

$B \rightarrow D\bar{D}h$ decays: a new (virtual)
laboratory for exotic particle searches

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28 04 2021

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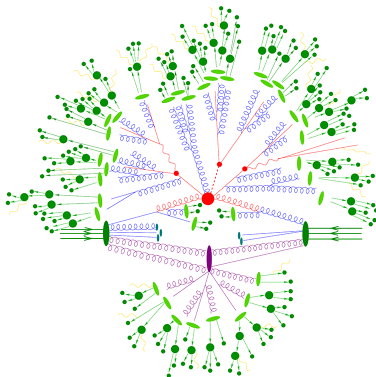




Outline

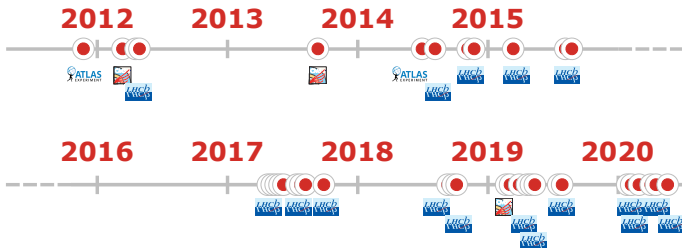
1. Introduction
2. Datasets
3. Model-independent analysis [arXiv:2009.00025] (published PRL)
4. Amplitude analysis [arXiv:2009.00026] (published PRD)
5. Reaction
6. Conclusion

The mystery of hadronisation



- QCD: successful and predictive. Perturbative at hard scales
- Hadronisation models in lieu of analytical solutions
- **Least-well understood aspect of the SM.** How to improve?

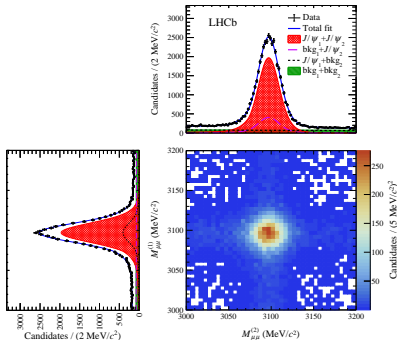
The allure of spectroscopy



- The LHC brought a wealth of new particles: **59 new hadrons**
- Great deal of attention: 1,398 citations
- Crucial inputs for hadronisation model-builders

Bump-hunting can get you far...

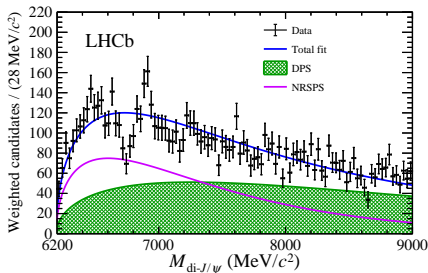
arXiv:2006.16957 LHCb combines $J/\psi \rightarrow \mu^+ \mu^-$ pairs:



- Striking correlated production, signal: $33, 570 \pm 230$
- Double parton scattering background has a lower $p_T^{J/\psi J/\psi}$: apply threshold cut or bin in this quantity

Bump-hunting can get you far...

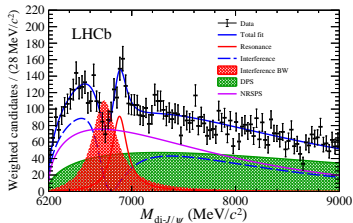
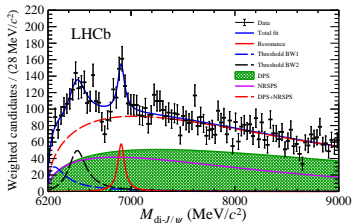
Constrain J/ψ masses and point J/ψ 's back to shared vertex



- Obvious narrow feature at 6.9 GeV/c²
- Broader component between 6.2 and 6.8 GeV/c²
- Overall distribution inconsistent with NRSPS+DPS at 3.4 σ

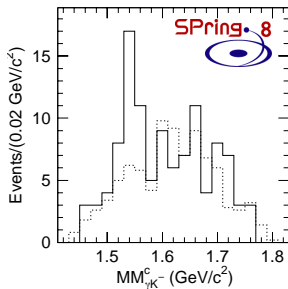
Bump-hunting can get you far...

Constrain $J\psi$ masses and point $J\psi$'s back to shared vertex



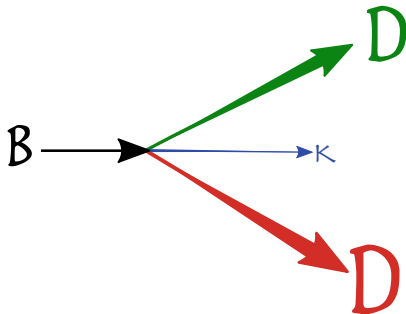
- **Model 1:** two on-threshold BW shapes, and narrow $X(6900)$
- **Model 2:** allow threshold BW and NRSPS components to interfere, and narrow $X(6900)$
- Both the threshold and $X(6900)$ structures significant at $> 5\sigma$
- **Interpretation:** $T_{ccc\bar{c}}$ resonance? Via feed-down?
Near-threshold enhancement due to rescattering? J^{PC} ?

... but beware the (original) pentaquark!

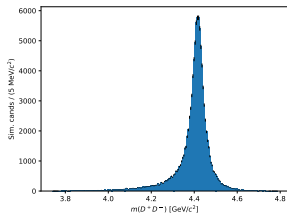


- $uudd\bar{s}$ state predicted in 1997 [arXiv:hep-ph/9703373](https://arxiv.org/abs/hep-ph/9703373)
- Excess seen in 2003 in $\gamma d \rightarrow K^+ K^- np$ [arXiv:hep-ex/0301020](https://arxiv.org/abs/hep-ex/0301020)
- Bumps 'confirmed' by 9 other experiments
- Un-discovered by CLAS, Belle, ... 'beautiful' post-mortum:
[arXiv:1003.1098](https://arxiv.org/abs/1003.1098)

The power of exclusive reconstruction



- Fully reconstructed decay
- Much more than a bump-hunt
- Toy $B^+ \rightarrow [\psi(4415) \rightarrow D^+ D^-] K^+$

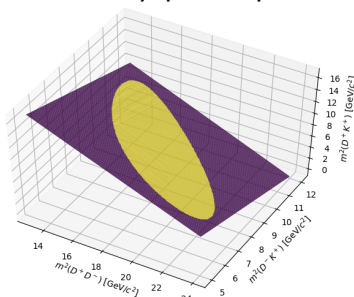


The power of exclusive reconstruction

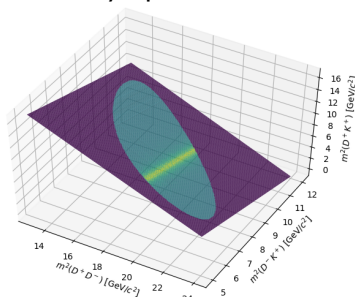
- Conservation of four-momentum in the decay:

$$m_B^2 + 2m_D^2 + m_K^2 = m_{D^+D^-}^2 + m_{D^-K^+}^2 + m_{D^+K^+}^2$$

Toy: phase-space



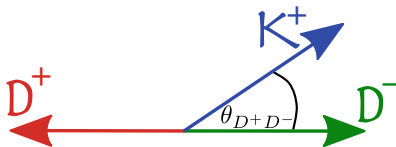
Toy: spin-0



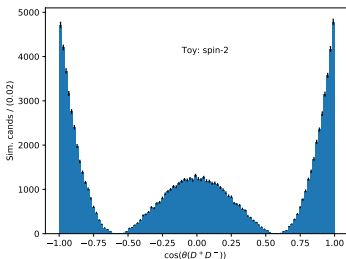
- Two degrees of freedom, within kinematic limits
- Intermediate resonances produce non-uniform structure

The power of exclusive reconstruction

- Strong $X \rightarrow 2P$ decay: resonances have $J^P = 0^+, 1^-, 2^+, \dots$
- Resonance spin dictates angular structure



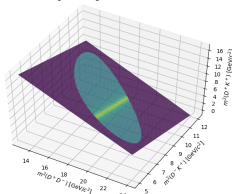
- Resonance (e.g. 2^+) decaying to $D^+ D^-$: intuitive $\theta_{D^+D^-}$ shape



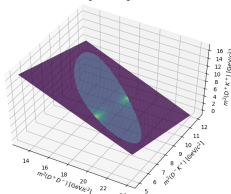
The power of exclusive reconstruction

- Spin-dependent helicity-angle maps onto phase-space plane

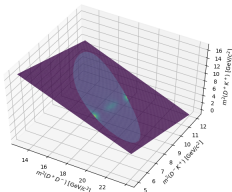
Toy: spin-0



Toy: spin-1



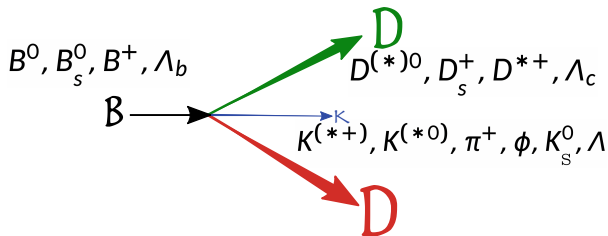
Toy: spin-2



- We'll always project onto one pair of these axes: 'Dalitz plot'

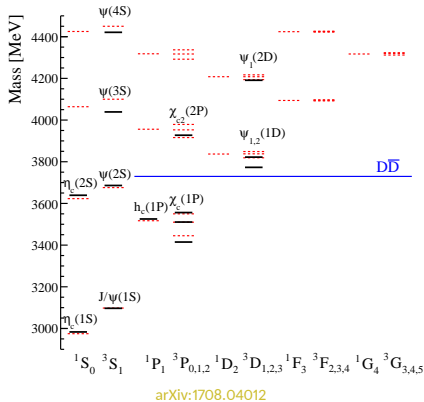
What do we mean by $B \rightarrow D\bar{D}h$?

- Huge family of topologically similar decays



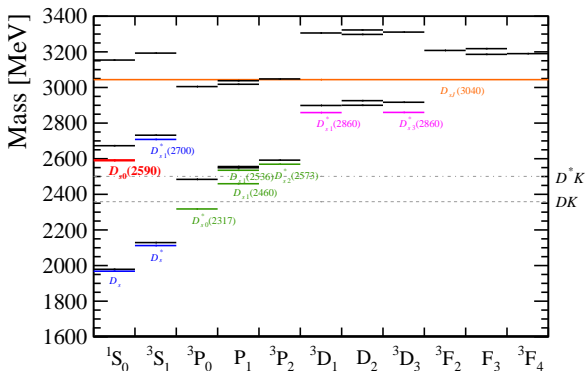
- Abundantly produced at LHC
- Efficient hadronic trigger
- Very clean topology
- Resonant structure explored for only three of the decays

Relevance: the charmonium spectrum



- Recent success probing with open-charm pairs [arXiv:1903.12240](https://arxiv.org/abs/1903.12240)
- Many states remain to be observed
- Sensitivity via $B \rightarrow \{D^+D^-, D^0\bar{D}^0, D_s^+D_s^-, \Lambda_c^+\Lambda_c^-\}K$

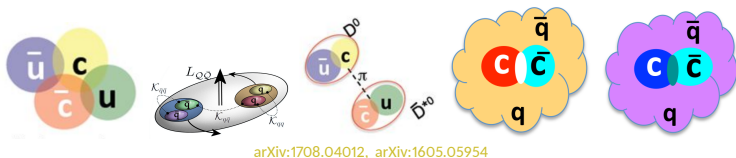
Relevance: the charm-strange spectrum



arXiv:2011.09112

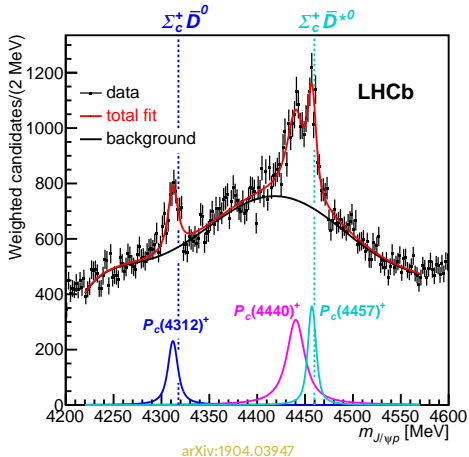
- Solid progress through $B \rightarrow Dhh$ amplitude analyses [arXiv:1407.7574](https://arxiv.org/abs/1407.7574)
- Large samples anticipated for many $B \rightarrow \bar{D}D^0K^+$ decays

Relevance: charmonium-like exotica



- Lots of exotic candidates with varying degrees of mystery...
- ... many models to describe them! More experiment needed
- Illucidate open questions e.g. $\chi_{c1}(3872)$ internal composition
 - Study production, lineshape, etc in $B^+ \rightarrow D^{*0} \bar{D}^0 K^+$ decays
- Study the charged charmonium-like states e.g. Z_c^+
 - Search in $B \rightarrow D^{*+} \bar{D}^{(*)0} K$ decays

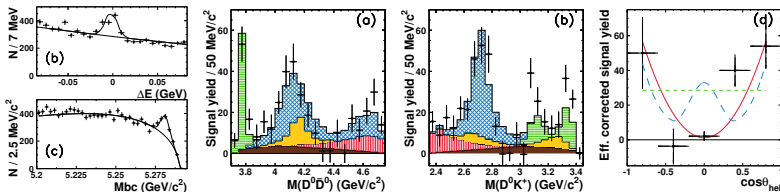
Relevance: pentaquarks



- Pentaquarks only seen in $\Lambda_b \rightarrow J/\psi p K$ decays
 - Same $c\bar{c}uud$ quark content in $\Lambda_b \rightarrow \Lambda_c^+ \bar{D}^0 K$ decays

Experimental success elsewhere: Belle

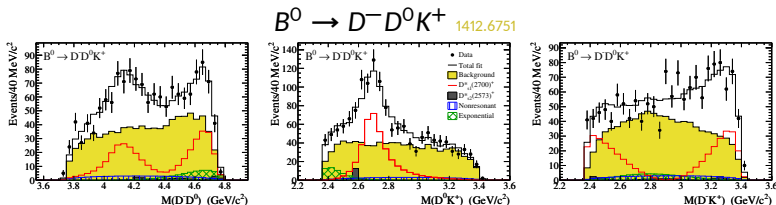
- $B^+ \rightarrow D^0 \bar{D}^0 K^+$: pioneering 2008 paper, $414 \text{ fb}^{-1} e^+ e^-$ [0707.3491](#)



- Clear observation of $D_{s1}(2700)^+ \rightarrow D^0 K^+$ resonance
- Strong evidence for its $J^P = 1^-$ character
- Signal of 399 ± 40 candidates
- Fighting an irreducible continuum background of similar size

Experimental success elsewhere: BaBar

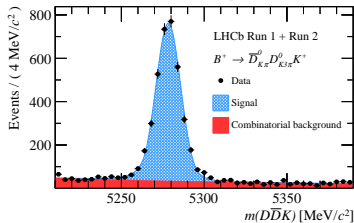
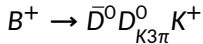
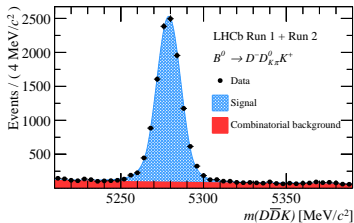
- BaBar added a second channel, $429 \text{ fb}^{-1} e^+ e^-$



- Signal of 567 ± 51 candidates
- Dominated by $D_{s1}(2700)^+ \rightarrow D^0 K^+$ (67% of model)
- Smaller 'exponential' component (10%)
- Again, challenging $\sim 60\%$ continuum background

An unprecedented dataset

- LHCb has:
 - **high-statistics**: order of magnitude improvement
 - **high-purity**: order of magnitude reduction in background
- (see recent LHCb branching fraction measurement: [2005.10264](#))





A simple study?

- $B^\pm \rightarrow D^+ D^- K^\pm$ interesting for charmonia; conventional resonances only expected in the $D^+ D^-$ channel
- Amplitude analysis should be an 'easy' study of charmonia...

Surprising phase-space structure!

- Paper 1: model-independent study of resonant structure in $B^+ \rightarrow D^+ D^- K^+$ decays
- Paper 2: amplitude analysis of the $B^+ \rightarrow D^+ D^- K^+$ decay



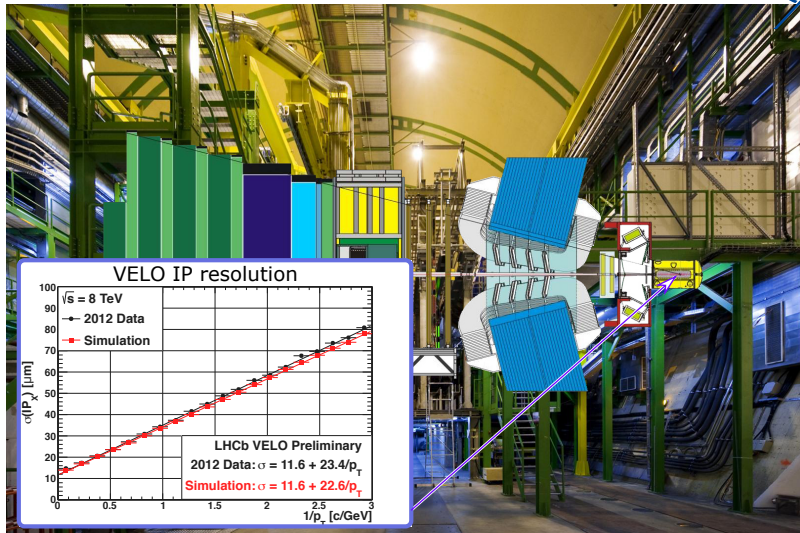
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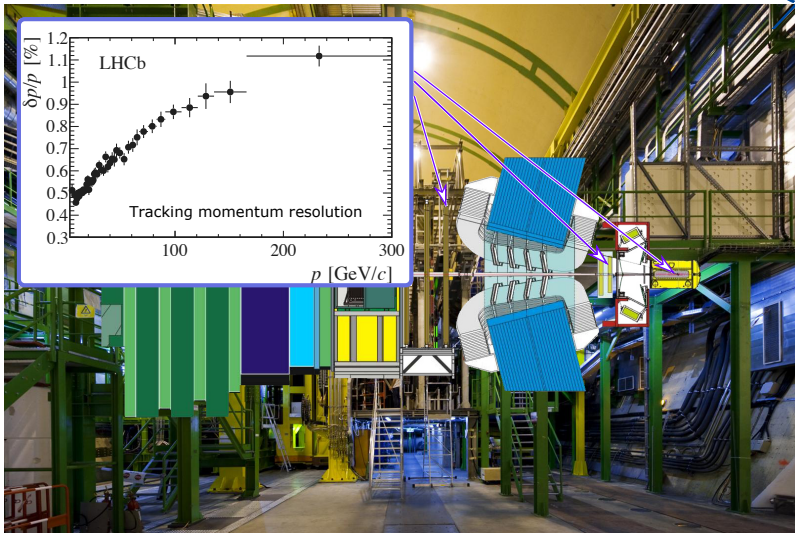
LHCb detector



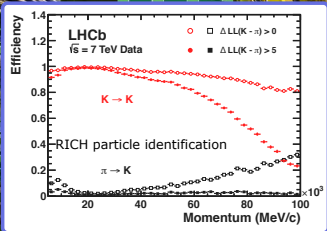
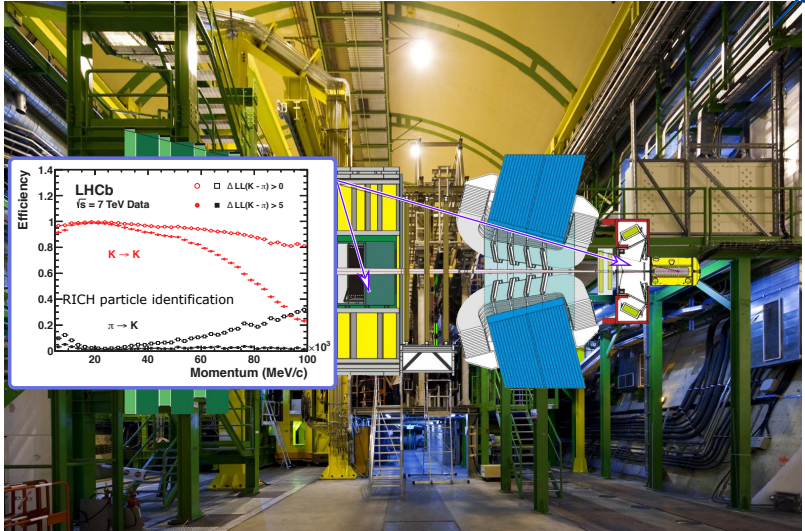
LHCb detector



LHCb detector

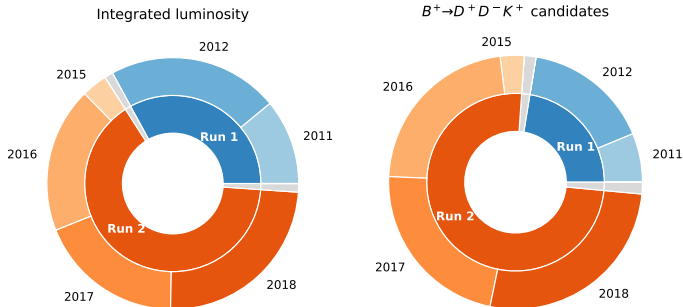


LHCb detector



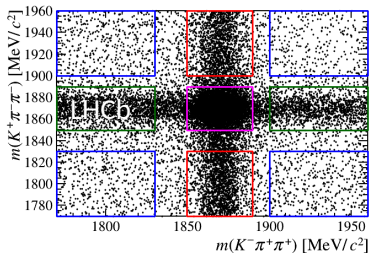
Full Run 1 + Run 2 pp datasets (9 fb^{-1})

- Reconstruct $B^+ \rightarrow [K^- \pi^+ \pi^+]_{D^+} [K^+ \pi^- \pi^-]_{D^-} K^+$
- Efficient hardware (and subsequent software) trigger
- UniformBDT [1305.7248](#) with topological and PID variables
- Optimise (significance \times purity)



Specific backgrounds

- Suppress peaking backgrounds producing the same final state:
 - Veto sharp inv. mass peaks for disconnected pairs of f.s. particles
 - Inspect B^\pm peak in D^+ and D^- sidebands, and cut on D^\pm FD



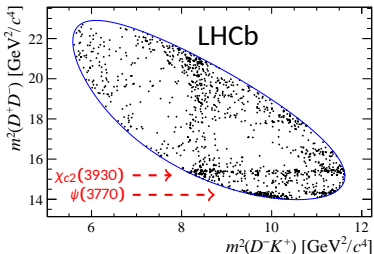
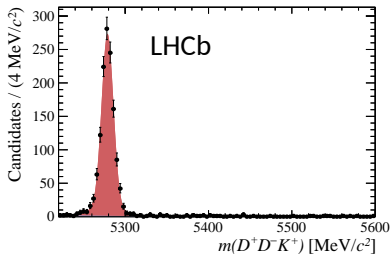
Charmless
Single charm

Remove with F.D. cuts;
typical 20% efficiency cost

- Negligible residual peaking background
- No dangerous partially-reconstructed backgrounds

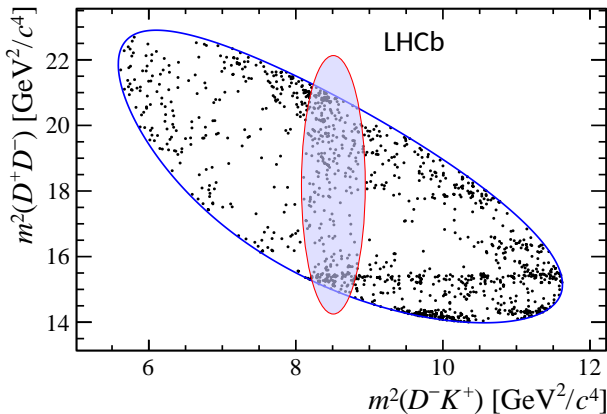
Resonant structure, paper 1,2: $B^+ \rightarrow D^+ D^- K^+$

- Published in September, full Run 1+2 [2009.00025](#), [2009.00026](#)



- 1,260 candidates enter the B^\pm mass window for Dalitz plot study
- Purity > 99.5%!
- Only expected resonances in one channel ($D^+ D^-$)

Sneak-peak: the phasespace structure



What is that???



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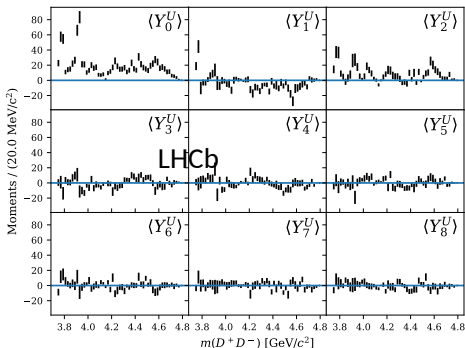
Model-independent analysis approach

- Can $D^+ D^- K^+$ phsp be described by $D^+ D^-$ partial-waves only?
- Resonances only expected in a single channel: 'simple'
- Method used in $B^0 \rightarrow \psi(2S) K^+ \pi^-$ [1510.01951](#),
 $B^0 \rightarrow \mathcal{Y} \psi K^+ \pi^-$ [1901.05745](#),
 $\Lambda_b \rightarrow \mathcal{Y} \psi p K^-$ [1604.05708](#), [CERN-THESIS-2016-086](#).

Procedure

1. Capture D^+D^- angular structure using orthonormal basis of Legendre polynomials in $h(D^+D^-) = \cos(\theta(D^+D^-))$:

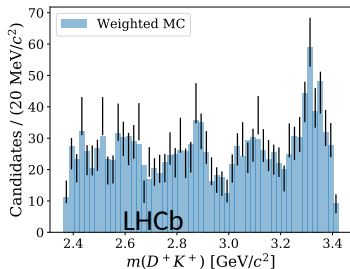
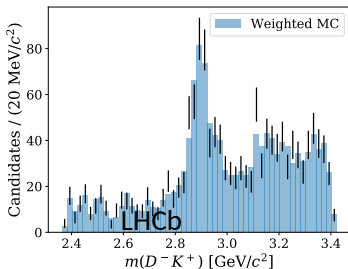
$$\langle Y_k^{U,j} \rangle = \sum_{l=1}^{N_j^{\text{Data}}} w_l P_k(h_l(D^+D^-)) \quad (1)$$



Procedure

- Apply weights to MC to visualise resulting $m(D^+K^-)$ shape:

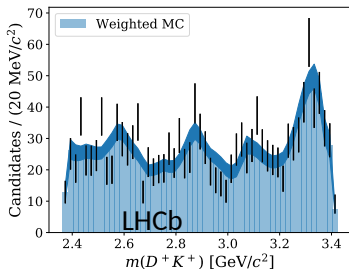
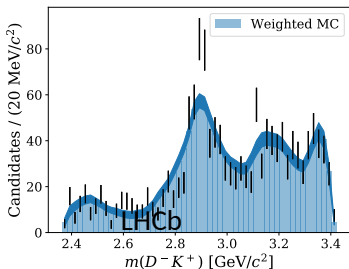
$$\eta_i = \frac{2}{N_j^{\text{Sim}}} \times \sum_{k=0}^{k_{\text{max}}} \langle Y_k^{U,j} \rangle P_k(h(D^+D^-)) \quad (2)$$



- Obviously high k_{max} allows to describe nearly everything

Procedure

- Truncate the expansion: up to spin-2 \rightarrow up to $k_{\max} = 4$:

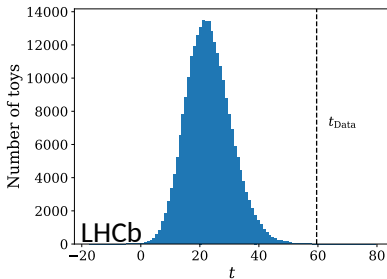


- Bootstrap to propagate uncertainty on moments $\langle Y_k^{U,j} \rangle$
- Clear problem describing the $D^+ K^-$ spectrum

Procedure

4. Construct PDF in $m(D^+K^-)$ to build a test-statistic:

$$t = -2 \sum_{l=1}^{N_{\text{Data}}} s_l \log \left(\frac{\mathcal{P}(m_l(D^-K^+) | H_0) / I_{H_0}}{\mathcal{P}(m_l(D^-K^+) | H_1) / I_{H_1}} \right) \quad (3)$$



- Ensemble of toys using $k_{\text{max}} = 4$; bootstrap efficiency models
- Evaluate t . t_{Data} discrepant at level of 3.9σ



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Formalism

Used the Laura++ Dalitz plot fitter^{1711.09854} to maximise

$$\mathcal{L} = \exp \left[- \sum_c \left(\frac{(p_c - \mu_c)^2}{2\sigma_c^2} \right) \right] \prod_{j=1}^{N_c} (N_{\text{sig}} \mathcal{P}_{\text{sig}}(\vec{x}_j) + N_{\text{bg}} \mathcal{P}_{\text{bg}}(\vec{x}_j))$$

with signal PDF,

$$\mathcal{P}_{\text{sig}}(\vec{x}) = \frac{1}{\mathcal{N}} \times \epsilon_{\text{total}}(\vec{x}) \times |\mathcal{A}_{\text{sig}}(\vec{x})|^2$$

and isobar construction for signal amplitude:

$$\mathcal{A}_{\text{sig}}(\vec{x}) = \sum_{j=1}^N c_j F_j(\vec{x})$$



Formalism

For a resonance in the $D^+ D^-$ channel, the amplitude is

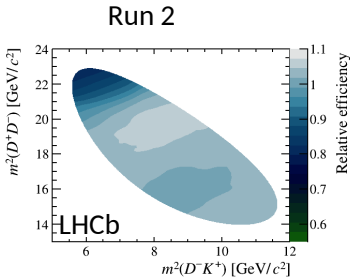
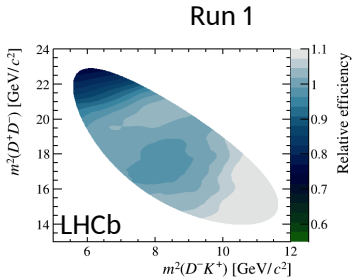
$$F(\vec{x}) = R(m(D^+ D^-)) \times T(\vec{p}, \vec{q}) \times X(|\vec{p}|) \times X(|\vec{q}|), \quad (4)$$

- R : relativistic Breit-Wigner for all resonances
- T : angular factor - non-relativistic Zemach tensor formalism
- X : Blatt-Weisskopf barrier factors

Efficiency variations

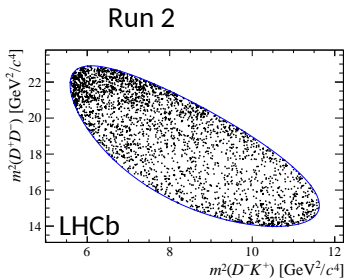
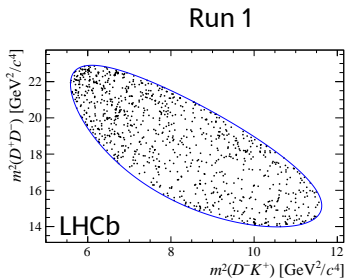
$$\epsilon_{\text{total}}(\vec{x}) = \epsilon_{\text{offline|reco}}(\vec{x}) \times \epsilon_{\text{reco|trig}}(\vec{x}) \times \epsilon_{\text{trig|geom}}(\vec{x}) \times \epsilon_{\text{geom}}(\vec{x}).$$

- Main variations at trigger, reconstruction, and stripping stages
- Uniform BDT achieves flat acceptance, as expected



Tiny background component

- Use $5.35 \text{ GeV}/c^2 < m(D^+D^-K^+) < 5.69 \text{ GeV}/c^2$, relaxing BDT
- Dalitz plots in the sidebands:





Signal model ingredients (1/2)

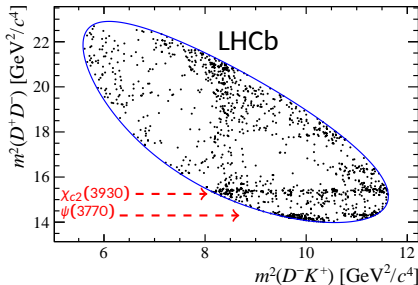
Expect natural J^P (\rightarrow pseudoscalars) and suppressed high-spin

Partial wave (J^{PC})	Resonance	Mass (MeV/ c^2)	Width (MeV/ c^2)
S wave (0^{++})	$\chi_{c0}(3860)$	3862 ± 39	201 ± 139
	$X(3915)$	3918.4 ± 1.9	20 ± 5
	Possible nonresonant contributions		
P wave (1^{--})	$\psi(3770)$	3778.1 ± 0.9	27.2 ± 1.0
	$\psi(4040)$	4039 ± 1	80 ± 10
	$\psi(4160)$	4191 ± 5	70 ± 10
	$\psi(4260)$	4230 ± 8	55 ± 19
	$\psi(4415)$	4421 ± 4	62 ± 20
D wave (2^{++})	$\chi_{c2}(3930)$	3921.9 ± 0.6	36.6 ± 2.1
F wave (3^{--})	$X(3842)$	$3842.71 \pm 0.16 \pm 0.12$	$2.79 \pm 0.51 \pm 0.35$

- Most values taken from PDG
- $m(\psi(3770))$ and $\{m, \sigma\}(\chi_{c2}(3930), X(3842))$ from [1903.12240](#)

Fit procedure

- Refit decay, constraining B^\pm & D^\pm masses: $\sigma(D^+D^-)$ improves from θ (10 MeV/c²) to θ (2 MeV/c²): neglect resolution
- Fit Run 1 and Run 2 data simultaneously, with separate efficiency, bg models and purity
- Minimisation repeated 100 times, randomising coefficients
- $\chi^2/ndof_{\text{effective}}$ computed with adaptive binning scheme



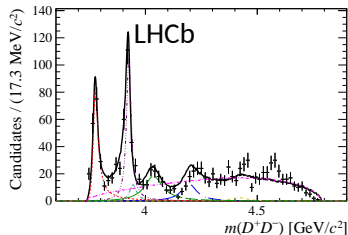


Fit procedure

- Always include $\psi(3770)$ and $\chi_{c2}(3930)$: clearly visible
- Further components included if significantly reduce NLL
- Complex coefficients vary for all except $\psi(3770)$
- Vary m & σ ; constrain $\psi(3770)/\psi(4040)/\psi(4160)/\psi(4415)$
- Better fit adding ' $\chi_{c0}(3930)$ '; no constraint on $\chi_{c1}(3930)$ m, σ
- Tried various nonresonant lineshapes (uniform, exponential, polynomial, cubic spline) with spin-0,1

Model excluding D^-K^+ resonances

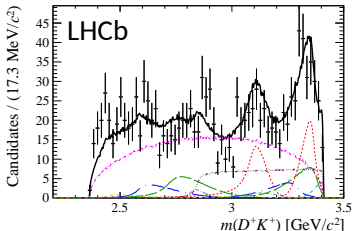
- $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, and $\psi(4415)$ resonances
- Nonresonant best described by an exponential S-wave lineshape in the D^-K^+ spectrum



- $\psi(3770) \rightarrow D^+ D^-$
- $\chi_{c0}(3930) \rightarrow D^+ D^-$
- $\chi_{c2}(3930) \rightarrow D^+ D^-$
- $\psi(4040) \rightarrow D^+ D^-$
- $\psi(4160) \rightarrow D^+ D^-$
- $\psi(4415) \rightarrow D^+ D^-$
- Nonresonant

Model excluding $D^- K^+$ resonances

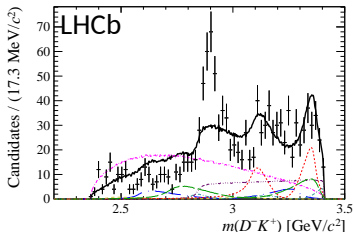
- $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, and $\psi(4415)$ resonances
- Reflections model the $D^+ K^+$ spectrum satisfactorily:



- $\psi(3770) \rightarrow D^+ D^-$
- $\chi_{c0}(3930) \rightarrow D^+ D^-$
- $\chi_{c2}(3930) \rightarrow D^+ D^-$
- $\psi(4040) \rightarrow D^+ D^-$
- $\psi(4160) \rightarrow D^+ D^-$
- $\psi(4415) \rightarrow D^+ D^-$
- Nonresonant

Model excluding $D^- K^+$ resonances

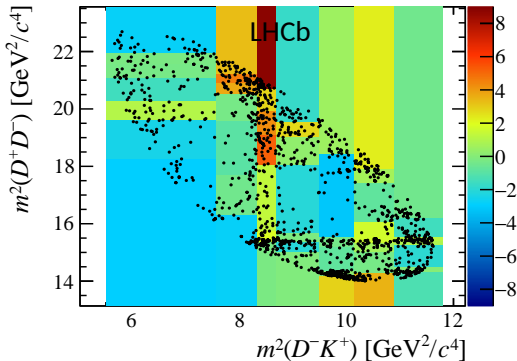
- $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, and $\psi(4415)$ resonances
- But the description of the $D^- K^+$ spectrum is severely deficient!



- $\psi(3770) \rightarrow D^+ D^-$
- $\chi_{c0}(3930) \rightarrow D^+ D^-$
- $\chi_{c2}(3930) \rightarrow D^+ D^-$
- $\psi(4040) \rightarrow D^+ D^-$
- $\psi(4160) \rightarrow D^+ D^-$
- $\psi(4415) \rightarrow D^+ D^-$
- **Nonresonant**

Model excluding D^-K^+ resonances

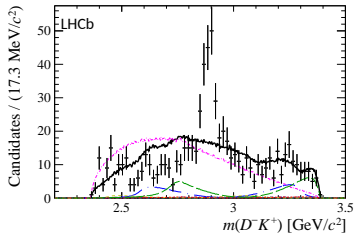
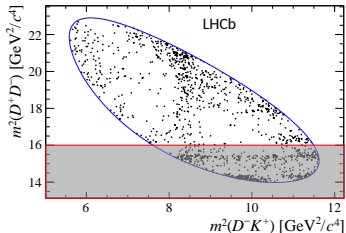
Goodness of fit:



- Largest deviations seen near $m(D^-K^+) \approx 2.9 \text{ GeV}/c^2$

Model excluding D^-K^+ resonances

- Clearer: $m(D^+D^-) > 4 \text{ GeV}/c^2$: cut away low-mass charmonia



- Bit of a show-stopper

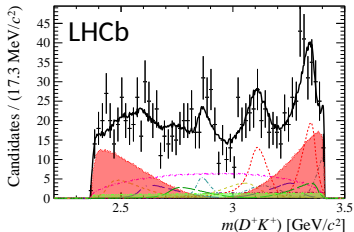
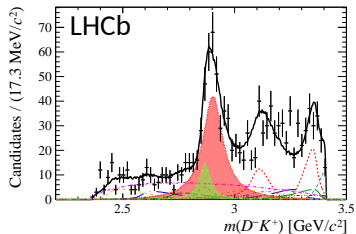
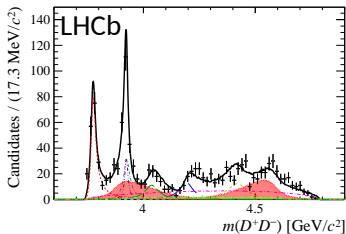


Model including $D^- K^+$ resonances

We had to do something about the $D^- K^+$ channel

- May well need more intricate theoretical study e.g. rescattering effects since suspiciously close to $D^* K^*$ threshold
- Simple approach: **new Breit-Wigners** (spin-0 and spin-1 needed)

Model including $D^- K^+$ resonances



- $\psi(3770) \rightarrow D^+ D^-$
- $\chi_{c0}(3930) \rightarrow D^+ D^-$
- $\chi_{c2}(3930) \rightarrow D^+ D^-$
- $\psi(4040) \rightarrow D^+ D^-$
- $\psi(4160) \rightarrow D^+ D^-$
- $\psi(4415) \rightarrow D^+ D^-$
- $X_0(2900) \rightarrow D^- K^+$
- $X_4(2900) \rightarrow D^- K^+$
- Nonresonant



Model including D^-K^+ resonances

Fit results: **coefficients**

Resonance	Magnitude	Phase (rad)	Fit fraction (%)
D^+D^- resonances			
$\psi(3770)$	1 (fixed)	0 (fixed)	$14.5 \pm 1.2 \pm 0.8$
$\chi_{c0}(3930)$	$0.506 \pm 0.064 \pm 0.017$	$2.162 \pm 0.184 \pm 0.034$	$3.7 \pm 0.9 \pm 0.2$
$\chi_{c2}(3930)$	$0.703 \pm 0.064 \pm 0.012$	$0.827 \pm 0.170 \pm 0.133$	$7.2 \pm 1.2 \pm 0.3$
$\psi(4040)$	$0.585 \pm 0.078 \pm 0.035$	$1.416 \pm 0.176 \pm 0.084$	$5.0 \pm 1.3 \pm 0.4$
$\psi(4160)$	$0.668 \pm 0.084 \pm 0.052$	$0.898 \pm 0.225 \pm 0.092$	$6.6 \pm 1.5 \pm 1.2$
$\psi(4415)$	$0.797 \pm 0.080 \pm 0.061$	$-1.458 \pm 0.197 \pm 0.091$	$9.2 \pm 1.4 \pm 1.5$
D^-K^+ resonances			
$X_0(2900)$	$0.619 \pm 0.079 \pm 0.025$	$1.091 \pm 0.193 \pm 0.095$	$5.6 \pm 1.4 \pm 0.5$
$X_1(2900)$	$1.449 \pm 0.086 \pm 0.032$	$0.367 \pm 0.102 \pm 0.049$	$30.6 \pm 2.4 \pm 2.1$
Nonresonant	$1.293 \pm 0.088 \pm 0.043$	$-2.410 \pm 0.119 \pm 0.508$	$24.2 \pm 2.2 \pm 0.5$

- Total fit fraction: 107%



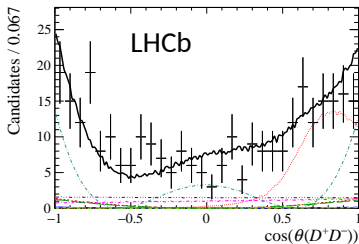
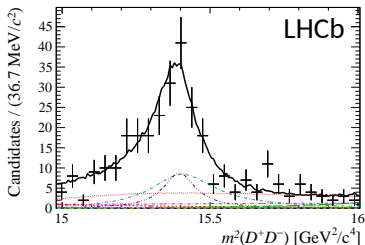
Model including D^-K^+ resonances

Fit results: lineshapes

Resonance	Mass (GeV/c ²)	Width (MeV/c ²)
$\chi_{c0}(3930)$	$3.9238 \pm 0.0015 \pm 0.0004$	$17.4 \pm 5.1 \pm 0.8$
$\chi_{c2}(3930)$	$3.9268 \pm 0.0024 \pm 0.0008$	$34.2 \pm 6.6 \pm 1.1$
$X_0(2900)$	$2.8663 \pm 0.0065 \pm 0.0020$	$57.2 \pm 12.2 \pm 4.1$
$X_1(2900)$	$2.9041 \pm 0.0048 \pm 0.0013$	$110.3 \pm 10.7 \pm 4.3$

Model including D^-K^+ resonances

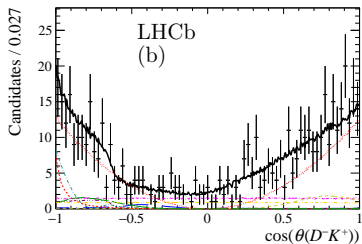
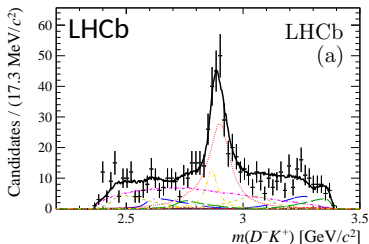
Zoom in on the $\chi_{cJ}(3930)$ ($15 \text{ GeV}/c^2 < m^2(D^+D^-) < 16 \text{ GeV}/c^2$):



- **Both** a spin-0 and spin-2 component are needed in this region
- Masses are consistent and spin-0 slightly narrower [2002.03311](#)

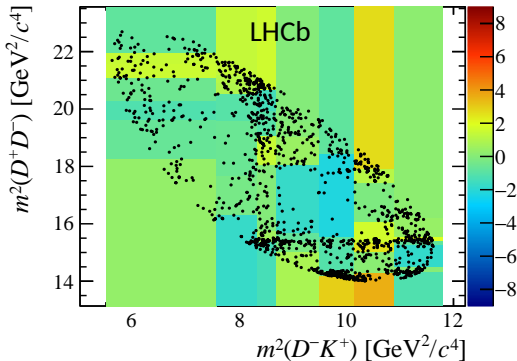
Model including D^-K^+ resonances

Focus on the new D^-K^+ states ($m(D^+D^-) > 4 \text{ GeV}/c^2$):



Model including D^-K^+ resonances

Goodness of fit:



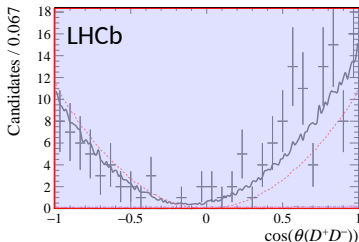
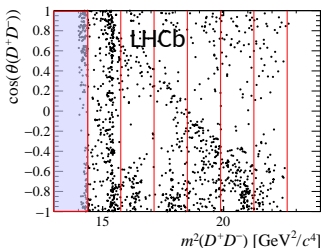
- The χ^2/ndf is $86.1/38.3 = 2.25$

Model including D^-K^+ resonances

Main areas of disagreement (1):

$$(m^2(D^-K^+), m^2(D^+D^-)) \sim (10.5 \text{ GeV}^2/c^4, 13.5 \text{ GeV}^2/c^4)$$

- Data exhibit large interference between S and P wave at low $m(D^+D^-)$, but fit does not introduce any S wave here:





Model including D^-K^+ resonances

Main areas of disagreement (2):

$$(m^2(D^-K^+), m^2(D^+D^-)) \sim (10.5 \text{ GeV}^2/c^4, 18.5 \text{ GeV}^2/c^4)$$

- Seems to originate at low values of $m^2(D^+K^+)$. No particular disagreement is seen in other projections of this region, and therefore it is not considered a source of concern.

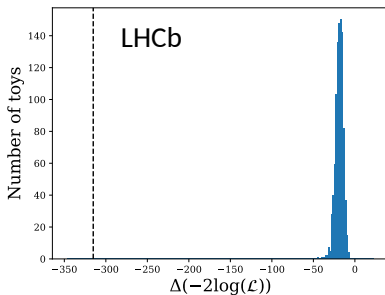
Conclusion

The fit is not perfect but the new features are too narrow or too prominent to be ignored



Significance of new D^-K^+ state

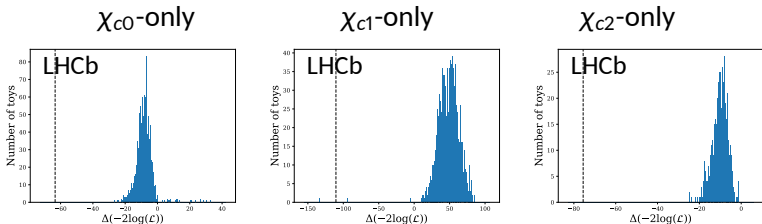
- Generate ~ 1000 toys from data fit with no D^-K^+ components
- Fit with model with and without the new components
- Find difference in NLL for the toy ensemble, and for the data:



- Overwhelmingly significant, $\gg 5\sigma$

Significance of $\chi_{cJ}(3930)$ spin conclusions

- Generate ~ 1000 toys from data fit with single $\chi_{c0,1,2}$ resonance
- Fit with model with that resonance or with both spin-0 and 2
- Find difference in NLL for the toy ensemble, and for the data:



- Strong preference for the spin-0 and spin-2 combination



Systematic uncertainties

Major sources:

- **Blatt-Weisskopf radii** conventionally set to 4 GeV^{-1} . Vary parent, charmonia, charm-strange radii separately. Dominant effect from the latter two ($\sim 50\% \sigma_{\text{stat}}$)
- **S wave modelling**: introduce 5% uniform NR component in toy ensemble and fit with standard model ($10 \rightarrow 80\% \sigma_{\text{stat}}$)
- **P wave modelling**: add $\psi(4320)$ with fixed parameters ($10 \rightarrow 100\% \sigma_{\text{stat}}$)
- **Limited MC statistics**: bootstrap efficiency models and repeat fit to data ($\sim 10\% \sigma_{\text{stat}}$)
- **Hardware trigger modelling in MC**: build alternative efficiency map using calibration samples ($\sim 10\% \sigma_{\text{stat}}$)



Outline

1. Introduction
2. Datasets
3. Model-independent analysis [arXiv:2009.00025] (published PRL)
4. Amplitude analysis [arXiv:2009.00026] (published PRD)
- 5. Reaction**
6. Conclusion



$cs\bar{u}\bar{d}$ tetraquark

- 0^+ state an isosinglet compact tetraquark
- Analogy to $bb\bar{u}\bar{d}$ predicted by lattice QCD
- Discussed in [2008.05993](#), [2008.07145](#), [2008.07295](#), [2008.07340](#)

Pro

Successfully explain the 0^+ state

Con

- (Most) struggle with 1^-
- Analogy to $bb\bar{u}\bar{d}$ doubtful (far from threshold)
- Accompanied by plethora of additional states (pro?)



Molecular bound state

- Genuine prediction (2010) for an isoscalar $D^* \bar{K}^* 0^+$ state
- Prediction in 1005.0335 refined (to get the right mass!) in 2008.11171
- More discussion in 2008.07389, 2008.07782, 2008.06894, 2008.07516, 2008.09516.

Pro

- *Successfully explain the 0^+ state*
- *Diquark-diantiquark picture gives 1^-*

Con

- *(Most) struggle with 1^-*
- *More 1^+ , 2^+ states expected*



Rescattering structure from nearby threshold

- Triangle diagram coupling B to DDK final state
- Assume single-pion exchange dominates: only possible between $D^* \bar{K}^*$ (not $D^* \bar{K}$, $D \bar{K}^*$, $D \bar{K}$)
- $D_1(2420) \bar{K} \rightarrow D^* \bar{K}^*$ scattering OK. Thresholds at $2.9 \text{ GeV}/c^2$.

Pro

- *Nice connection to suspicious thresholds*
- *Natural explanation of 1^- with $D_1(2420) \bar{K}$ in S wave*
- *Discussed in 2008.07190 and 2008.12838*

Con

- *Only (so far) tested in fit to 1D mass projection*



What next?

Confirmation:

- Does the state reappear in $B^0 \rightarrow D^0 D^- K^+$ and $B^+ \rightarrow D^- K^+ \pi^+$?

Composition:

- Is the structure also present in $B^+ \rightarrow D^+ \bar{D}^0 K_S^0$ (also $cs\bar{u}\bar{d}$)?

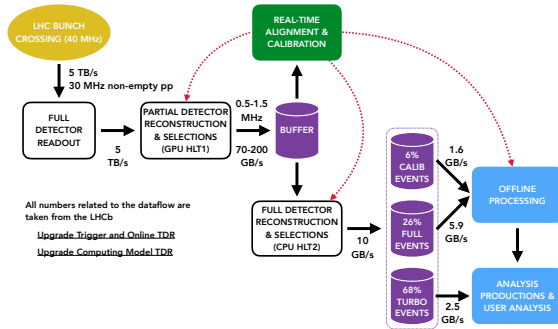
Extension:

- Is it an isosinglet/triplet? Do additional states appear in $B^+ \rightarrow D^0 \bar{D}^0 K^+$ ($\bar{c}uu\bar{s}$)?
- Is there a 1^+ partner in $B^+ \rightarrow D^+ D^-^* K^+$?

What next?

Run 3

- Major changes to DAQ pipeline

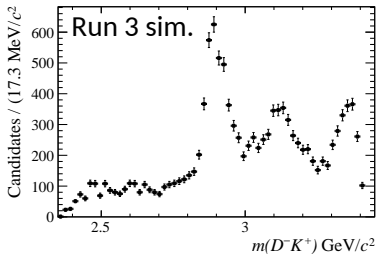
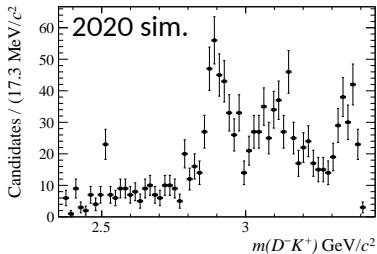


- Consequently improved trigger efficiency
- Run 3 (2021-2023) anticipated to carry an order of magnitude greater statistical weight vis-a-vis Run 1+2.

What next?

SIMULATED projection for Run 1+2 vs Run 3 datasets

- Generate pseudo-experiments from $B^+ \rightarrow D^+ D^- K^+$ model



- Radical increase in sensitivity just by middle of this decade



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Summary

- LHCb is a powerhouse for new, exotic particle discovery. We can go far with a simple bump-hunt ($X(6900)$), but even further exploiting a fully-reconstructed decay
- **First** analysis of $D^+ D^- K^+$ resonant structure
- **First** model-independent evidence for $D^+ D^- K^+$ structure that cannot be accounted for by charmonium resonances
- **First** amplitude model of $D^+ D^- K^+$
- Model-dependent **discovery** of exotic structure in $D^- K^+$
- **Discovery** of contributions from spin-0 and spin-2 components in the region of the existing ' $\chi_{c2}(3930)$ '

Resonance	Mass (GeV/c ²)	Width (MeV/c ²)	Fit fraction (%)
$\chi_{c0}(3930)$	3.924 ± 0.002	17.4 ± 5.2	3.7 ± 0.9
$\chi_{c2}(3930)$	3.927 ± 0.003	34.2 ± 6.7	7.2 ± 1.2
$X_0(2900)$	2.866 ± 0.007	57.2 ± 12.9	5.6 ± 1.5
$X(2900)$	2.804 ± 0.005	110.3 ± 11.5	20.6 ± 3.2



Outlook

- The tide of LHCb results in $B \rightarrow D\bar{D}h$ decays broke in 2020. Did we answer as many questions as we raised?
- We have surely demonstrated
 - **high-statistics**: \sim order of magnitude wrt B-factories
 - **high-purity**: order of magnitude reduction in background
- A great deal of work undoubtedly remains ahead
- As models become more detailed / new features emerge, continued theory input will be needed
- Approaching data-taking will provide a step-change in sensitivity



Backup: constraints compared to PDG

Expect natural J^P (\rightarrow pseudoscalars) and suppressed high-spin

Partial wave (J^{PC})	Resonance	Mass (MeV/ c^2)	Width (MeV/ c^2)
P wave (1^{--})	$\psi(3770)$ (PDG)	3773.4 ± 0.4	27.2 ± 1.0
	$\psi(3770)$ (1903.12240)	3778.1 ± 0.9	27.2 ± 1.0
D wave (2^{++})	$\chi_{c2}(3930)$ (PDG)	3922.2 ± 1.0	35.3 ± 2.8
	$\chi_{c2}(3930)$ (1903.12240)	3921.9 ± 0.6	36.6 ± 2.1

- Most values taken from PDG
- $m(\psi(3770))$ and $\{m, \sigma\}(\chi_{c2}(3930), X(3842))$ from [1903.12240](#)