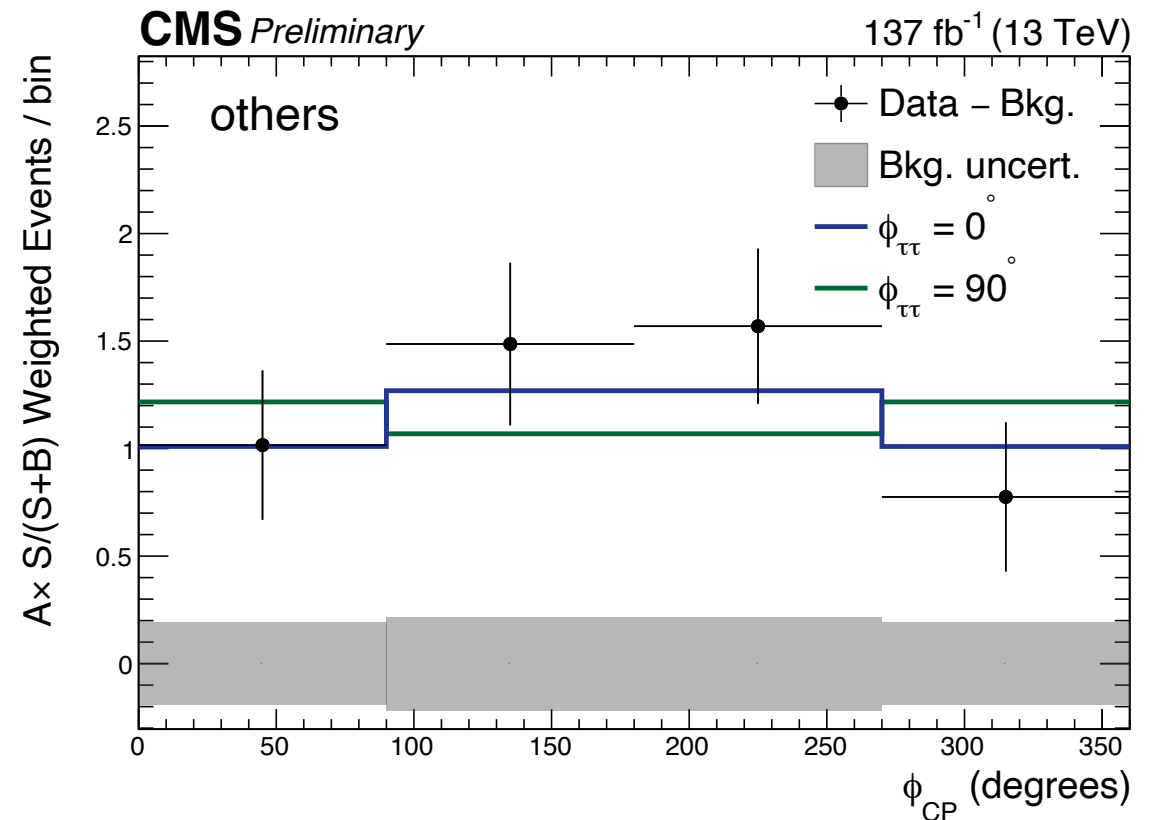
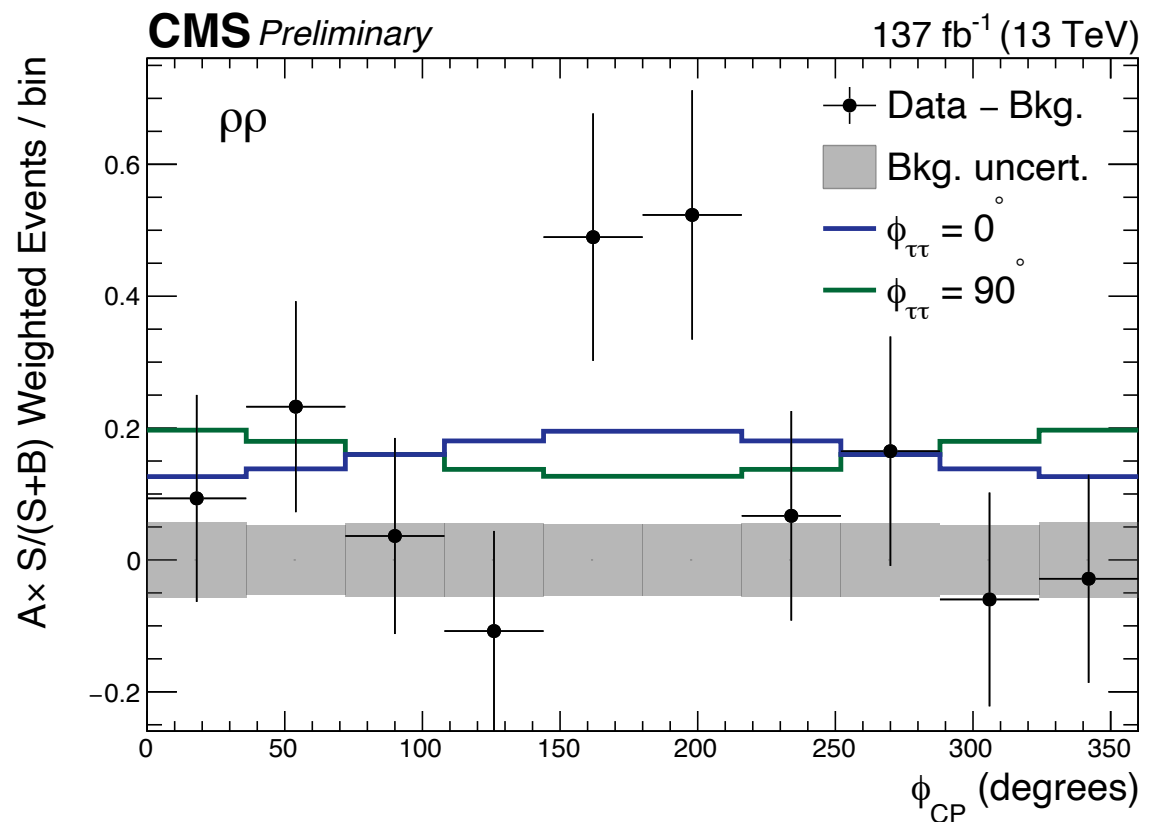
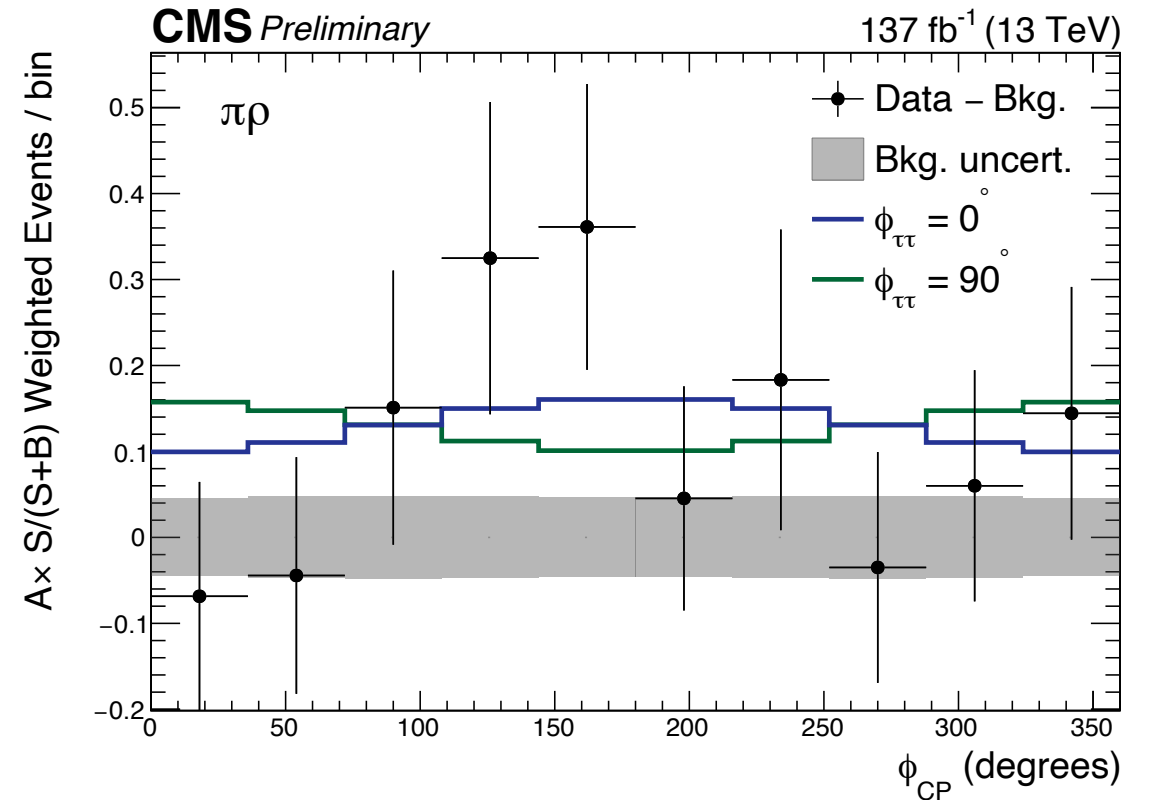
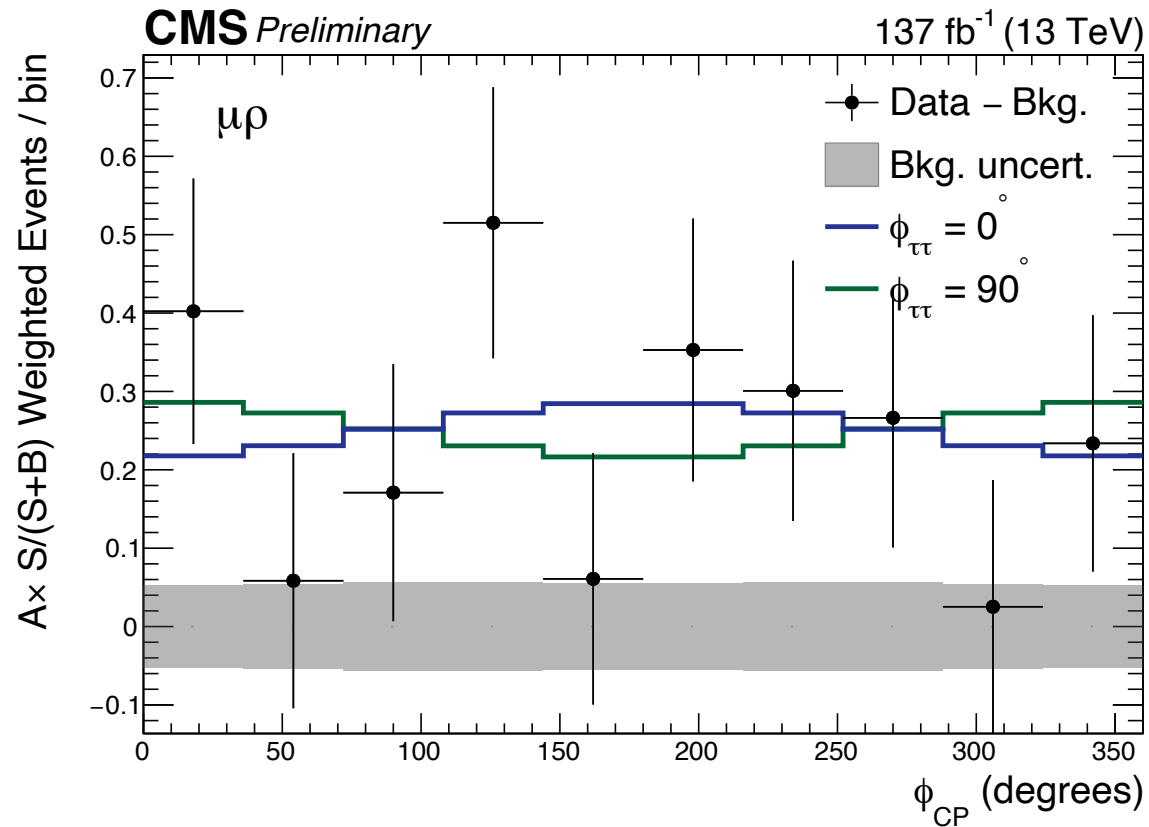


Checks using $Z \rightarrow \tau\tau$: $\tau_h \rightarrow a_1 v \rightarrow \pi^- \pi^0 \pi^+ v$

- Check of $Z \rightarrow \tau\tau$ using α -splitting for $\tau_h \rightarrow a_1 v \rightarrow \pi^- \pi^0 \pi^+ v$
- Definition in paper by [Stefan Berge et al.](#)



ϕ_{CP} distribution by channel



Polarimetric vectors

- Polarimetric vectors for $\tau_h \rightarrow \pi \nu$ and $\tau_h \rightarrow \rho \nu$ decays

$$\tau^\pm \rightarrow \pi^\pm \nu : \vec{h} = -\vec{n}_\pi$$

$$\tau^\pm \rightarrow \rho^\pm \nu \rightarrow \pi^\pm \pi^0 \nu : \vec{h} = m_\tau \frac{2(qN)\vec{q} - q^2\vec{N}}{2(qN)(qP) - q^2(NP)}$$

m_τ : τ mass

q : $\pi^\pm - \pi^0$

N : $\nu = \tau^\pm - \pi^\pm - \pi^0$

P : τ^\pm

} 4-vectors

- Defined in rest frame of τ 's
- More complicated for a_1 decays but parameterisation from the CLEO collaboration exists ([Phys. Rev. D61 \(2000\) 012002](#))

Future ee colliders

- Circular Electron-Positron Collider (CEPC): [arXiv:811.10545](https://arxiv.org/abs/1808.07248)
- Future Circular Collider (FCC)-ee: [Eur. Phys. J. ST 228, no.2, 261-623 \(2019\)](https://arxiv.org/abs/1902.00013)
- International Linear Collider: [arXiv.org:1306.6352](https://arxiv.org/abs/1306.6352)
- Integrated luminosities / energies used to compute sensitivities in [arXiv:2012.13922](https://arxiv.org/abs/2012.13922):

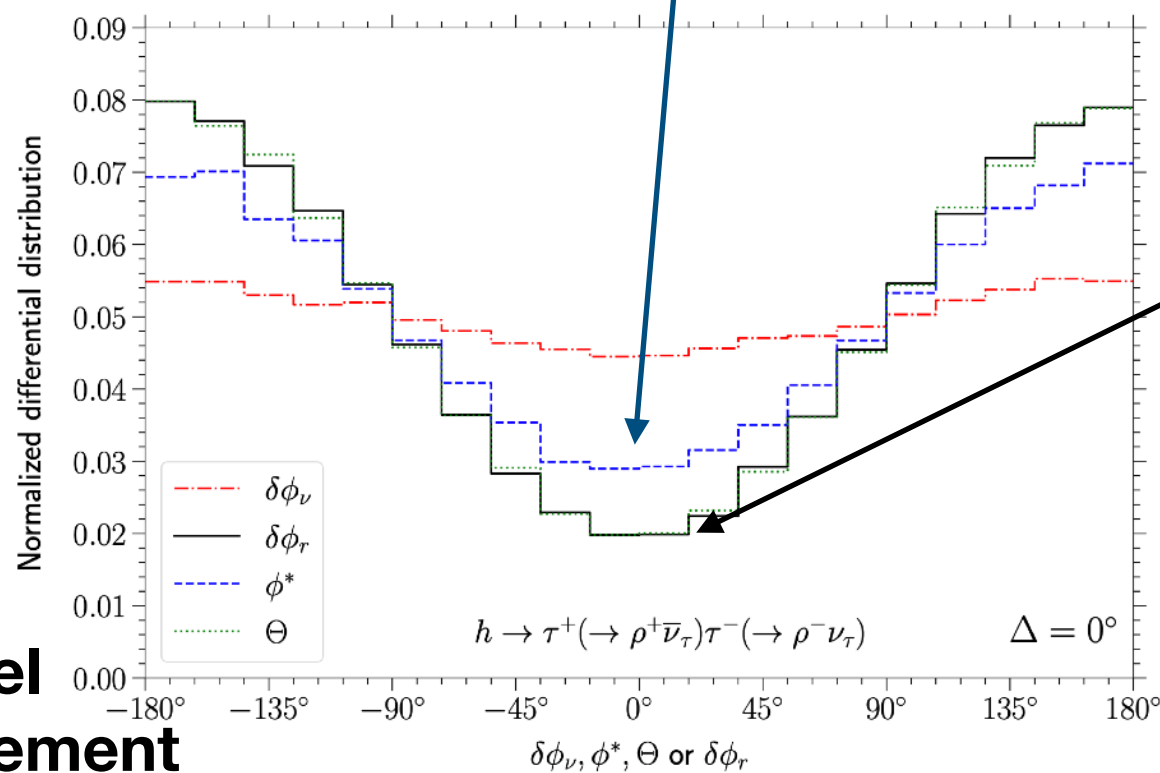
	Integrated luminosity	\sqrt{s}	Number of Higgs bosons
CEPC [7]	5.6 ab^{-1}	240 GeV	1.1×10^6
FCC-ee [8]	5 ab^{-1}	240 GeV	1.0×10^6
ILC [9]	2 ab^{-1}	250 GeV	0.64×10^6

Table 1: Configurations (integrated luminosity, energy \sqrt{s} , and Higgs production rate) at the future lepton colliders CEPC, FCC-ee, and ILC.

Future measurements: lepton colliders

- Lepton colliders have advantage of being able to constrain Higgs 4-vector in both transverse and longitudinal directions
 - Much cleaner environment which is good for precision measurements
 - Can fully constrain system (i.e estimate neutrinos) in several channels
 - Once system is constrained can estimate polarimetric vector, \mathbf{h} , for each taus - \mathbf{h} points in most likely direction of tau spin
 - Angle between \mathbf{h} 's, $\delta\phi_r$, sensitive to $\phi_{\tau\tau}$
- Several publications out there that estimate sensitivity at ee colliders e.g [arXiv:2012.13922](https://arxiv.org/abs/2012.13922) - summarised below

ϕ_{CP} - as used by CMS



	68% C.L. for $m = 1$
CEPC	2.9°
FCC-ee	3.2°
ILC	3.8°

Results here take into account $\rho\rho$, $\pi\rho$, and $\pi\pi$ channels only

$\rho\rho$ channel

~ 30% improvement