

Heavy Flavour Content of the Proton

Paul Thompson, Birmingham Seminar, 8th October 2008

- Reminder of HERA and kinematics
- Why measure proton structure (PDFs)?
- Why measure heavy flavours?
- Experimental Techniques
- charm and beauty cross sections at HERA
- Outlook

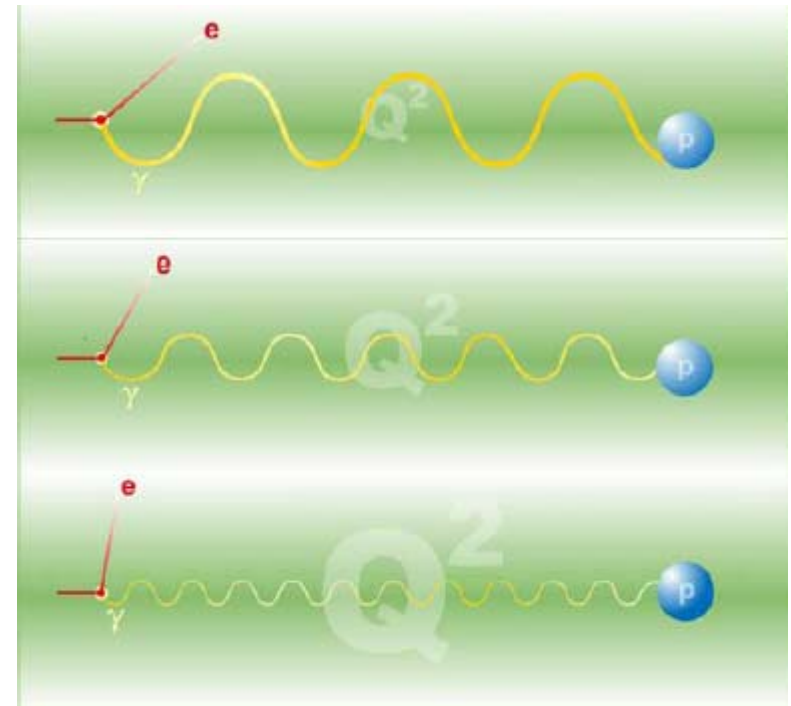
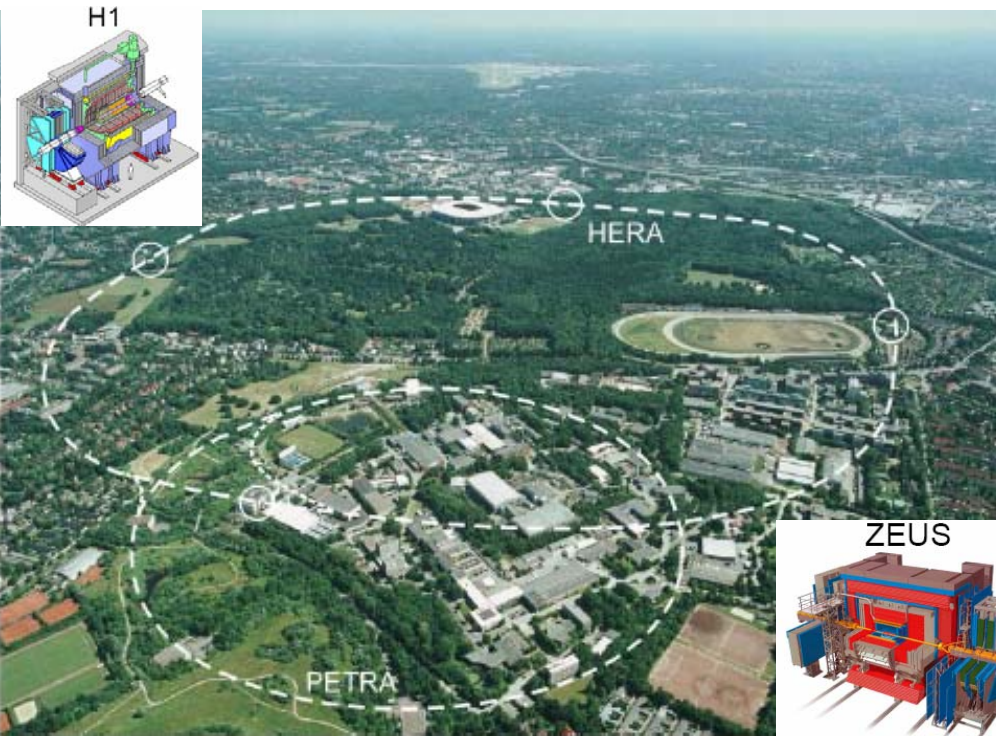
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ISMD 2008

15-20 September 2008



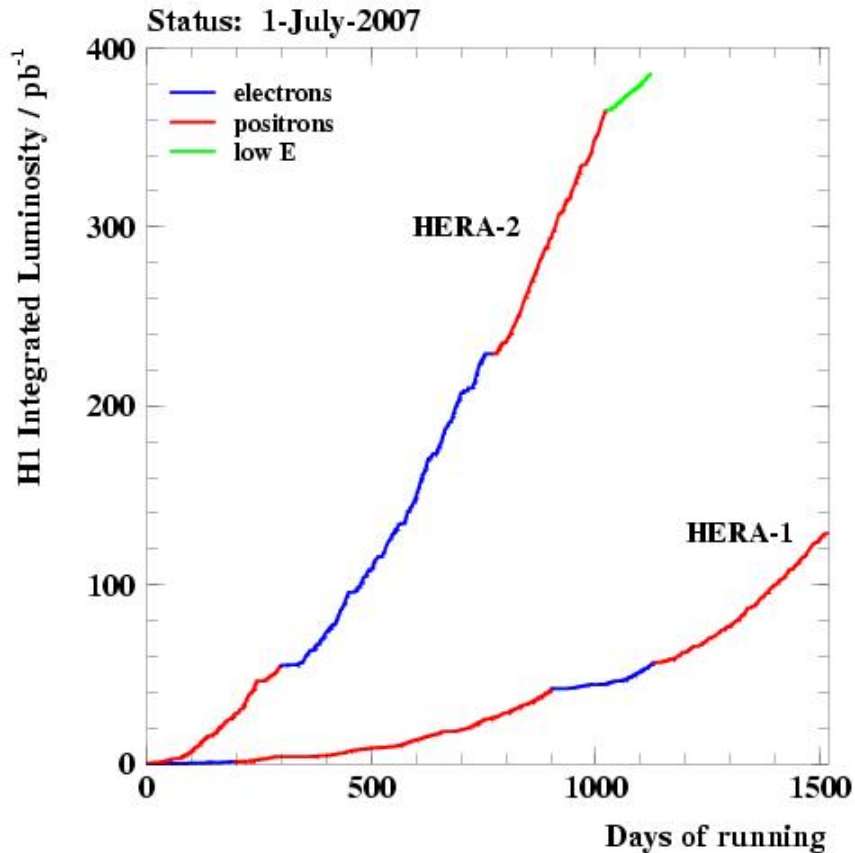
HERA ep collider



- Collided protons with e^\pm 92-07
- E_e : 27.5 GeV
- E_p : 920 GeV
- Centre of mass energy : $\sqrt{s} = 320 \text{ GeV}$

- Q^2 corresponds to the spatial resolution of probe
 - $\lambda \sim 1/\sqrt{Q^2}$ $Q_{\text{max}}^2 \sim 10^5 \text{ GeV}^2$
 - $\lambda_{\text{min}} \sim 10^{-18} \text{ m} \sim R_{\text{proton}} / 1000$
- Deep Inelastic Scattering - DIS*

Available Data



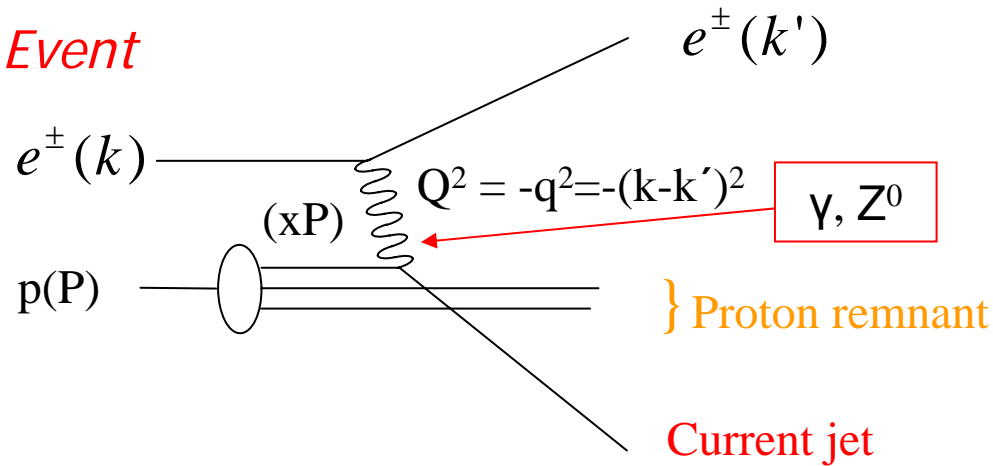
- In total $\sim 500\text{pb}^{-1}$ of high energy data collected per experiment
- luminosity upgrade in 2001
- detectors adjusted to accommodate focussing magnets
- Low energy running to measure F_L

Many preliminary analyses on full HERA II data

Working on final publication and combination of results

Deep Inelastic Scattering (DIS)

Neutral Current Event



- DIS cross section can be described in terms of:

- Q^2 : Virtuality of the intermediate boson
- x : Bjorken scaling factor

$$Q^2 = s x y$$

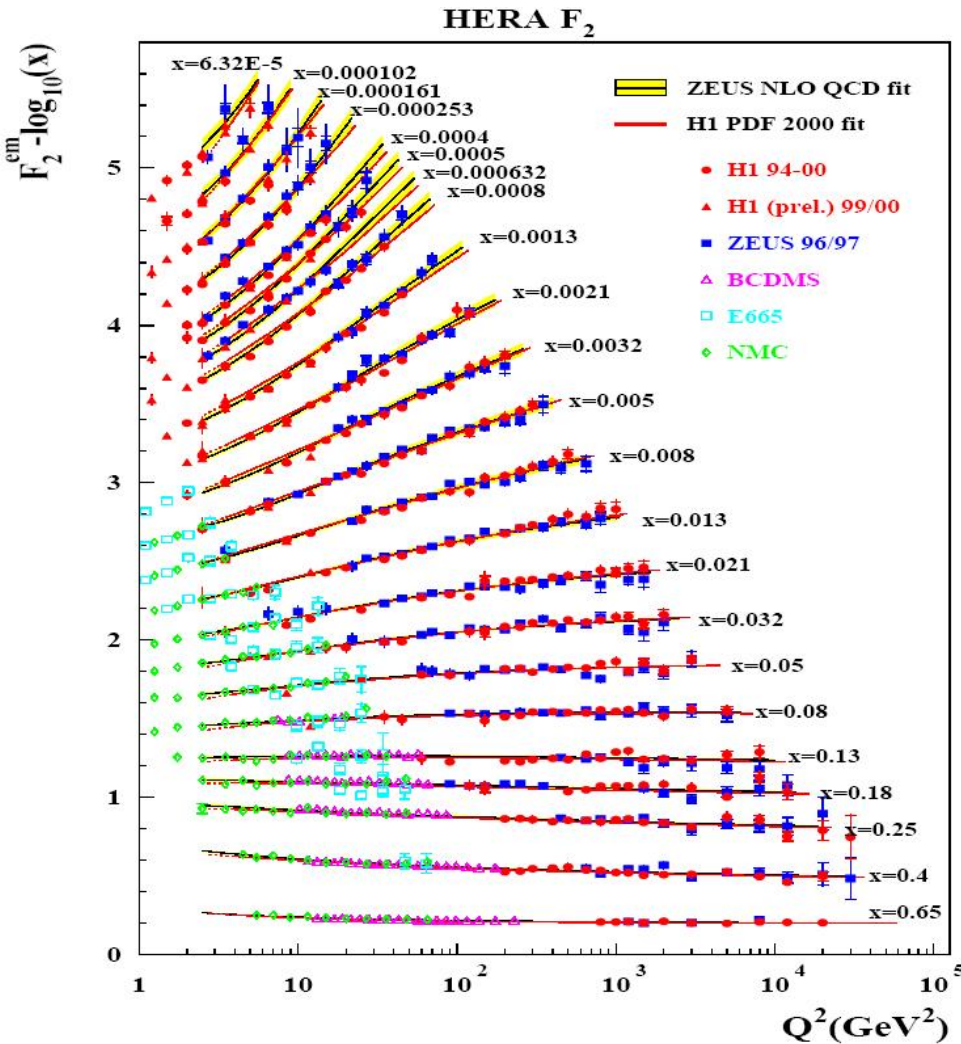
-fraction of proton's momentum carried by struck quark

- y : Inelasticity

-energy fraction transferred from lepton in proton rest frame

Neutral Current Cross Section F_2

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} Y_+ [F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \pm xF_3(x, Q^2)]$$



F_2 – dominant contribution to the cross section

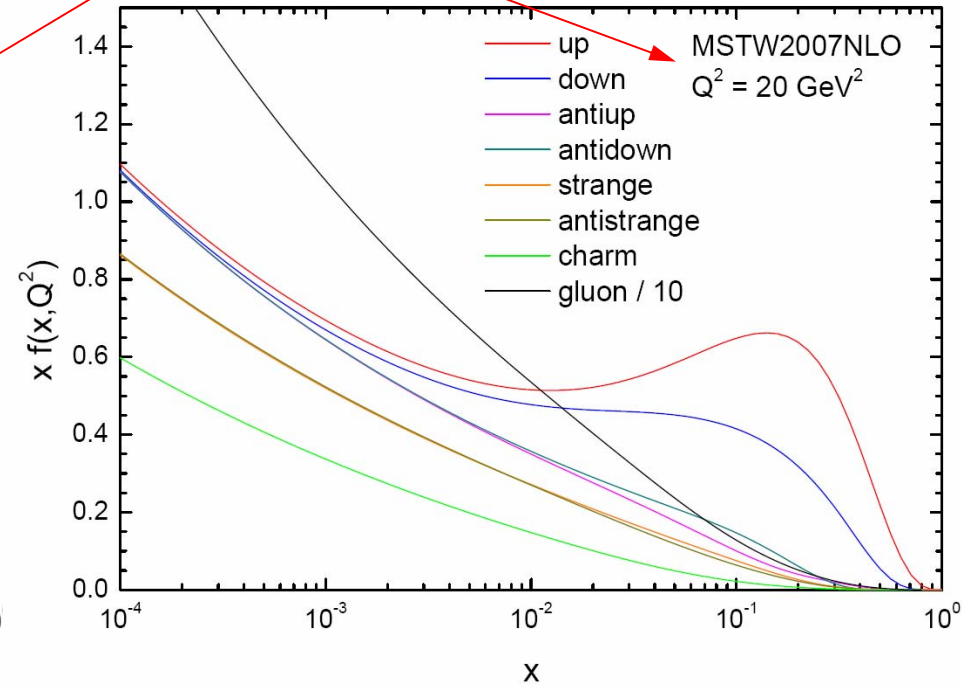
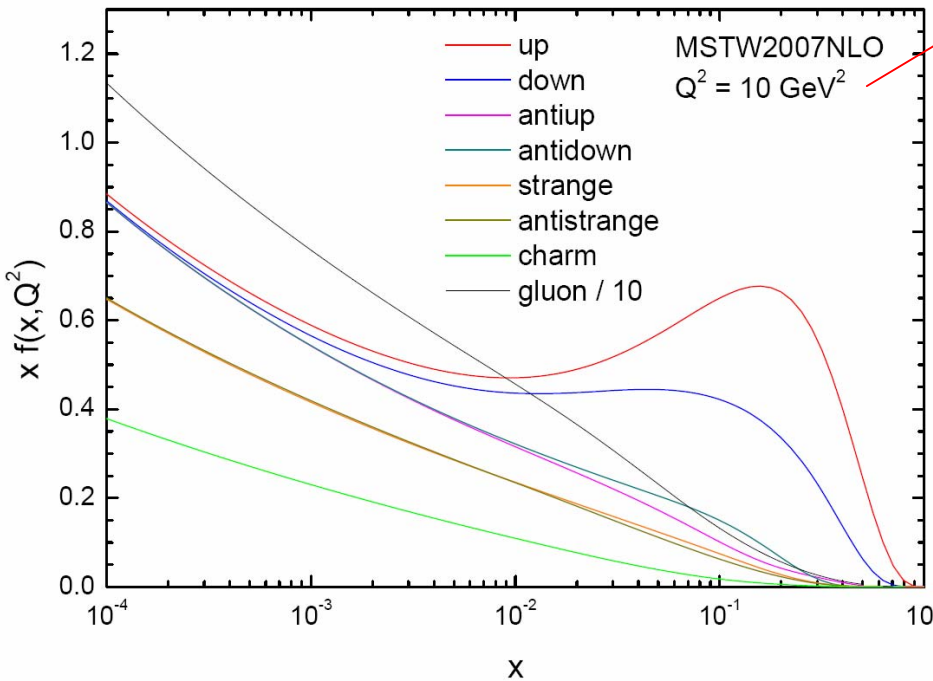
$$F_2 = \sum_q e_q^2 x (q + \bar{q})$$

Scaling violations indicate presence of gluons

Data evolution with Q^2 (at fixed x) described by perturbative QCD

QCD Factorisation and Proton PDF

DGLAP

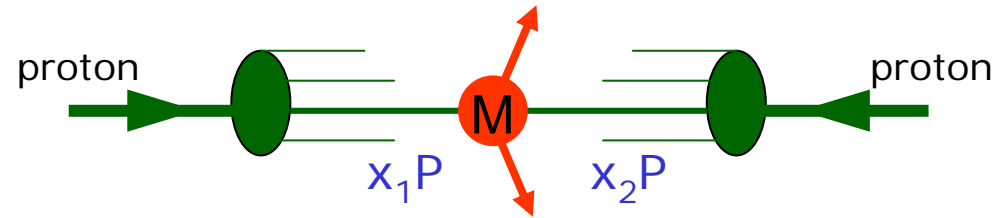


$$F_2(x, Q^2) = \sum_k f_k(\mu) \otimes C_k^j(Q, m, \alpha_s(\mu))$$

f_k are parton density functions – parameterised at Q_0^2 and evolved to high Q^2 using DGLAP equations

C_k^j perturbative coefficient functions

PDFs for the LHC

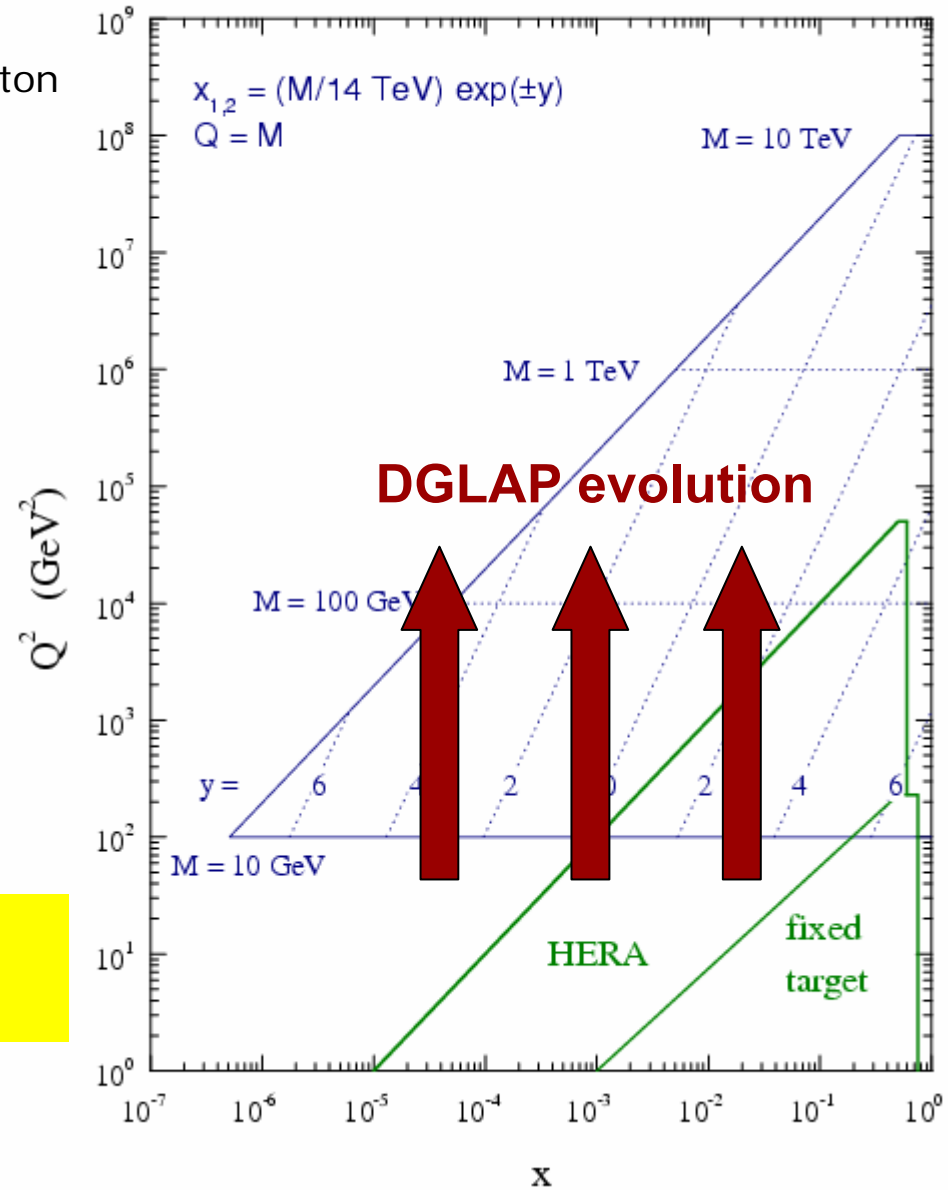


momentum fractions x_1 and x_2 determined by mass and rapidity of X

x dependence of $f(x, Q^2)$ determined by fit to data, Q^2 dependence determined by **DGLAP** equations

full NNLO DGLAP now known*, also with small x , QED etc improvements

LHC parton kinematics



*Moch, Vermaseren, Vogt (2004)

Why do we need PDFs?

- high precision (SM and BSM) cross section predictions require precision pdfs: $\delta\sigma_{\text{th}} = \delta\sigma_{\text{pdf}} + \dots$
- improved signal and background predictions \rightarrow easier to spot new physics deviations
- ‘standard candle’ processes (e.g. $\sigma(Z)$) to
 - check formalism (factorisation, DGLAP, ...)
 - measure machine luminosity?
- learning more about pdfs from LHC measurements. e.g.
 - high- E_T jets \rightarrow gluon?
 - $W^+, W^-, Z^0 \rightarrow$ quarks?
 - forward DY \rightarrow small x ?
 - ...

How Important Is PDF Precision?

- **Example 1:** $\sigma(M_H=120 \text{ GeV})$ @ LHC

$$\delta\sigma_{\text{pdf}} \approx \pm 3\%, \quad \delta\sigma_{\text{ptNNLO}} \approx \pm 10\%$$

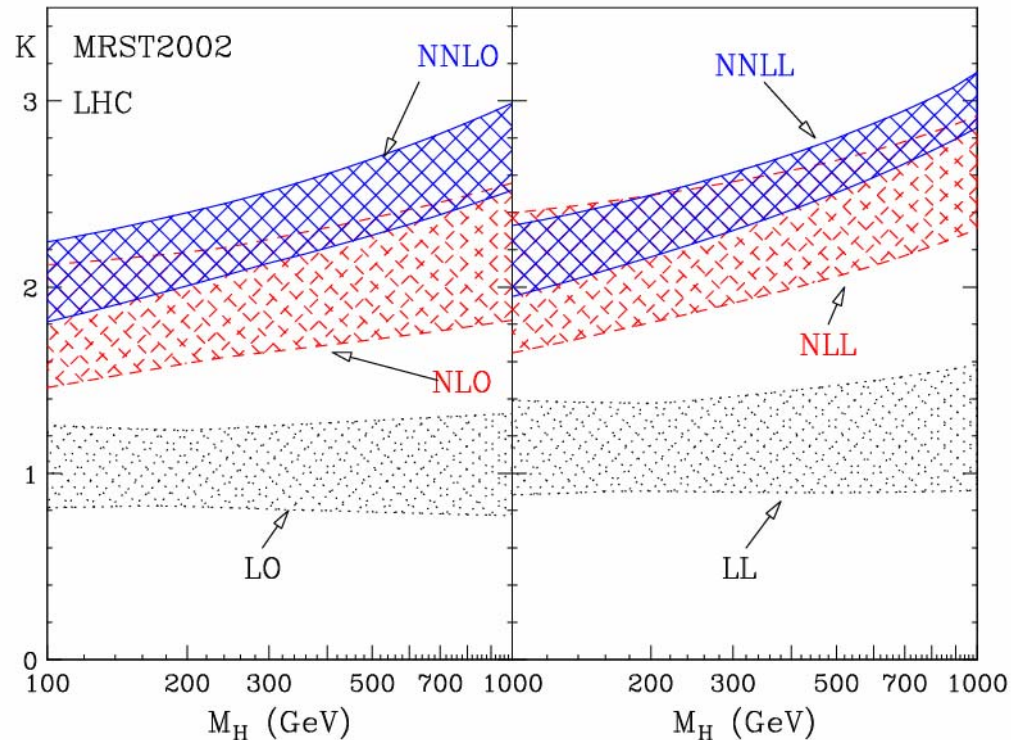
$$\delta\sigma_{\text{ptNNLL}} \approx \pm 8\%$$

$$\rightarrow \delta\sigma_{\text{theory}} \approx \pm 9\%$$

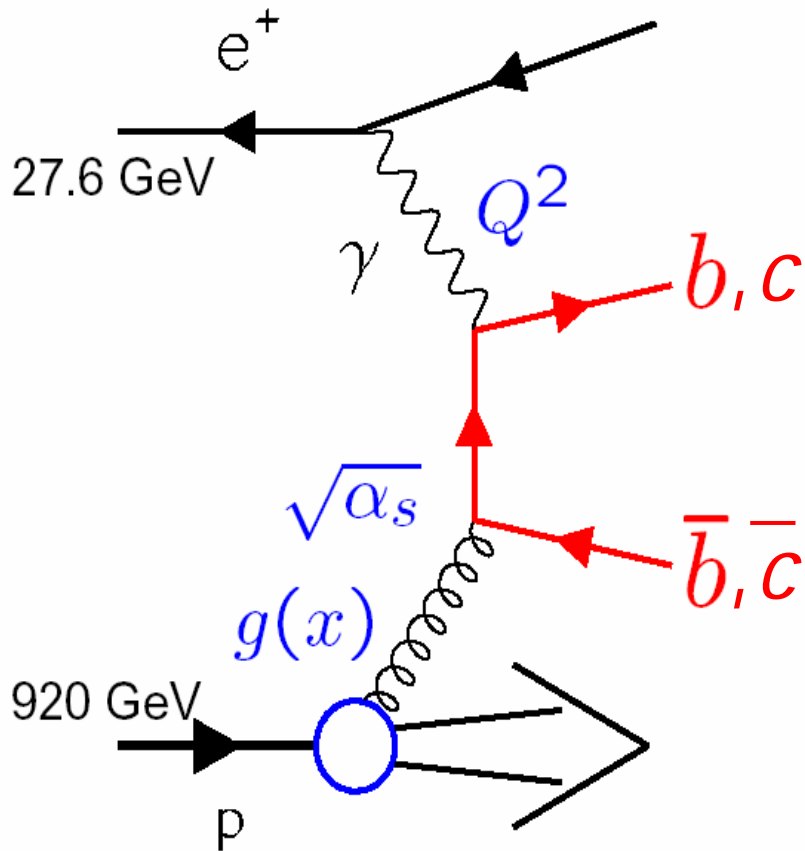
- **Example 2:** $\sigma(Z^0)$ @ LHC

$$\delta\sigma_{\text{pdf}} \approx \pm 3\%, \quad \delta\sigma_{\text{ptNNLO}} \approx \pm 2\%$$

$$\rightarrow \delta\sigma_{\text{theory}} \approx \pm 4\%$$



Production of Heavy Quarks at HERA



Predominantly via boson gluon fusion

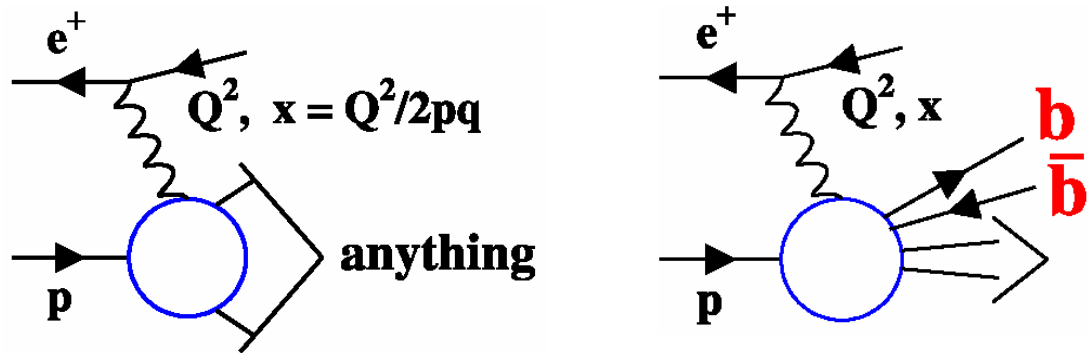
Test of perturbative QCD:

multi-scale problem (Q^2, m_b^2, p_t^2)

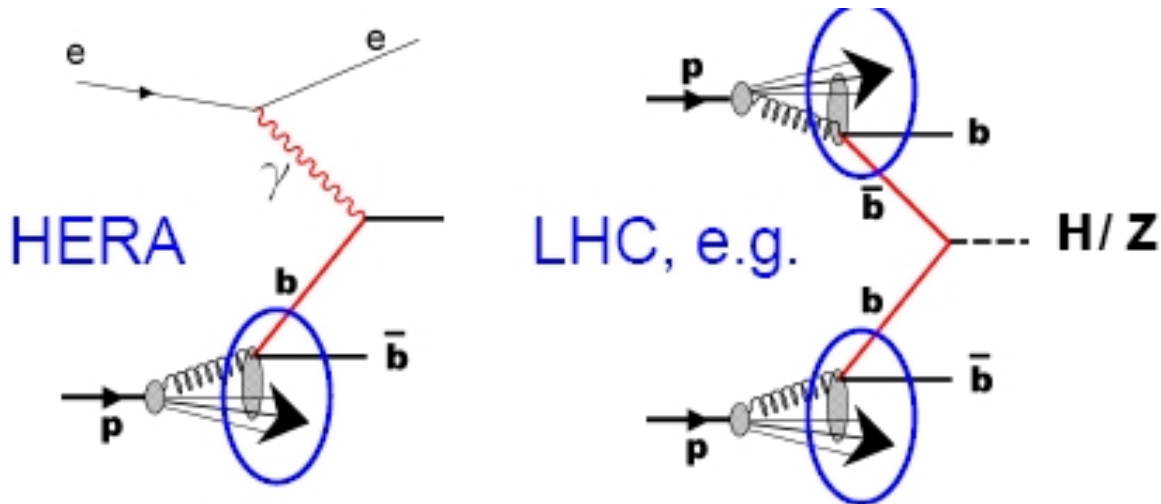
Directly sensitive to gluon density in the proton (PDFs)

F_2^{cc} and F_2^{bb}

At HERA we can measure the contribution of c and b to the total DIS cross section F_2^{bb} and F_2^{cc}



F_2^{bb} measurements at high Q^2 important for LHC e.g. $bb \rightarrow H$

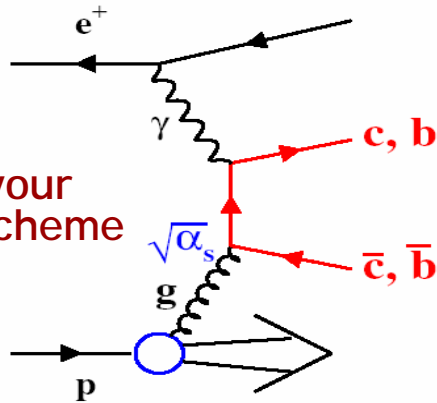


Predictions for Heavy Quark Production

Massive scheme: $\rightarrow m_b$

- **b massive**
- **neglects** $[\alpha_s \ln(Q^2/m_b^2)]^n$

\rightarrow **Perturbative production:**

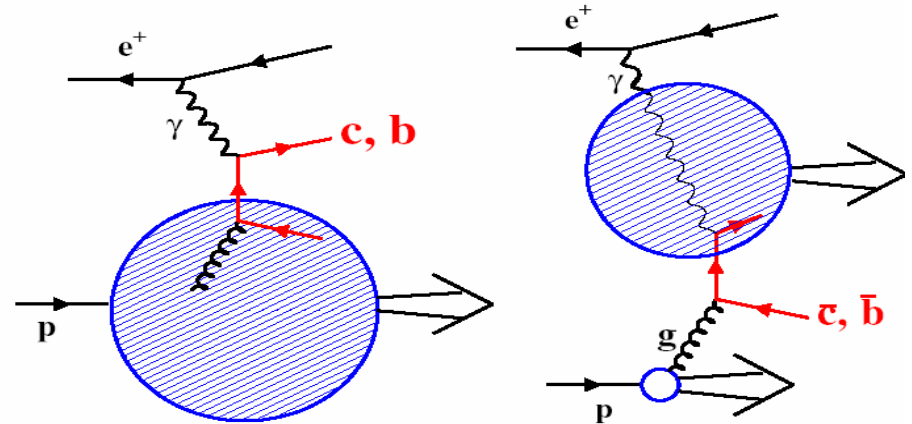


Fixed Flavour Number Scheme (FFNS)

Massless scheme: $\rightarrow p_T, Q^2$

- **b massless!!!**
- **Resums** $[\alpha_s \ln(Q^2/m_b^2)]^n$

\rightarrow **b also in Proton and Photon!**



Variable schemes (VFNS):

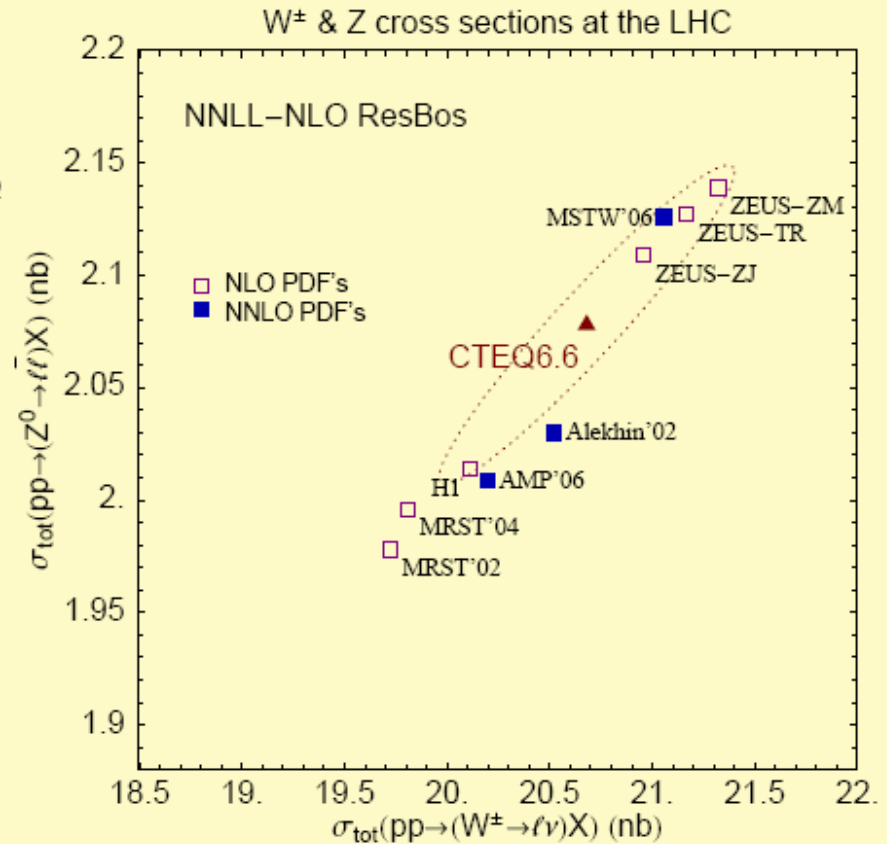
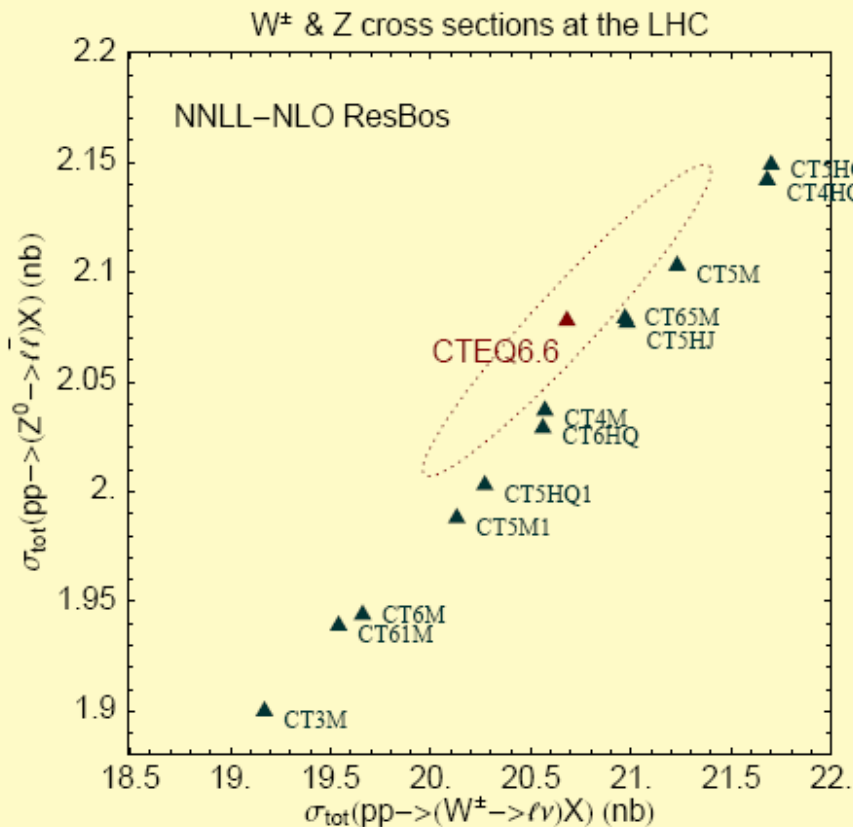
\rightarrow **at small Q^2 massive, at large Q^2 massless**

General Mass VFNS (GM VFNS)

Zero Mass Variable Number Scheme (ZM VFNS)

CTEQ6.5 uses a *General Mass* scheme changed from a *massless* in CTEQ6.1
MRSTW improved their *General Mass* scheme from MRST2004 to MSTW2006

Impact on W, Z @ LHC

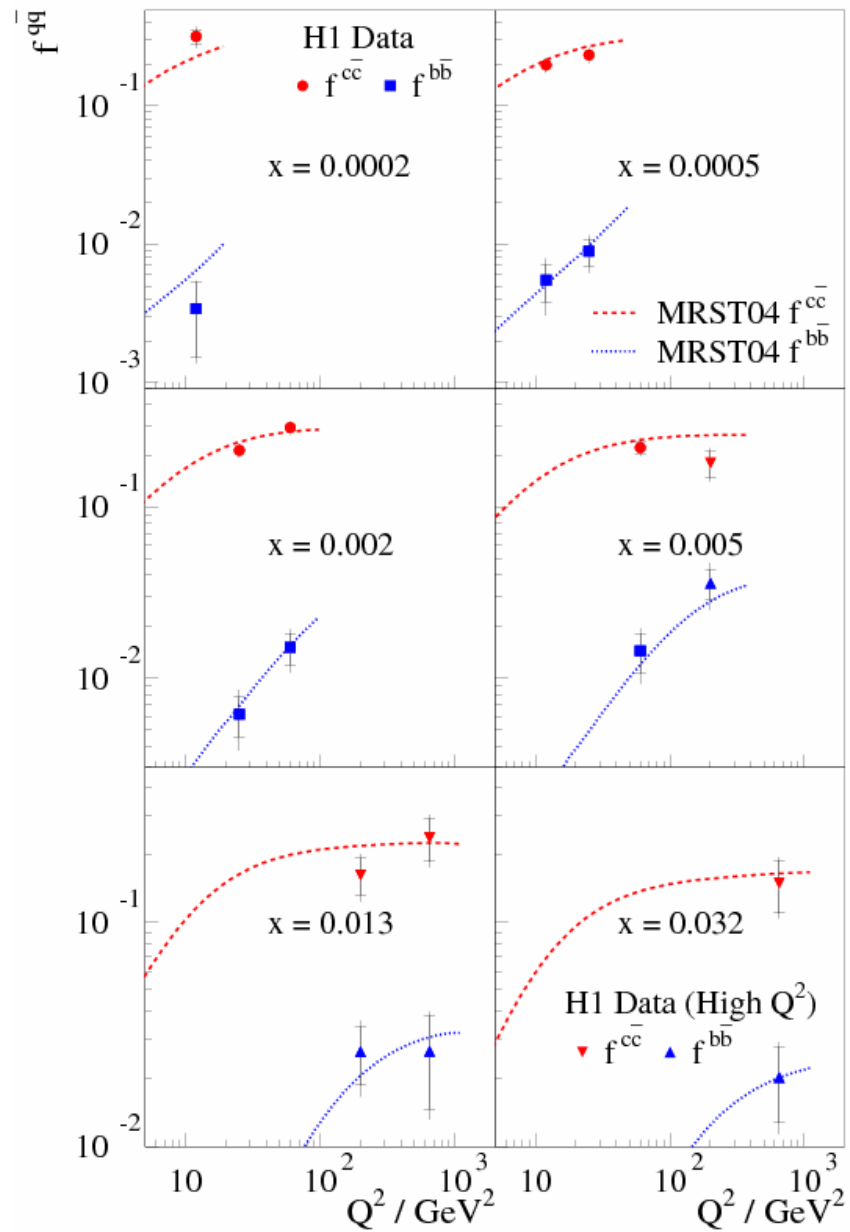


- Correct heavy flavour treatment affects light partons!
- changes in CTEQ 6.1 -> CTEQ 6.6 due to c, b, s treatment
- Improved agreement between latest PDFs

Heavy Quark contribution to DIS cross section

HERA I result:

- fraction of total DIS cross section from **charm** and **beauty**
- large charm fraction (~30%)
- small beauty fraction ~% (lower at low Q^2)
- mass thresholds visible
- reasonable description by pQCD

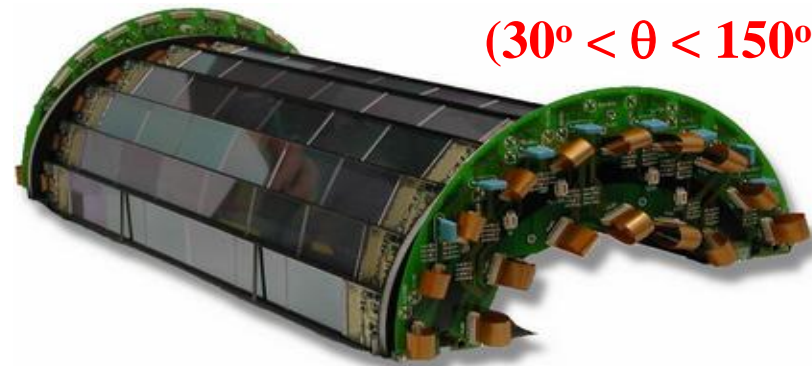


Flavour Tagging - Vertex Detectors

H1

Central Silicon Tracker

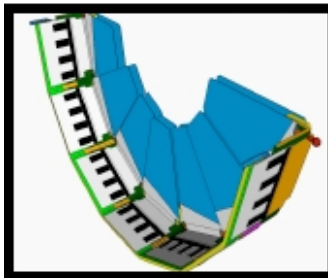
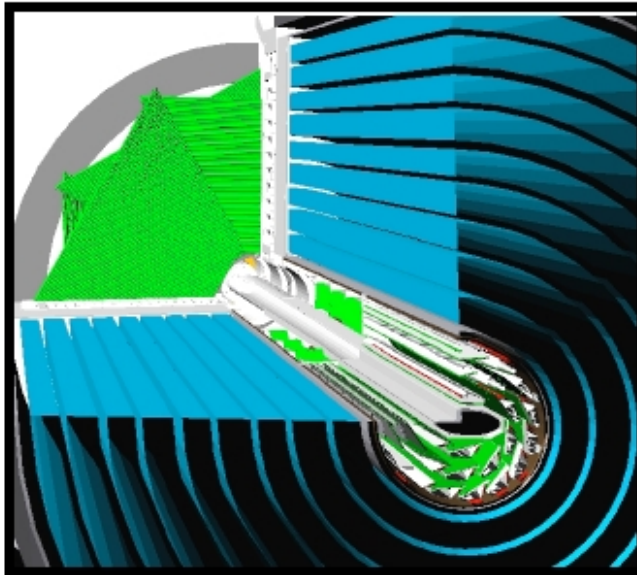
$(30^\circ < \theta < 150^\circ)$



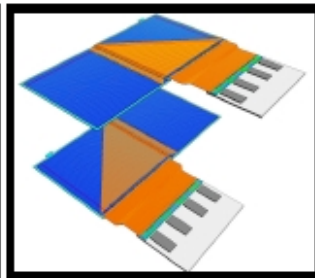
- Double layer double sided strips
- Precise determination of impact parameter in transverse plane
- Resolution of $|\delta|$ for hits in both layers;

$$33\mu\text{m} \oplus \frac{90\mu\text{m}}{P_T} [\text{GeV}]$$

ZEUS tracking (MVD)



Half Wheel



Barrel module

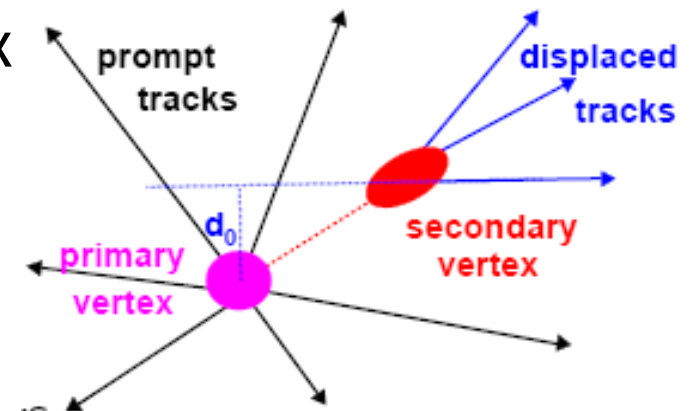
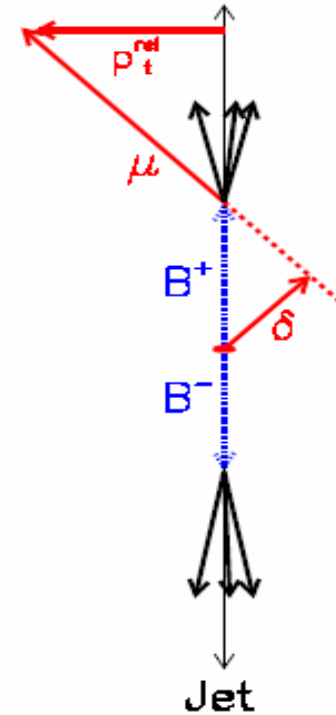
Installed for HERA II

Installed 1997 (first pub 2004)!

Tagging Heavy Quarks (b)

Beauty quarks rarely produced, use properties of beauty hadrons:

- semileptonic decays (μ, e)
- mass
 - transverse momentum p_t^{rel} relative to jet axis
- lifetime (vertex detectors)
 - reconstruction of a secondary vertex
 - impact parameter δ

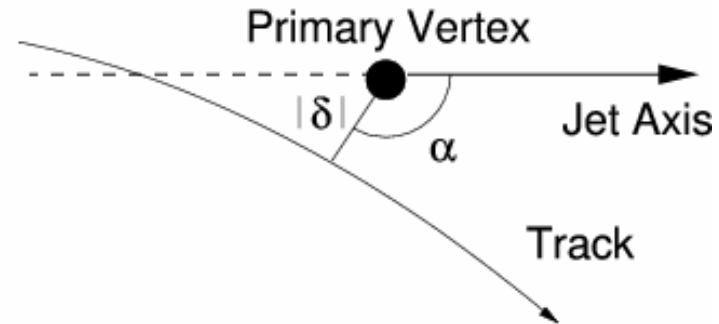
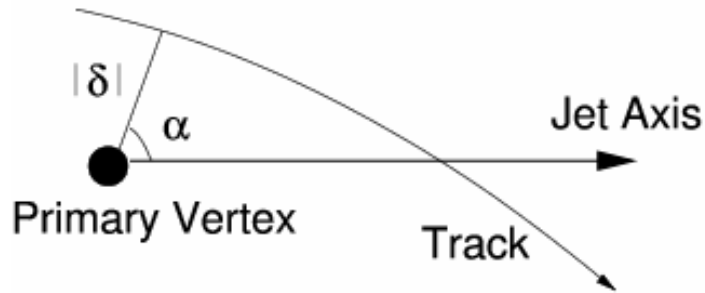


Signed Impact Parameter δ

Signed impact parameter δ , Significance = $\delta/\sigma(\delta)$

$$\alpha < 90^\circ \rightarrow \delta = +|\delta|$$

$$\alpha > 90^\circ \rightarrow \delta = -|\delta|$$



Charm and beauty asymmetric (positive) due to lifetime

Light flavours mostly symmetric (resolution dominates)

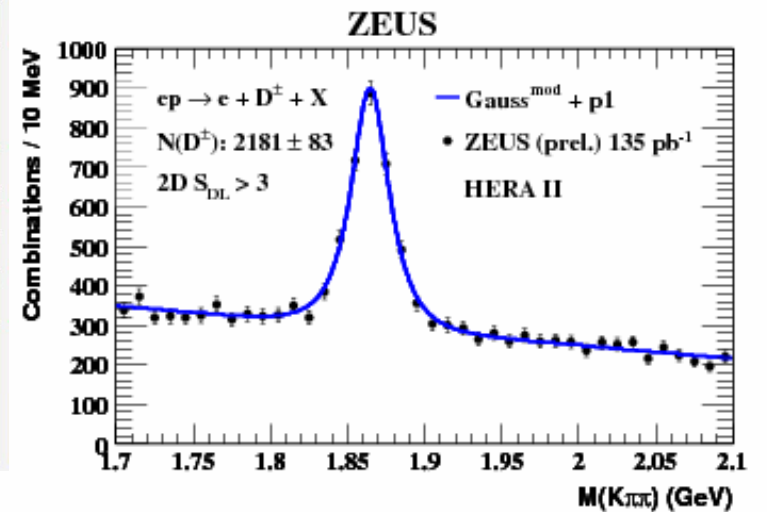
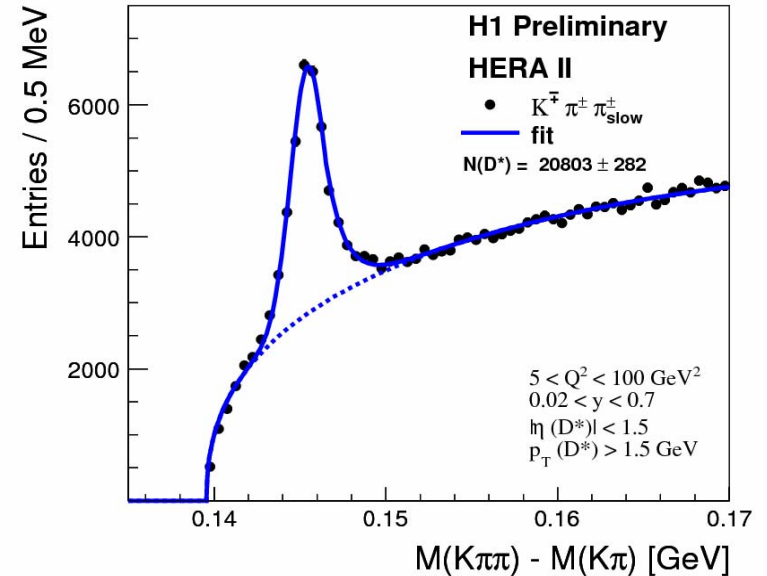
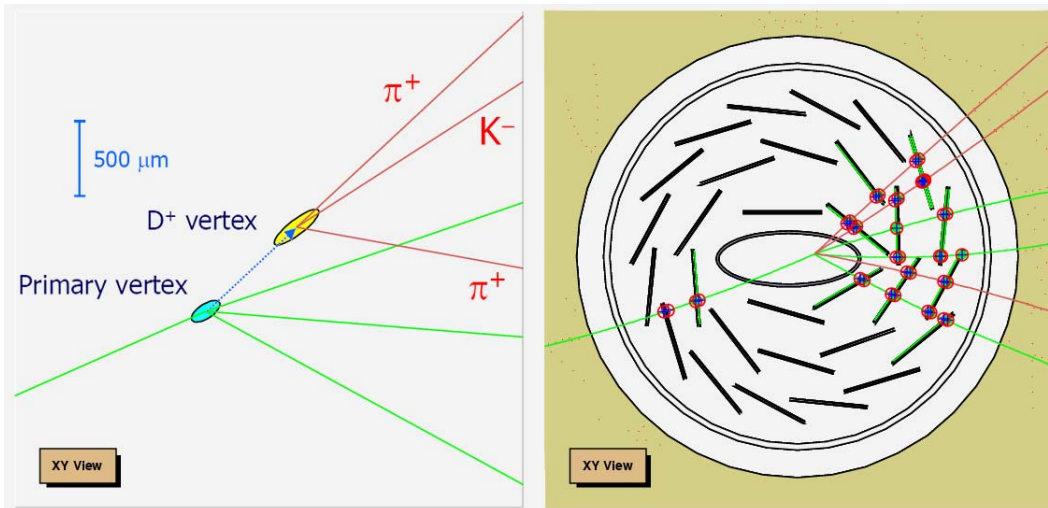
Similarly for secondary vertices (≥ 2 tracks), decay length L and decay length significance = $L/\sigma(L)$

Tagging Heavy Quarks (c)

resonances D^* , D^+ , D^0 , ...

Full HERA II statistics ($\sim 350\text{pb}^{-1}$)

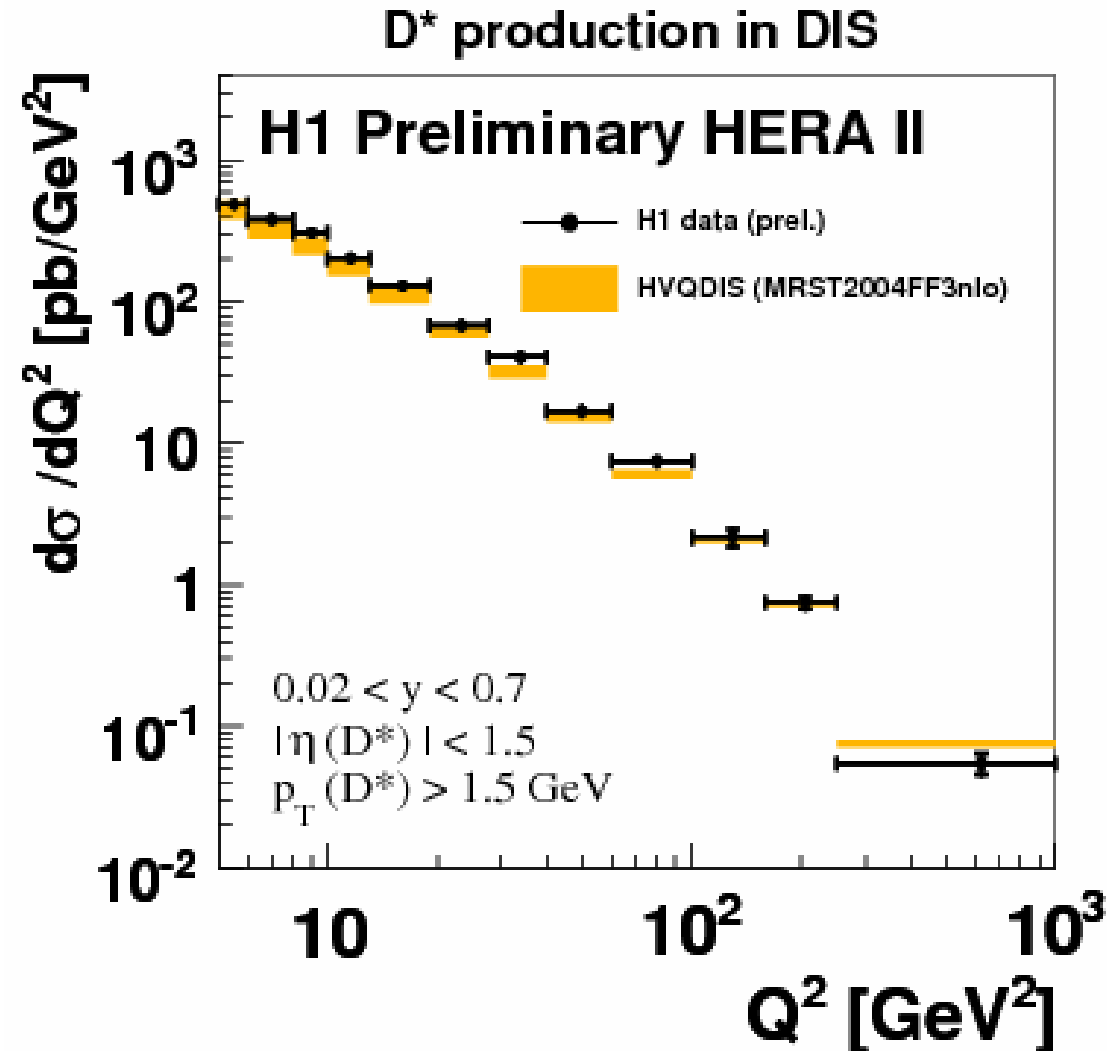
resonances and decay length
tagging using vertex detectors



D* Cross Section

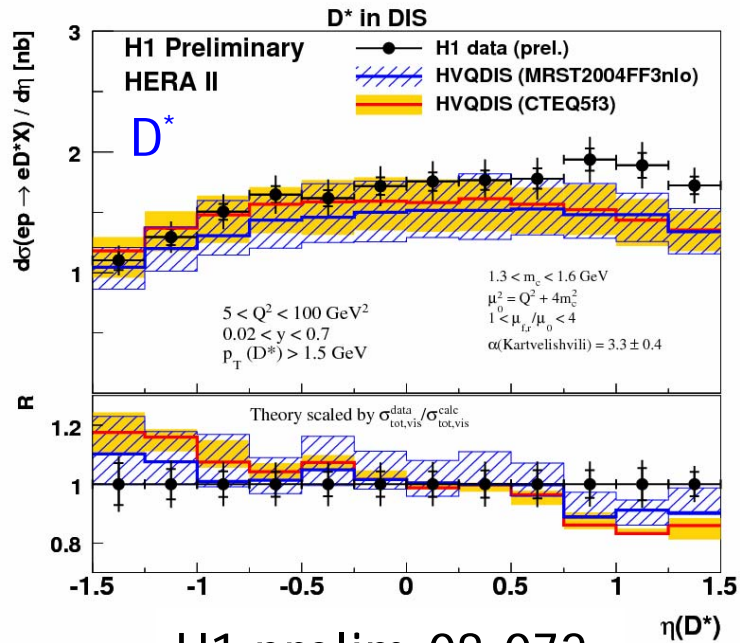
H1 prelim-08-072

H1 prelim-08-074



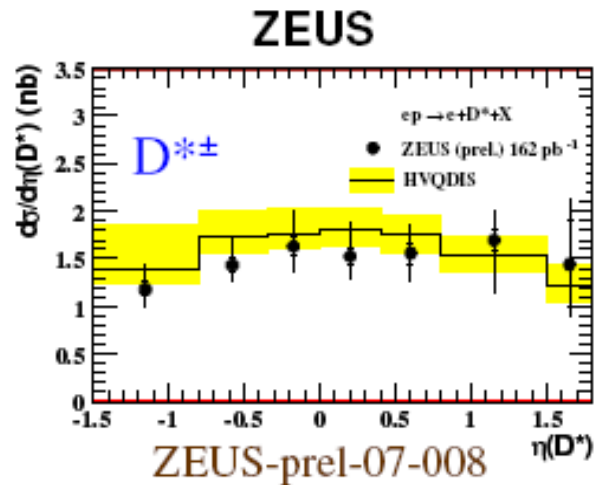
- good description by NLO calculation (HVQDIS) in wide Q^2 range
- Also at large Q^2 , where massive approach not expected to be appropriate

D* Cross Section

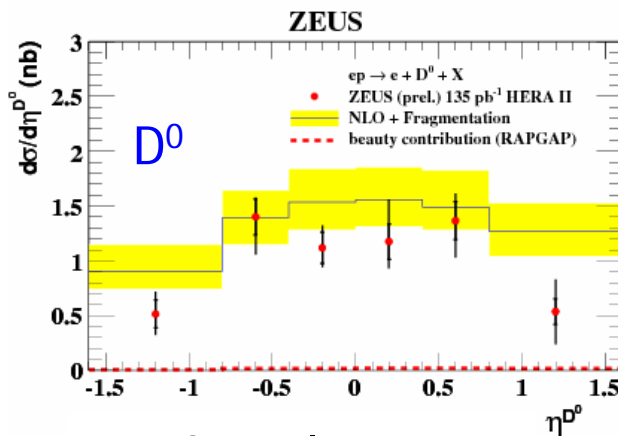


H1 prelim-08-072

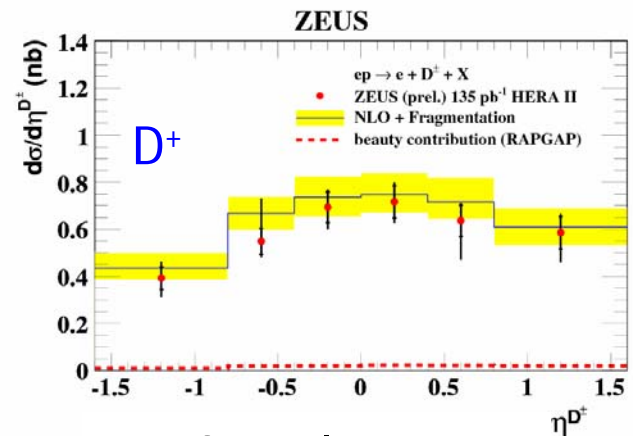
- differential cross sections of several D mesons measured
- reasonably described by NLO QCD (HVQDIS)
- double differential in x and Q^2 allows extraction of F_2^{cc}



ZEUS-prel-07-008



ZEUS-prel-07-034

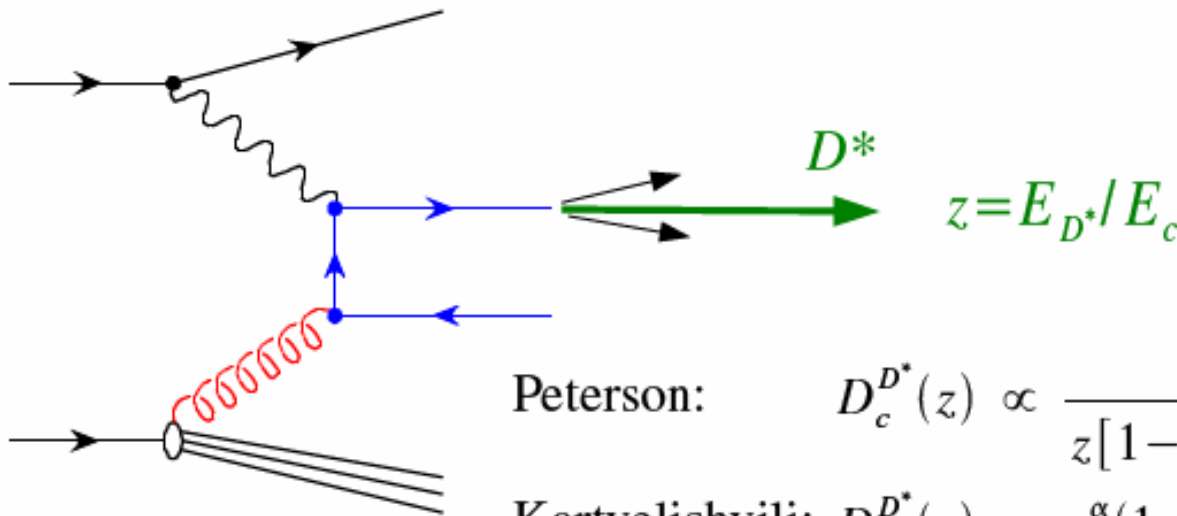


ZEUS-prel-07-009

D* Fragmentation

$$\sigma_{D^*} \propto f_{g/p} \otimes \hat{\sigma} \otimes D_c^{D^*}(z)$$

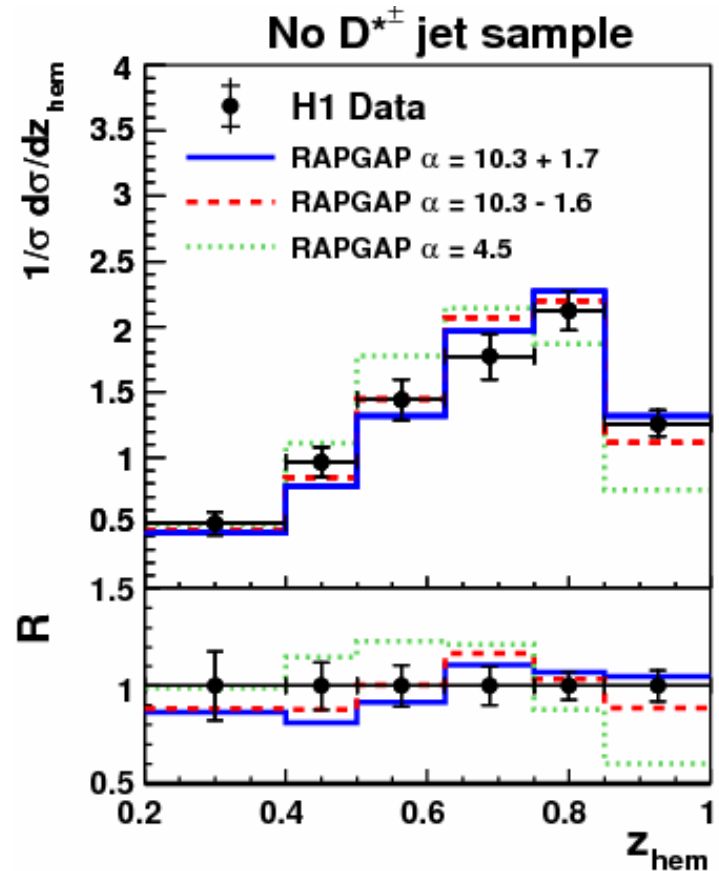
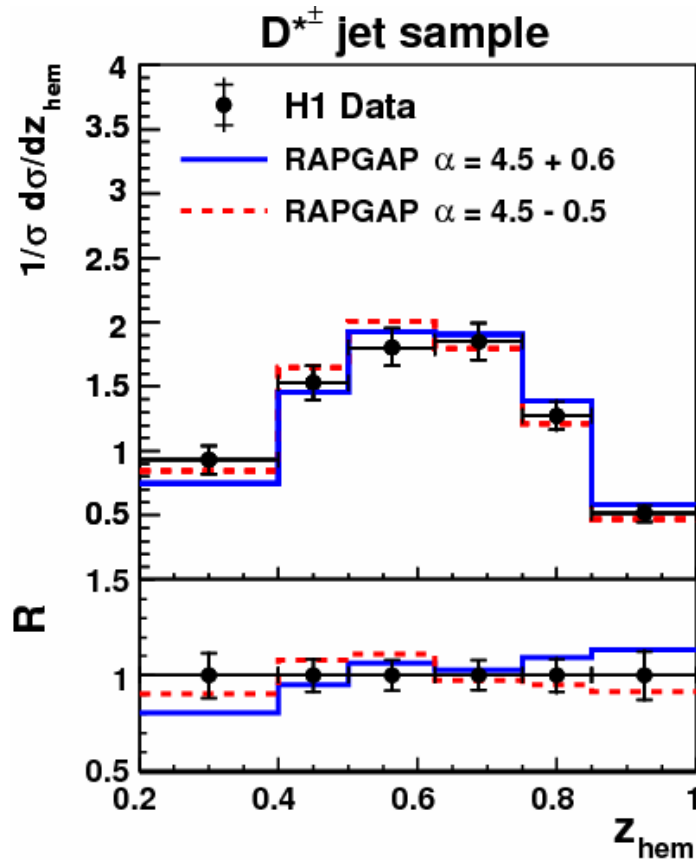
parton density function (non-perturbative)
 parton scattering cross section (perturbative)
 fragmentation function (non-perturbative)



Peterson: $D_c^{D^*}(z) \propto \frac{1}{z[1-(1/z)-\epsilon/(1-z)]^2}$

Kartvelishvili: $D_c^{D^*}(z) \propto z^\alpha(1-z)$

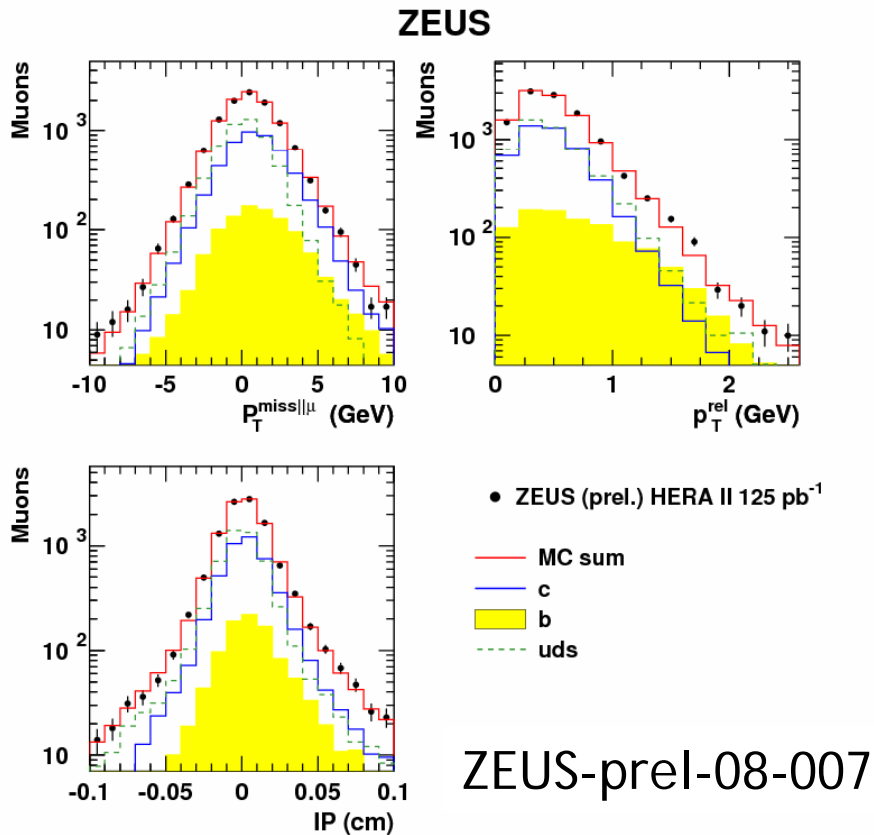
D* Fragmentation



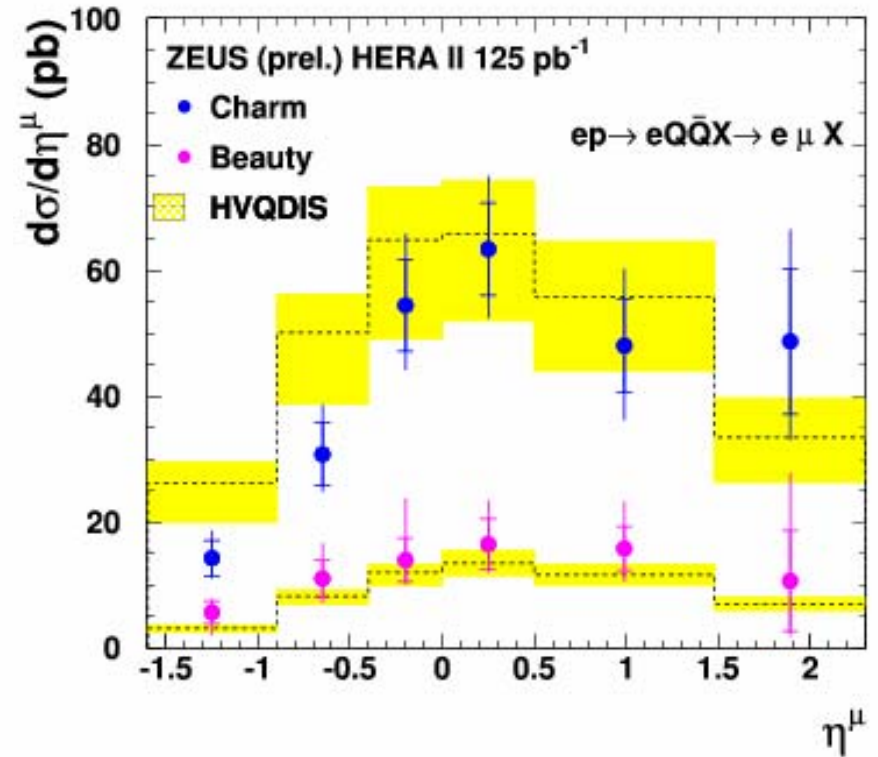
- RAPGAP MC: $p_{T,\text{jet}} > 3 \text{ GeV}$, parameters consistent with e^+e^-
- no jet sample (low photon gluon COM) needs harder frag.
- Similar story for NLO QCD

Charm and Beauty Cross Section

- combine $p_{T}^{\text{miss}||\mu}$, p_{T}^{rel} and impact parameter distributions
- use 3D fit to decompose into beauty, charm and light flavour

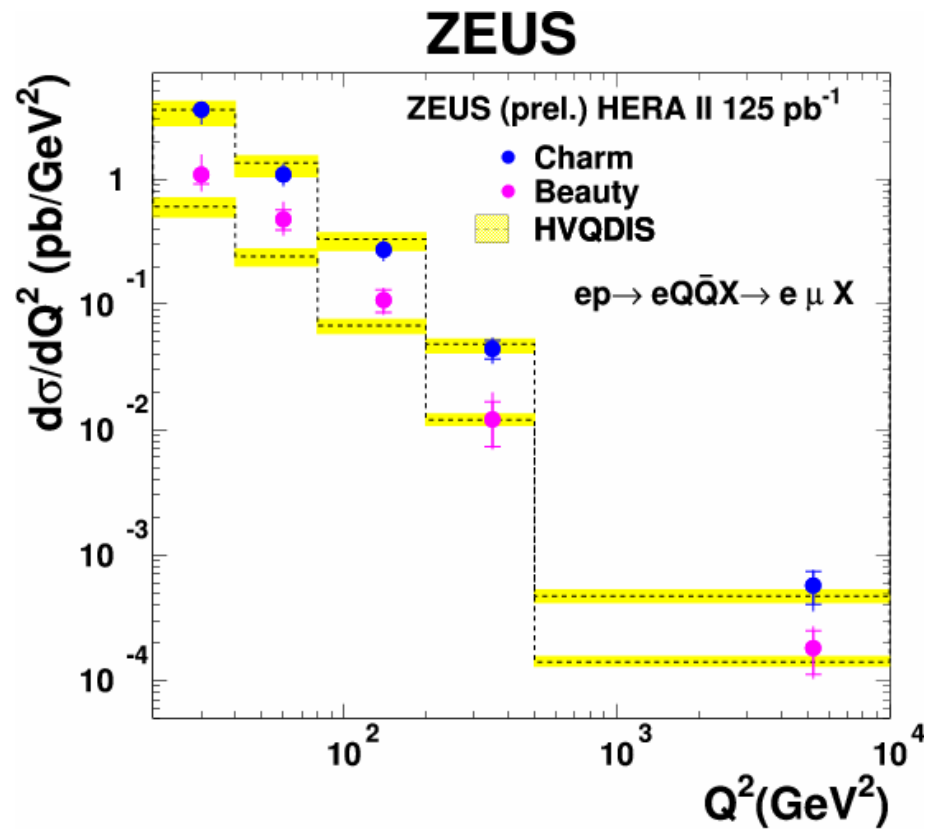
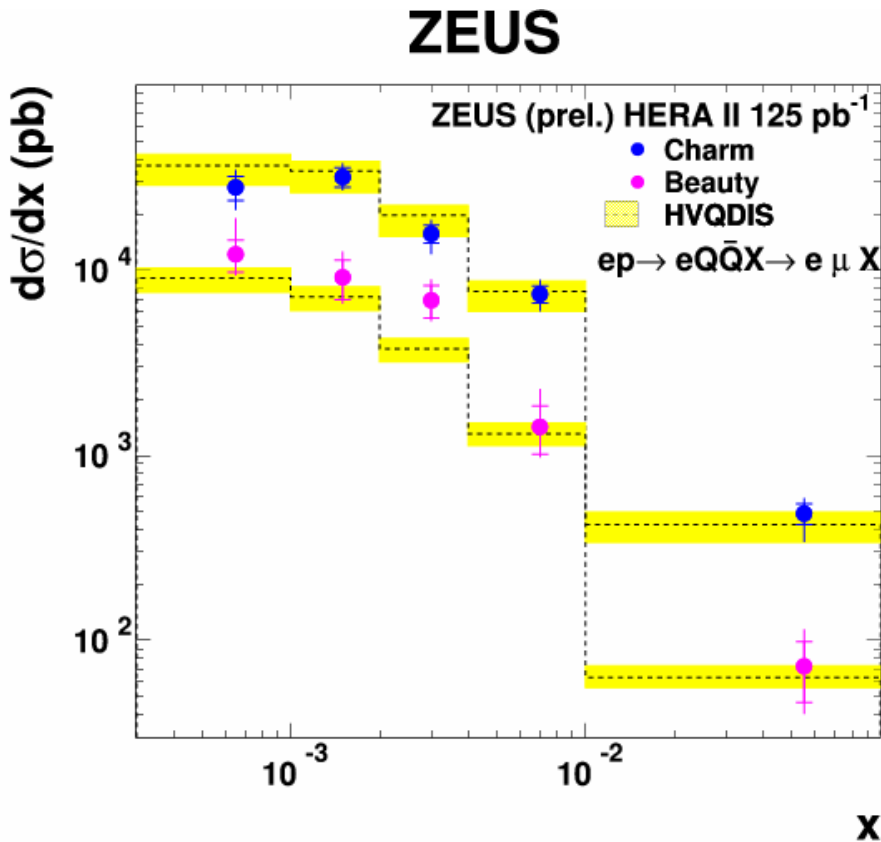


ZEUS



- $Q^2 > 20 \text{ GeV}^2$, $0.01 < y < 0.7$, $P_{T\mu} > 1.5 \text{ GeV}$, $-1.6 < \eta_\mu < 2.3$
- c and b cross sections described by NLO QCD(HVQDIS)

Charm and Beauty Cross Section



- beauty tends to be above NLO QCD at low Q^2
- may be measured double differentially in x , Q^2 and extrapolated to full phase space to compare F_2^{cc} , F_2^{bb}

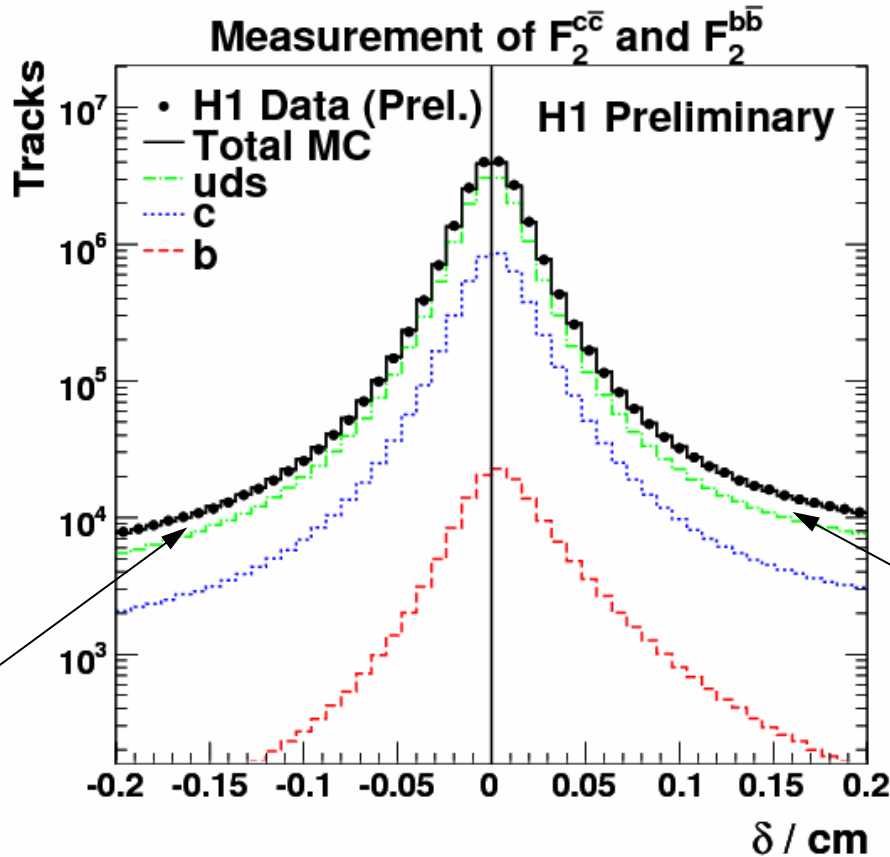
H1 Inclusive Analysis

H1 prelim-08-173

- Publication on HERA I data (54 pb^{-1}) in 2004 & 2005
- H1 CST rebuilt to account for HERA II beamline
- Preliminary analysis on full HERA II data (190 pb^{-1}) this summer (H1prelim-08-173)
- Inclusive analysis: use all tracks with hits in silicon detector ($p_t > 0.3 \text{ GeV}$)
- Precise determination of impact parameter in transverse plane
- Divide events into 1 track, 2 track and ≥ 3 track samples

Signed Impact Parameter (H1)

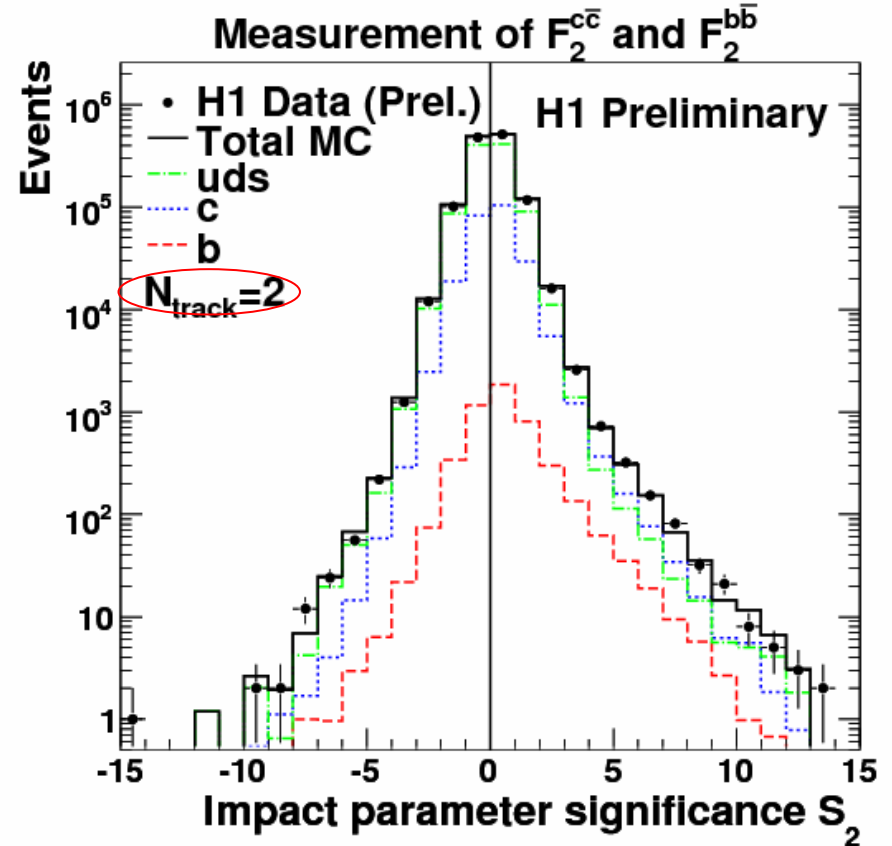
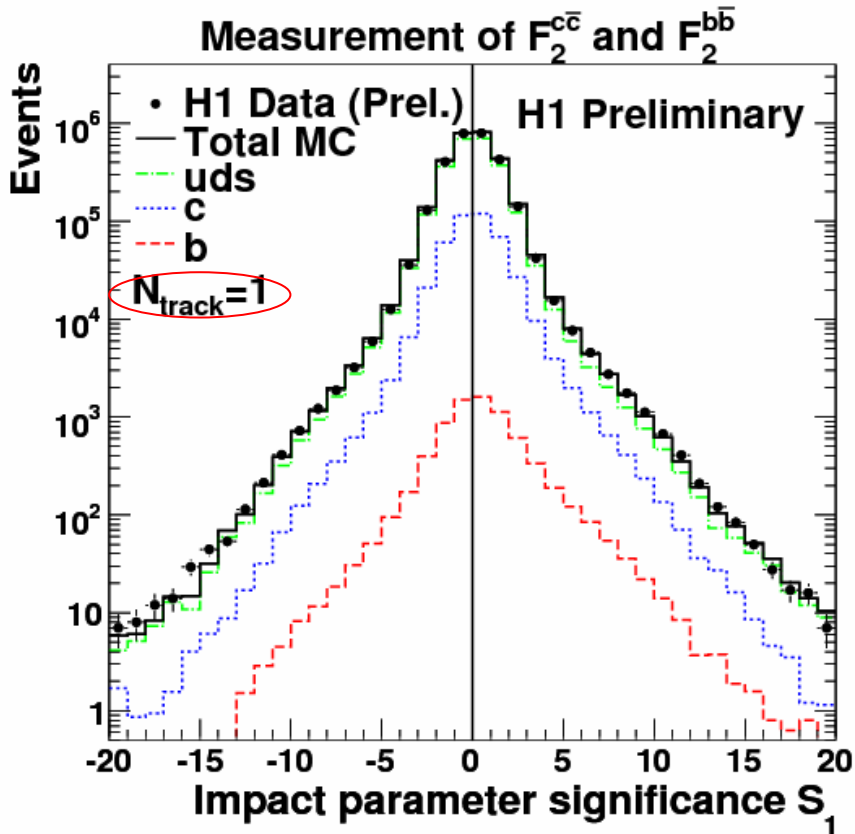
H1 prelim-08-173



Charm and beauty asymmetric due to lifetime, Light flavours mostly symmetric

MC describes resolution!

Significance



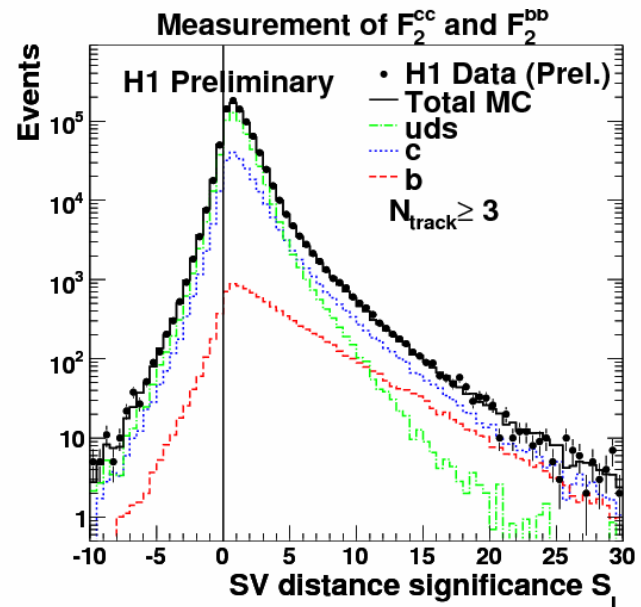
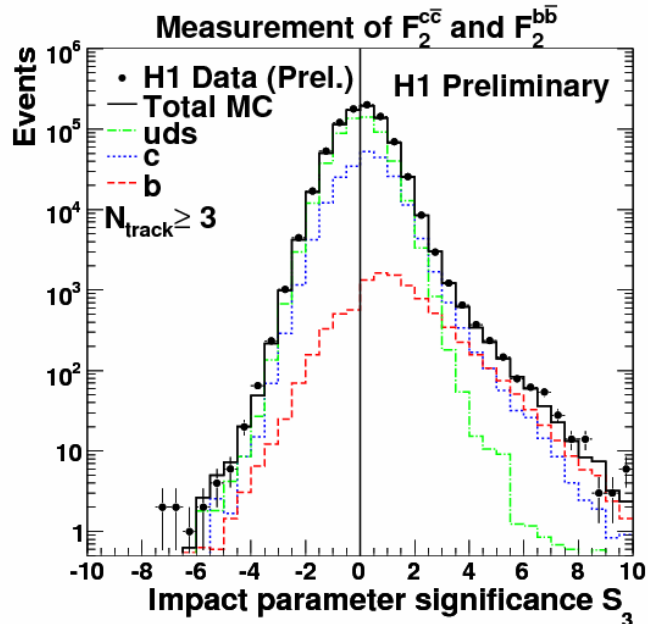
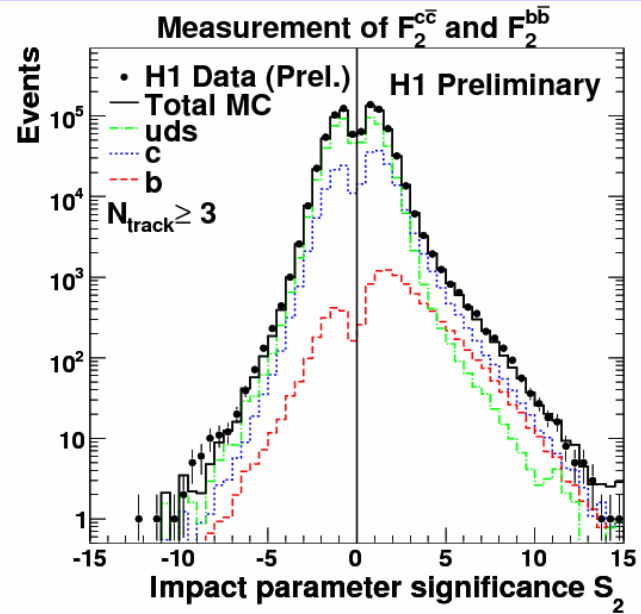
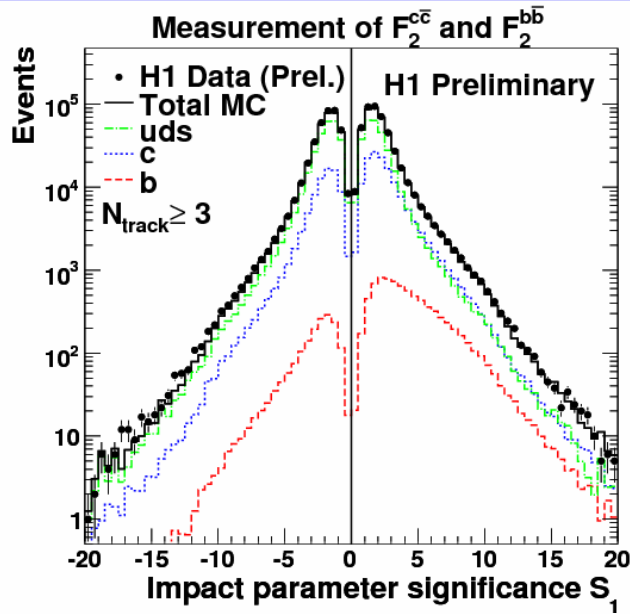
Significance for $N_{\text{track}}=1$

2nd highest significance for $N_{\text{track}}=2$

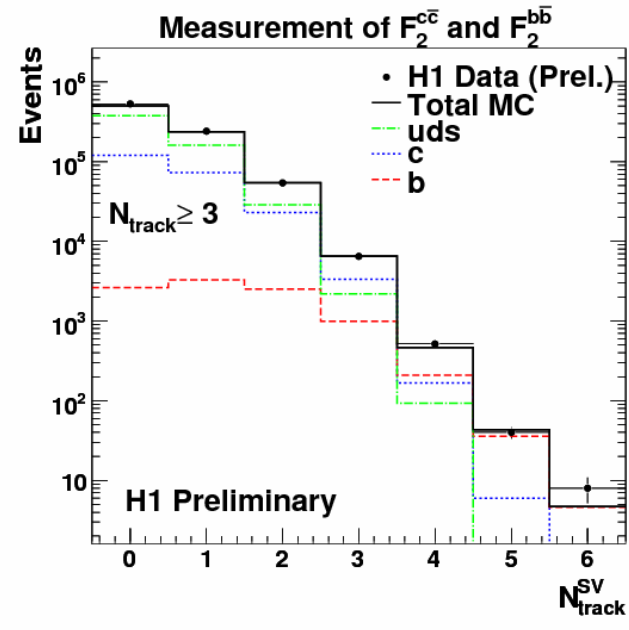
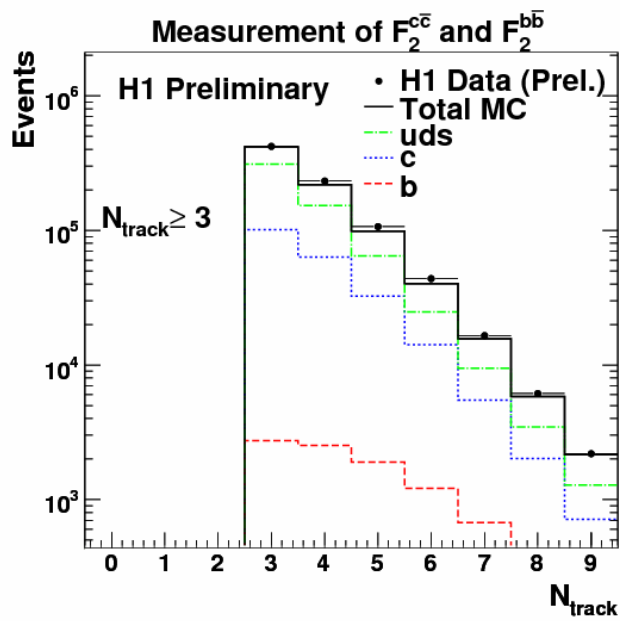
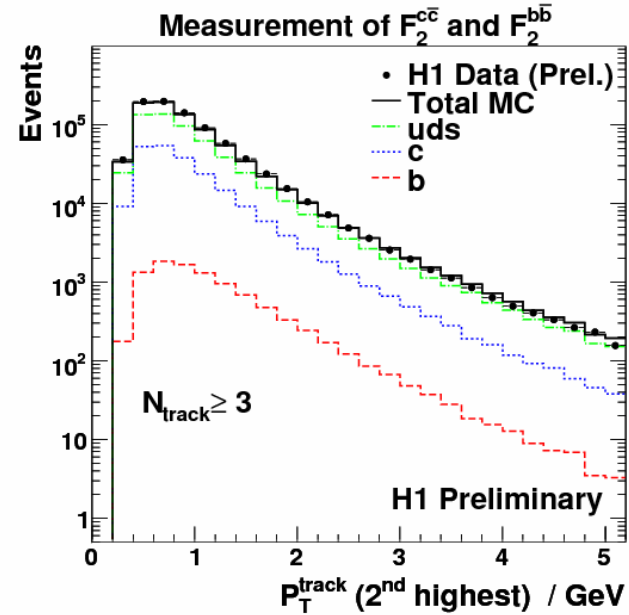
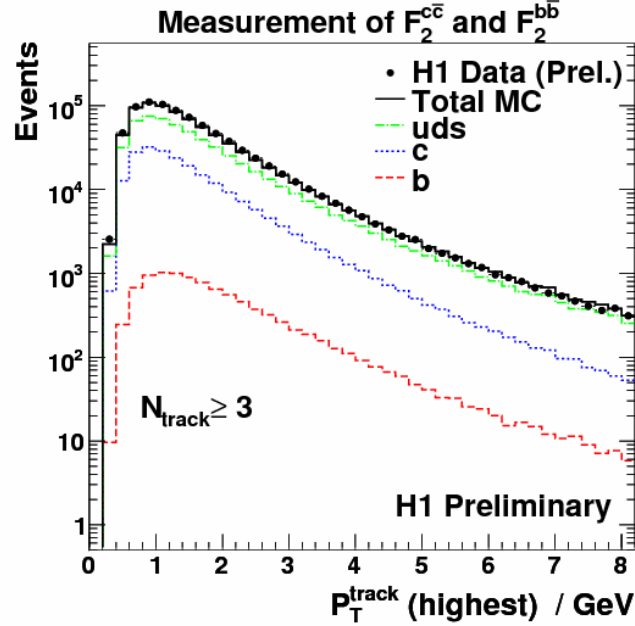
Neural Network

- Improve c, b separation power (especially at low Q^2): use neural network for ≥ 3 track events
- Choose inputs which are different for c and b , and largely physics model independent
- Inputs: S_1, S_2, S_3, S_L , track p_t , 2nd highest track p_t , number of CST tracks, number of tracks associated to secondary vertex
- Network trained with b as “signal” c as “background”. Light flavours will be subtracted out due to their symmetry (see later)

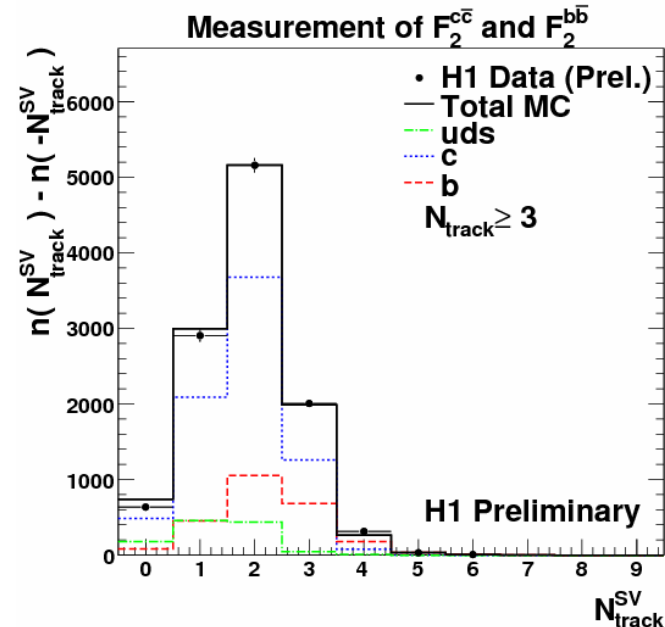
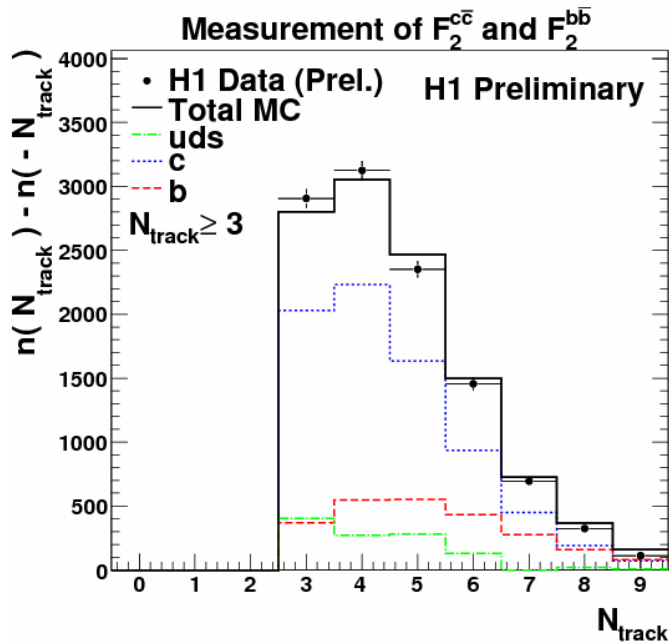
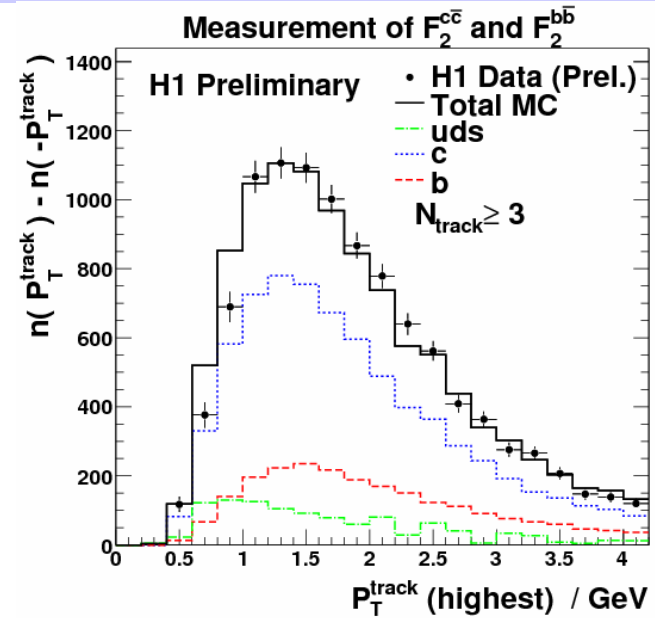
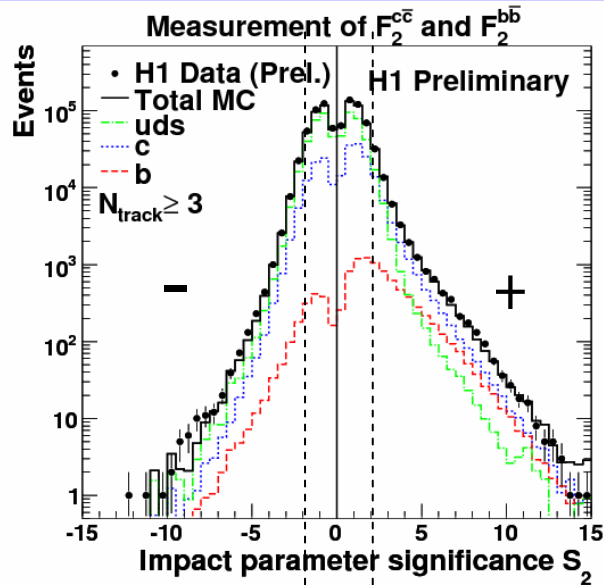
Neural Network Inputs



Neural Network Input

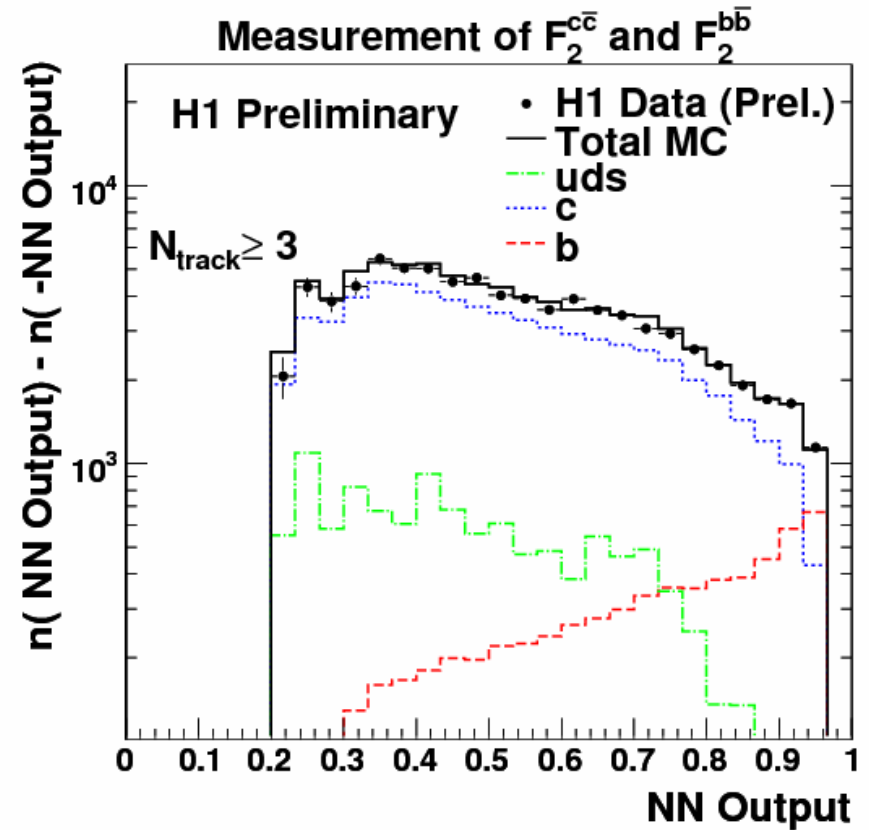
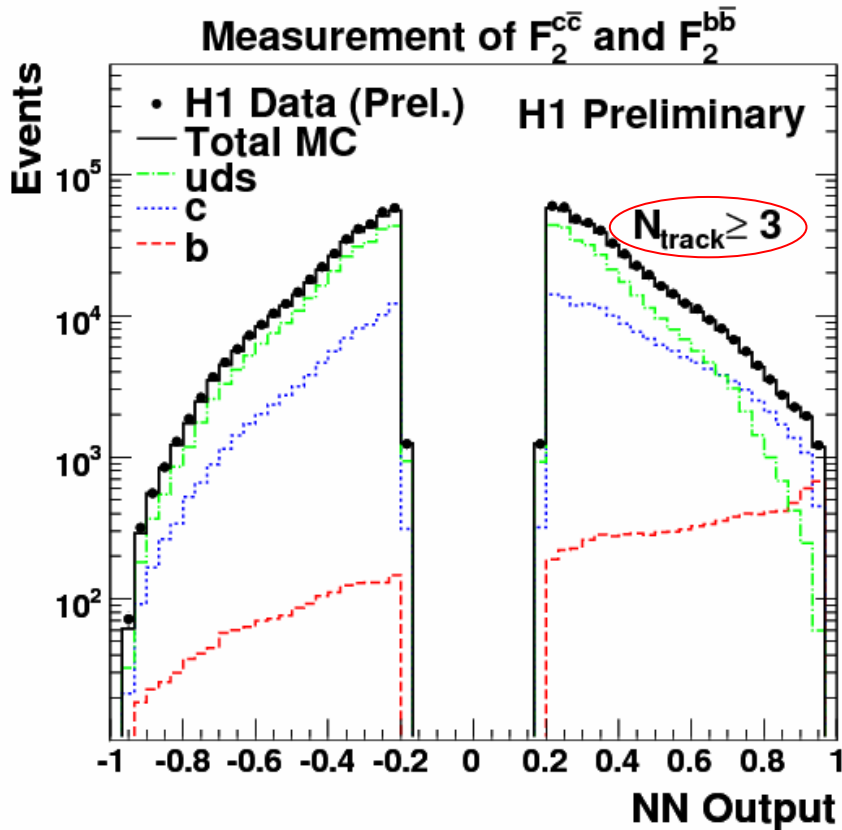


Neural Network Input (Neg. subtracted)



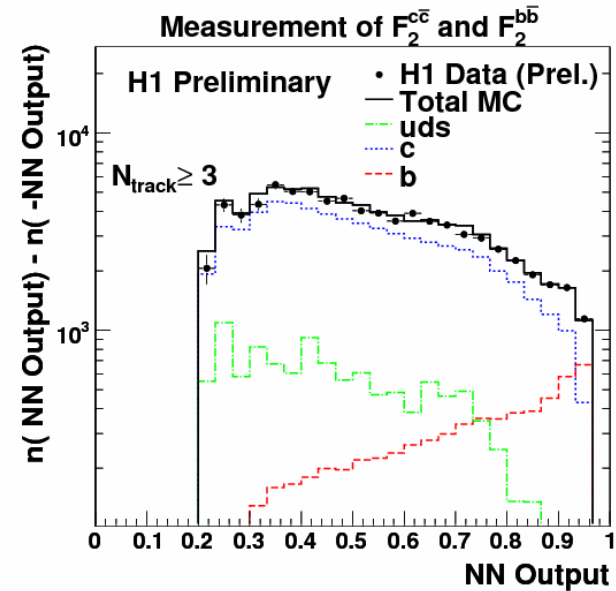
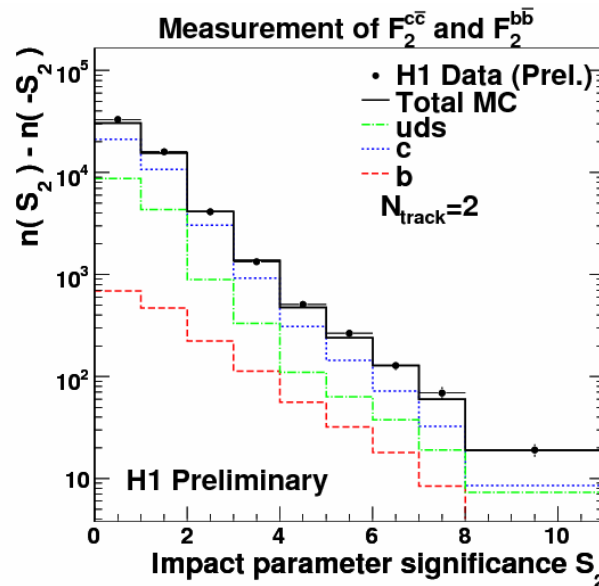
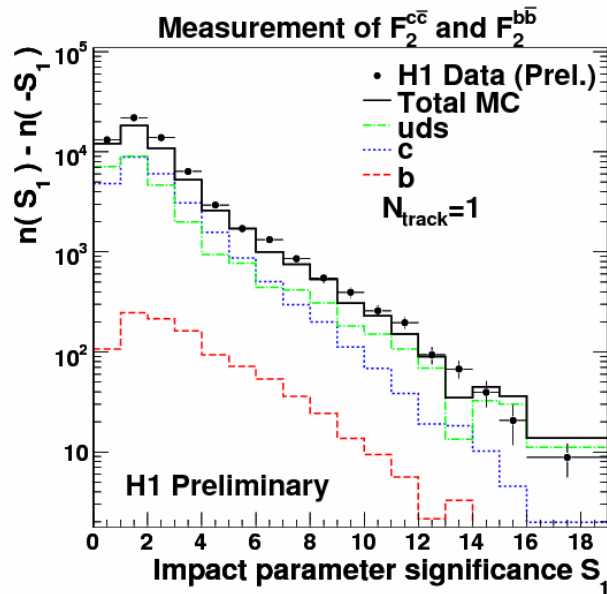
Neural Network Output

- Sign given by S_1 . Subtract -'ve from +'ve to reduce systematic error due to resolution and light contribution



Extracting Flavour Fractions

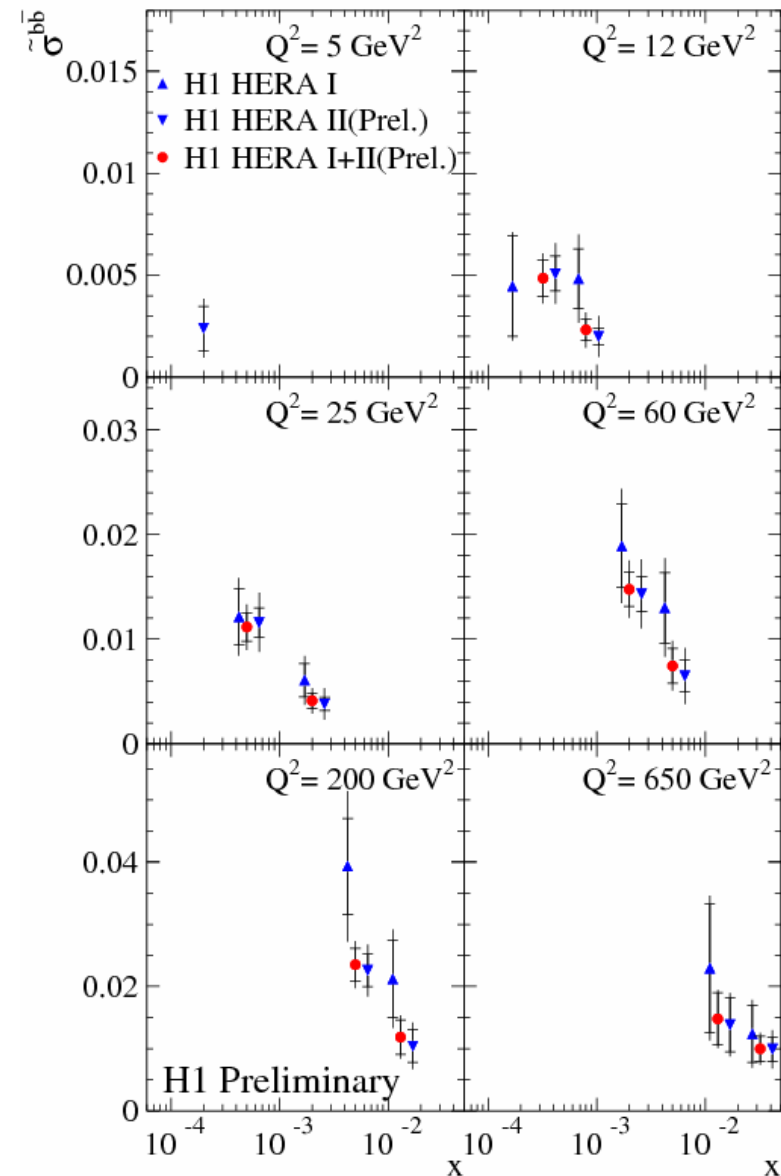
These distributions are fitted for ρ_c, ρ_b in each x, Q^2 bin with ρ_{uds} constrained by total number of DIS events



$$f_c = \frac{\rho_c \cdot N_c^{\text{gen}}}{\rho_c \cdot N_c^{\text{gen}} + \rho_b \cdot N_b^{\text{gen}} + \rho_{uds} \cdot N_{uds}^{\text{gen}}}$$

Inclusive b cross section (H1)

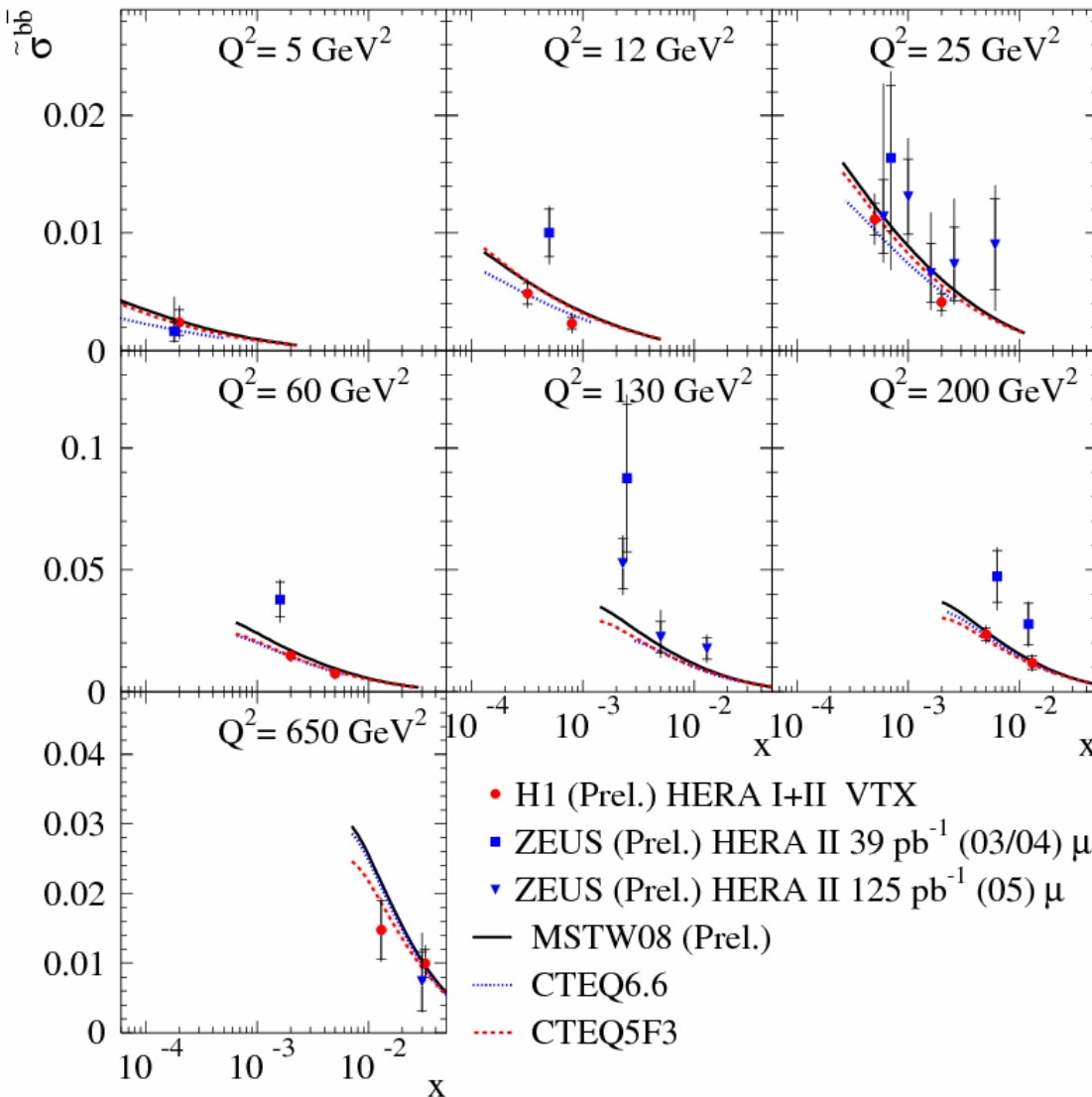
H1 BEAUTY CROSS SECTION IN DIS



- HERA I agrees with HERA I
- HERA II reaches lower Q^2 (NN)
- HERA I and HERA II data combined for improved precision

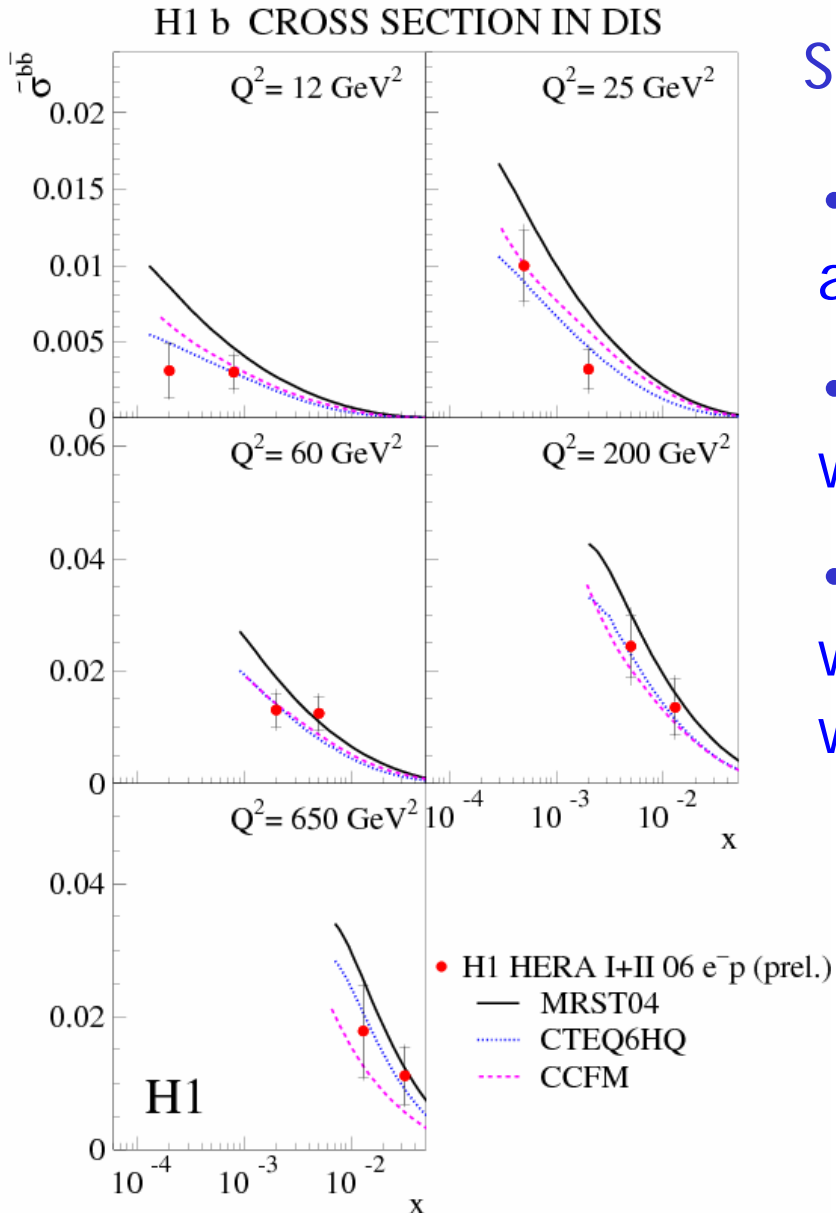
Inclusive b Cross Section (HERA)

H1+ZEUS BEAUTY CROSS SECTION in DIS



- comparison of different methods [acceptance]
 - Inclusive (H1VTX) [$>90\%$]
 - μp_t^{rel} (ZEUS 03/04 μ) [20-35%]
 - $\mu p_t^{\text{rel}} + \delta$ (ZEUS 05 μ) [25-50%]
- ZEUS tend to be higher than H1
- generally described by NLO QCD (FFNS, GM-VFNS)

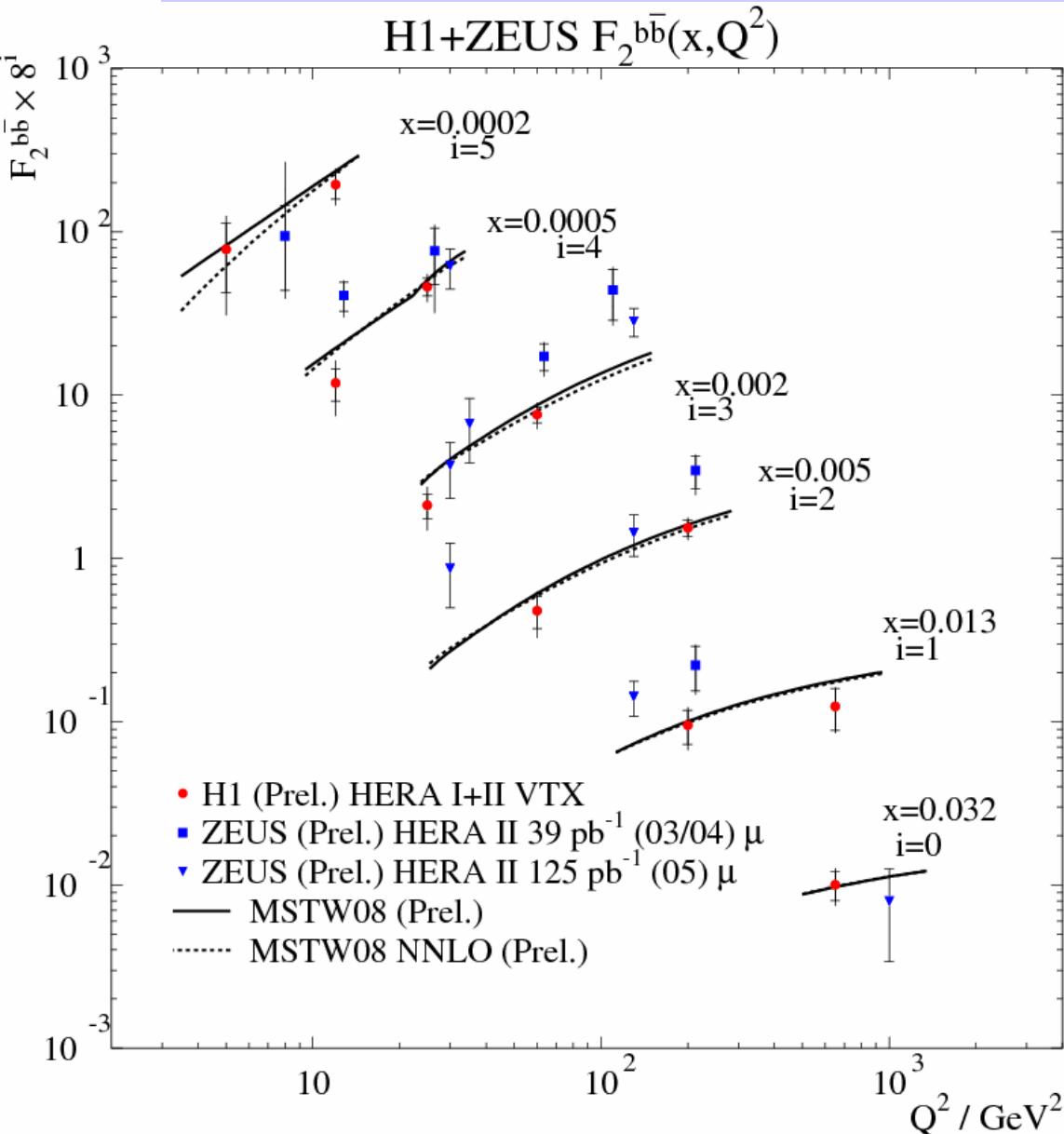
Improvements in Theory



Status summer 2007 (e^- data)

- MRST04 factor 2 larger than CTEQ at $Q^2=12 \text{ GeV}^2$
- Chance to distinguish models with full HERA II data
- Since then MSTW08 was released which is in much better agreement with CTEQ (and data)!

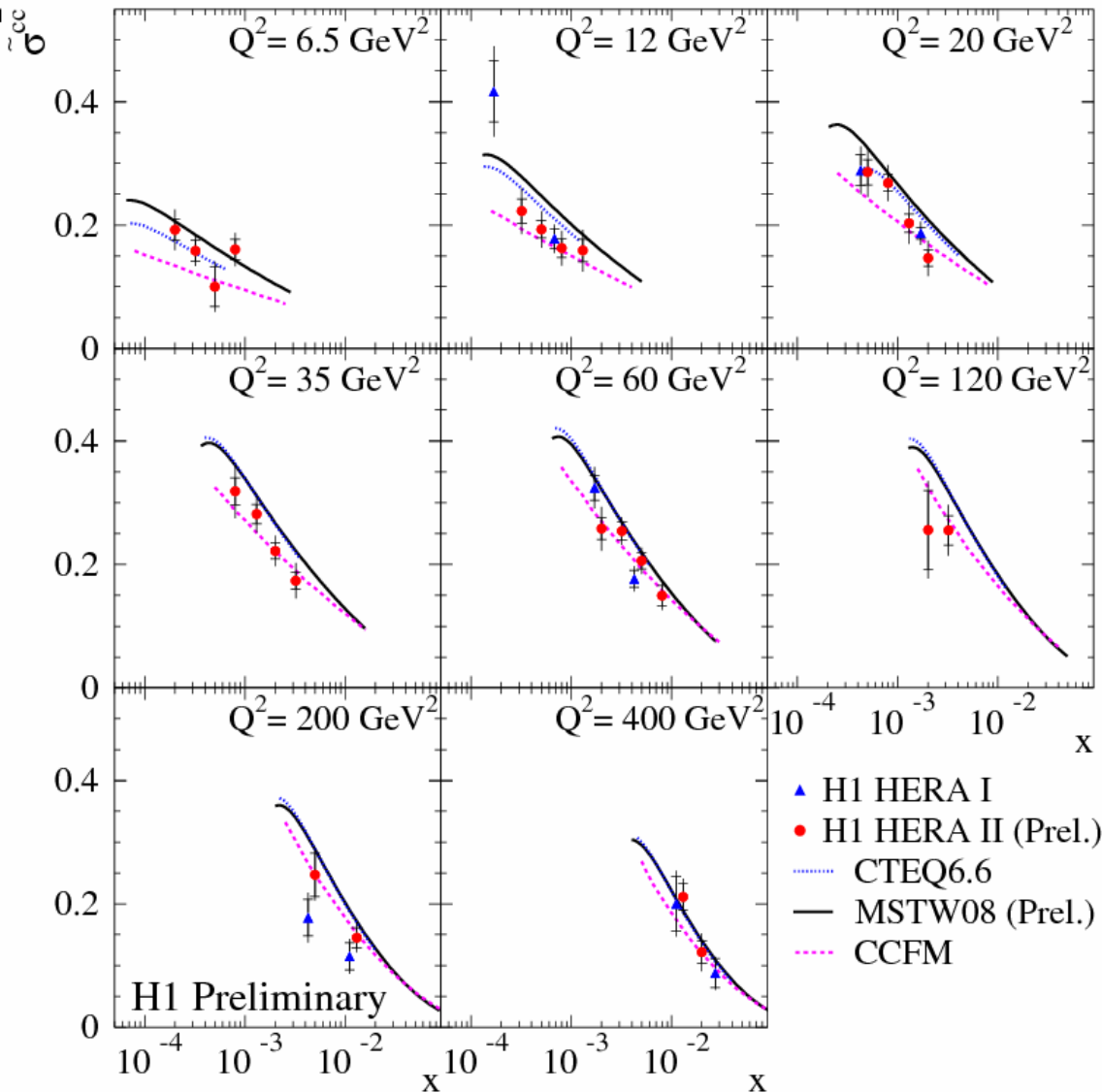
Measurements of $F_2^{b\bar{b}}$ (HERA)



- Beauty structure function versus Q^2
- NNLO predictions available
- Differences between NLO and NNLO small except for $Q^2 < (m_b)^2$

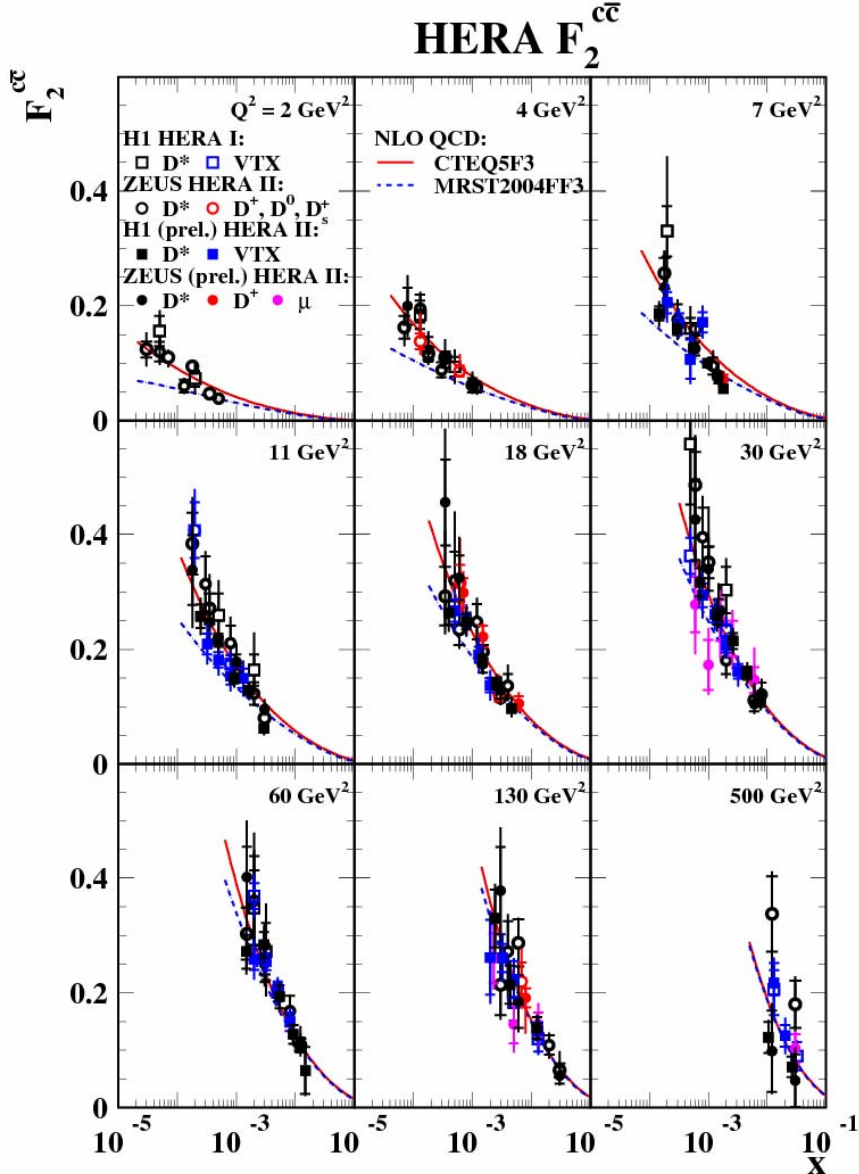
Inclusive Charm Cross Section (H1)

H1 CHARM CROSS SECTION IN DIS



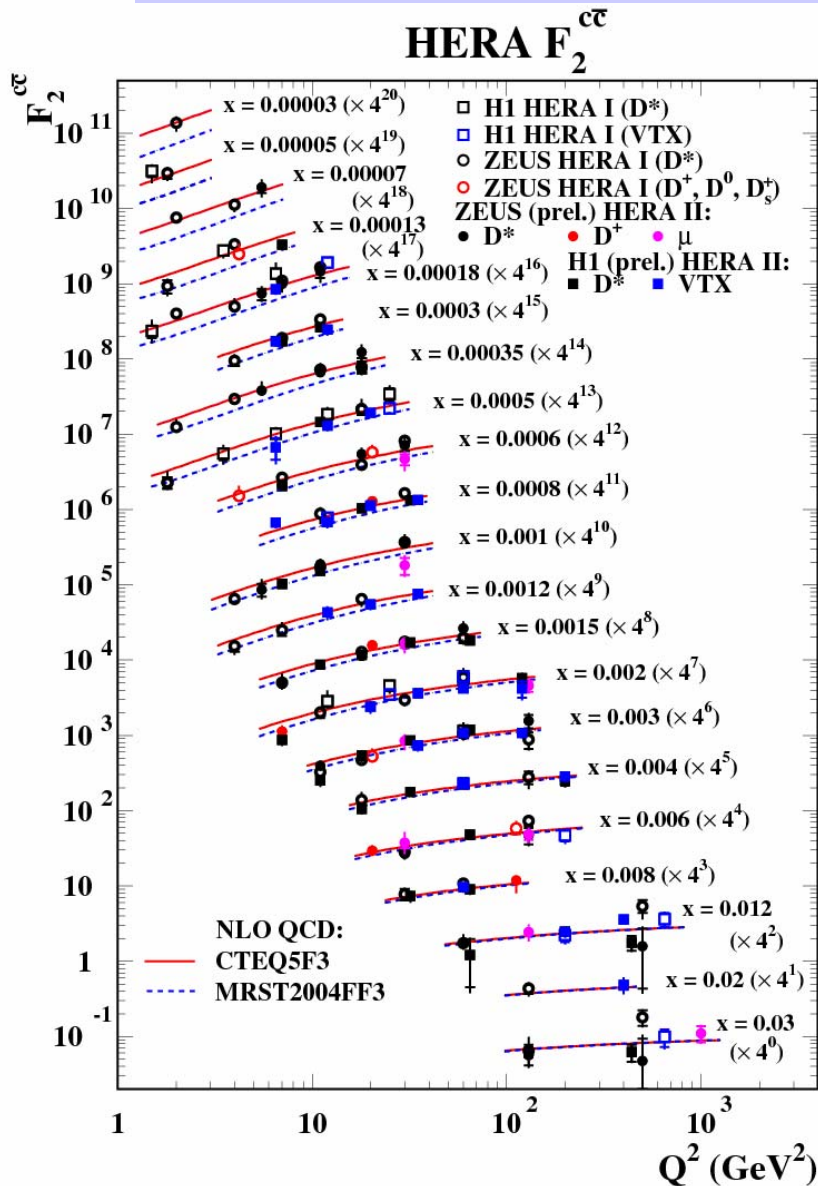
- HERA I agrees with HERA II
- HERA II has finer binning for charm and reaches lower Q^2
- Reasonable description by GM VFNS PDFs from CTEQ and MSTW
- Also by PDF based on CCFM evolution.

Inclusive Charm Cross Section (HERA)



- comparison of different methods [acceptance]
- Inclusive (H1 HERA I II VTX) [$>70\%$]
- Mu ptrel+ δ (ZEUS HERA II μ) [25-50%]
- D^* cross sections [20-70%]
- different methods agree well
- wealth of precise measurements
- combine to improve precision

Measurements of $F_2^{c\bar{c}}$ (HERA)



- Charm measurements span large range in Q^2 and x
- Theory differences for $Q^2 < (2m_c)^2$
- These are the “massive” FFNS PDFs (because the D^* measurements involve model dependent extrapolations) and are not the latest GM VFNS technology

Conclusions

- Wealth of new measurements of the heavy flavour content of the proton from HERA data.
- Extraction of structure functions F_2^{cc} and F_2^{bb} allow comparison of many different measurement techniques.
- Data are described by latest (N)NLO pQCD calculations.
- Final results with full HERA statistics expected soon
- Data help to constrain theory mass treatments and PDFs in time for LHC!

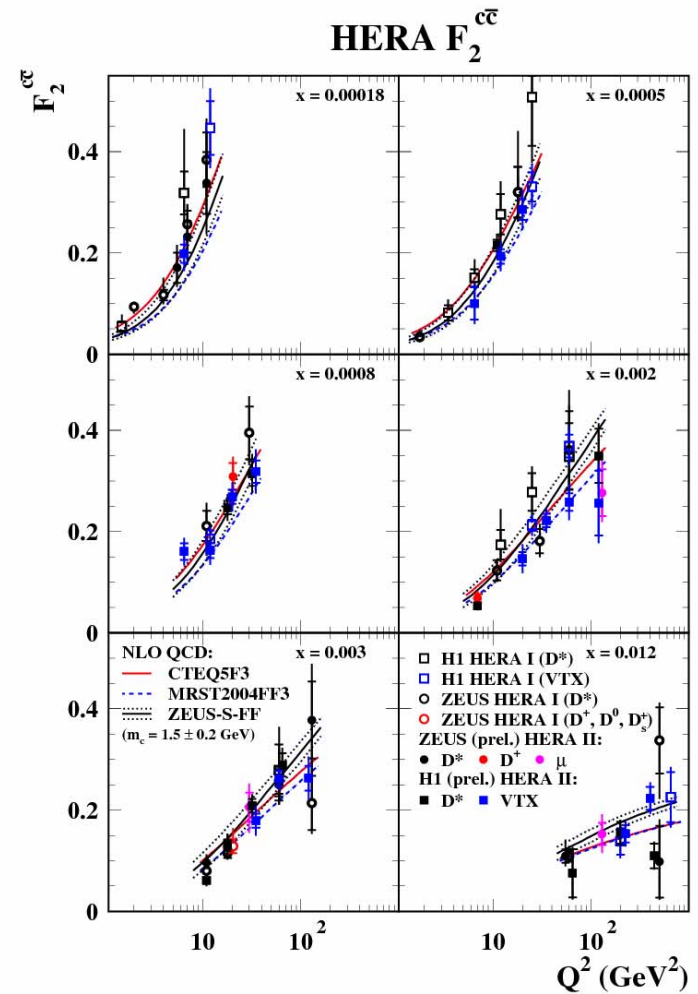
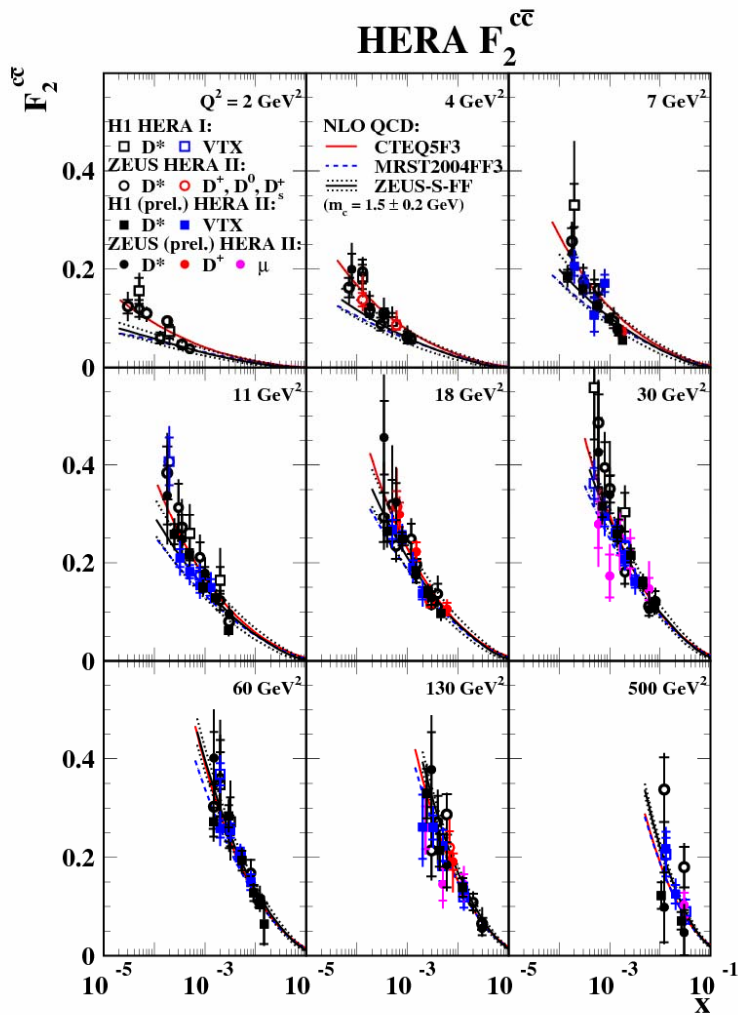
Hope there are more prizes to discover at the LHC...!



Annual CERN Road Race Sept. 2008

Back Up

Scale Uncertainty (c)



Scale Uncertainty (b)

