

# Jets, Jets, Higgs & Jets

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Edinburgh**

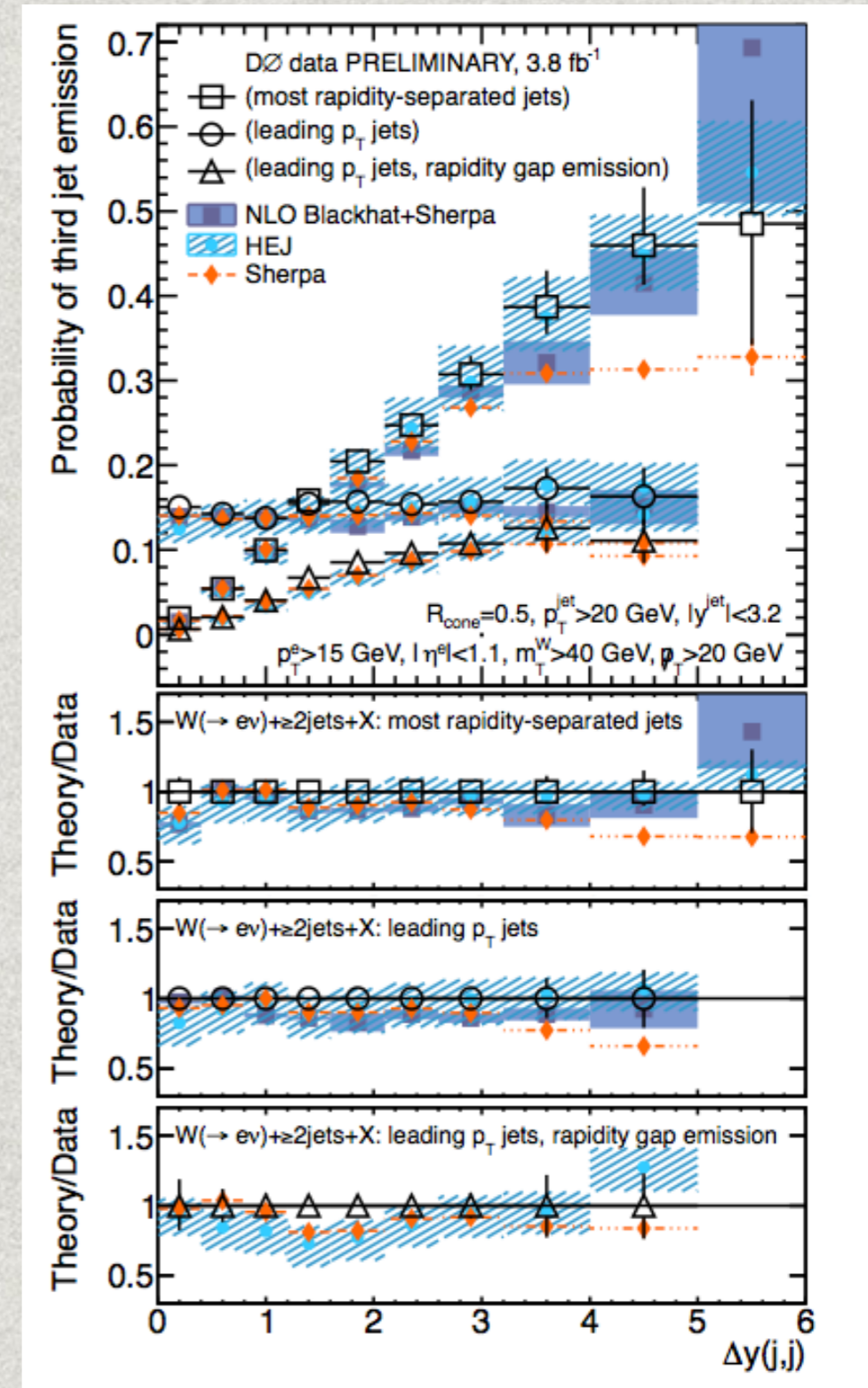
**Mostly HEJ = with J. Andersen, T. Hapola, J. Medley,  
J. Cockburn, H. Brooks**

**Birmingham Seminar**

**6 May 2015**

# Outline

- \* Introduction
- \* High Energy Jets
- \* Comparisons to Data
- \* Higgs Plus Jets

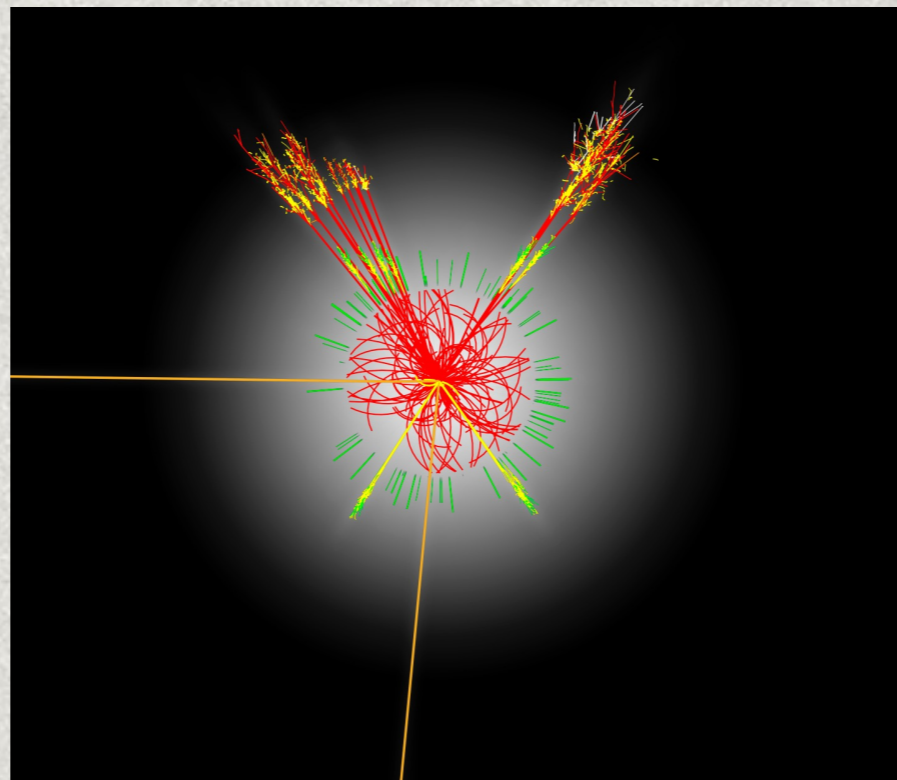


# Why Study Jets?

- \* Complex Standard Model Process  
Therefore complex test of tools
- \* Test models of jet vetoes etc. here before Higgs
- \* **IF** new physics is hiding, need precision to find it
- \* Many tools available... with different strengths

# Scales

- \* In this talk will concentrate on hard-scattering matrix element - high scale



ATLAS Experiment © 2014 CERN

- \* Will neglect underlying event and shower effects - low scale
- \* Very interesting physics, but not today!

# Higher Orders

- Already seen (n+1)-jet rates are not small

e.g. ATLAS Z+jets

$$\frac{(n+1)\text{-jet rate}}{n\text{-jet rate}} \approx 0.2, n=1, \dots, 6 (!)$$

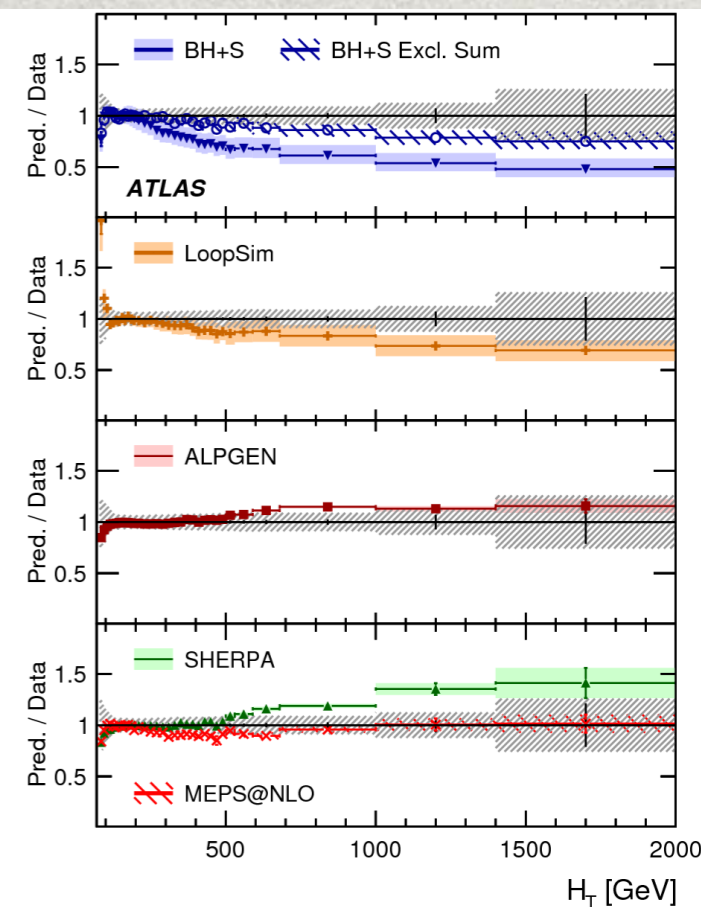
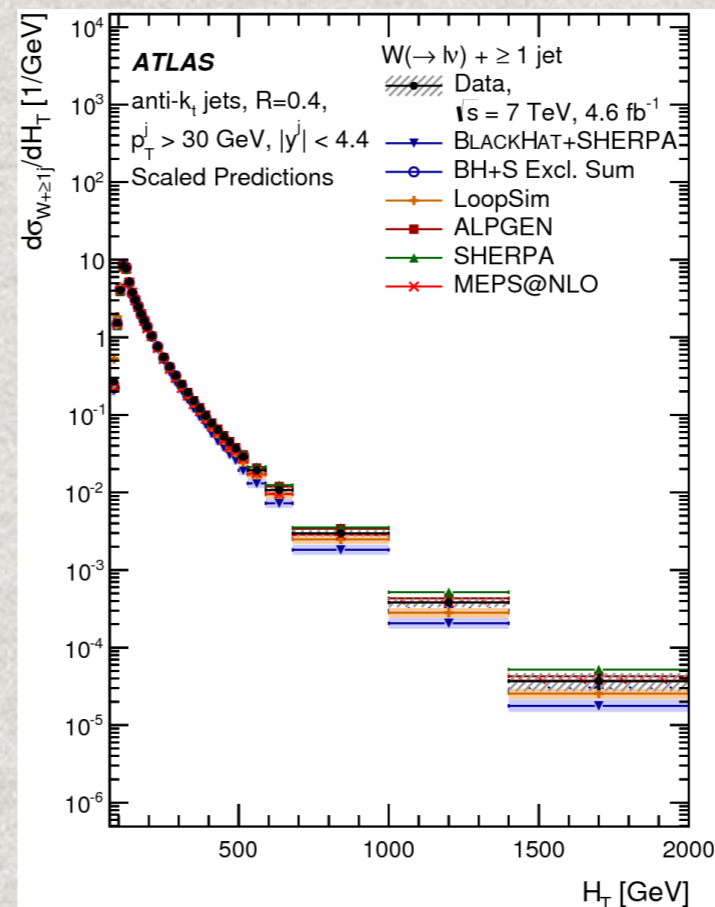
Rises to 0.3 after VBF cuts!

arXiv:1304.7098

ATLAS W+jets arXiv:1409.8639

- NLO is only one more emission

Consistently need to combine orders to describe data



# Merging Higher Orders

- \* NLO + Parton Shower: **POWHEG, MC@NLO**
- \* New approaches available to merge NLO at different orders. **Lönnblad & Prestel (UNLOPS), Plätzer**
- \* Alternatively: calculate all-orders in the first place!
- \* **High Energy Jets** provides systematic description of hard, wide-angle emissions at all orders
- \* **Price**: have to approximate the matrix element

# What is “all-order”?

$$\begin{aligned}\sigma = & \alpha_s^2 (a_2(s^2/t^2) + b_2) \\ & + \alpha_s^3 (a_3(s^2/t^2) \log(s/t) + b_3(s^2/t^2) + c_3) \\ & + \alpha_s^4 (a_4(s^2/t^2) \log^2(s/t) + b_4(s^2/t^2) \log(s/t) + \dots) \\ & + \dots\end{aligned}$$

\* LO = **first line**

# What is “all-order”?

$$\begin{aligned}\sigma = & \alpha_s^2 (a_2(s^2/t^2) + b_2) \\ & + \alpha_s^3 (a_3(s^2/t^2) \log(s/t) + b_3(s^2/t^2) + c_3) \\ & + \alpha_s^4 (a_4(s^2/t^2) \log^2(s/t) + b_4(s^2/t^2) \log(s/t) + \dots) \\ & + \dots\end{aligned}$$

- \* LO = first line
- \* NLO = **first two lines**



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- \* LO = first line
- \* NLO = first two lines
- \* Leading-log = **the ‘a’-terms**

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- \* LO = first line
- \* NLO = first two lines
- \* Leading-log = the ‘a’-terms
- \* In practice, merge **LO and LL**

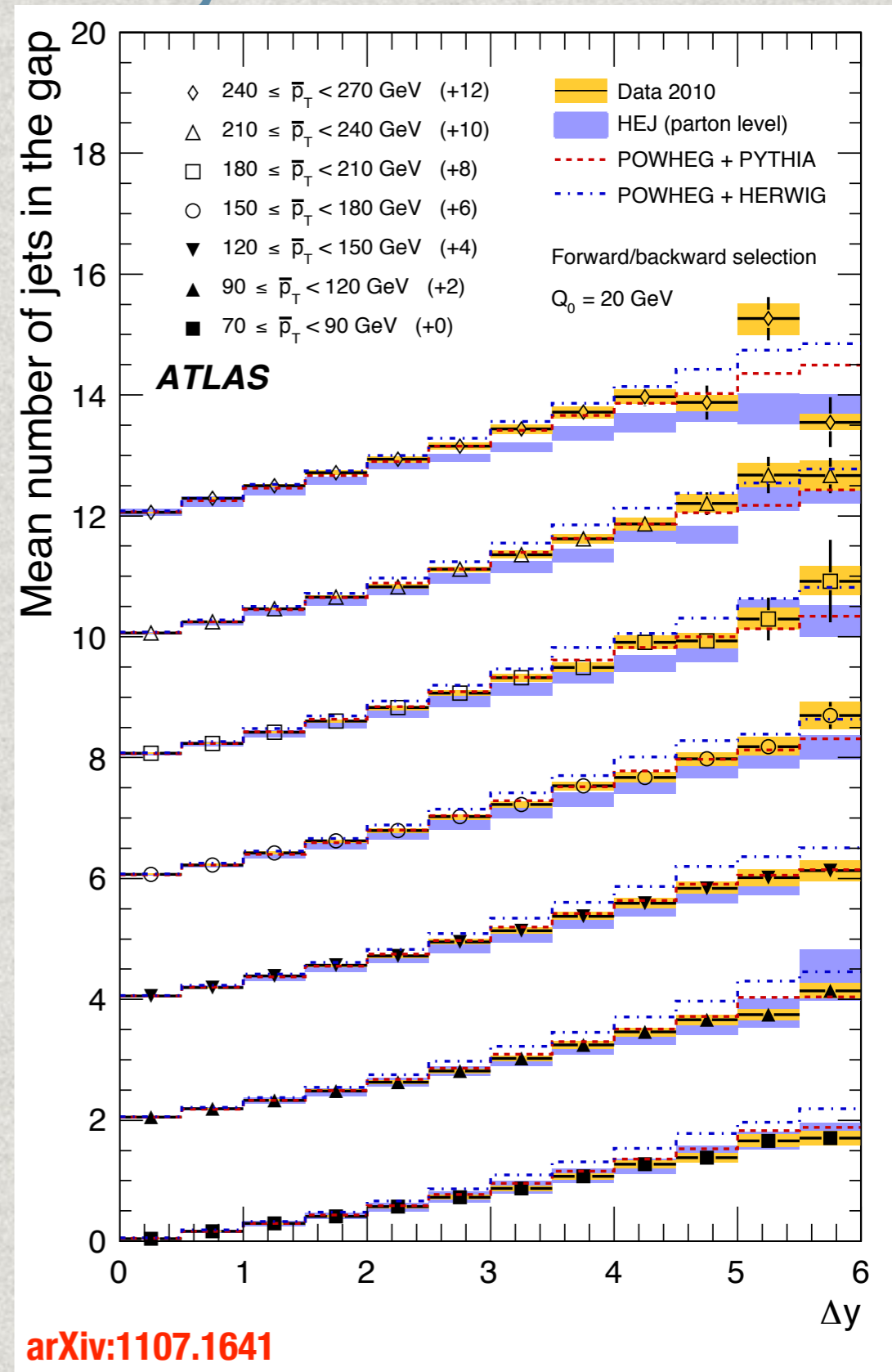
# ATLAS: jet veto analysis

Plot average number of additional jets.

More than one extra jet on average for  $\Delta y > 3$   
Clearly beyond NLO!

Tagging = most forward/  
backward

Good agreement with  
POWHEG+PYTHIA & HEJ



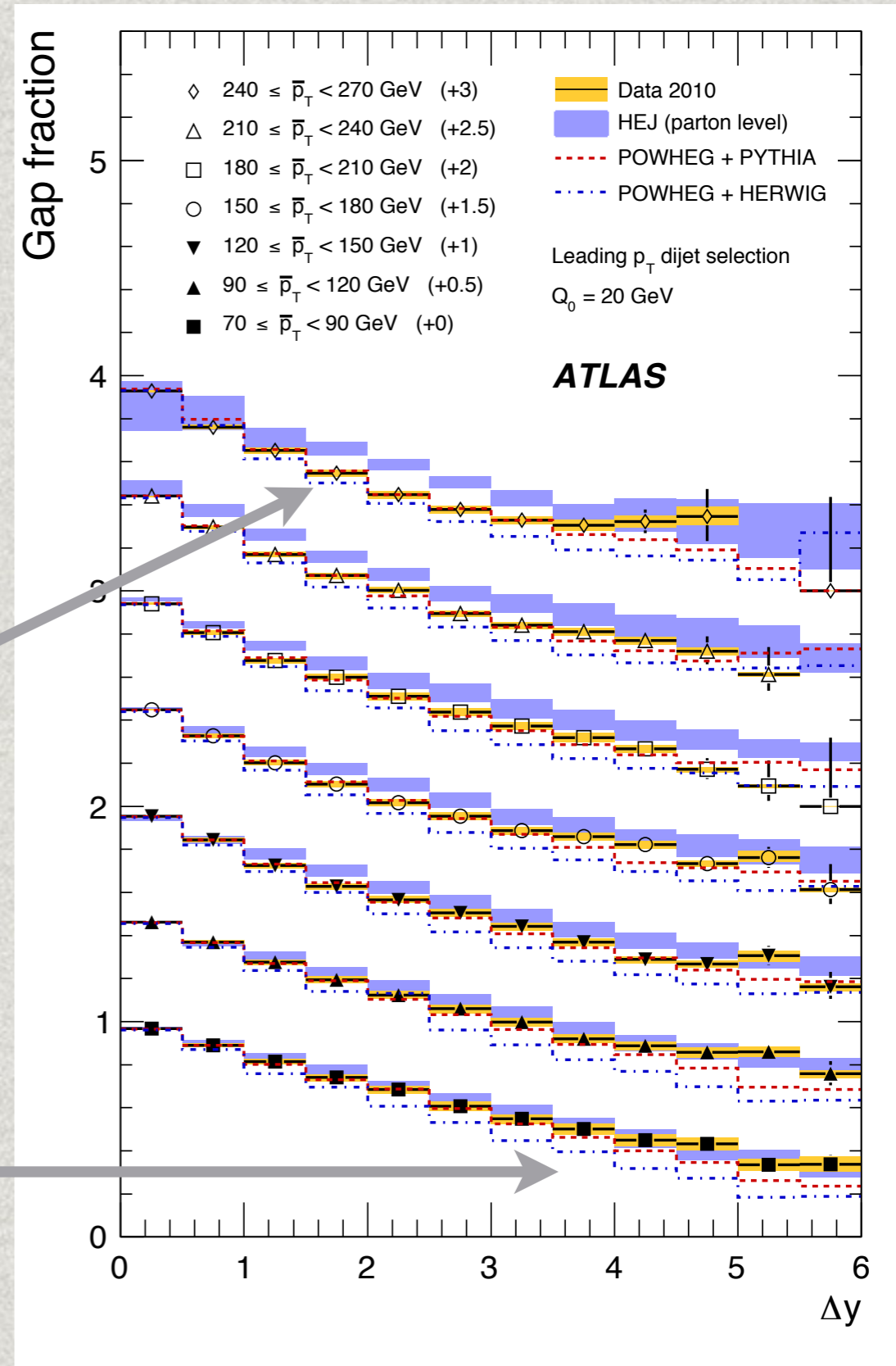
# ATLAS: gap fraction

$$\text{Gap Fraction} = \frac{\sigma(\text{no jets in gap})}{\sigma(2j \text{ inclusive})}$$

Now, tagging jets are leading  $p_T$

Hierarchy in  $p_T$  (up to factor 10!)  
 $p_T$  evolution not in HEJ

Evolution in rapidity  
 HEJ description good,  
 POWHEG undershoots

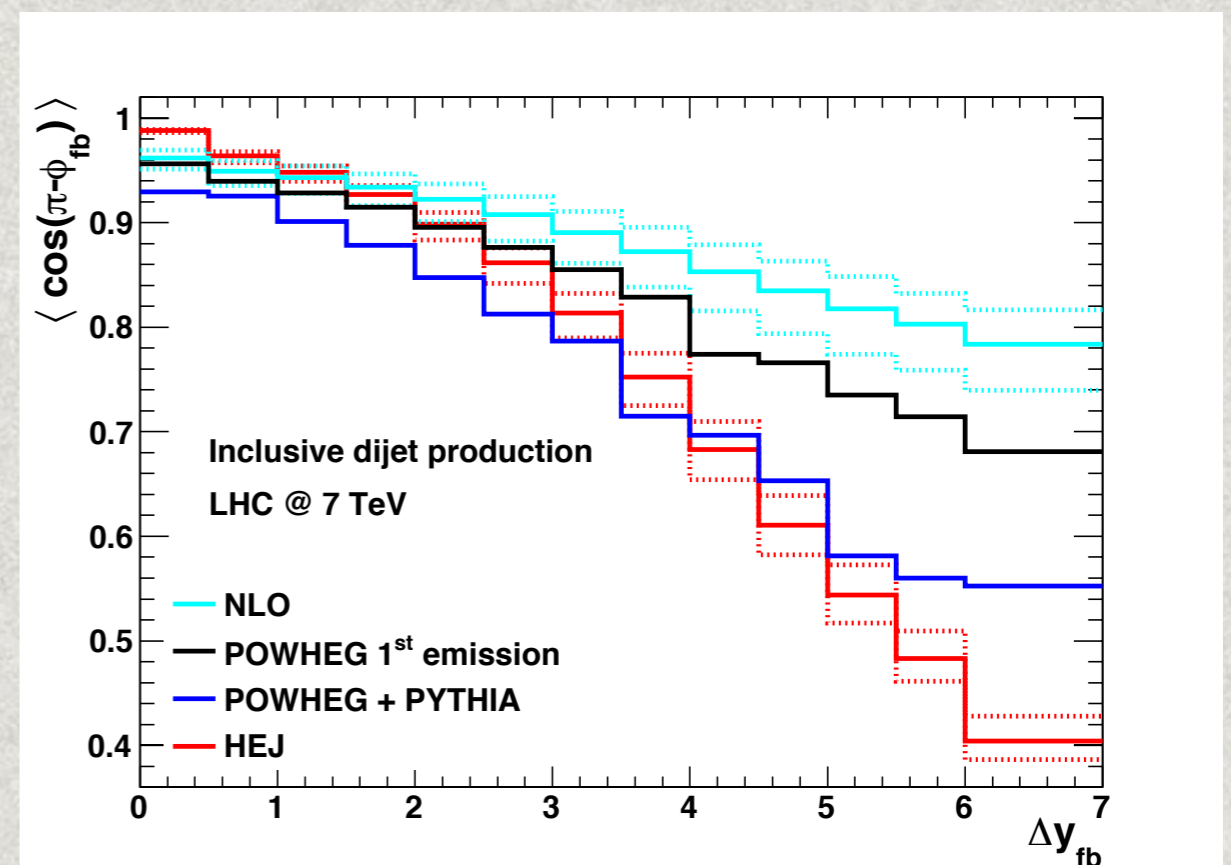
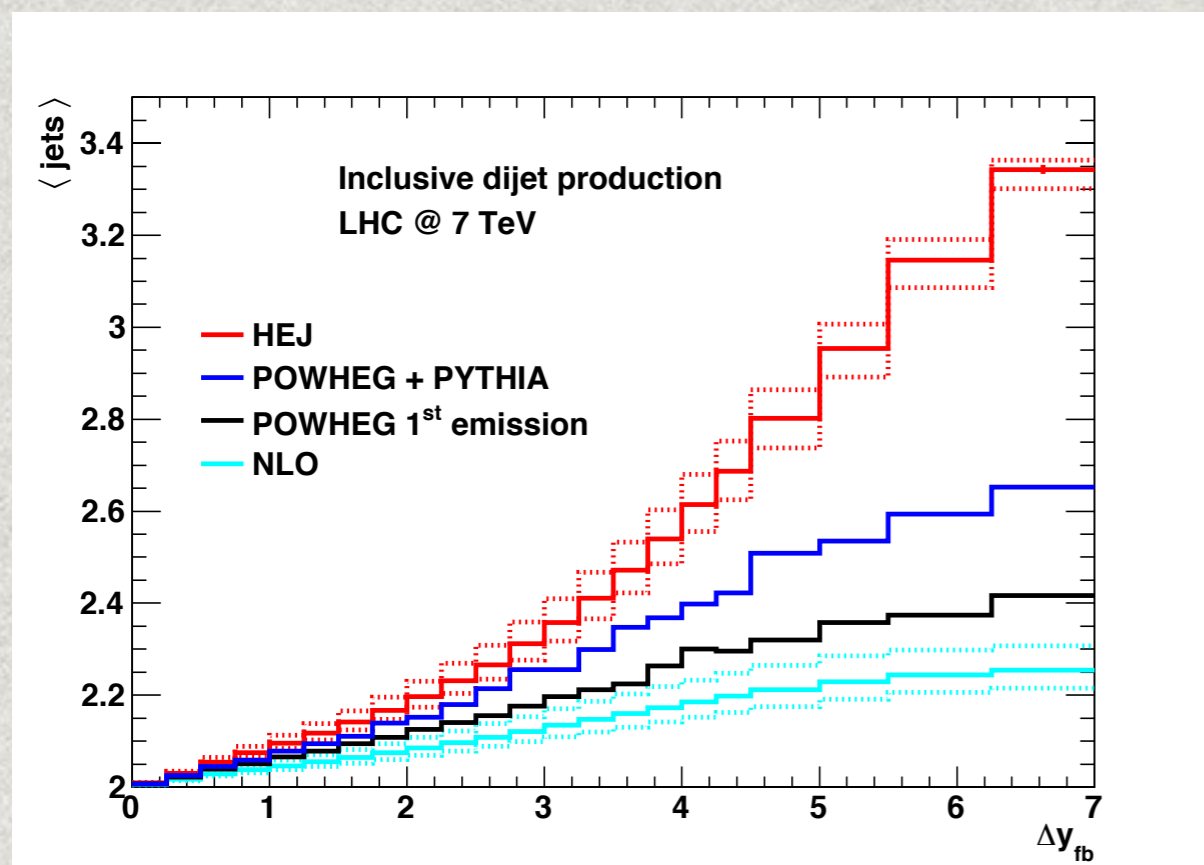


# DiJet Comparison

POWHEG+PYTHIA and HEJ gave very similar predictions  
Can they be distinguished?

Choose cuts which do not induce  $p_T$  hierarchy

$$p_{T,j} > 35 \text{ GeV}, p_{T,j1} > 45 \text{ GeV}, |y_j| < 4.7$$



In some cases, yes,...

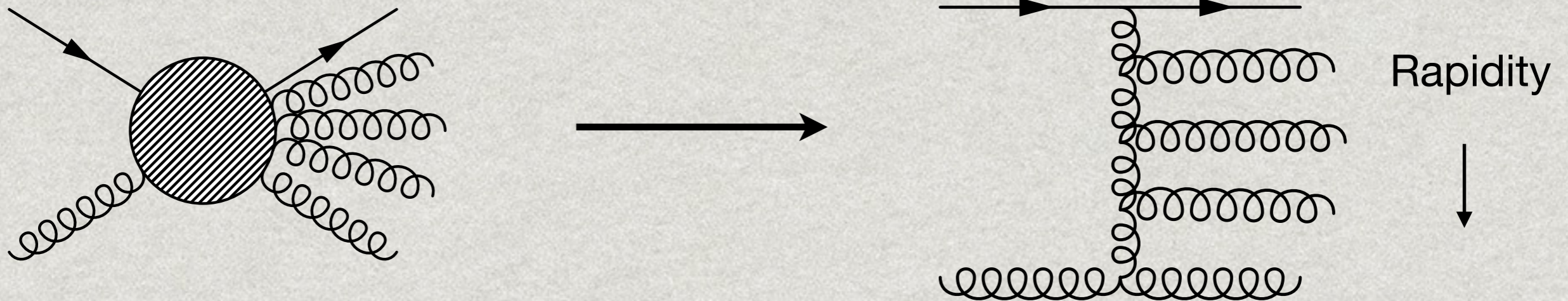
others, no.

# High Energy Limit

- \* The High Energy (Multi-Regge) limit is:

$$s_{ij} \rightarrow \infty, \quad |p_{\perp_i}| \sim |p_{\perp_j}|, \quad i, j = 1, \dots, n$$

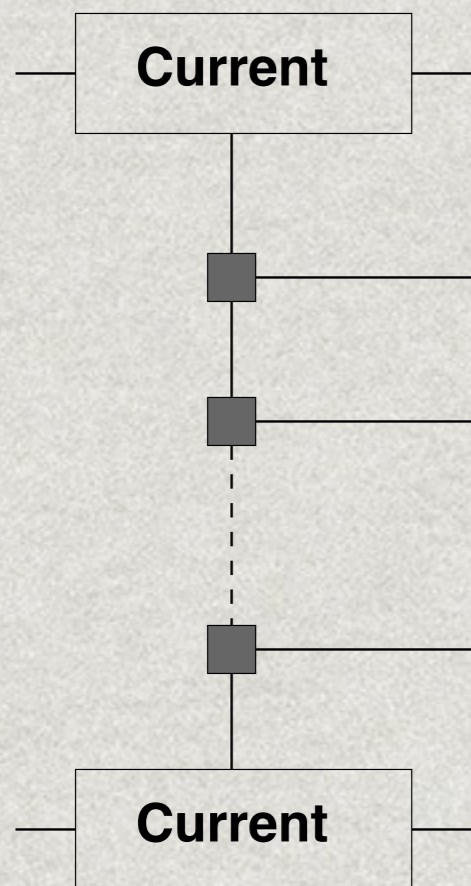
In practice, particles spread out in rapidity



- \* Dominant Momentum Configurations in HE limit correspond to those which would allow maximum t-channel gluon exchanges:
- \* Other orderings are logarithmically suppressed.

# A HEJ Amplitude

- \* All scattering amplitudes factorise in this limit  
⇒ Can exploit this to build a simple approximation.



Decreasing  
Rapidity

- \* A HEJ amplitude is structured:

current-current  
x product-of-emissions

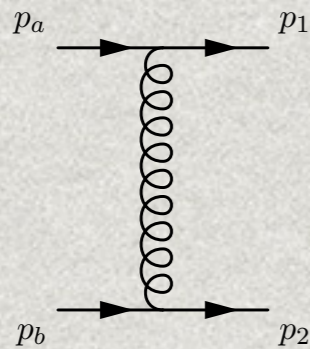


Applies to loop diagrams too (needed to regulate soft).

# Pieces I: Currents

Pieces independent of rest of chain - pick convenient processes to derive them

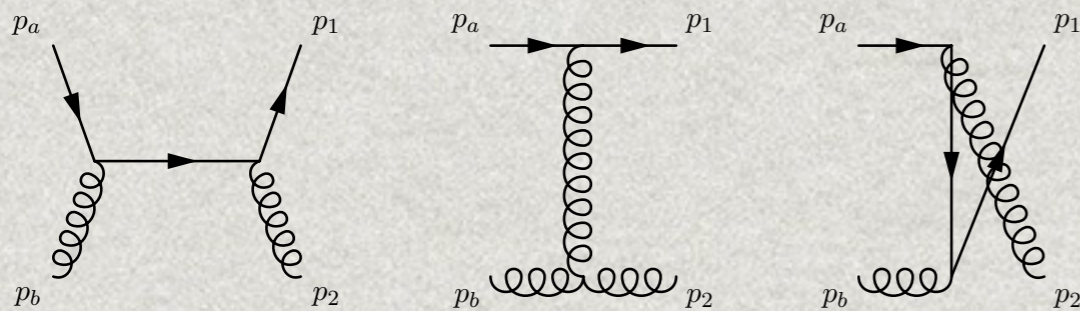
- \* Incoming quarks: straight-forward



$$\frac{8g_s^4}{9} \frac{|j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_2)|^2}{\hat{t}^2} = \frac{4g_s^4}{9} \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$$

- \* Incoming gluons: surprisingly so!

- \* Exact result:  $\frac{g_s^4 C_{CAM}}{6} \frac{|j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_2)|^2}{\hat{t}^2}$



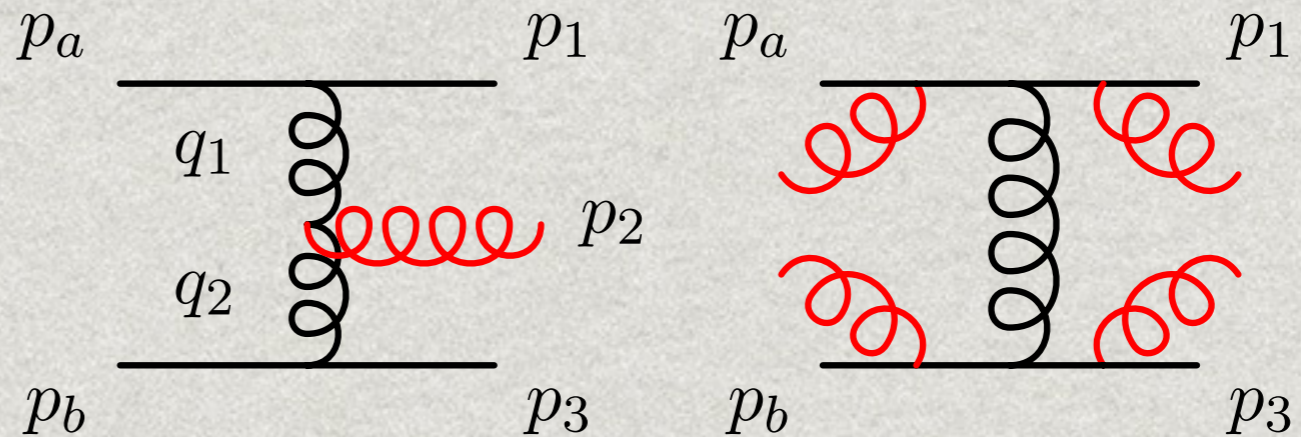
with  $C_{CAM} = \frac{1}{2} \left( C_A - \frac{1}{C_A} \right) \left( \frac{p_b^-}{p_2^-} + \frac{p_2^-}{p_b^-} \right) + \frac{1}{C_A}$

- \* Only t-pole remains explicitly



# Pieces II: Emission Vertices

\* Use  $qQ \rightarrow qqQ$

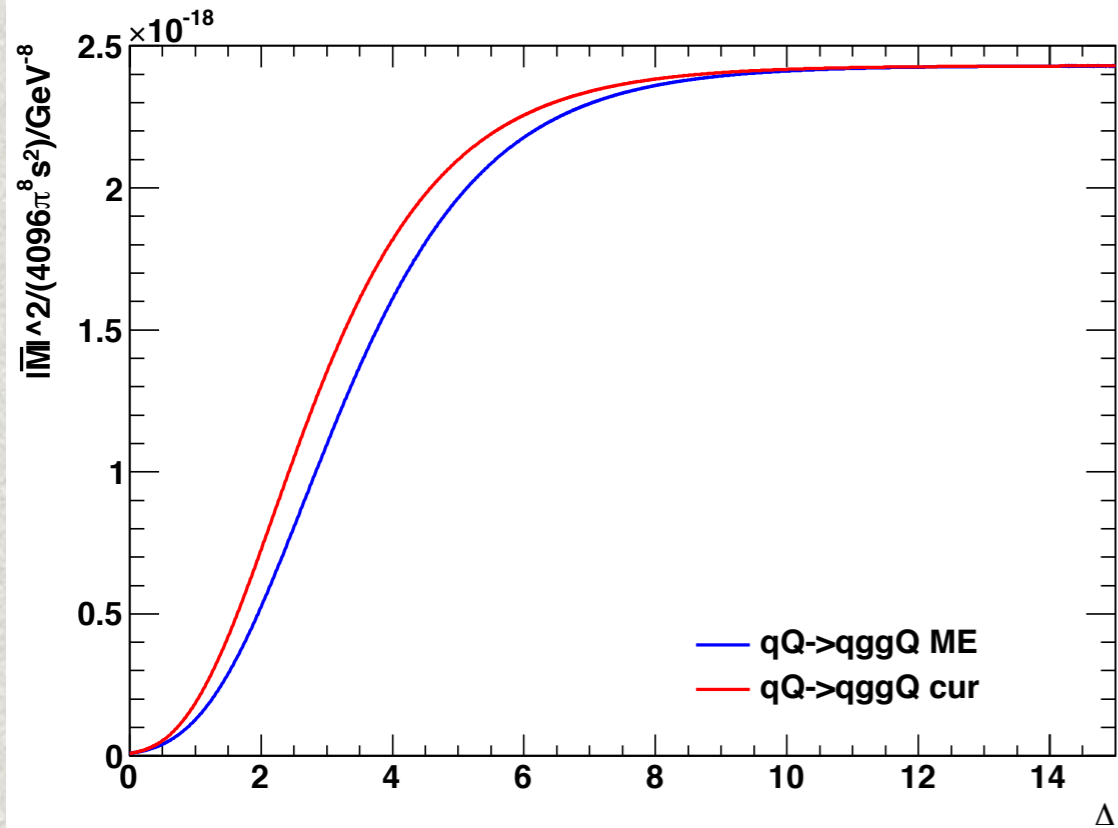


\* In HE limit, colour factors combine to give

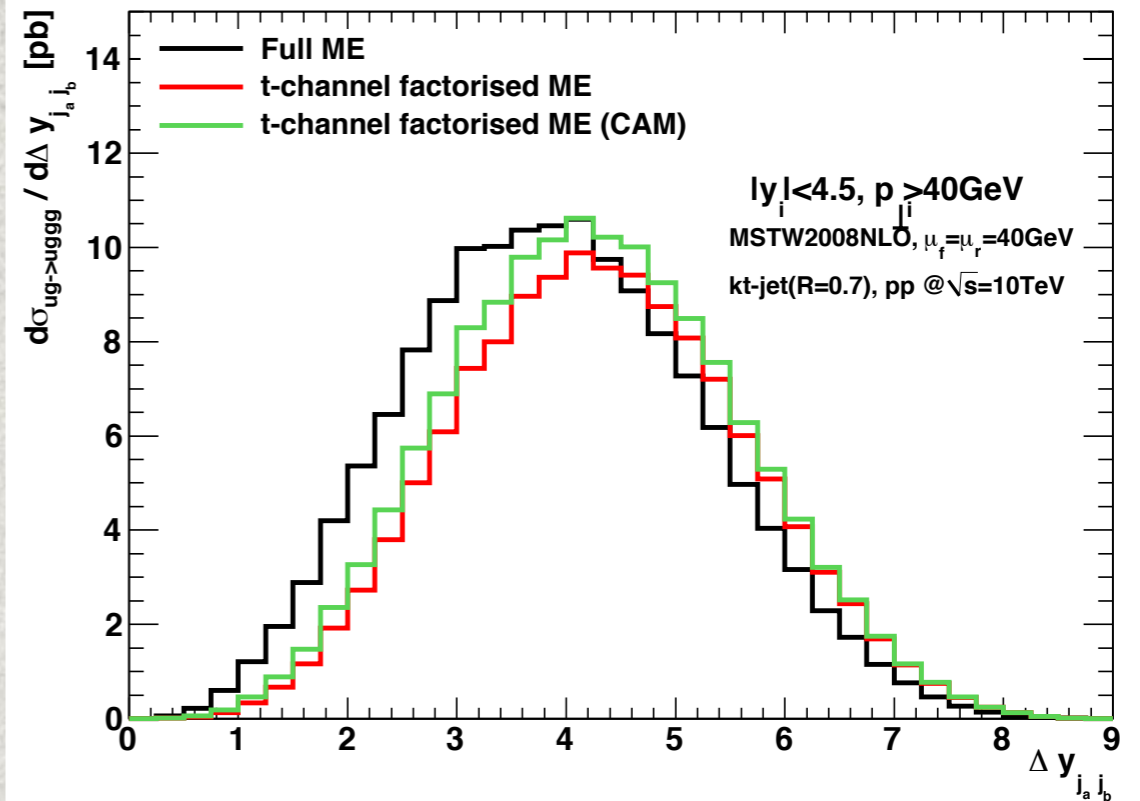
$$\begin{aligned}
 \mathcal{A}_{qQ \rightarrow qqQ} &= g_s^3 C_g \varepsilon_\rho^* \frac{j^\mu(p_a, p_1) \cdot j_\mu(p_b, p_3)}{q_1^2 q_2^2} V^\rho(q_1, q_2) \\
 V^\rho(q_1, q_2) &= - (q_1 + q_2)^\rho \\
 &+ \frac{p_a^\rho}{2} \left( \frac{q_1^2}{p_2 \cdot p_a} + \frac{p_2 \cdot p_b}{p_a \cdot p_b} + \frac{p_2 \cdot p_3}{p_a \cdot p_3} \right) + p_a \leftrightarrow p_1 \\
 &- \frac{p_b^\rho}{2} \left( \frac{q_2^2}{p_2 \cdot p_b} + \frac{p_2 \cdot p_a}{p_b \cdot p_a} + \frac{p_2 \cdot p_1}{p_b \cdot p_1} \right) - p_b \leftrightarrow p_3.
 \end{aligned}$$

Gauge invariant in *all* of phase space.

# Does It Work?



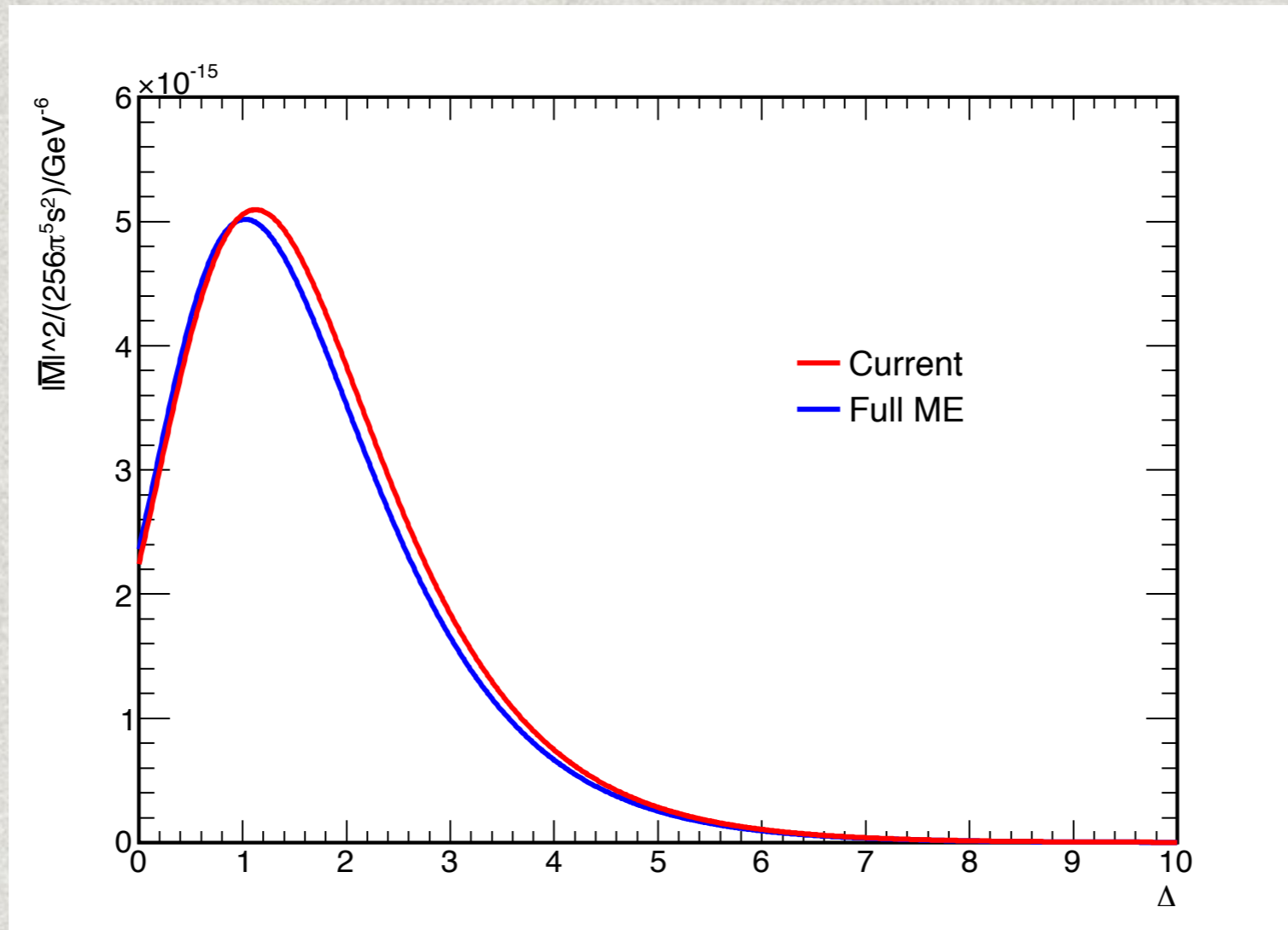
qQ  $\rightarrow$  qggQ



qg  $\rightarrow$  qggg

# Even when it's not supposed to!

Gluon now pulled forward of both quarks:



us  $\rightarrow$  usg

# Pieces III: Regulation

Last part is to regulate divergences when  $p_i \rightarrow 0$

HE limit of virtual corrections is given by the Lipatov Ansatz

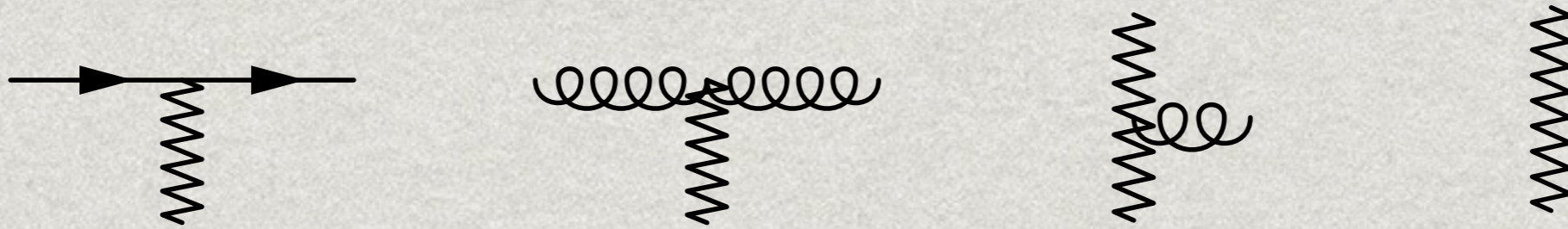
$$\text{Wavy line} = \frac{1}{t_i} \exp[\hat{\alpha}(q_i)(y_{i-1} - y_i)]$$

$$\hat{\alpha}(q_i) = \alpha_s C_A t_i \int \frac{d^{2+2\epsilon} k_\perp}{(2\pi)^{2+2\epsilon}} \frac{1}{k_\perp^2 (q_i - k)_\perp^2}$$
$$\rightarrow -g_s^2 C_A \frac{\Gamma(1-\epsilon)}{(4\pi)^{2+\epsilon}} \frac{2}{\epsilon} (\mathbf{q}^2/\mu^2)^\epsilon$$

Proved to next-to-leading log

Fadin, Fiore, Kozlov & Reznichenko: hep-ph/0602006

# Assembly



Build fully-flexible Monte Carlo from these

Merge with exact LO if cluster into 2, 3 or 4 jets

Add missing momentum configurations for 2,3 & 4j

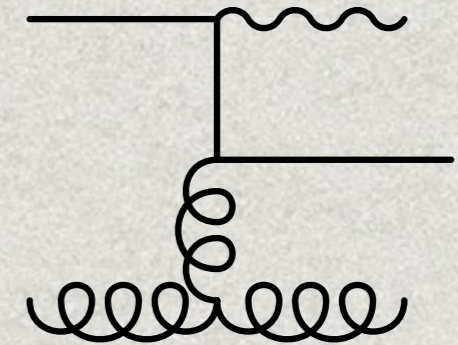
Publicly available at

<http://cern.ch/hej>

Jets, W+jets, Higgs+jets, HEJ+ARIADNE

# Extension to Ws

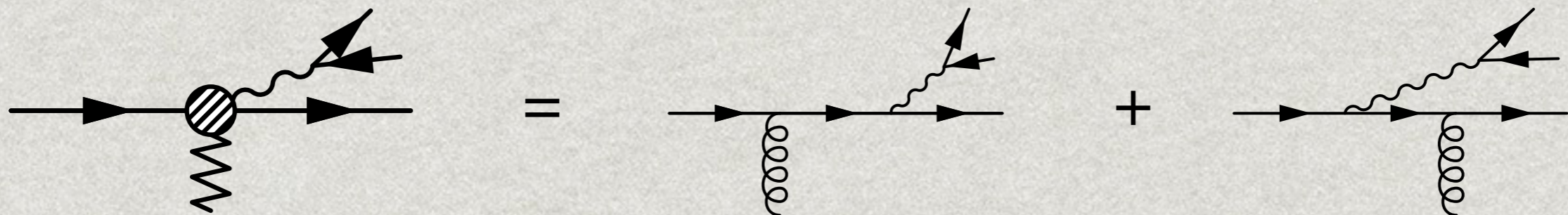
qg-channel dominant for  $W+nj$  at LHC



Treated in HE limit before, with constraint on decays

Andersen, Del Duca, Maltoni & Stirling: [hep-ph/0105146](https://arxiv.org/abs/hep-ph/0105146)

In HEJ:



No constraints on decay products of  $W$  (or  $Z/\gamma^*$ )

Andersen, Hapola & JMS [arXiv:1206.6763](https://arxiv.org/abs/1206.6763)

# In a Nutshell:

- \* High Energy Jets describes QCD emissions at large  $s_{ij}$

⇒ Captures hard jet production

$$s_{ij} = 2p_{Ti}p_{Tj} (\cosh(y_i - y_j) - \cos(\phi_i - \phi_j))$$

- \* Opposite limit to a parton shower, which sums large contributions at small  $s_{ij}$

⇒ Good at jet substructure, underestimates rate/hardness

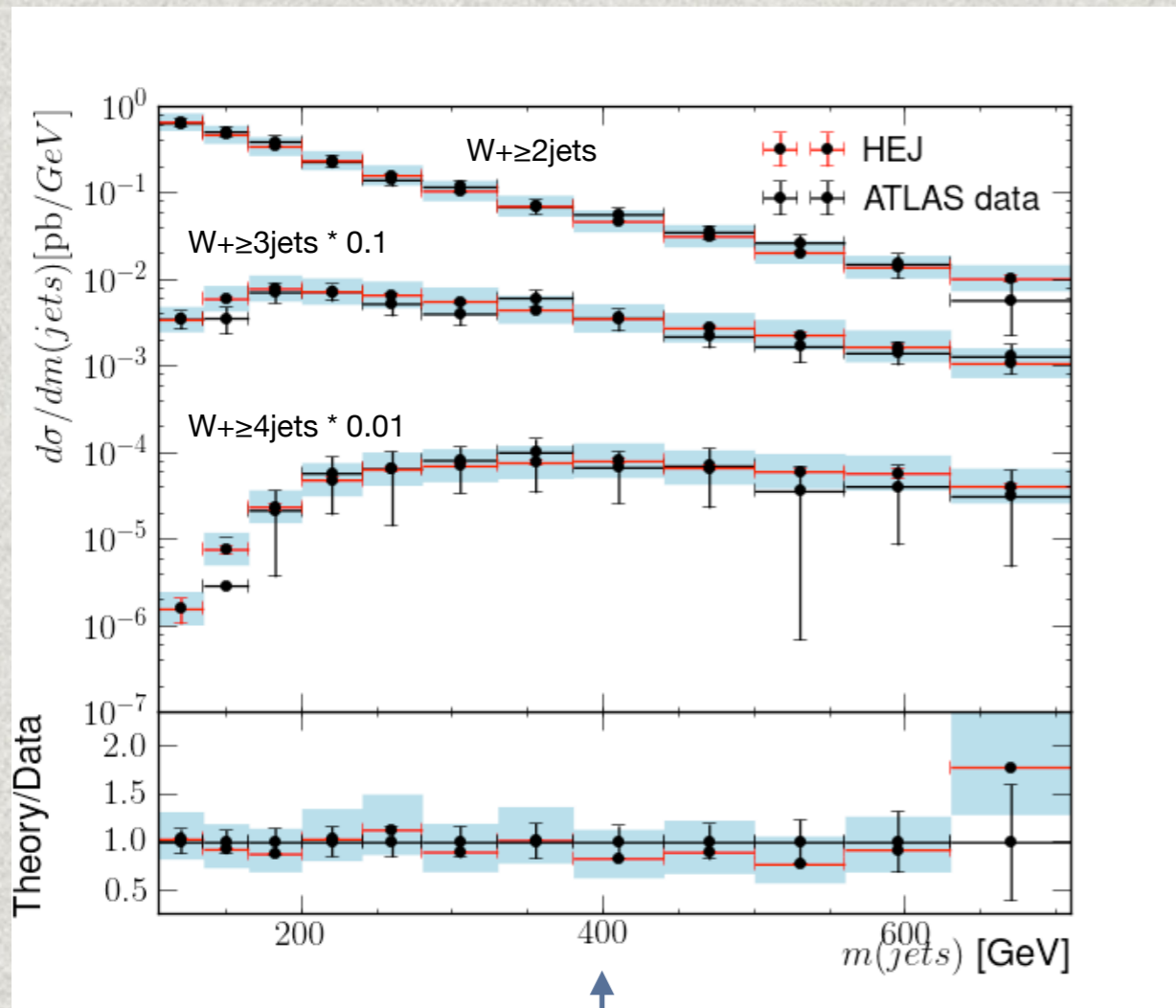
- \* Can combine both (but not straight-forward).

More Results



# ATLAS 2010 $W$ +dijets

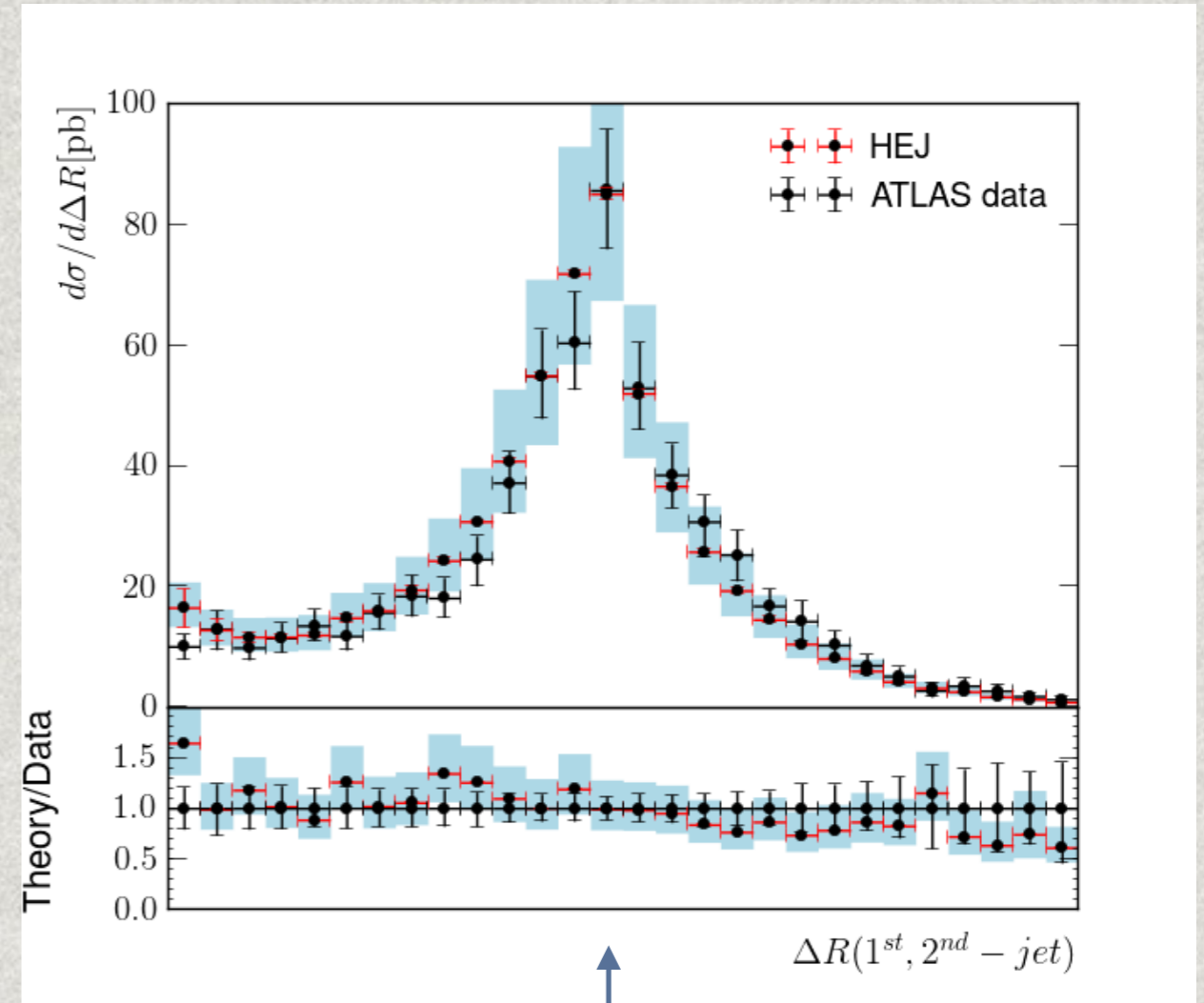
HEJ again gives good description:



Note large impact of higher orders!

**ATLAS (2010) data** [arXiv:1201.1276](https://arxiv.org/abs/1201.1276)

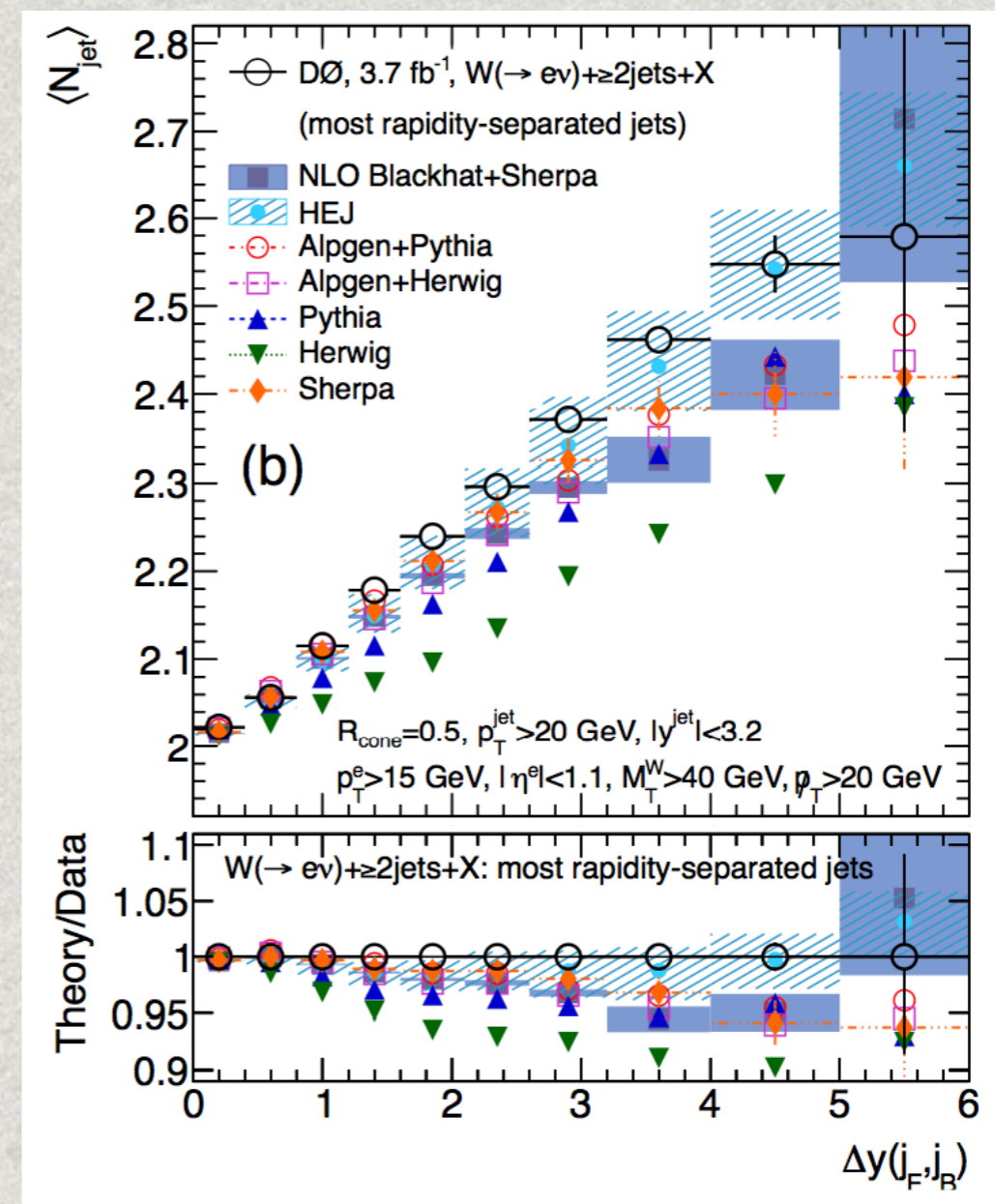
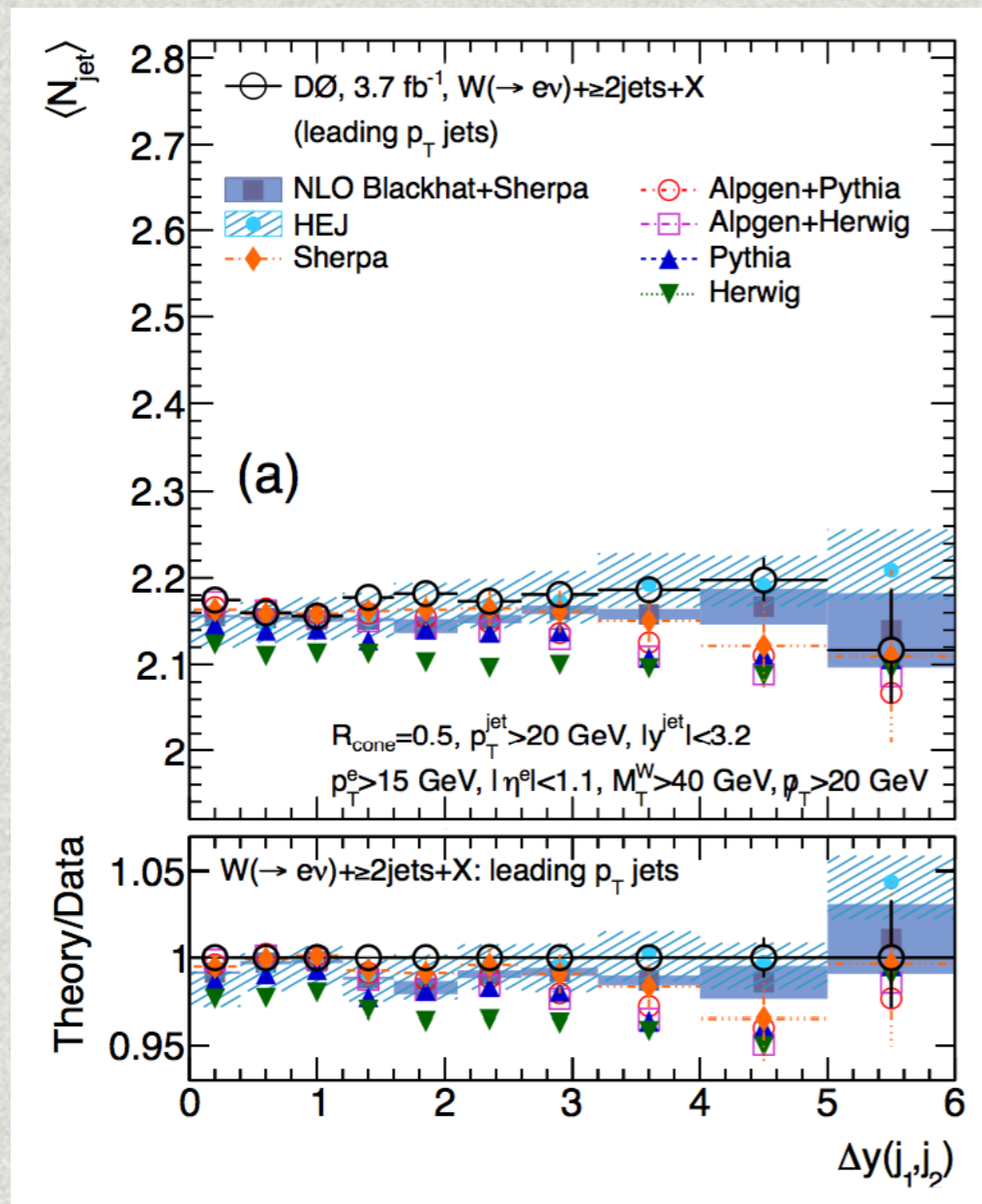
**Andersen, Hapola & JMS** [arXiv:1206.6763](https://arxiv.org/abs/1206.6763)



Traditionally very hard to describe  
(testing ground for state-of-the-art)  
HEJ gives good description

# DØ $W+J$ ets

Really thorough analysis: 40 observables!

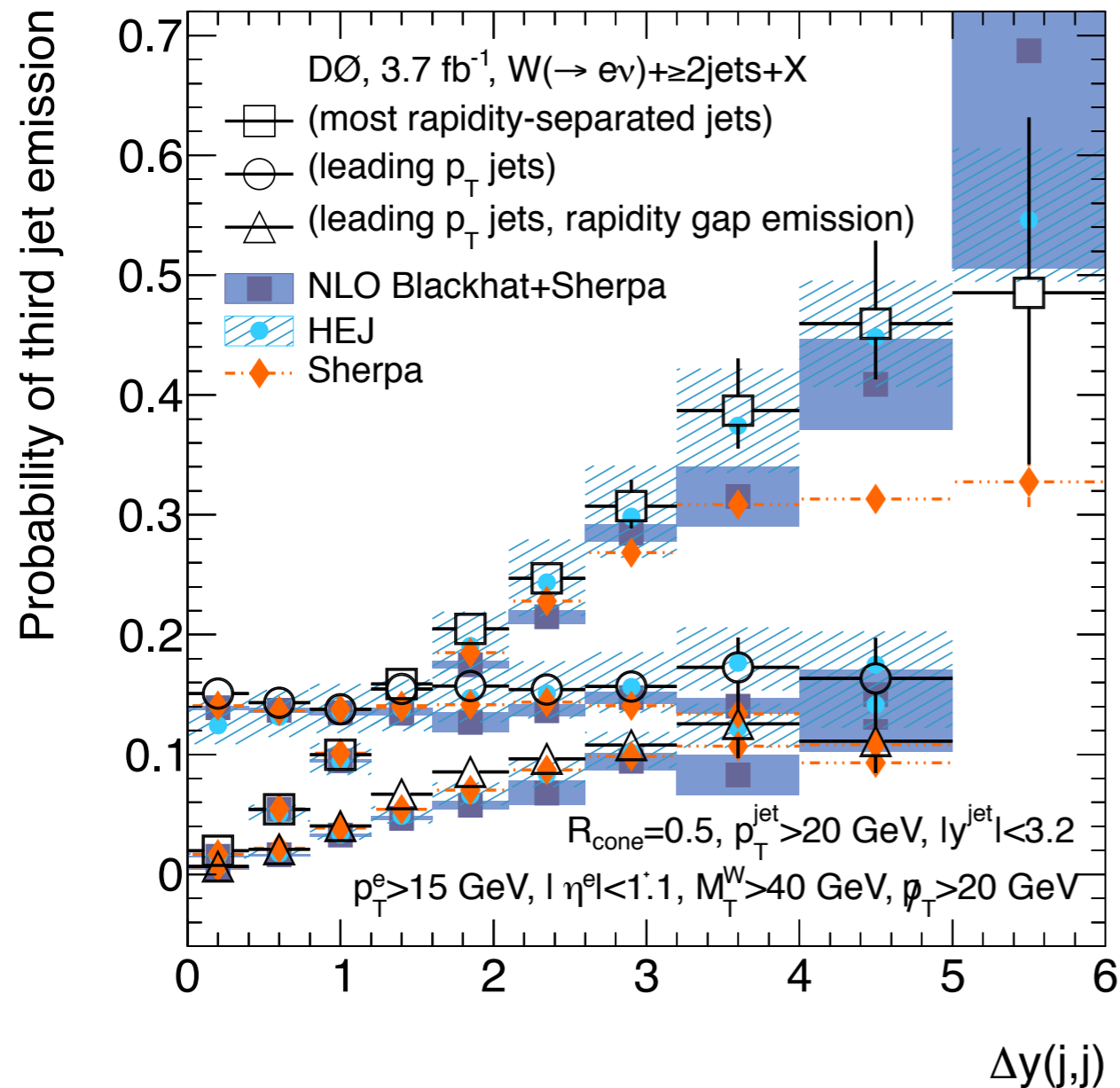


This is the difference between:  
Leading Jets

Most forward/backward Jets

# D0 $W+Jets$

Probability of third jet emission versus  $\Delta y$  of:



\* Most forward/backward Jets

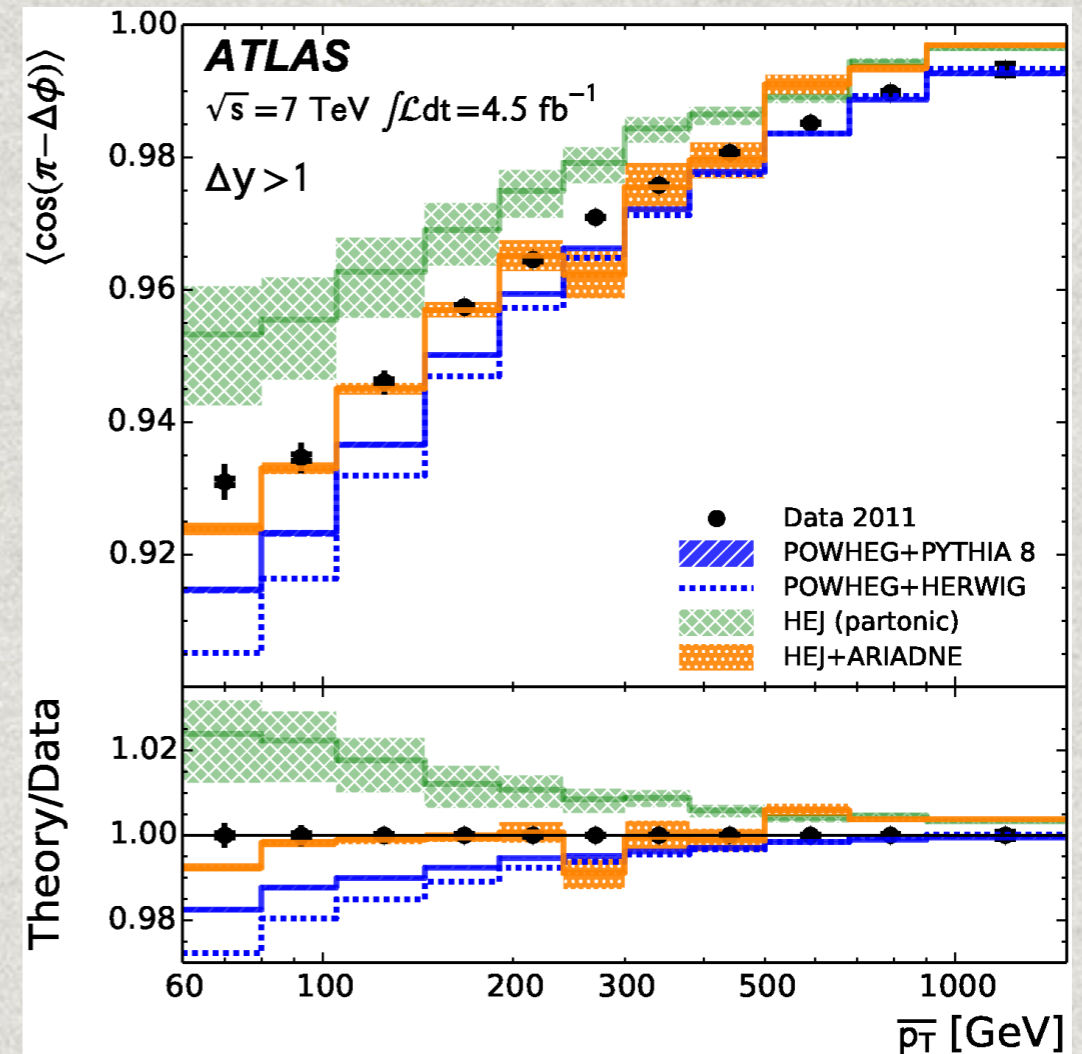
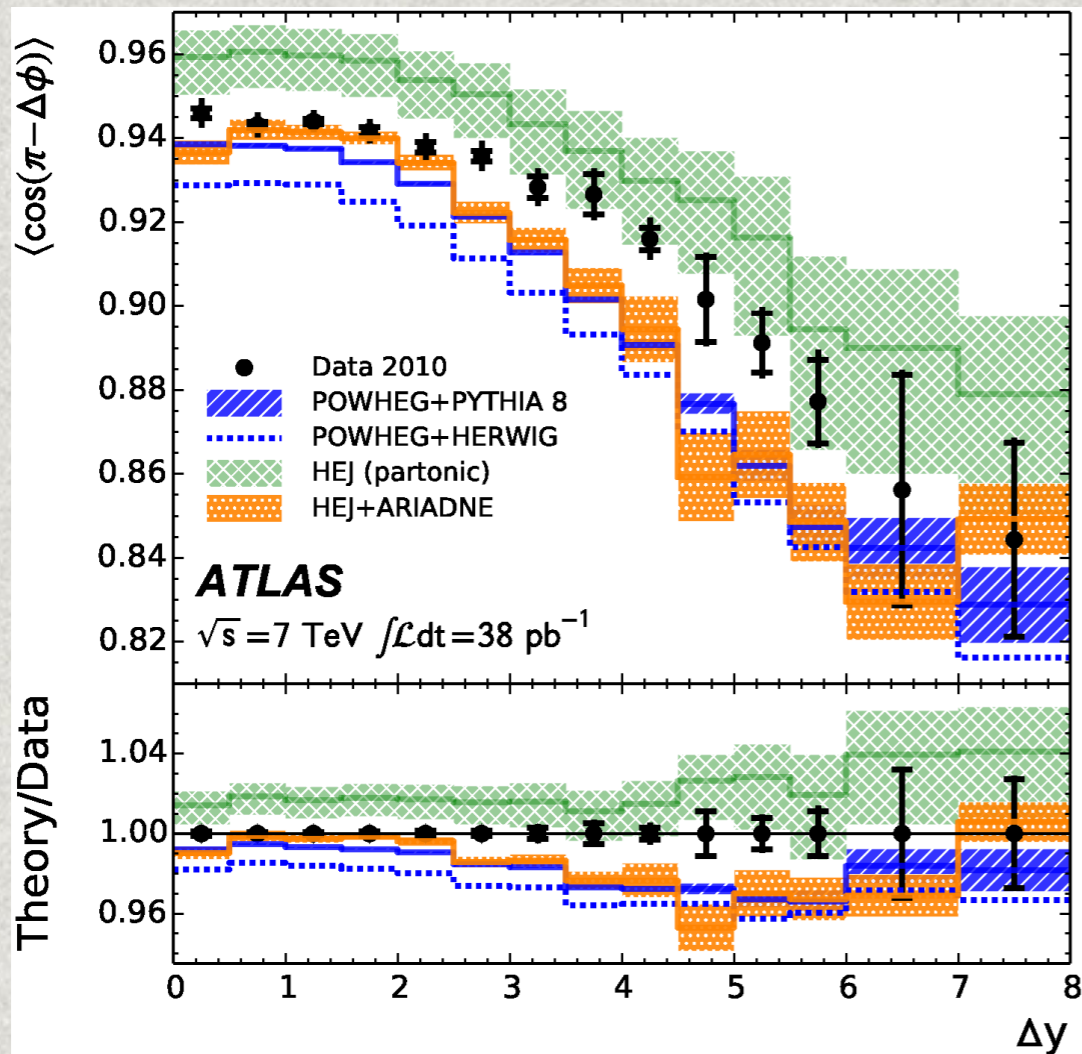
\* Hardest Jets

\* Hardest Jets, counting only jets between

arXiv:1302.6508

How you choose 2 jets matters!!

# ATLAS jet veto update



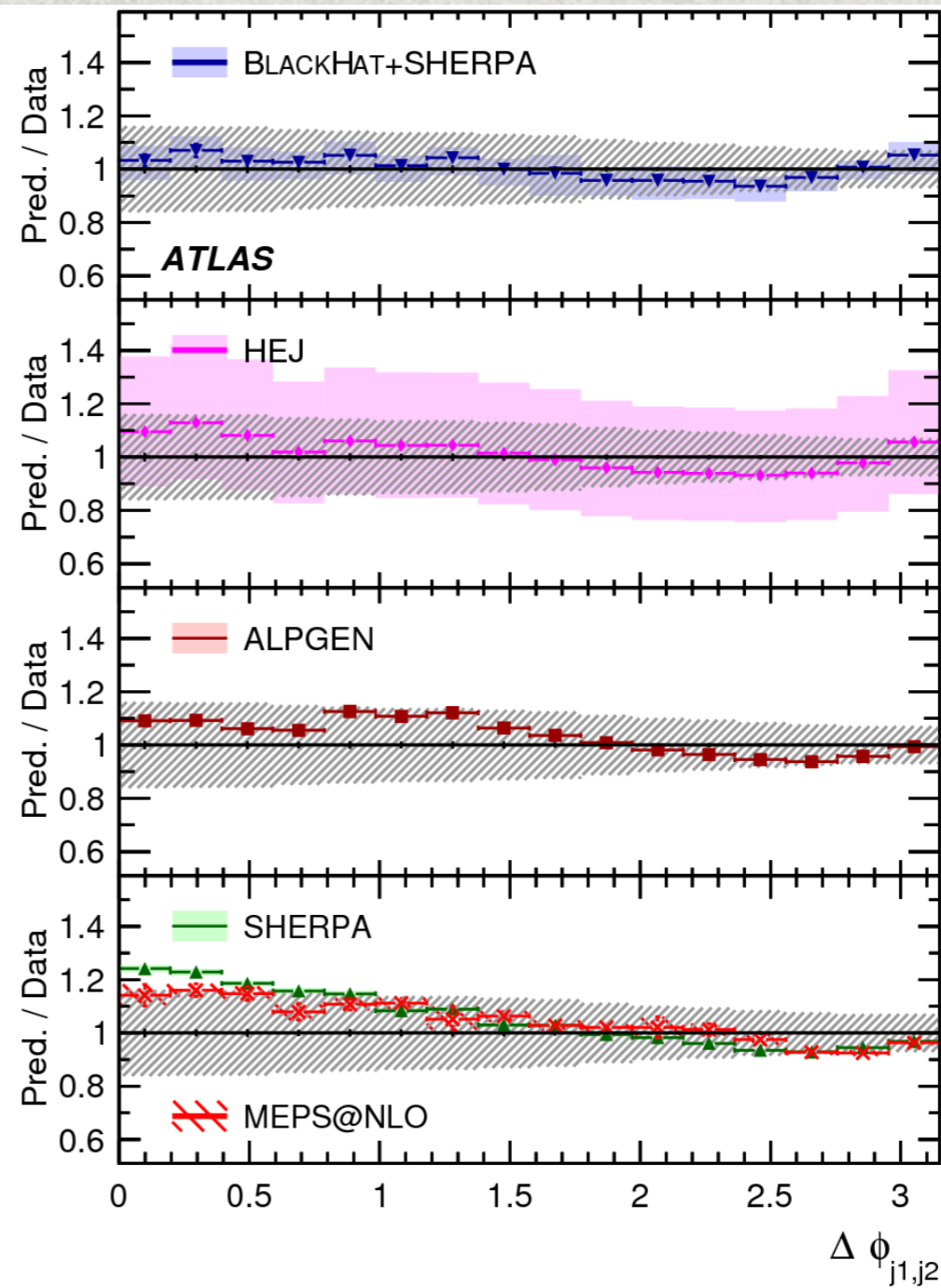
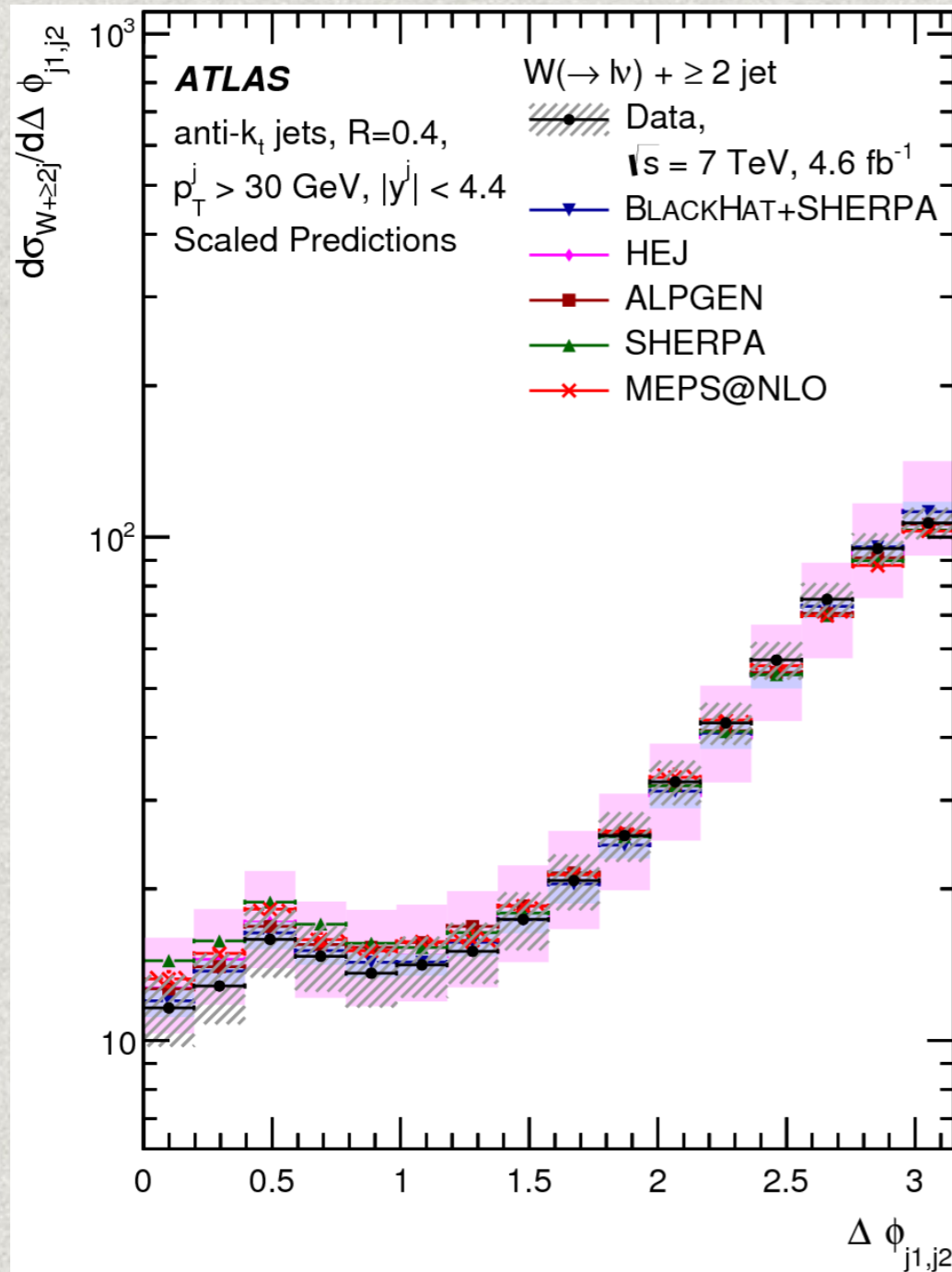
arXiv:1407.5756

$\langle \cos(\pi - \Delta\phi) \rangle$  measures angular decorrelation

Large impact of shower in this set-up

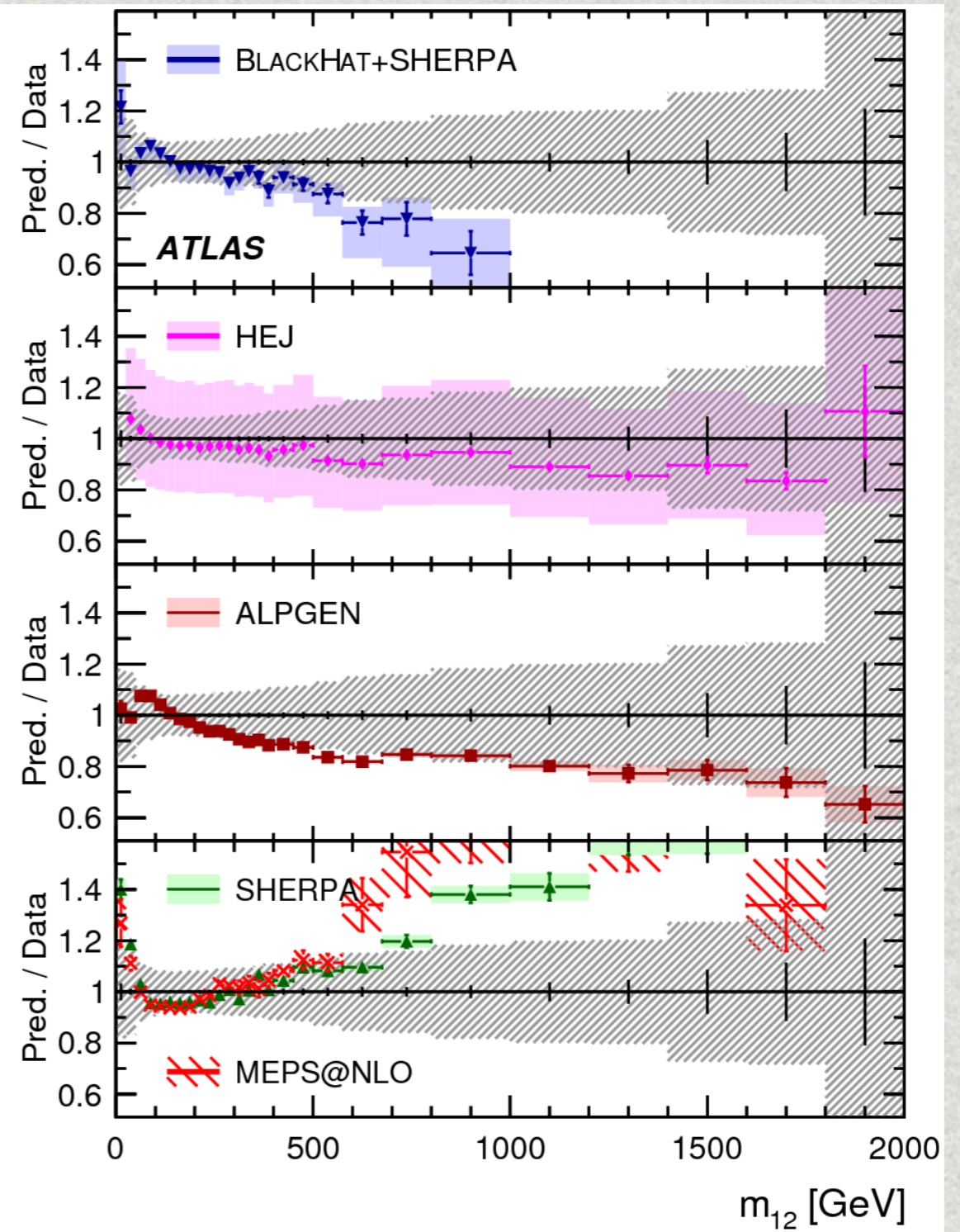
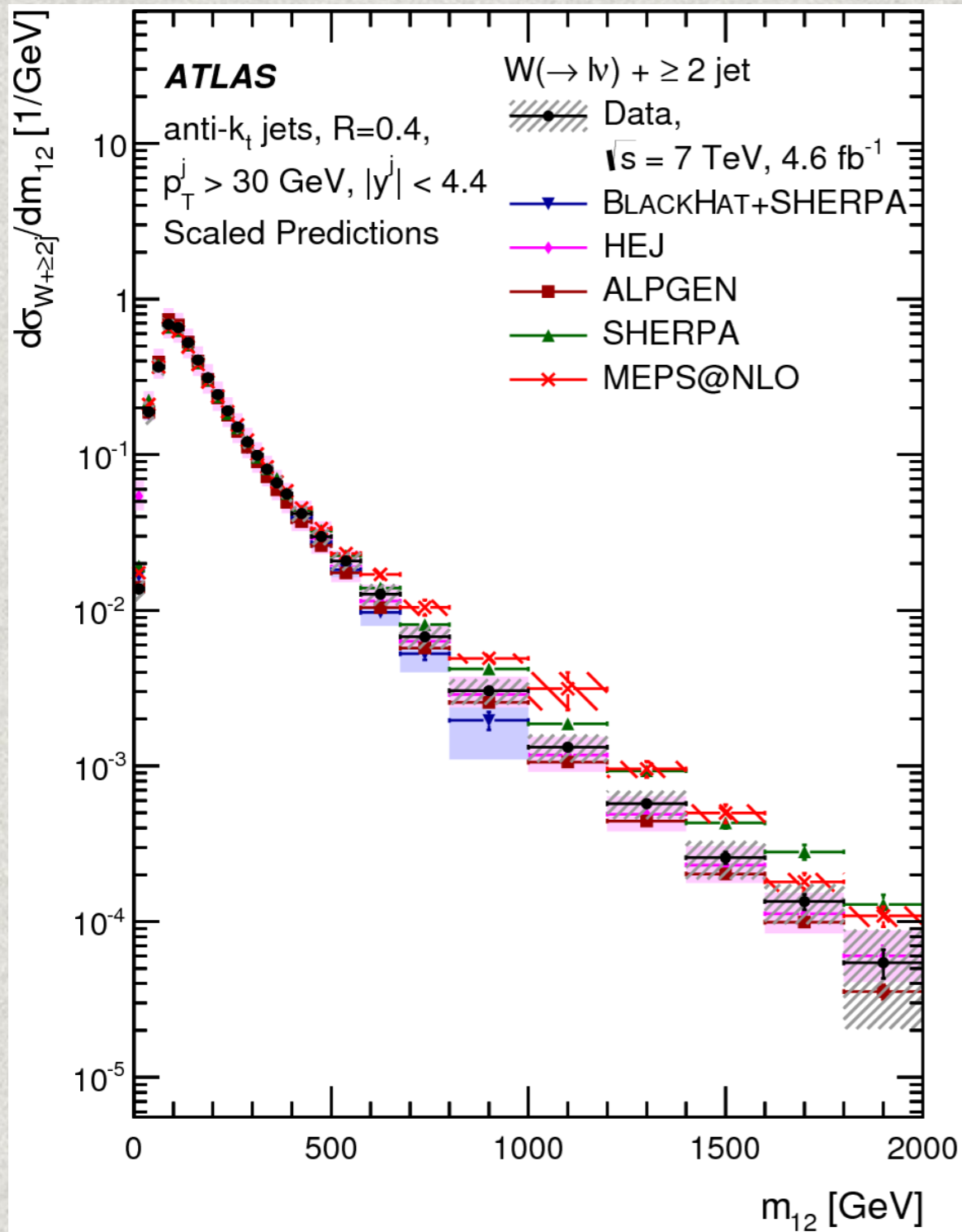
$$\overline{p_T} > 50 \text{ (60) GeV}, \quad Q_0 > 20 \text{ (30) GeV}, \quad |y_j| < 4.4 \text{ (2.4)}$$

# ATLAS 2011 $W+Jets$



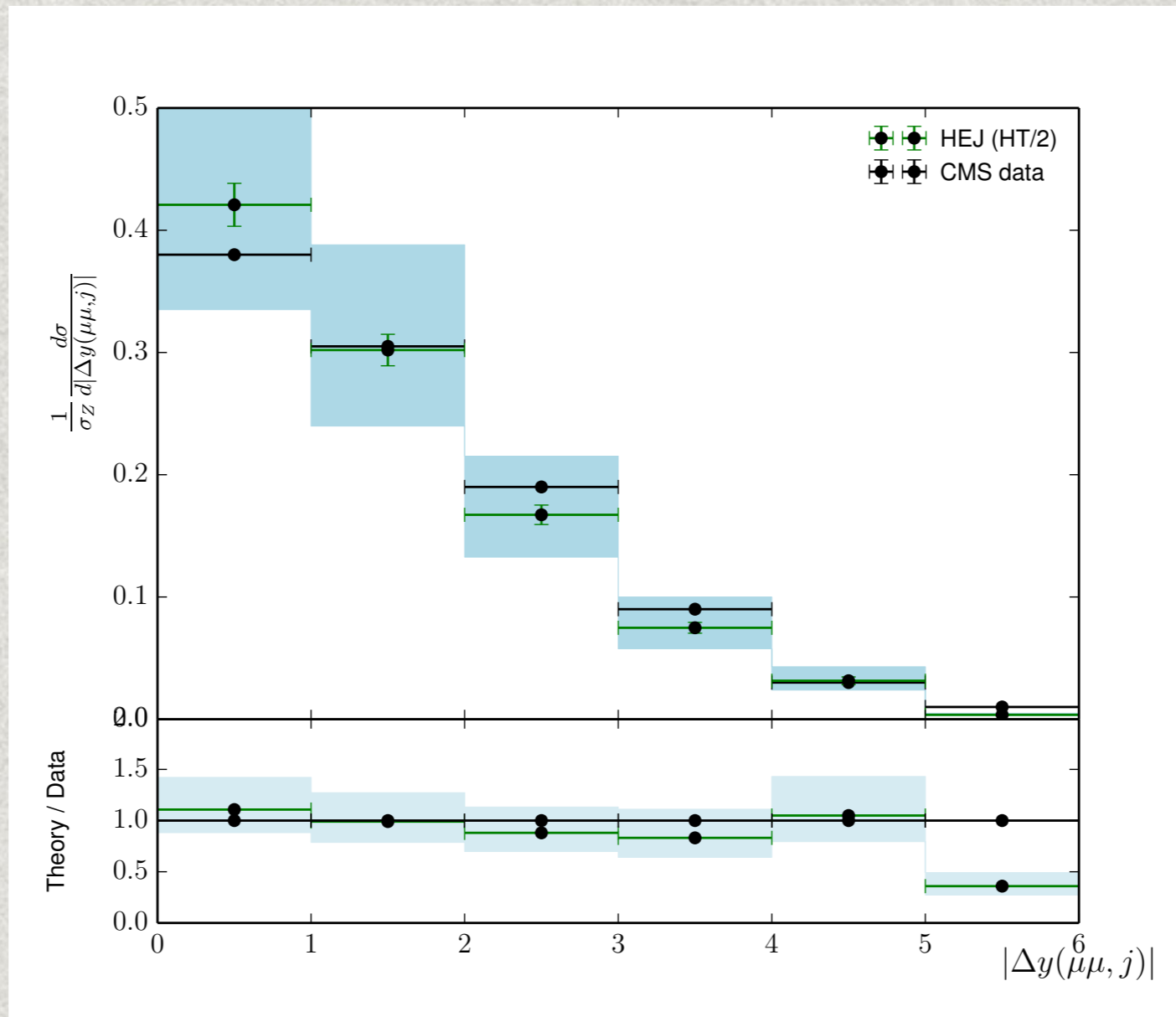
Many interesting distributions studied up to 5 jets

# ATLAS 2011 $W+Jets$



Clearly illustrates the improvement at large invariant mass

# CMS 2011 Z+Jets



Mass window:  $60 \text{ GeV} < m_{\mu\mu} < 120 \text{ GeV}$

HEJ = PRELIMINARY

# Higgs Plus Dijets



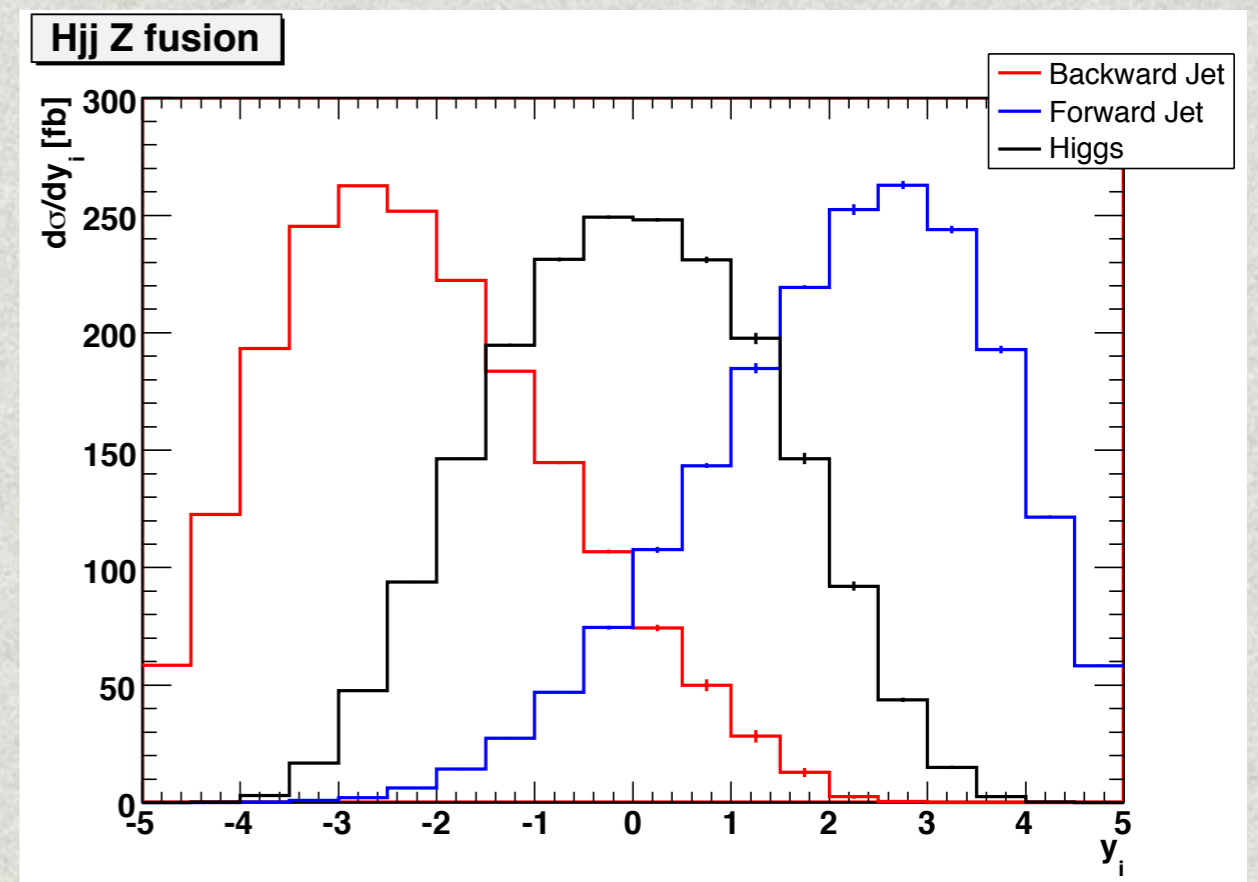
# Higgs Plus Dijets

- \* Vector Boson Fusion is 2nd largest production channel
- \* Key opportunity to study VVH vertex
- \* Use distinctive topology to select events

Here:

$$p_{T,j} > 20 \text{ GeV}, |\eta_j| \leq 5,$$

$$R_{jj} > 0.6$$



# Higgs Plus Dijets

Typical “VBF” cuts:

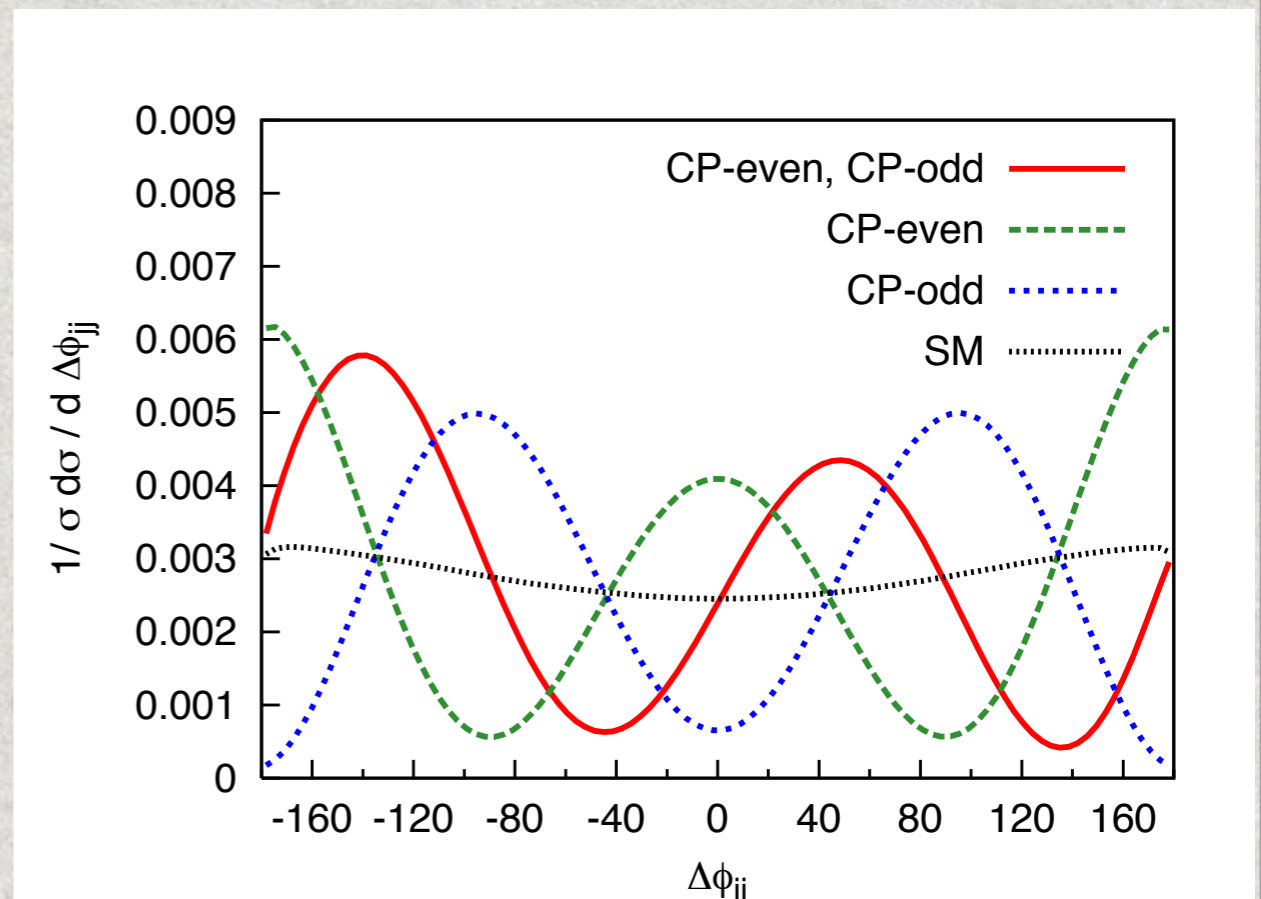
$$p_{T,j} > 25 \text{ GeV}, |\eta_j| \leq 5, |\Delta\eta_{jj}| > 2.8, m_{jj} > 400 \text{ GeV}$$

Puts us right into the difficult region!

Want to use azimuthal angle between jets to study CP structure of the vertex:

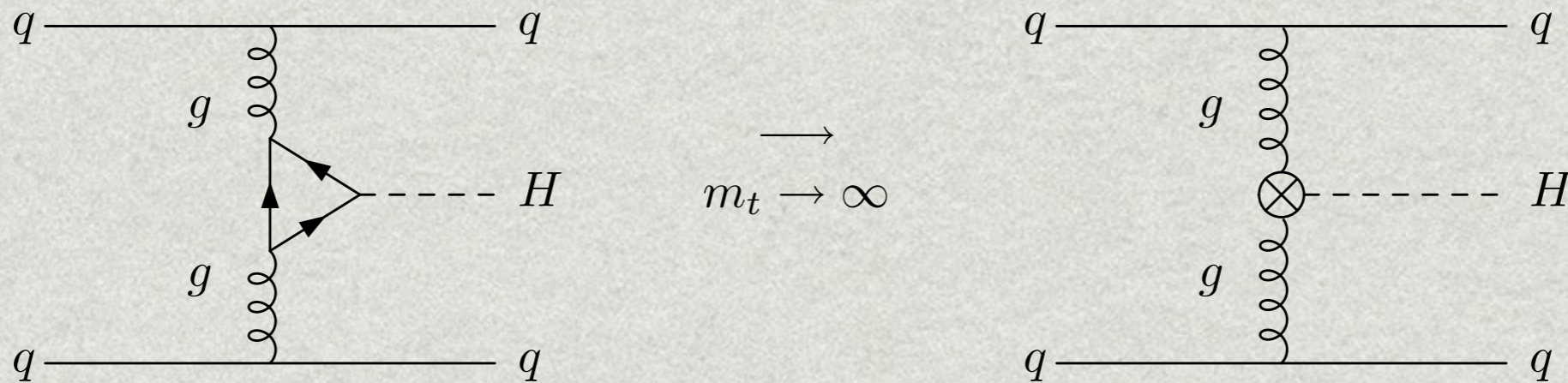
HE limit tells you how to extend to n jets

Andersen, Arnold & Zeppenfeld [arXiv:1001.3822](https://arxiv.org/abs/1001.3822)



Figy, Hankele, Klämke & Zeppenfeld [hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)

# Higgs Plus Jets



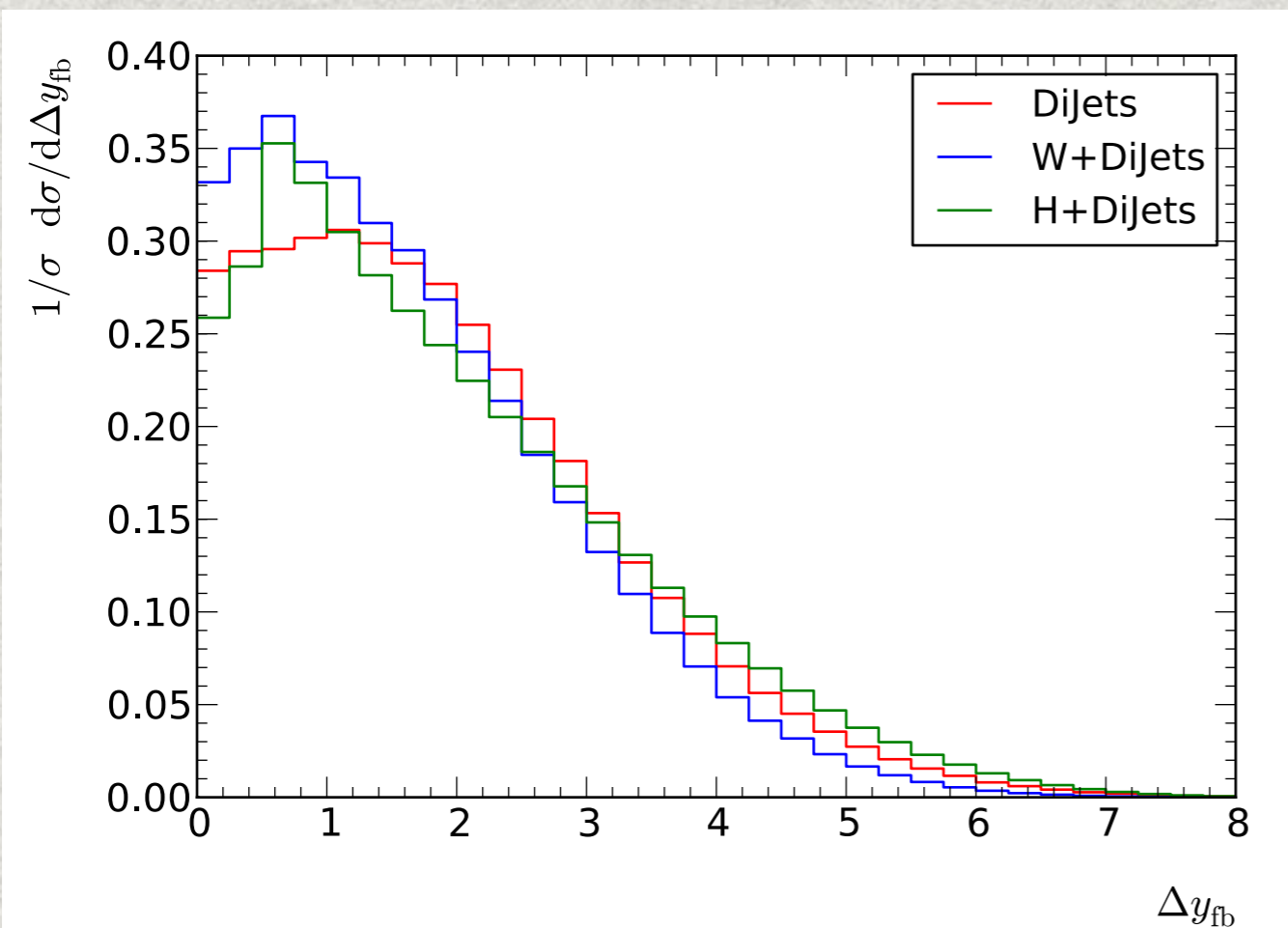
In heavy top-mass limit:  $V_{Hgg}(p^\mu, q^\nu) = \frac{i\alpha_s}{3\pi v} (p \cdot q g^{\mu\nu} - p^\nu q^\mu)$

- \* Different CP structure so can contaminate study.
- \* Interesting to study in own right
- \* Gluons expected to radiate more  
 $\therefore$  use a “jet veto” between tagged jets to separate

# Multi-Jet Descriptions

To extract couplings cleanly, need to separate Weak Boson Fusion and Gluon-Gluon Fusion (ideally both!)


From now on, will focus on Gluon-Gluon Fusion.



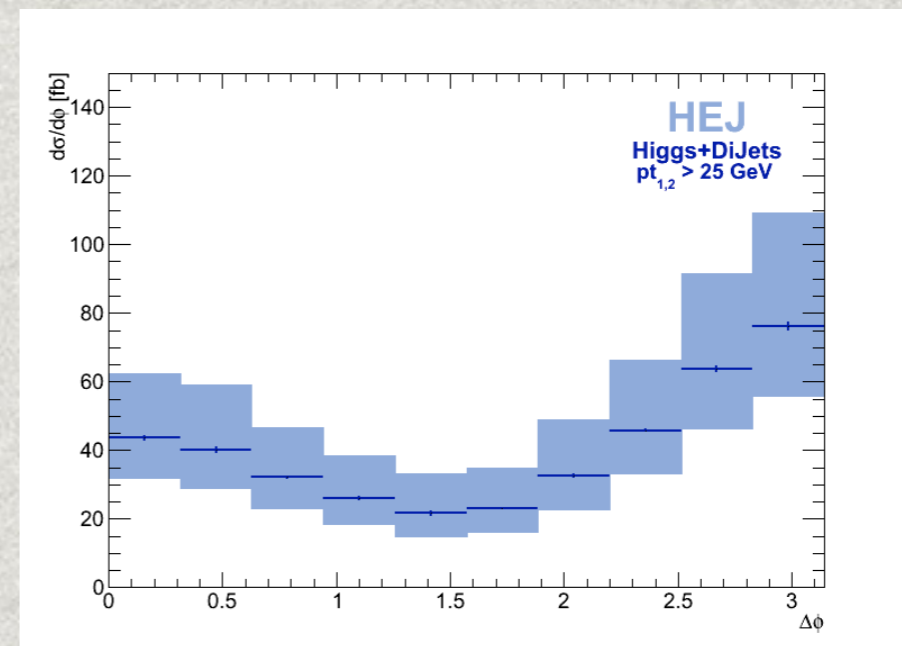
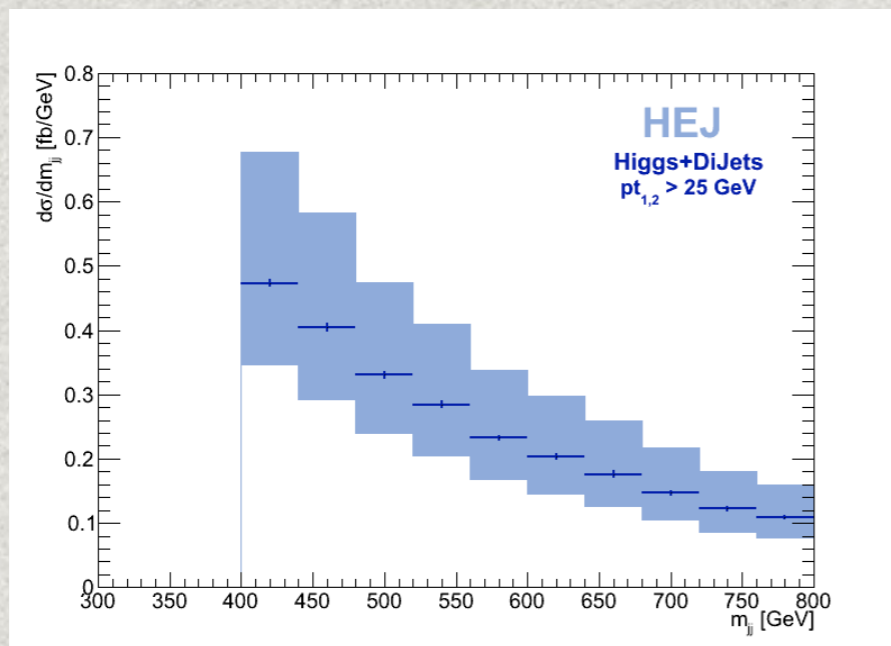
Jet radiation patterns universal across processes.

Use existing data to test descriptions.

# Higgs in HEJ

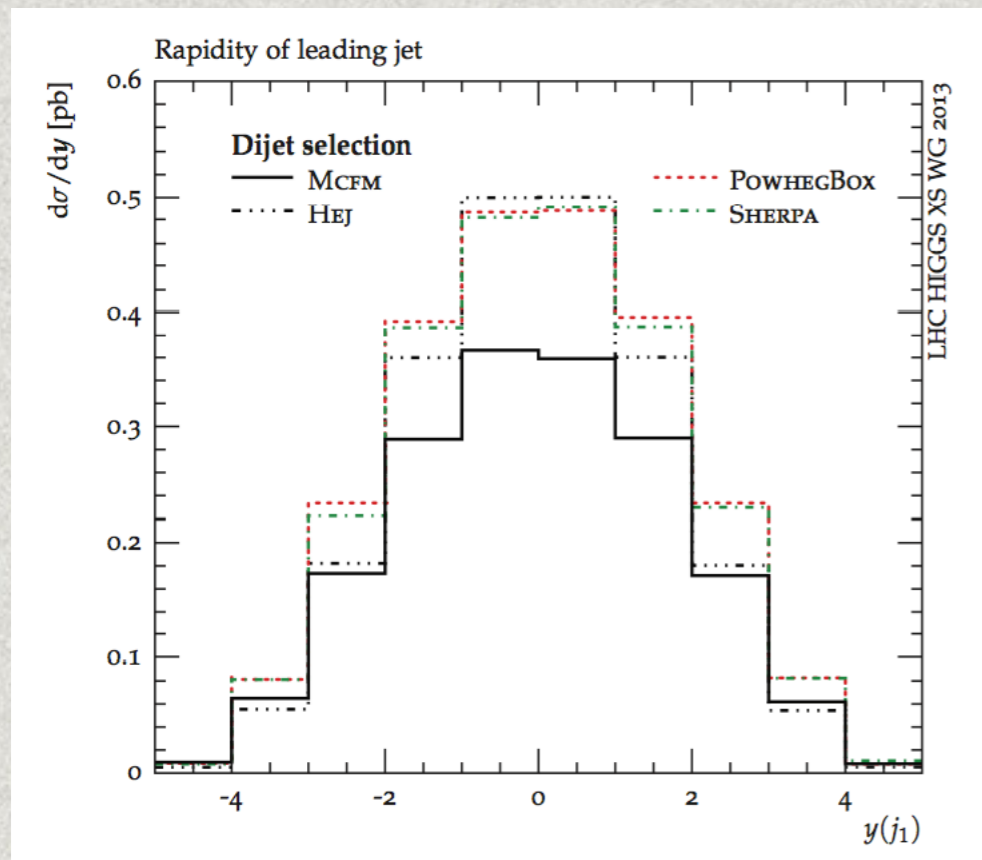

$$\frac{j^\mu j_\mu}{\hat{t}} \rightarrow \frac{j^\mu j^\nu}{q_1^2 q_2^2} (g_{\mu\nu} q_1 \cdot q_2 - q_{1\nu} q_{2\mu})$$

Insert this in the gluon chain according to rapidity

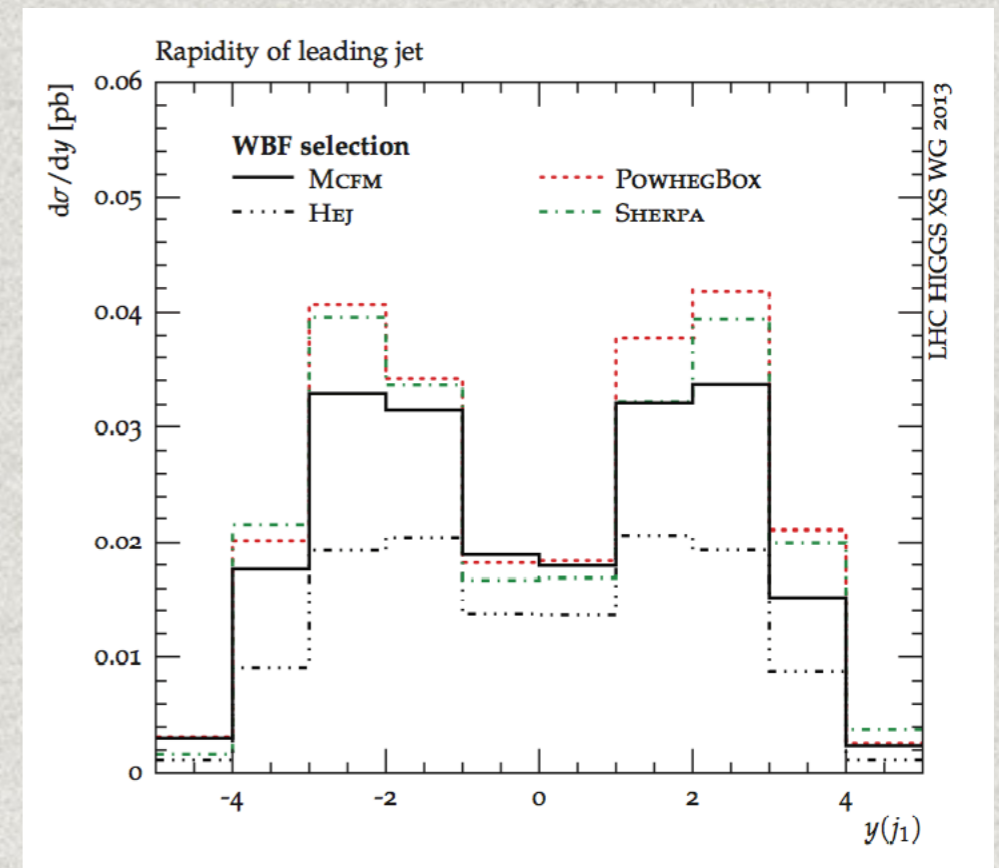


Now also includes one un-ordered gluon emission

# Higgs XS WG YR3 2013

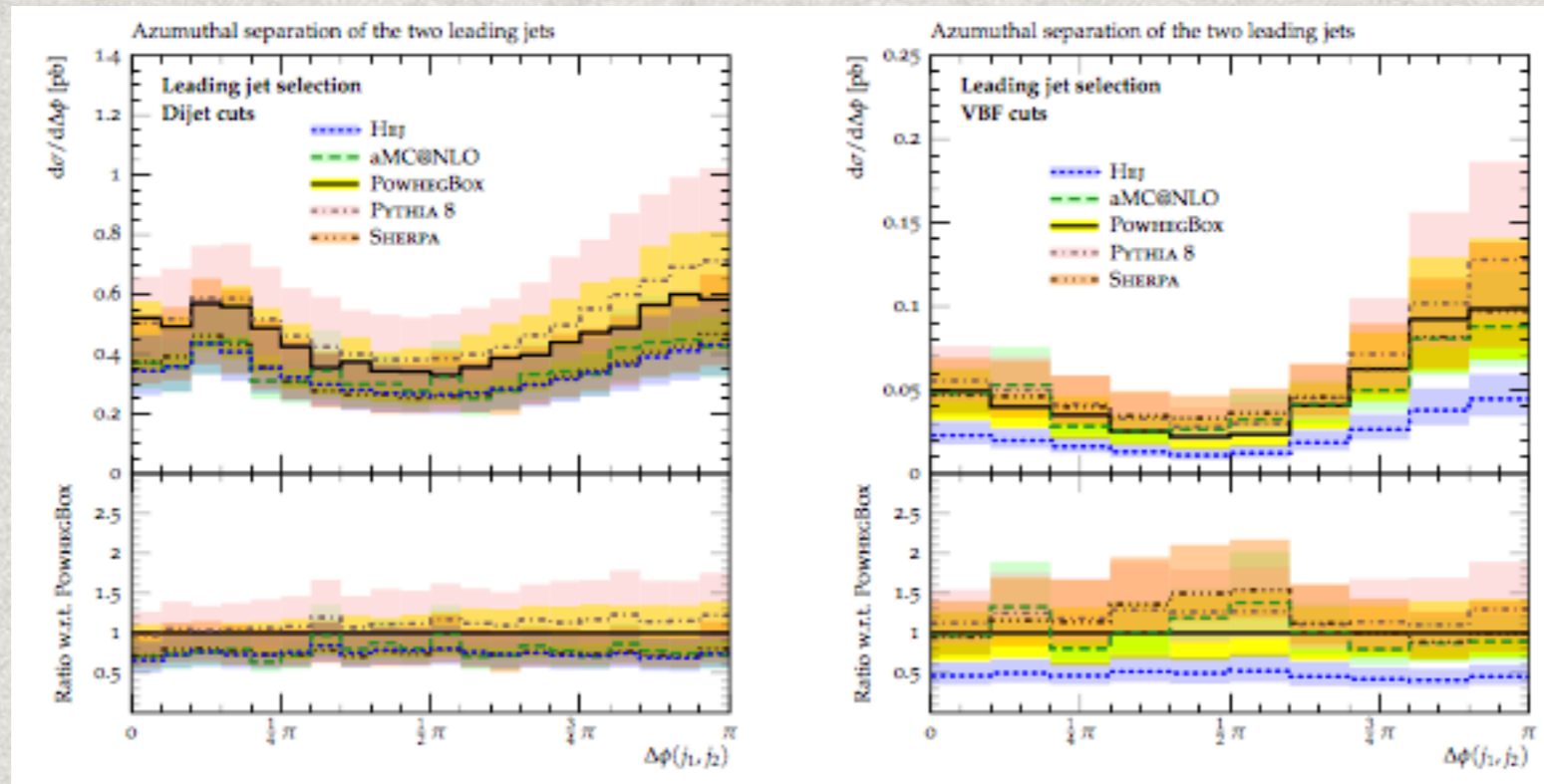


+VBF cuts



- ✱ Difference in shape expected
- ✱ Impact on cross section:  
About 10% for MCFM, POWHEG & SHERPA; 6% for HEJ
- ✱ 2 effects: if well-separated jets, will typically emit a (harder) jet in between; otherwise Regge-suppression

# Variation in Theory



Cross sections in the forward-backward selection

Generator	$\sigma_{\text{dijet}}$ [pb]	$\sigma_{\text{dijet}}$ [pb]	$\sigma_{\text{VBF}}$ [pb]	$\sigma_{\text{VBF}}$ [pb]	$\sigma_{\text{VBF}}$ [pb]
		$y_{j_{\text{bw}}} < y_h < y_{j_{\text{fw}}}$		$y_{j_{\text{bw}}} < y_h < y_{j_{\text{fw}}}$	$y_{j_{\text{bw}}} < y_{j_3} < y_{j_{\text{fw}}}$
HEJ	$1.053^{+0.374}_{-0.253}$	$0.384^{+0.130}_{-0.089}$	$0.103^{+0.044}_{-0.028}$	$0.086^{+0.035}_{-0.022}$	$0.0585^{+0.0323}_{-0.0190}$
aMC@NLO	$1.106^{+0.316}_{-0.272}$	$0.512^{+0.147}_{-0.127}$	$0.183^{+0.058}_{-0.047}$	$0.163^{+0.050}_{-0.041}$	$0.0796^{+0.0237}_{-0.0198}$
POWHEGBOX	$1.426^{+0.328}_{-0.415}$	$0.658^{+0.199}_{-0.214}$	$0.197^{+0.068}_{-0.068}$	$0.177^{+0.060}_{-0.061}$	$0.0878^{+0.0472}_{-0.0394}$
PYTHIA 8	$1.590^{+0.612}_{-0.385}$	$0.716^{+0.282}_{-0.175}$	$0.220^{+0.093}_{-0.055}$	$0.195^{+0.082}_{-0.049}$	$0.0726^{+0.0288}_{-0.0173}$
SHERPA	$1.073^{+0.462}_{-0.225}$	$0.499^{+0.229}_{-0.099}$	$0.218^{+0.102}_{-0.052}$	$0.189^{+0.091}_{-0.045}$	$0.1129^{+0.0656}_{-0.0296}$

Les Houches 2013  
arXiv:1405.1067

See update at this year's Les Houches workshop!

# Summary

- \* Hard QCD radiation feature of LHC collisions
- \* Data has clearly shown effects beyond pure NLO
- \* Flexible MC description from HEJ  
Built from HE properties of amplitudes
- \* Lots of interesting physics in jet data with  
important applications to Higgs+Jets studies

<http://cern.ch/hej>