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Searches for rare and BSM top quark processes at the ATLAS experiment

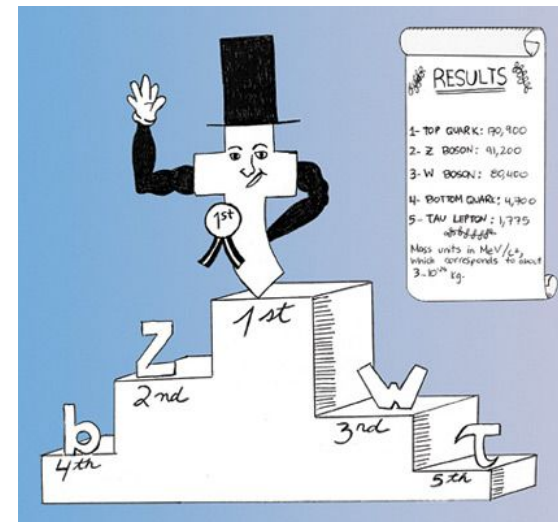
Birmingham HEP Seminar

03/05/23

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- Top phenomenology driven by its mass
 - Heaviest known elementary particle
 - $Y_t \sim 1 \rightarrow$ large coupling to Higgs
 - Potentially large couplings to hypothetical new particles
- ATLAS Run 2 dataset: huge sample of top events
 - ~ 115 mn top pairs, ~ 40 mn single top
 - Clear decay signature $\sim 100\%$ to Wb ($|V_{tb}| \sim 1$)
 - Unprecedented sensitivity to rare SM top processes
 - Possibility to probe possible new physics interactions



- No new physics searches at the LHC have yet been fruitful
- Raises possibility that $\Lambda_{\text{NP}} \gg \Lambda_{\text{EW}} \rightarrow$ motivates indirect searches for non-SM couplings
 - Observation of 4 top quark production
 - Searches for flavour-changing neutral current (FCNC) interactions of the top quark
 - Search for charged lepton flavour-violating (CLFV) interactions of the top quark
- All measurements discussed are from Run 2 (2015-2018) using the full 13 TeV dataset of 140 fb^{-1}

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- Raises possibility that $\Lambda_{\text{NP}} \gg \Lambda_{\text{EW}} \rightarrow$ motivates indirect searches for non-SM couplings
 - Observation of 4 top quark production } **Sensitive to BSM corrections/MC modelling**
 - Searches for FCNC interactions of the top quark } **Unobservable in SM \rightarrow evidence would point to BSM**
 - Search for CLFV interactions of the top quark }
- All measurements discussed are from Run 2 (2015-2018) using the full 13 TeV dataset of 140 fb^{-1}

- For Λ_{NP} significantly greater than experimental sensitivity, we can employ an EFT approach
 - E.g. Fermi theory of β -decay - point-like four fermion interaction
 - Perform calculations without knowledge of short-distance theory
- Construct effective Lagrangian in terms of SM fields:

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{i,n} \frac{c_i^{(n)}}{\Lambda^{n-4}} \mathcal{O}_i^{(n)}$$

Operators introducing new interactions

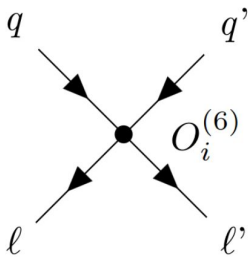
Familiar SM ("renormalisable")

Encodes strength of coupling

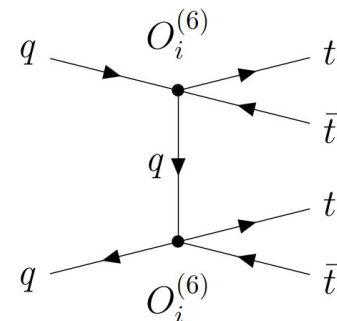
- SMEFT: 59 independent dim-6 operators (assuming B-conservation)

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	Q_{qqq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

CLFV-inducing



Enhanced four top cross-section



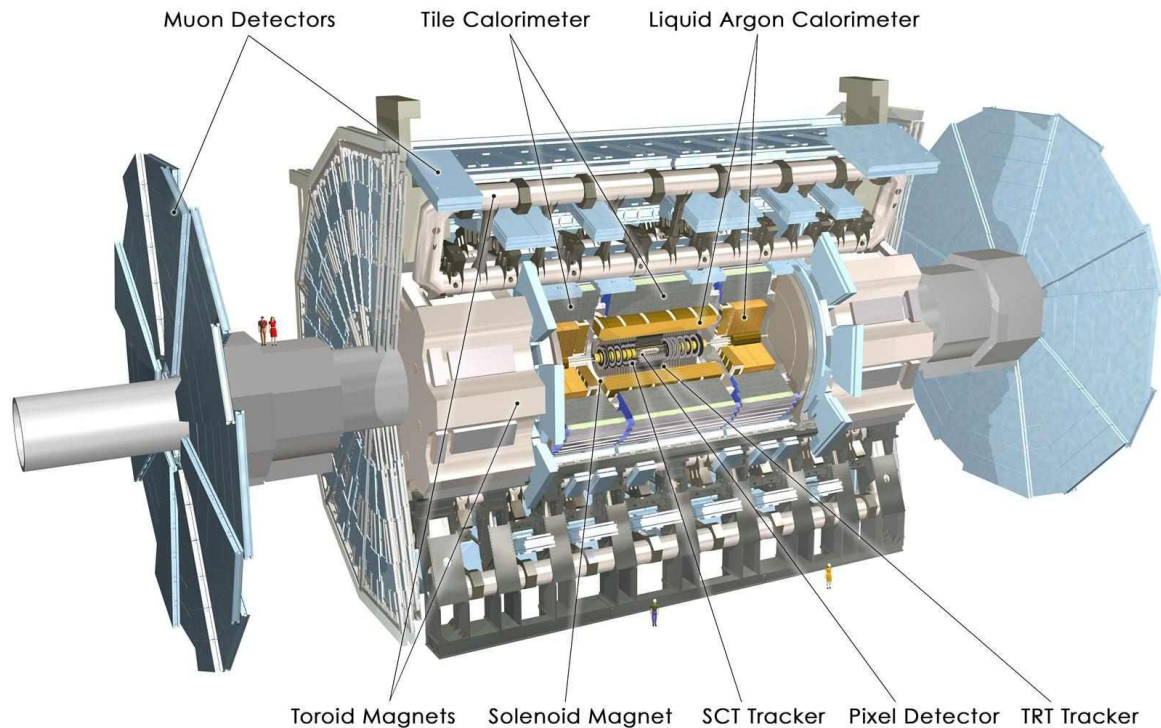
p,r,s,t = flavour/family indices

Table 3: Four-fermion operators.

(arXiv:1008.4884)

The ATLAS experiment

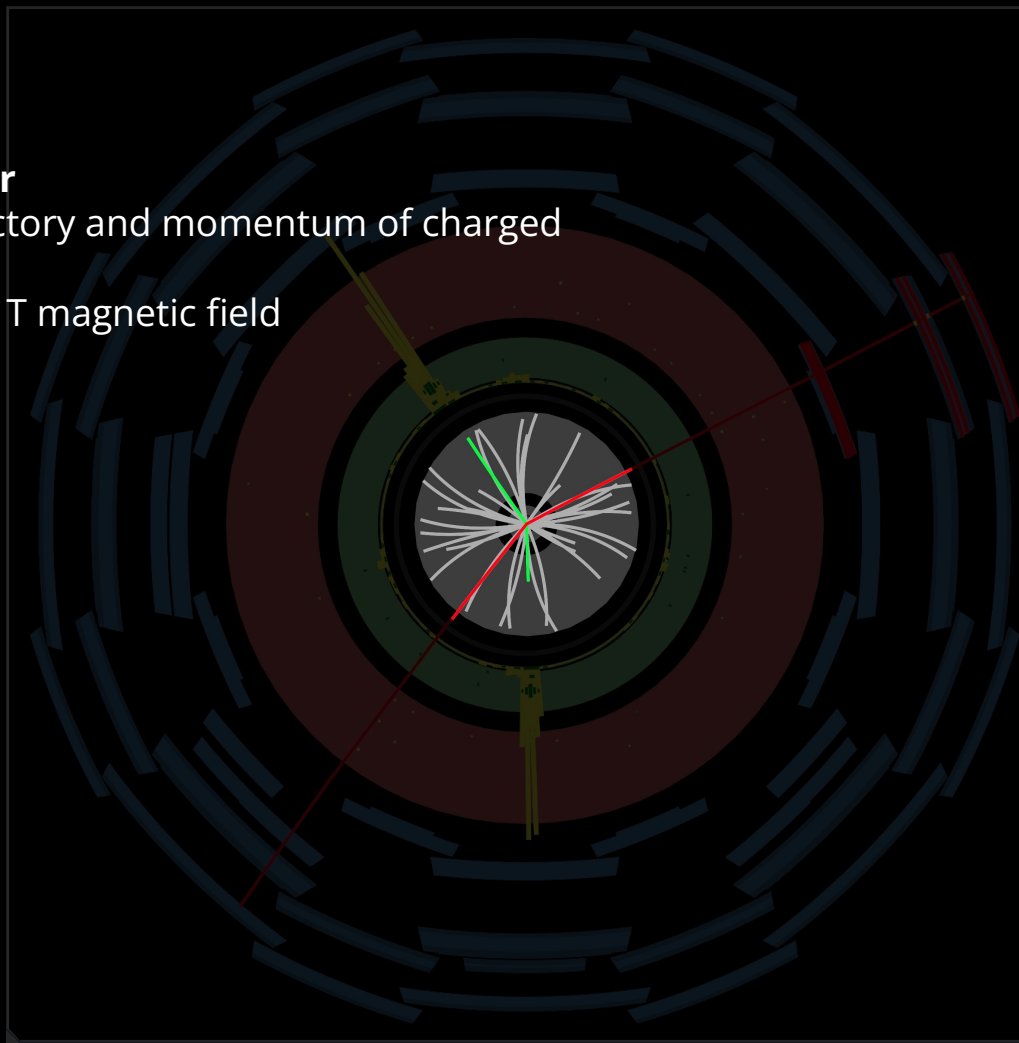
- Multipurpose particle detector
 - Forward-backward symmetric
 - Almost full 4π coverage around interaction point
- LHC bunch crossing rate ~ 40 MHz
 - Most crossings result only in soft QCD interactions
- Two-level trigger system to select potentially interesting physics events at rate of ~ 1 kHz



Inner detector

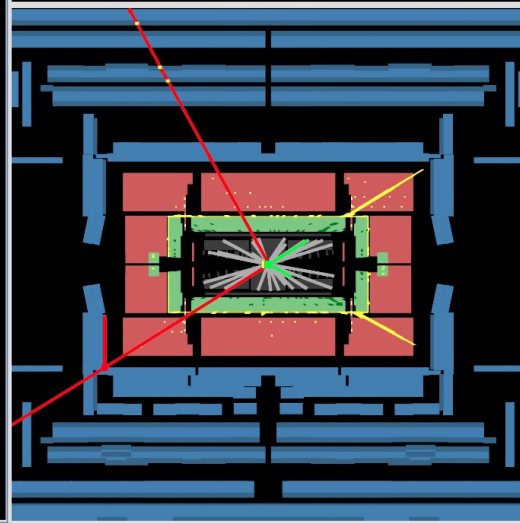
Measure trajectory and momentum of charged particles

Immersed in 2 T magnetic field



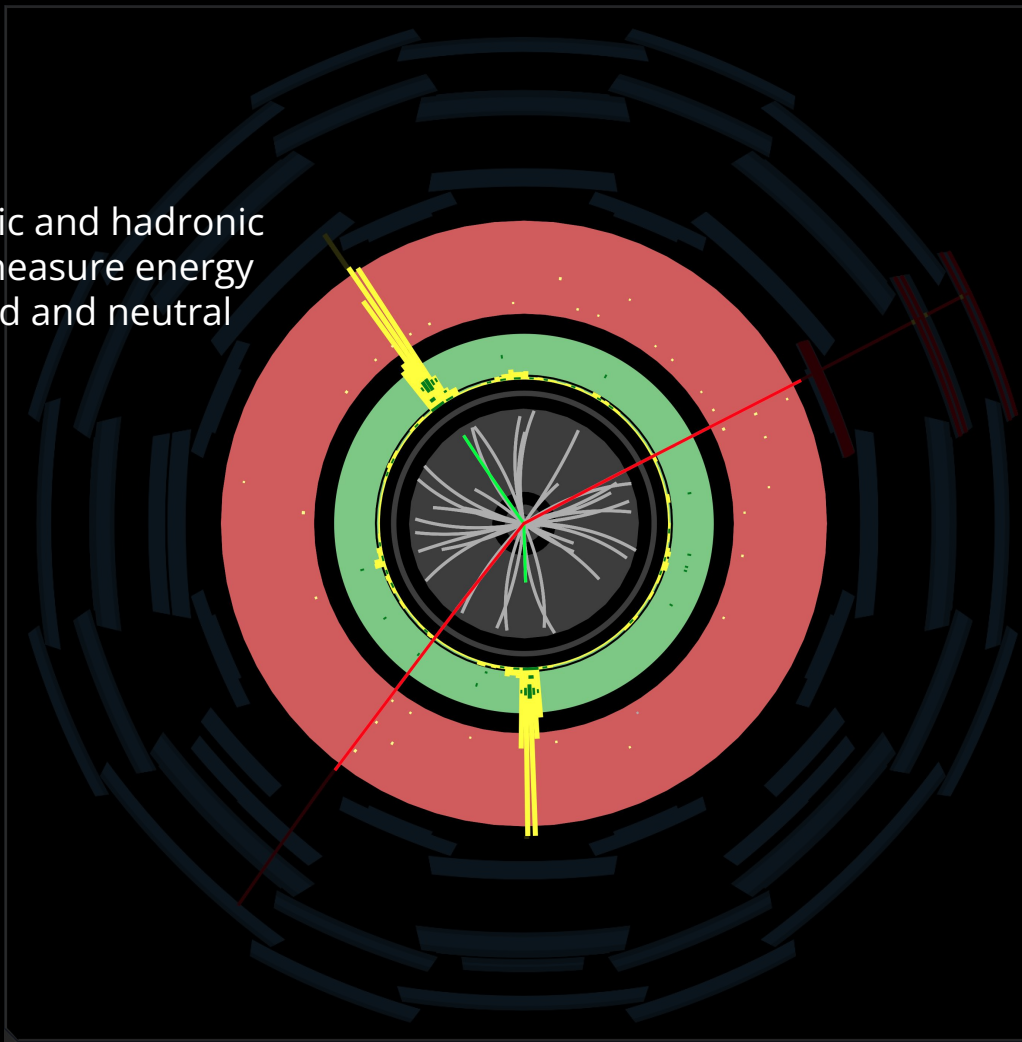
Run Number: 271421, Event Number: 287349506

Date: 2015-07-12 09:53:46 CEST



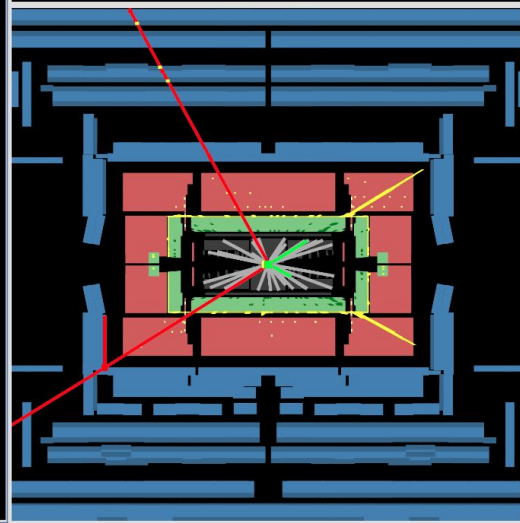
Calorimeters

Electromagnetic and hadronic calorimeters measure energy of both charged and neutral particles

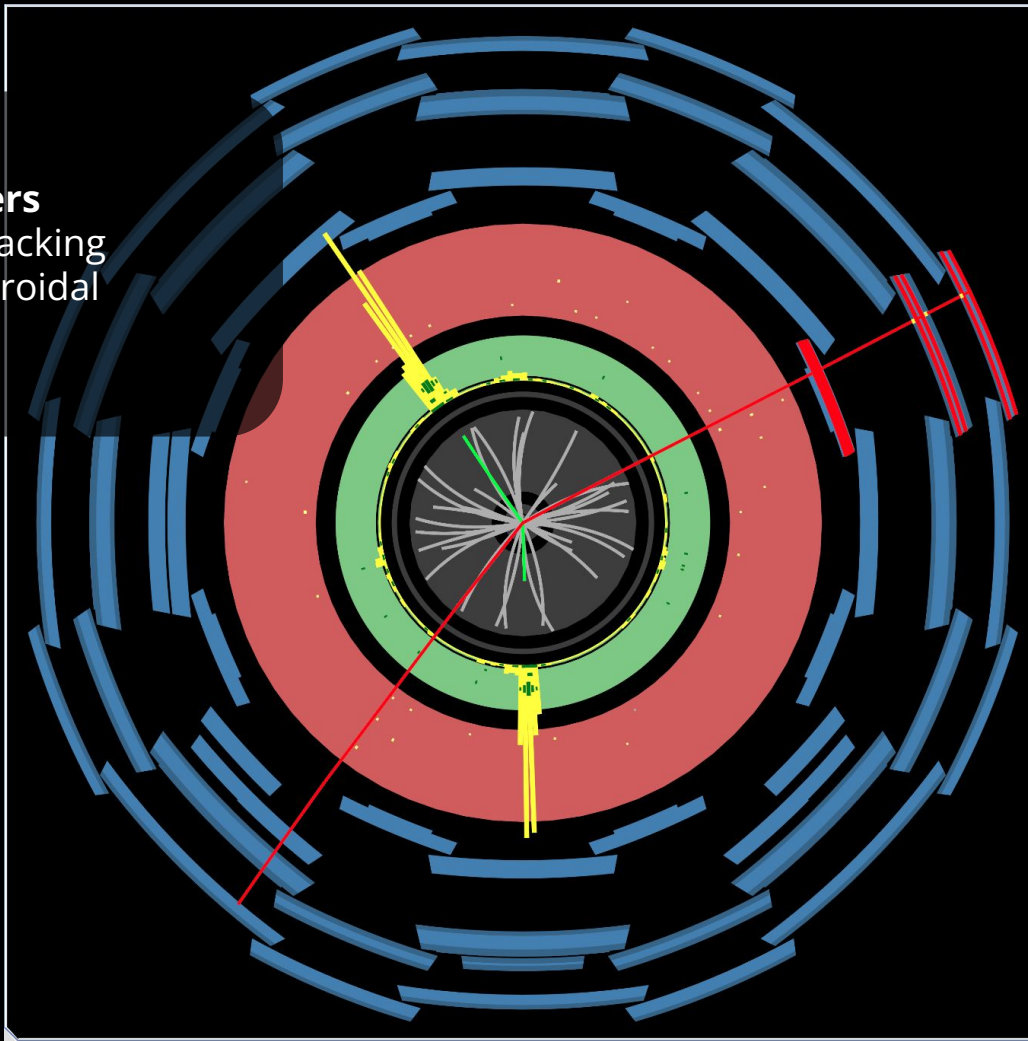


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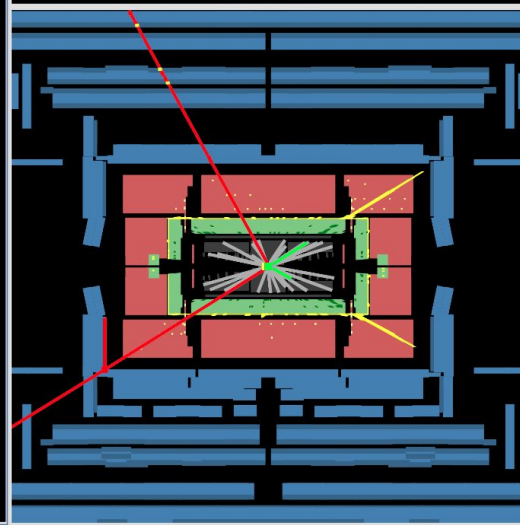


Muon chambers
Large-radius tracking
chambers in toroidal
magnetic field

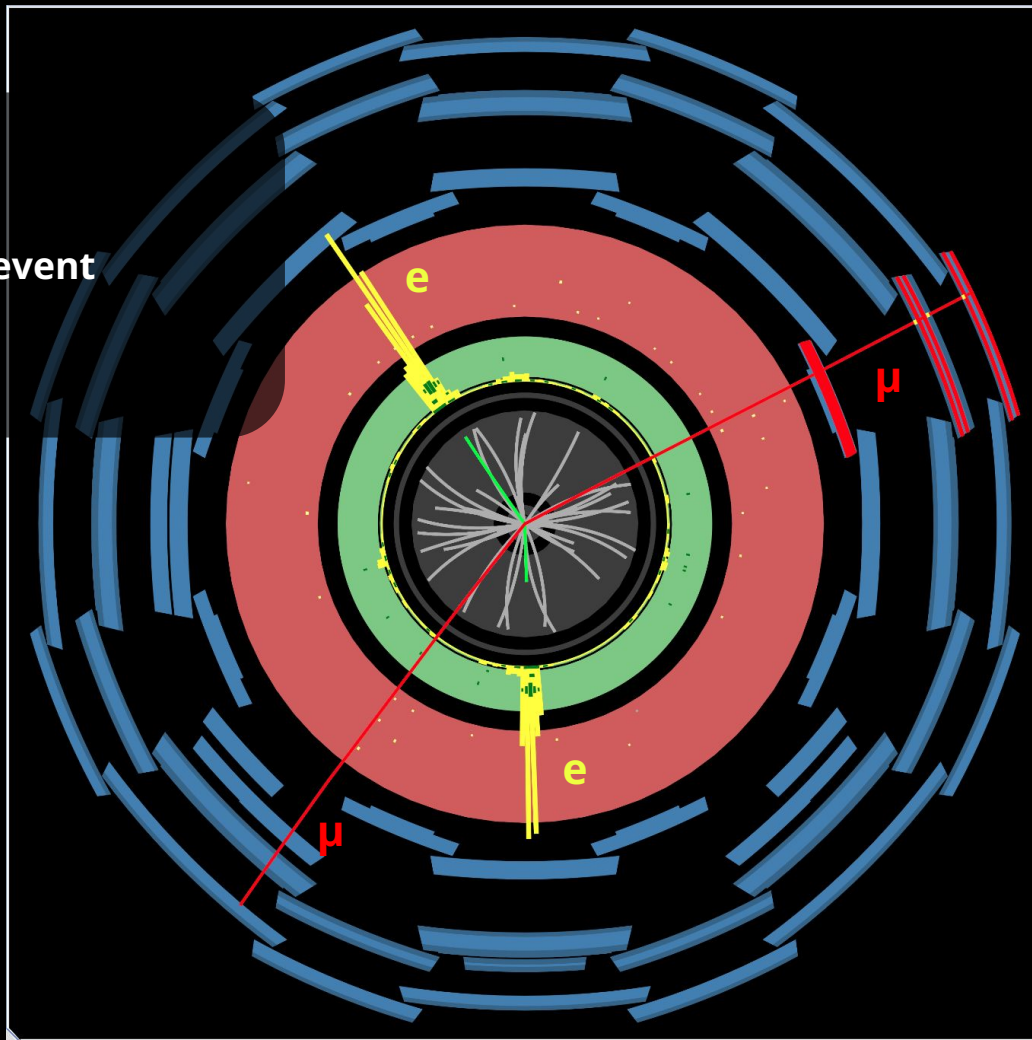


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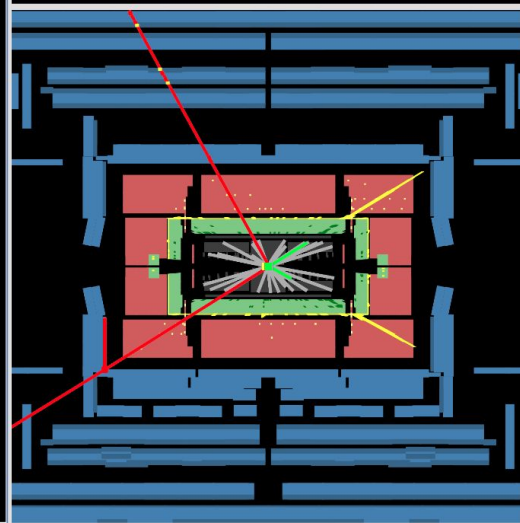


ZZ candidate event



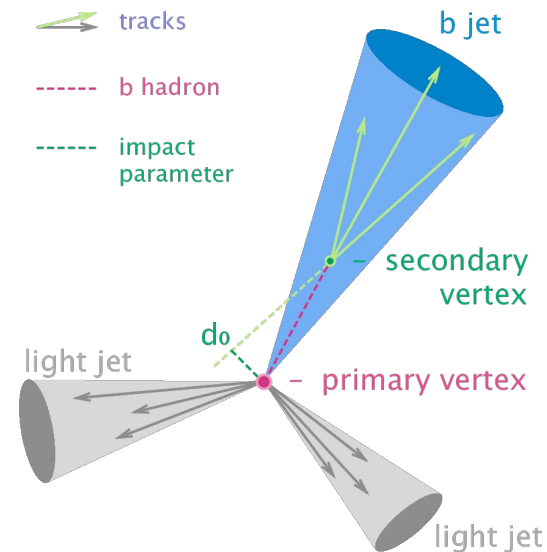
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- Select events of interest based on triggers
 - Analyses discussed today use single-lepton or dilepton triggers
- Apply reconstructed object selections to events passing trigger(s)
 - Electrons, photons, muons
 - Jets (collimated shower of hadrons from quarks/gluons)
 - Hadronically-decaying tau leptons
 - Missing transverse energy (MET) → neutrinos, mis-calibration, BSM?

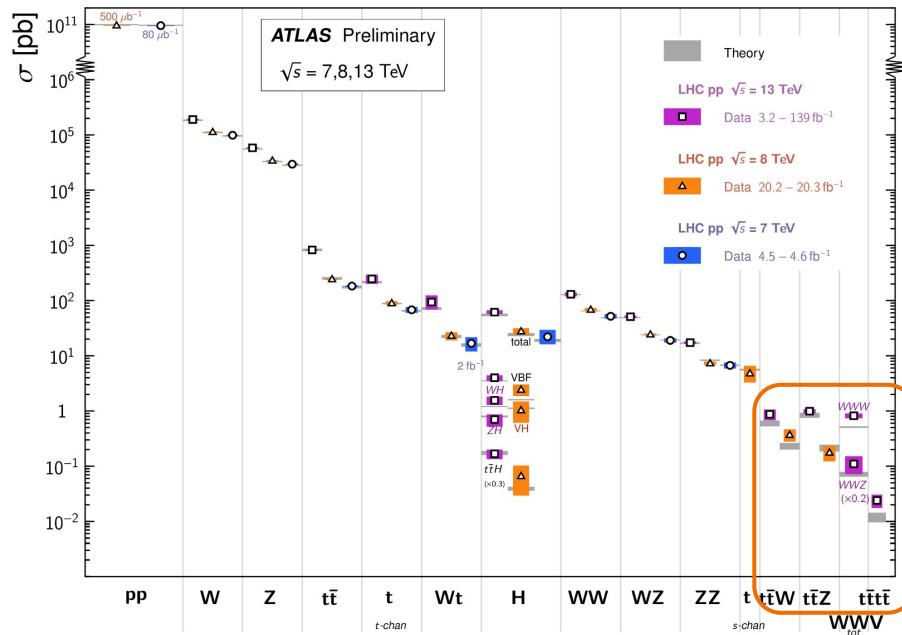
- B-tagging:
 - Determine likelihood that a jet originated from a B-hadron decay (as opposed to C- or light hadron decay)
- Events categorised into regions by event kinematics/further object selection
 - SRs - signal-dominated regions → sensitivity to process of interest
 - CRs - signal-depleted regions → correct/modelling background processes
- Profile likelihood fit across all regions
 - Systematic uncertainties profiled as nuisance parameters



Rare SM top processes

Standard Model Total Production Cross Section Measurements

Status: February 2022



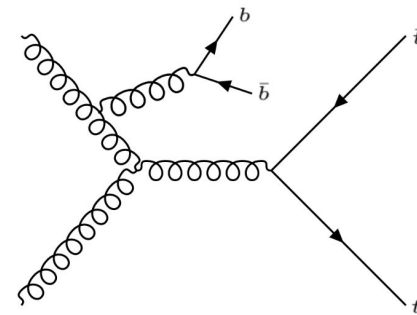
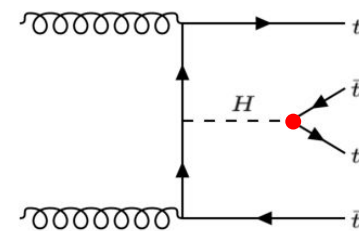
Motivation

- Very rare SM process ($\sigma_{4t}^{\text{SM}} = 12.0 \pm 2.4 \text{ fb}$)
- Many BSM models predict enhancements to σ_{4t}
 - E.g. gluino pair production, 2HDM
 - Sensitivity to four-fermion EFT couplings
- Also sensitive to CP properties of y_t

Measurement channels

- $1\ell/2\ell\text{OS}$ (57% BR)
 - Large irreducible $t\bar{t} + \text{HF}$ → significant theoretical uncertainties
- $2\ell\text{SS}/3\ell$ (13% BR) → [arXiv:2303.15061](https://arxiv.org/abs/2303.15061)
 - Low background (dominated by $t\bar{t}H/Z/W + \text{jets}$)

EW $4t$ production -
sensitivity to y_t



$t\bar{t} + b\bar{b}$ production

Four top production - background estimation

- Low background 2ℓSS/3ℓ channel
- Signature: high jet multiplicity, high b-jet multiplicity, high overall energy
- Data-driven background estimations to correct MC modelling
 - Dedicated CRs for non-prompt/fake leptons
 - **Dedicated correction to $\bar{t}tW$**

Region	Channel	N_j	N_b	Other selection	Fitted variable
CR Low m_{γ^*}	SS, ee or $e\mu$	$4 \leq N_j < 6$	≥ 1	ℓ_0 or ℓ_1 is from virtual photon (γ^*) decay ℓ_0 and ℓ_1 are not from photon conversion	counting
CR Mat. Conv.	SS, ee or $e\mu$	$4 \leq N_j < 6$	≥ 1	ℓ_0 or ℓ_1 is from photon conversion	counting
CR HF μ	$e\mu\mu$ or $\mu\mu\mu$	≥ 1	$= 1$	$100 < H_T < 300$ GeV $E_T^{\text{miss}} > 50$ GeV total charge is ± 1	$p_T^{\ell_2}$
CR HF e	eee or $ee\mu$	≥ 1	$= 1$	$100 < H_T < 275$ GeV $E_T^{\text{miss}} > 35$ GeV total charge is ± 1	$p_T^{\ell_2}$
CR $t\bar{t}W^+ + \text{jets}$	SS, $e\mu$ or $\mu\mu$	≥ 4	≥ 2	$ \eta(e) < 1.5$ when $N_b = 2$: $H_T < 500$ GeV or $N_j < 6$ when $N_b \geq 3$: $H_T < 500$ GeV total charge > 0	N_j
CR $t\bar{t}W^- + \text{jets}$	SS, $e\mu$ or $\mu\mu$	≥ 4	≥ 2	$ \eta(e) < 1.5$ when $N_b = 2$: $H_T < 500$ GeV or $N_j < 6$ when $N_b \geq 3$: $H_T < 500$ GeV total charge < 0	N_j
CR 1b(+)	2LSS+3L	≥ 4	$= 1$	ℓ_0 and ℓ_1 are not from photon conversion $H_T > 500$ GeV total charge > 0	N_j
CR 1b(-)	2LSS+3L	≥ 4	$= 1$	ℓ_0 and ℓ_1 are not from photon conversion $H_T > 500$ GeV total charge < 0	N_j
SR	2LSS+3L	≥ 6	≥ 2	$H_T > 500$	GNN score

$$H_T = \sum_j^{N_{jets}} p_T^j + \sum_\ell^{N_\ell} p_T^\ell$$

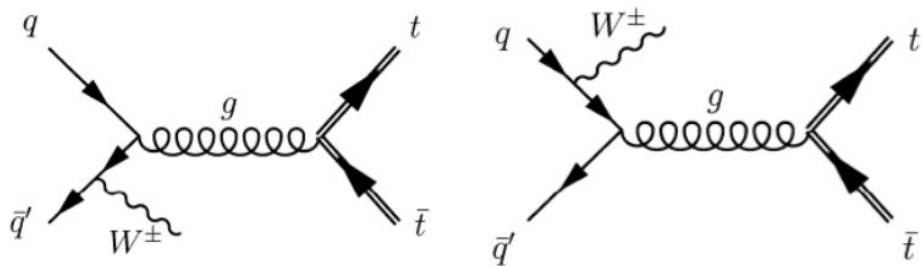
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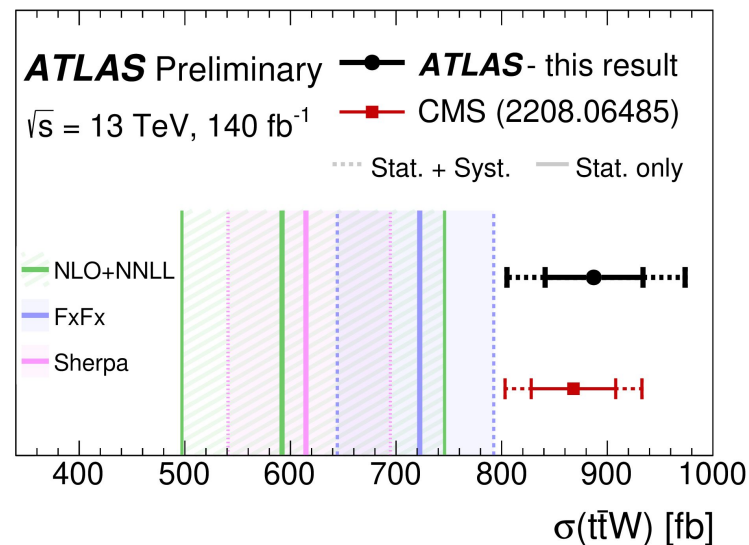
$$H_T = \sum_j^{N_{\text{jets}}} p_T^j + \sum_\ell^{N_\ell} p_T^\ell$$

LO ttW production



- Observed in Run 1, differential measurements now available
- Irreducible background to many multi-lepton analyses (incl. ttH)
- **Theory seen to consistently underestimate cross-section**
- Currently nothing to explain discrepancy → ideally use data-driven treatments

[ATLAS-CONF-2023-019](#)



- Jet multiplicity-dependent correction: derive four scaling factors using four CRs

$$a_0 \quad a_1 \quad \text{NF}_{t\bar{t}W^+(4\text{jet})} \quad \text{NF}_{t\bar{t}W^-(4\text{jet})}$$

- Rely on known scaling properties of QCD jets at hadron colliders *
 - For low N_{jets} expect Poisson scaling $\rightarrow N(j+1)/N(j) = \text{const}/(1+j)$
 - At high N_{jets} expect fixed probability of additional emission $\rightarrow N(j+1)/N(j) = \text{constant}$

$$\text{NF}_{t\bar{t}W(j)} = \text{NF}_{t\bar{t}W^+(4\text{jet})} \times \prod_{j'=4}^{j-1} \left[a_0 + \frac{a_1}{1 + (j' - 4)} \right] + \text{NF}_{t\bar{t}W^-(4\text{jet})} \times \prod_{j'=4}^{j-1} \left[a_0 + \frac{a_1}{1 + (j' - 4)} \right]$$

Scaling factor for events
with $j > 4$ jets

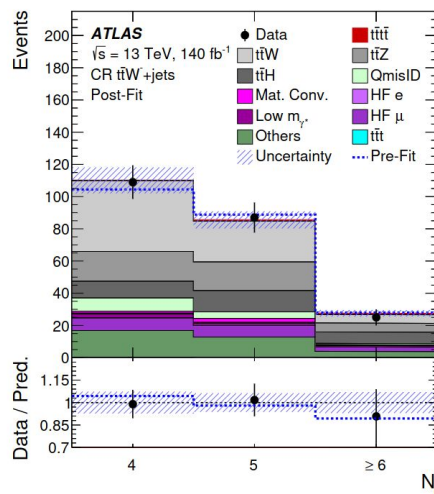
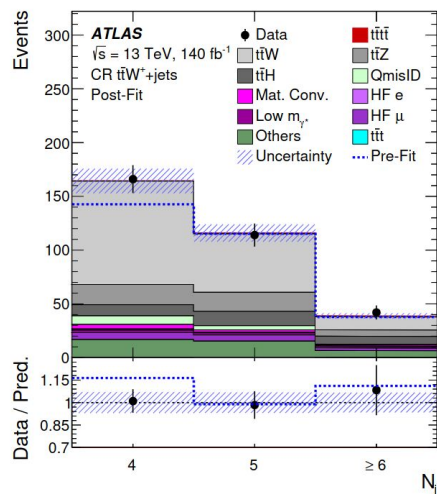
"Staircase" scaling

Poisson scaling

Four top production - ttW background estimation

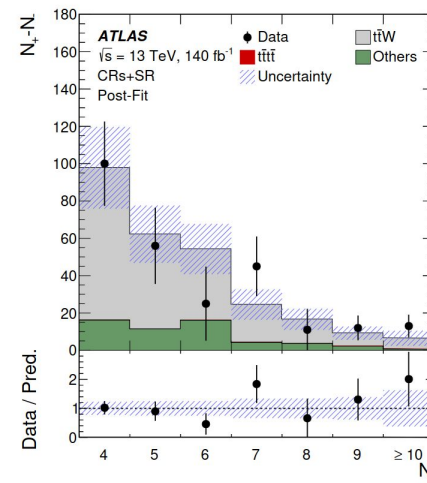
$$NF_{t\bar{t}W(j)} = NF_{t\bar{t}W^+(4jet)} \times \prod_{j'=4}^{j'-1} \left[a_0 + \frac{a_1}{1 + (j' - 4)} \right] + NF_{t\bar{t}W^-(4jet)} \times \prod_{j'=4}^{j'-1} \left[a_0 + \frac{a_1}{1 + (j' - 4)} \right]$$

ttW background	a_0	a_1	$NF_{t\bar{t}W^+(4jet)}$	$NF_{t\bar{t}W^-(4jet)}$
Value	0.51 ± 0.10	$0.22^{+0.25}_{-0.22}$	$1.27^{+0.25}_{-0.22}$	$1.11^{+0.31}_{-0.28}$

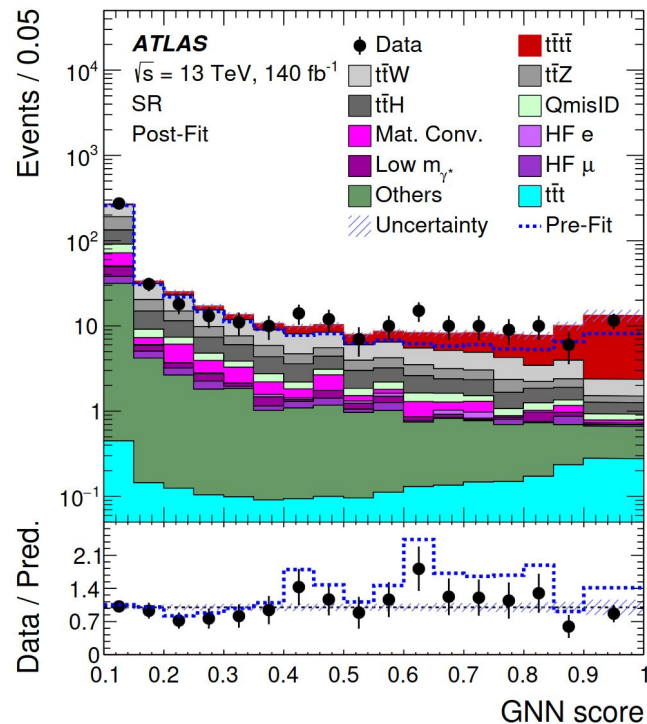
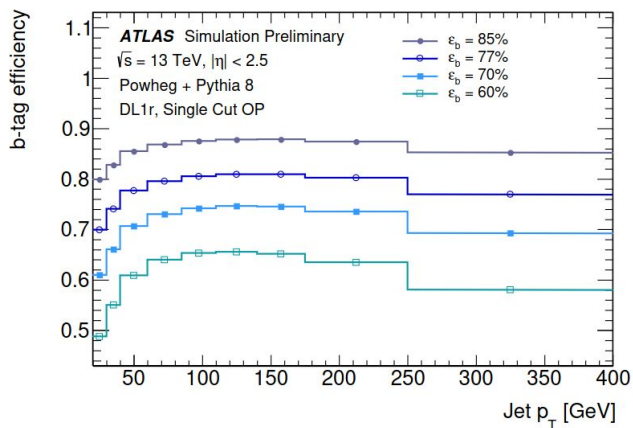


Left: ttW control regions

Right: difference of events with total +ve and -ve charge in all regions



- Fully-connected graph neural network
 - Reconstructed $j/\ell/E_T^{\text{miss}}$ as nodes
 - Angular separations encoded in edges
- 6-way splitting for training/application using SR
- Key input: pseudo-continuous b-tagging scores - categorise how likely jets are to contain b -hadrons



Four tops - results

arXiv:2303.15061

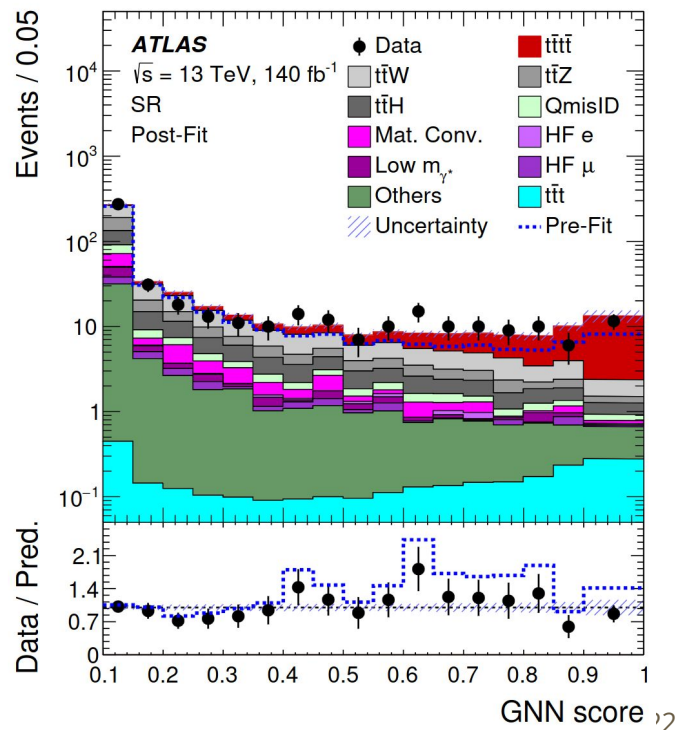


$$\mu = 1.89_{-0.35}^{+0.37}(\text{stat})_{-0.37}^{+0.62}(\text{syst}) = 1.89_{-0.51}^{+0.73}$$

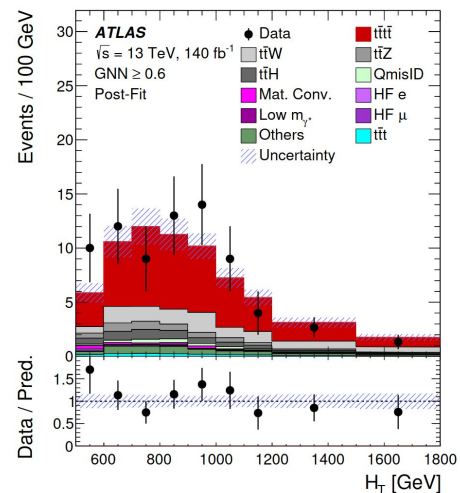
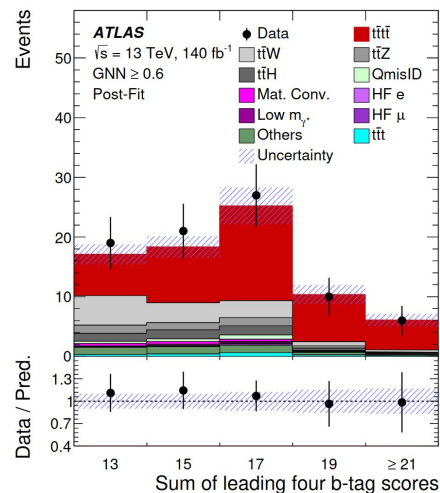
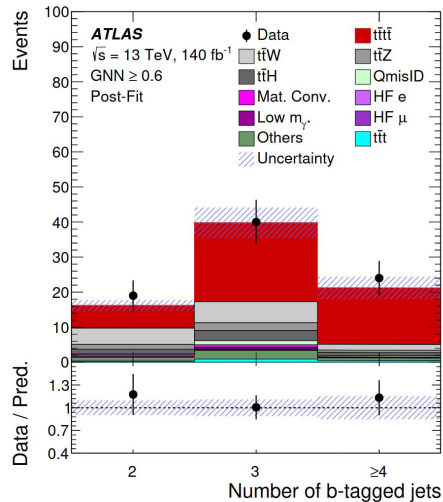
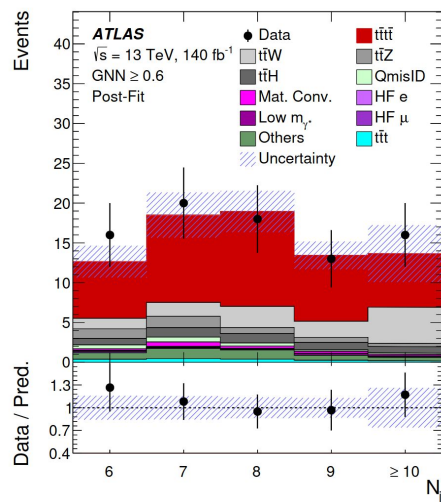
$$\sigma_{t\bar{t}\bar{t}} = 22.7_{-4.4}^{+4.7}(\text{stat})_{-3.4}^{+4.6}(\text{syst}) \text{ fb} = 22.7_{-5.5}^{+6.6} \text{ fb.}$$

- Profile likelihood fit across SR and all CRs
- Observed (exp.) significance: 6.1σ (4.3σ)
- Dominant systematics from modelling of signal and data-driven estimate of $t\bar{t}W$ background
- CMS also [report](#) observation with 5.5σ

Observation of 4 tops production!



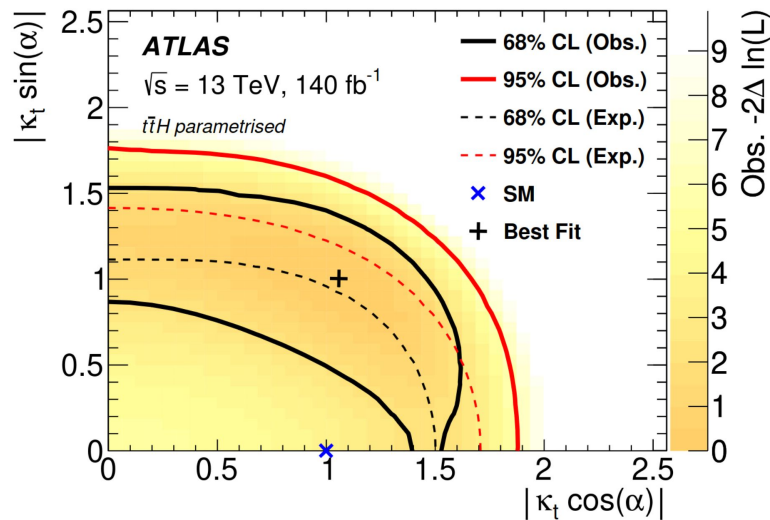
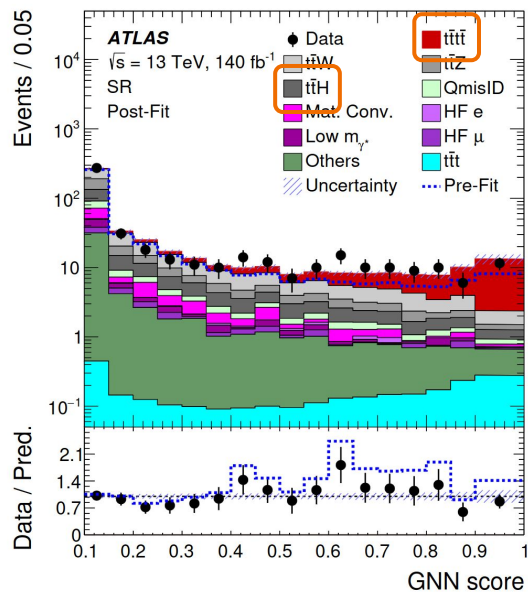
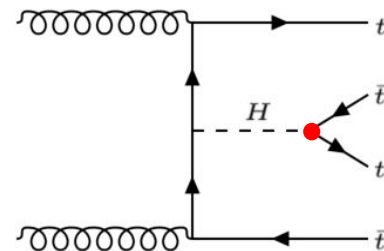
S+B model shows good agreement with observed data in high GNN score region



Four tops \rightarrow top Yukawa coupling

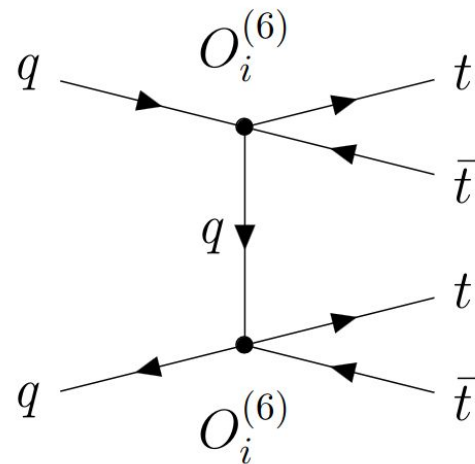
arXiv:2303.15061

- Sensitive to Yukawa coupling strength (κ_t) and CP mixing angle (α)
- Parametrise four top signal and $t\bar{t}H$ GNN distributions in κ_t and α



- BSM physics could enhance four top cross-section
- New physics with strong couplings to tops should show up in four top production

$$\sigma_{t\bar{t}t\bar{t}} = \sigma_{t\bar{t}t\bar{t}}^{SM} + \frac{1}{\Lambda^2} \sum_i C_i \sigma_i^{(1)} + \frac{1}{\Lambda^4} \sum_{i \leq j} C_i C_j \sigma_{i,j}^{(2)}$$



Operators	Expected C_i/Λ^2 [TeV $^{-2}$]	Observed C_i/Λ^2 [TeV $^{-2}$]
O_{QQ}^1	[-2.4,3.0]	[-3.5,4.1]
O_{Qt}^1	[-2.5,2.0]	[-3.5,3.0]
O_{tt}^1	[-1.1,1.3]	[-1.7,1.9]
O_{Qt}^8	[-4.2,4.8]	[-6.2,6.9]

Limits comparable with those found by CMS - [JHEP11 \(2019\) 082](#)

Four tops \rightarrow three tops?

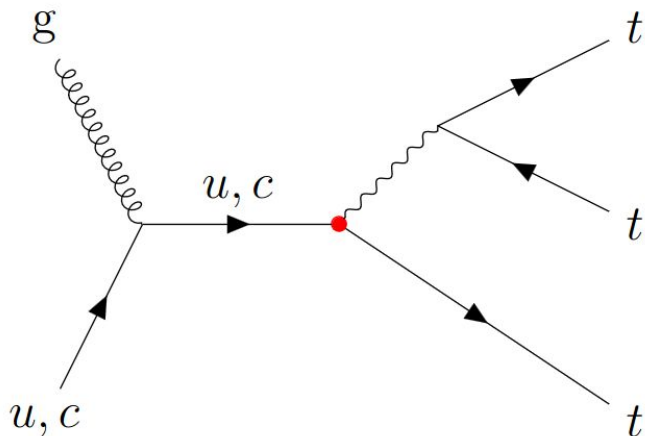
arXiv:2303.15061

- Set limits on cross-section of very rare 3 tops process ($\sigma_{3t}^{\text{SM}} = 1.67 \text{ fb}$)
- Three top cross-section expected to be significantly enhanced by top FCNC couplings

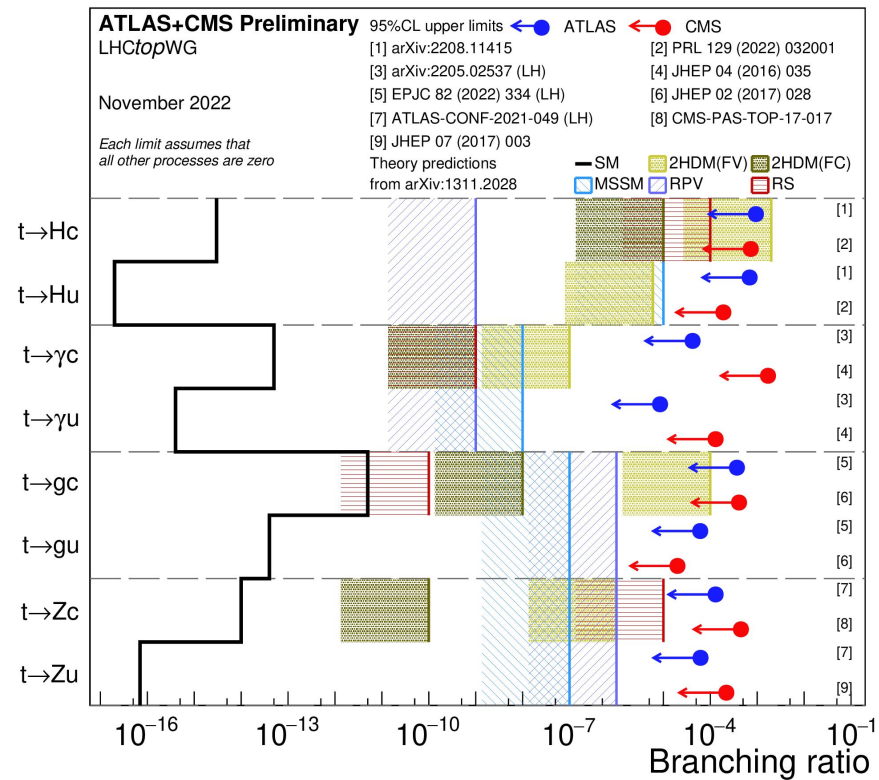
Processes	95% CL cross section interval [fb]	
	$\mu_{t\bar{t}t} = 1$	$\mu_{t\bar{t}t} = 1.9$
$t\bar{t}t$	[4.7, 60]	[0, 41]
$t\bar{t}tW$	[3.1, 43]	[0, 30]
$t\bar{t}tq$	[0, 144]	[0, 100]

$\sigma_{t\bar{t}t} = \sigma_{t\bar{t}tW} + \sigma_{t\bar{t}tq}$

Possible top FCNC interaction with SM boson



Search for FCNC interactions of the top quark



Flavour universality broken by Yukawa couplings of Higgs to fermion fields

Fermion mass terms generated through EWSB:

$$m_f = \frac{v}{\sqrt{2}} y_f$$

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} D\psi \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + |D_\mu \phi|^2 - V(\phi) \end{aligned}$$

Complex Yukawa matrices can be diagonalised by rotations in flavour space to obtain physical fermion masses

This however introduces a flavour-violating term in CC interactions with W:

$$\mathcal{L}_{cc} = \frac{g}{\sqrt{2}} (\bar{u}_L \gamma^\mu \underbrace{(V_u^\dagger V_d)}_{V_{CKM}} d_L + \bar{\nu}_L \gamma^\mu \underbrace{(V_\nu^\dagger V_e)}_{\text{Absence of } \nu_R \text{ in SM}} e_L) W_\mu^+ + h.c.$$

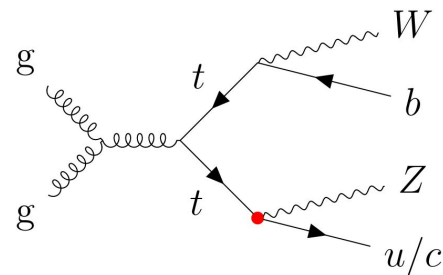
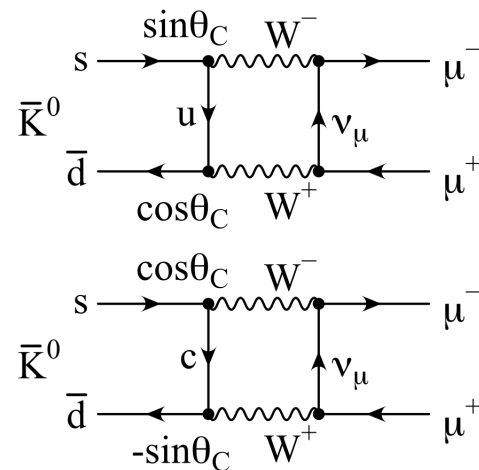
[arXiv:1709.00294](https://arxiv.org/abs/1709.00294)

Absence of ν_R in SM
allows $V_e = V_\nu \rightarrow$ no
LFV in lepton sector

- No LFV in lepton sector
- In quark sector, LFV restricted to charged-current interactions

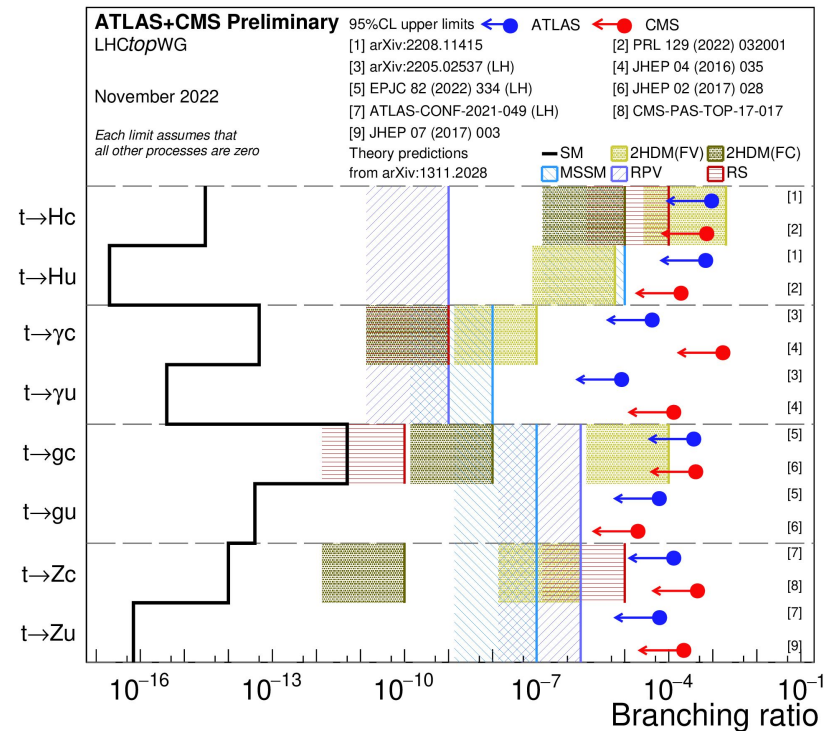
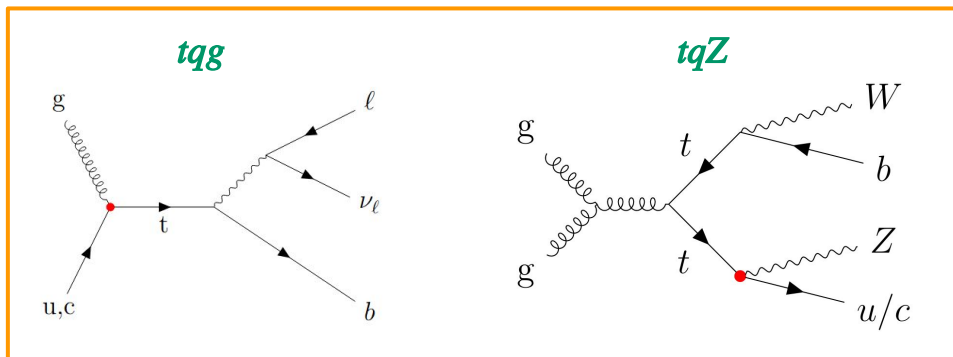
Why search for FCNCs in top interactions?

- Forbidden at tree level in the Standard Model
- Heavily suppressed at loop level through GIM mechanism
- Top FCNC searches performed at LEP, HERA Tevatron
- Large top mass \rightarrow many channels
 - Search in both single top production and top pair decay



Why search for FCNCs in top interactions?

- SM predictions: BR $\sim 10^{-12}$ to 10^{-17}
- Wide variety of BSM models predict FCNCs with rates observable at LHC
- Describe FCNC couplings in terms of EFT framework

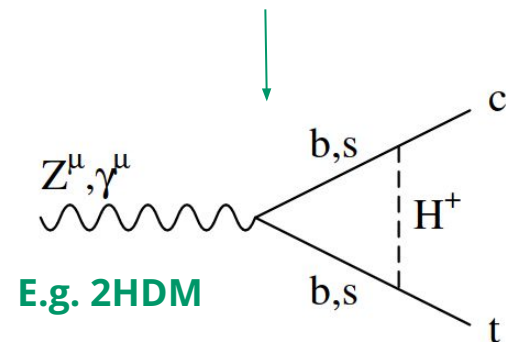
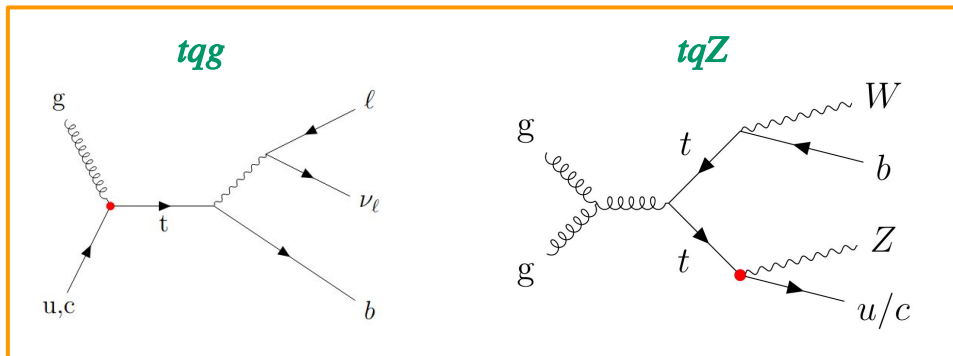


Why search for FCNCs in top interactions?

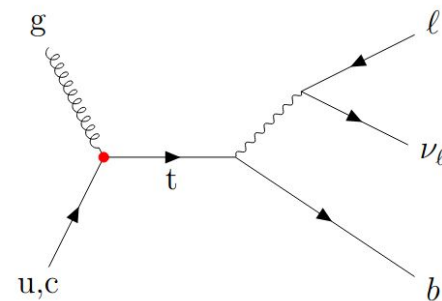
- SM predictions: BR $\sim 10^{-12}$ to 10^{-17}
- Wide variety of BSM models predict FCNCs with rates observable at LHC
- Describe FCNC couplings in terms of EFT framework

Dimension-6 EFT operators sensitive to top FCNCs

$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$
Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$
Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$

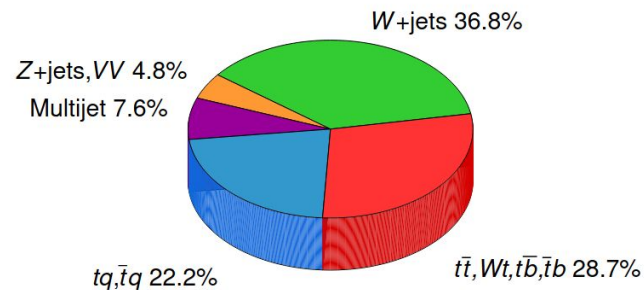


- Search for **single top production** via FCNC tqg vertex ($q = u/c$)
 - Single lepton, 1 b -tagged jet and MET
- Dedicated high-purity b -tagging calibration to suppress $W + b\bar{b}$
- Data-driven estimate for events with fake leptons from multi-jet background
- Neural networks (NNs) used to discriminate between $u+g \rightarrow t$, $c+g \rightarrow t$ and background
 - Kinematic input variables including reconstructed top kinematics



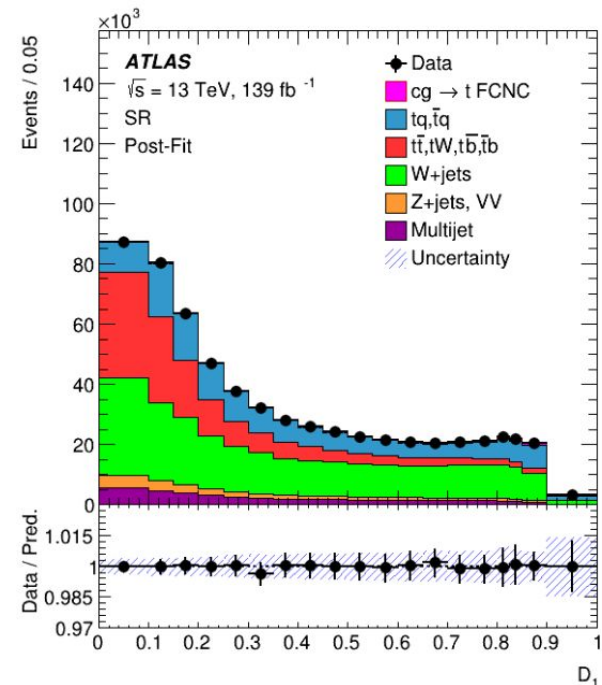
ATLAS
SR

$\sqrt{s}=13$ TeV, 139 fb⁻¹

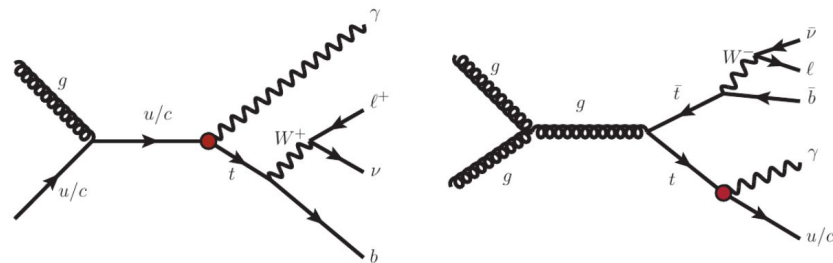


- Profile likelihood fit to NN discriminants in SR
- Dominant uncertainties:
 - *ugt*: MC stat uncertainty and modelling of W+jets
 - *cgt*: parton shower modelling of FCNC *cgt* and SM *tq* processes

$$\left. \begin{aligned}
 \mathcal{B}(t \rightarrow u + g) &< 0.61 \times 10^{-4} \\
 \mathcal{B}(t \rightarrow c + g) &< 3.7 \times 10^{-4} \\
 \frac{|C_{uG}^{ut}|}{\Lambda^2} &< 0.057 \text{ TeV}^{-2} & \frac{|C_{uG}^{ct}|}{\Lambda^2} &< 0.14 \text{ TeV}^{-2}
 \end{aligned} \right\} (95\% \text{ CL})$$



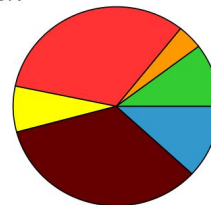
- Search for FCNC $tq\gamma$ in **top production and decay**
 - Single lepton, high $p_T \gamma$, MET
- CRs for main backgrounds with prompt photons ($t\bar{t}\gamma$, $W\gamma$ +jets)
- Data-driven corrections to rate of electron/hadron $\rightarrow \gamma$ fakes



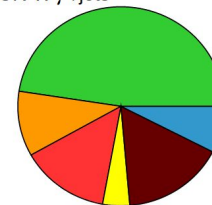
ATLAS Simulation
 $\sqrt{s} = 13 \text{ TeV}$

■ other prompt γ	■ $t\bar{t}\gamma$
■ $h \rightarrow \gamma$ fakes	■ $e \rightarrow \gamma$ fakes
■ $Z\gamma$ +jets	■ $W\gamma$ +jets

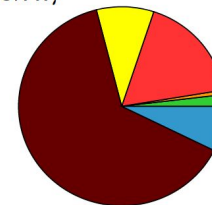
SR



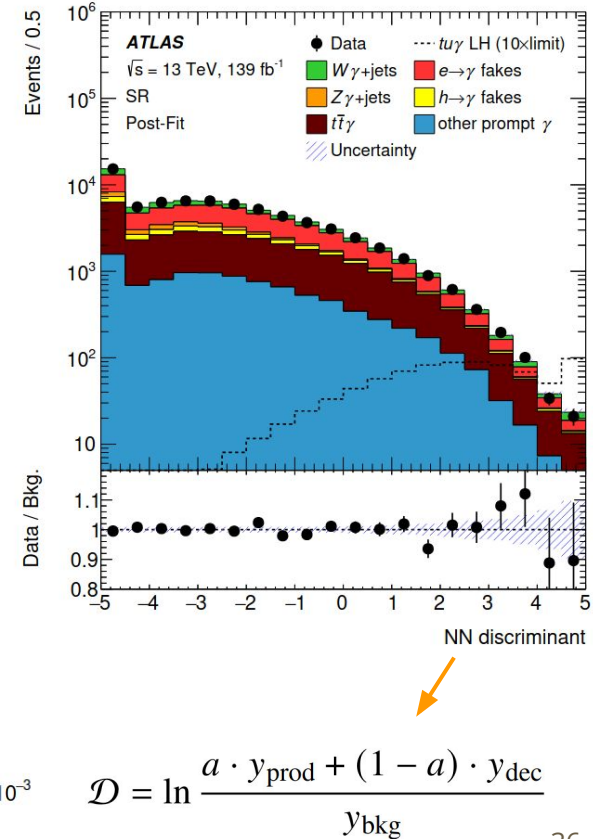
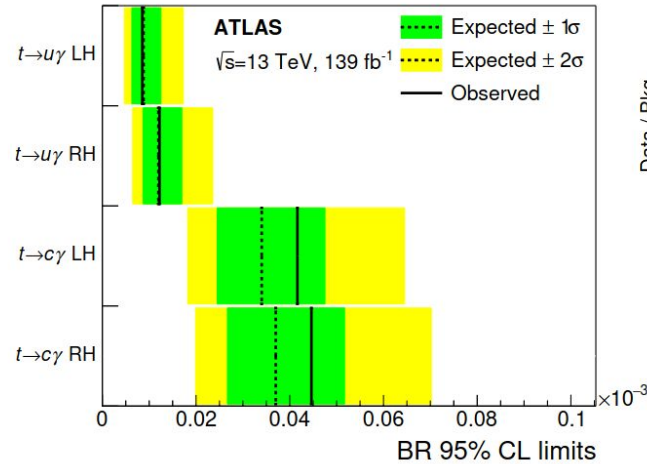
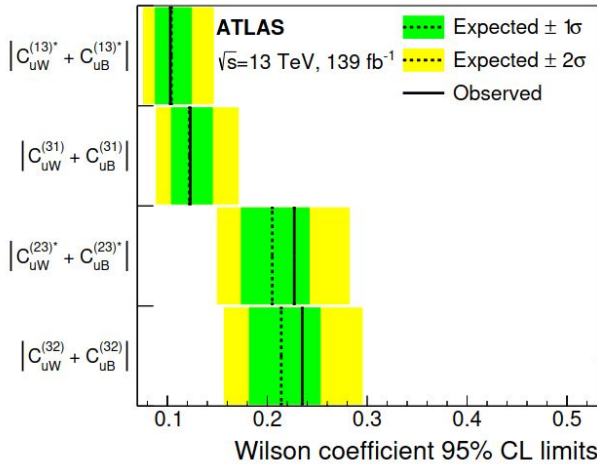
CR $W\gamma$ +jets



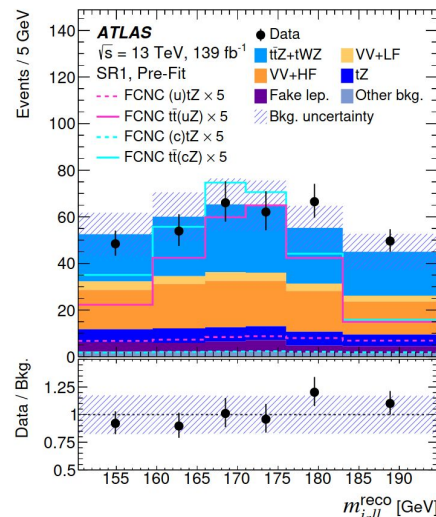
CR $t\bar{t}\gamma$



- Multiclass deep neural networks to split events into two signal modes and background
- Dominant uncertainties:
 - Limited statistics ($t\bar{u}\gamma$), $tq\gamma$ theory cross-section, $h \rightarrow \gamma$ estimate ($tc\gamma$)



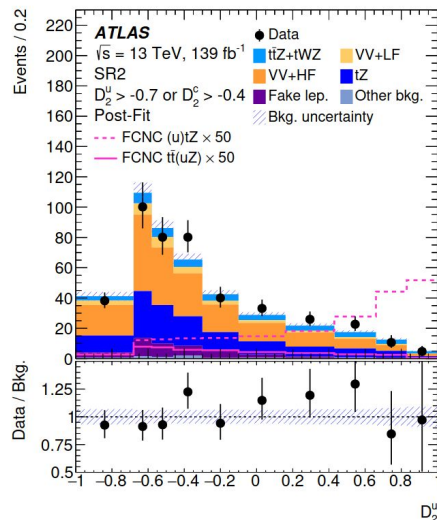
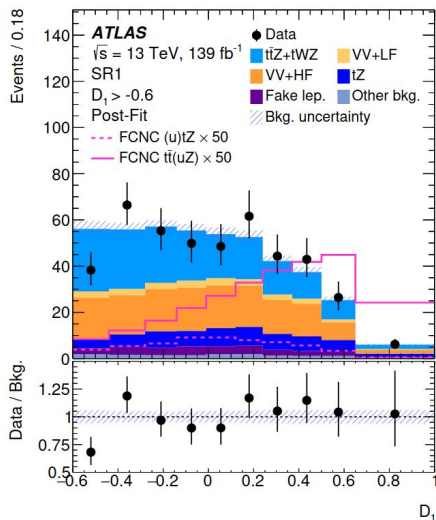
- Search for FCNC tqZ in **top production and decay**
 - Tripleton event selection (*low background channel*)
- Two SRs targeting production and decay processes
 - Split by mass of reconstructed top(s)
- Additional CRs for dominant (diboson, $t\bar{t}Z$) and fake lepton ($t\bar{t}$) backgrounds



Reconstructed top mass assuming $t \rightarrow qZ$ decay

Common selections		
Exactly 3 leptons with $p_T(\ell_1) > 27$ GeV		
≥ 1 OSSF pair, with $ m_{\ell\ell} - m_Z < 15$ GeV		
SR1	SR2	SR2
≥ 2 jets	1 jet	2 jets
1 b -jet	1 b -jet	1 b -jet
–	$m_T(\ell_W, \nu) > 40$ GeV	$m_T(\ell_W, \nu) > 40$ GeV
$ m_{j_a \ell\ell}^{\text{reco}} - m_t < 2\sigma_{t_{\text{FCNC}}}$	–	$ m_{j_a \ell\ell}^{\text{reco}} - m_t > 2\sigma_{t_{\text{FCNC}}}$
–	$ m_{j_b \ell_W \nu}^{\text{reco}} - m_t < 2\sigma_{t_{\text{SM}}}$	$ m_{j_b \ell_W \nu}^{\text{reco}} - m_t < 2\sigma_{t_{\text{SM}}}$

- GBDTs used for S/B discrimination
 - Reconstructed top kinematics provide key inputs
- Dominant uncertainty: limited statistics



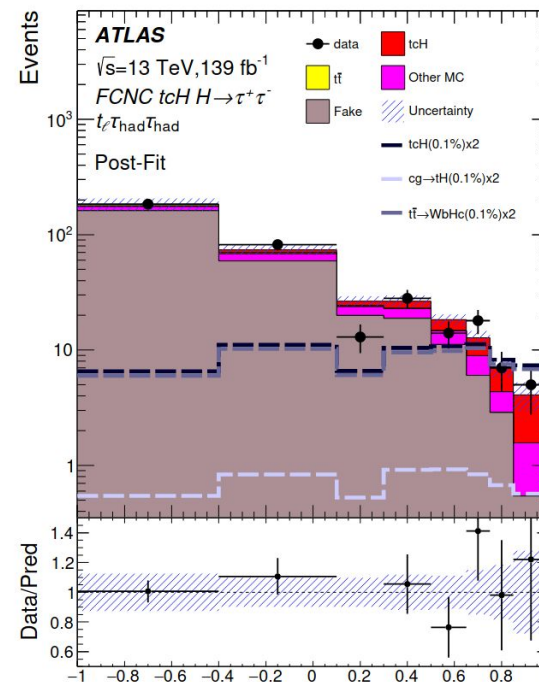
Observable	Vertex	Coupling	Observed	Expected
SRs+CRs				
$\mathcal{B}(t \rightarrow Zq)$	tZu	LH	6.2×10^{-5}	$4.9^{+2.1}_{-1.4} \times 10^{-5}$
$\mathcal{B}(t \rightarrow Zq)$	tZu	RH	6.6×10^{-5}	$5.1^{+2.1}_{-1.4} \times 10^{-5}$
$\mathcal{B}(t \rightarrow Zq)$	tZc	LH	13×10^{-5}	$11^{+5}_{-3} \times 10^{-5}$
$\mathcal{B}(t \rightarrow Zq)$	tZc	RH	12×10^{-5}	$10^{+4}_{-3} \times 10^{-5}$
$ C_{uW}^{(13)*} $ and $ C_{uB}^{(13)*} $	tZu	LH	0.15	$0.13^{+0.03}_{-0.02}$
$ C_{uW}^{(31)} $ and $ C_{uB}^{(31)} $	tZu	RH	0.16	$0.14^{+0.03}_{-0.02}$
$ C_{uW}^{(23)*} $ and $ C_{uB}^{(23)*} $	tZc	LH	0.22	$0.20^{+0.04}_{-0.03}$
$ C_{uW}^{(32)} $ and $ C_{uB}^{(32)} $	tZc	RH	0.21	$0.19^{+0.04}_{-0.03}$

Observable	Vertex	Coupling	Observed	Expected
SR1+CRs				
$\mathcal{B}(t \rightarrow Zq)$	tZu	LH	9.7×10^{-5}	$9.6^{+3.6}_{-2.9} \times 10^{-5}$
$\mathcal{B}(t \rightarrow Zq)$	tZu	RH	9.7×10^{-5}	$9.6^{+3.6}_{-2.9} \times 10^{-5}$
$\mathcal{B}(t \rightarrow Zq)$	tZc	LH	9.7×10^{-5}	$9.6^{+3.6}_{-2.9} \times 10^{-5}$
$\mathcal{B}(t \rightarrow Zq)$	tZc	RH	9.0×10^{-5}	$6.6^{+2.9}_{-1.8} \times 10^{-5}$

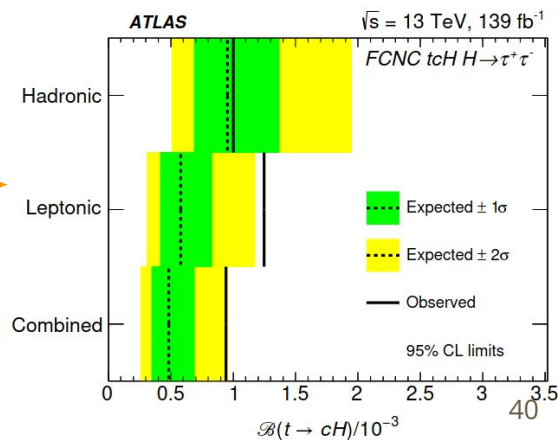
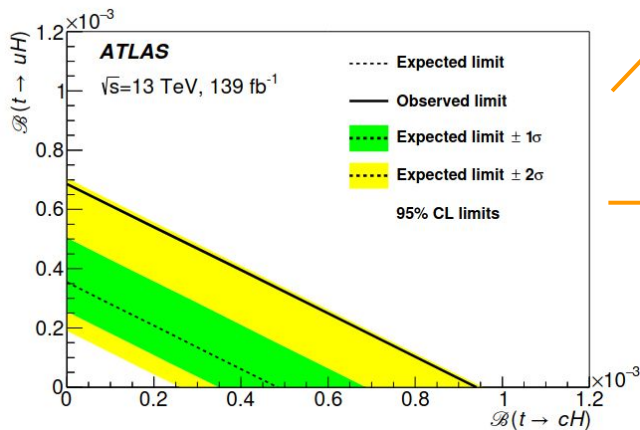
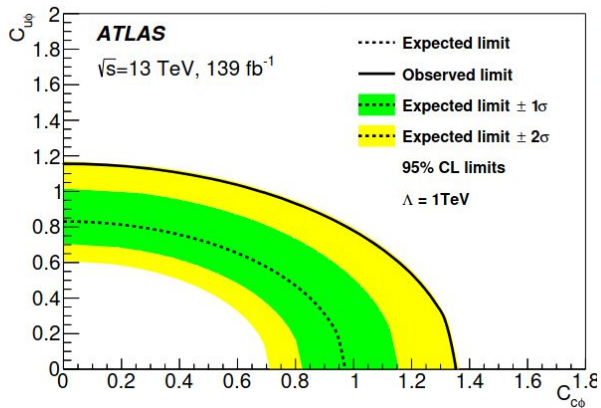
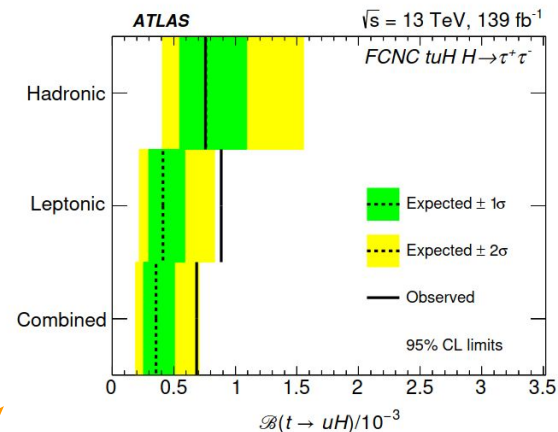
Sensitive to same EFT operators as $tq\gamma$

- Search for FCNC tqH in **top production and decay**
 - **Require $H \rightarrow \tau\tau$ decay**
- Many SRs targeting different top and τ -lepton decays channels
- Data-driven background estimates for fake τ_{had} and fake/non-prompt light leptons
- BDTs used for S/B discrimination
 - Rely on event kinematics for training (including kinematic reconstruction where possible)

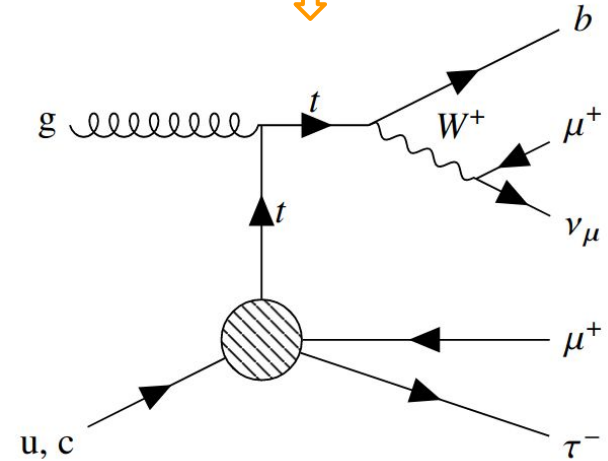
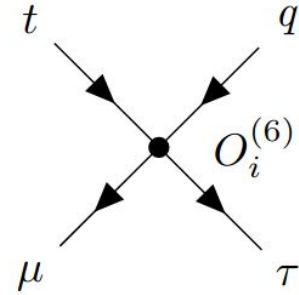
BDT discriminant in most sensitive SR



- Profile likelihood fit to 7 SRs and 6 CRs
- Observe slight excess (2.3σ) above expected background
- Dominant uncertainties: statistics, MC statistics, fake estimation



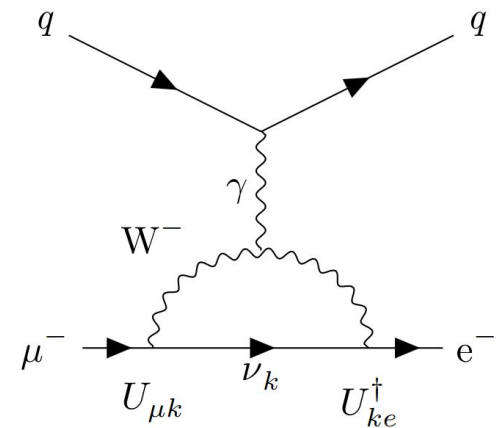
Search for CLFV interactions of the top quark



- Neutrino oscillations \rightarrow LFV in lepton sector but far beyond any experimental sensitivity

$$\text{BR}(\mu \rightarrow e\gamma) \simeq \frac{\Gamma(\mu \rightarrow e\gamma)}{\Gamma(\mu \rightarrow e\nu\bar{\nu})} = \frac{3\alpha}{32\pi} \left| \sum_{k=1,3} \frac{U_{\mu k} U_{ek}^* m_{\nu_k}^2}{M_W^2} \right|^2$$

[arXiv:1709.00294](https://arxiv.org/abs/1709.00294)



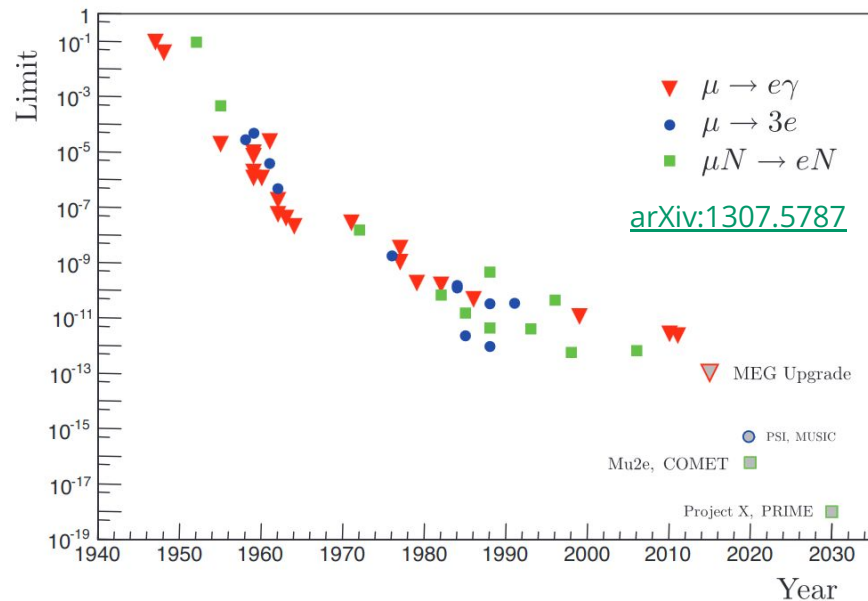
- New physics which introduces additional terms involving lepton fields in Lagrangian will in general lead to LFV

SUSY
LQs
2HDMs

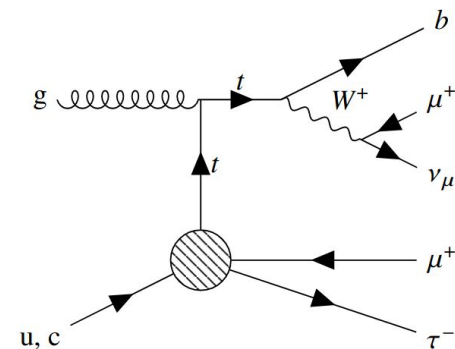
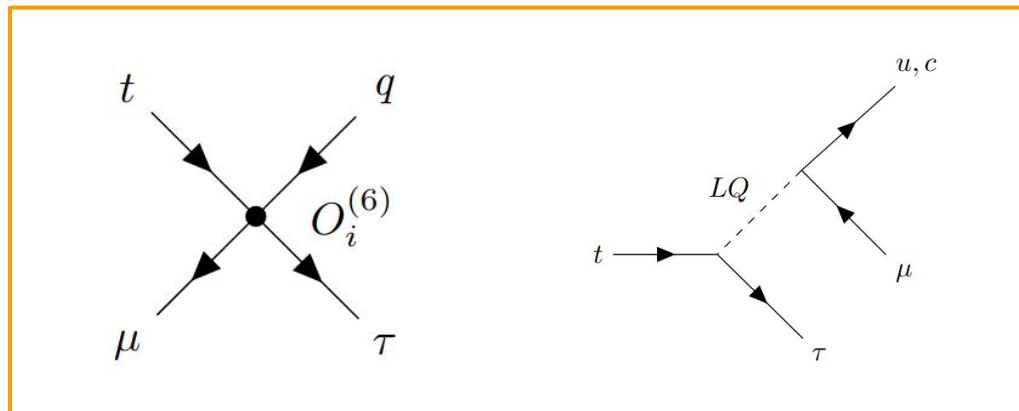
Why search for CLFV in top quark interactions?

- Best sensitivity typically in muon channels
 - Best CLFV limits from MEG:
 $B(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ (90% CL) *
- Models predicting CLFV in muons also apply to taus, often additionally enhanced due to larger mass (e.g. LQs)
- **Searches for LFV involving taus, tops, H, Z require colliders**

History of $\mu \rightarrow e\gamma$, $\mu N \rightarrow eN$, and $\mu \rightarrow 3e$



* [Eur. Phys. J. C 76, 434 \(2016\)](#) 43

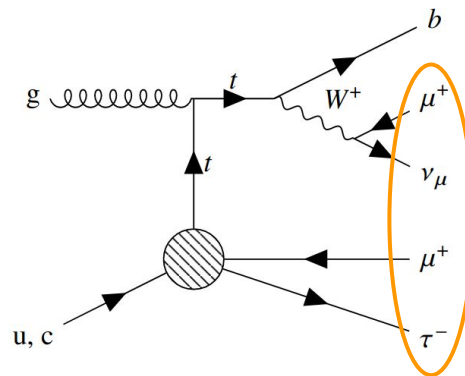


- First direct search for $t\mu\tau q$ coupling
- Complements searches for $te\mu q$ coupling by ATLAS ([arXiv:1809.09048](https://arxiv.org/abs/1809.09048)) and CMS ([JHEP 06 \(2022\) 082](https://arxiv.org/abs/2206.082), [CMS PAS TOP-22-005](https://arxiv.org/abs/2206.005))

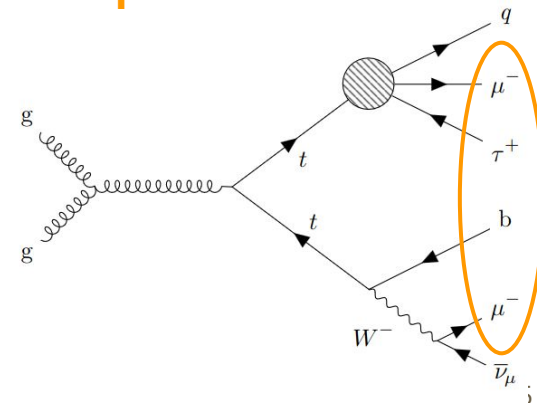
CLFV in top quark interactions

(ATLAS-CONF-2023-001)

- Signal includes single top production and top quark pair decay
- Tripleton selection including *hadronic taus*
- Same-sign muons in SR → significant background reduction

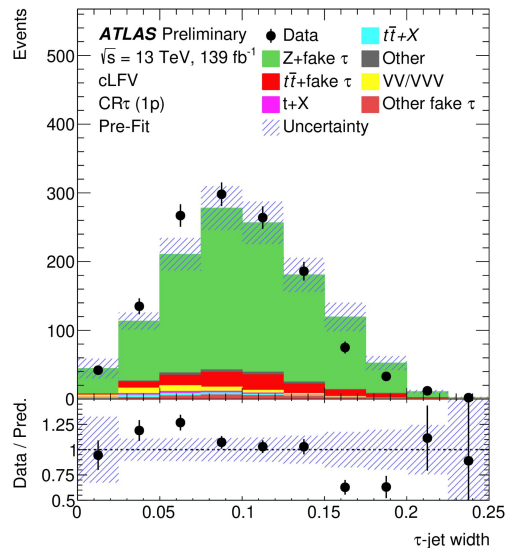


Tripleton selection

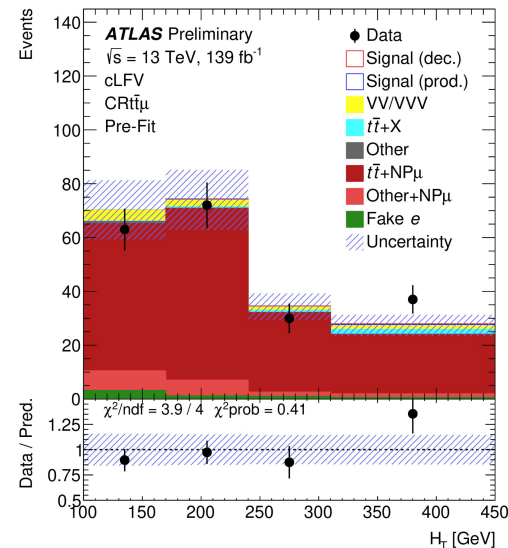


	SR1	SR2	CR τ	CR $t\bar{t}\mu$
Lepton flavour		$2\mu 1\tau_{\text{had-vis}}$		$2\mu 1e (\ell_3 = \mu)$
N_{jets}	≥ 2	1	≥ 2	≥ 2
$N_{b\text{-tags}}$	1	1	1	≤ 2
Muon p_T cut	$> 15 \text{ GeV}$	$> 15 \text{ GeV}$	$> 15 \text{ GeV}$	$> 10 \text{ GeV}$
Lowest p_T muon selection	<i>Tight</i>	<i>Tight</i>	<i>Tight</i>	<i>Loose</i>
Muon charges	SS	SS	OS	-
$ m_{\mu\mu}^{OS} - M_Z $	-	-	$< 10 \text{ GeV}$	$> 10 \text{ GeV}$

- Data-driven background estimations for fake background processes
- Scale factors to correct rate of fake τ_{had} background
- Correct normalisation of non-prompt background in fit



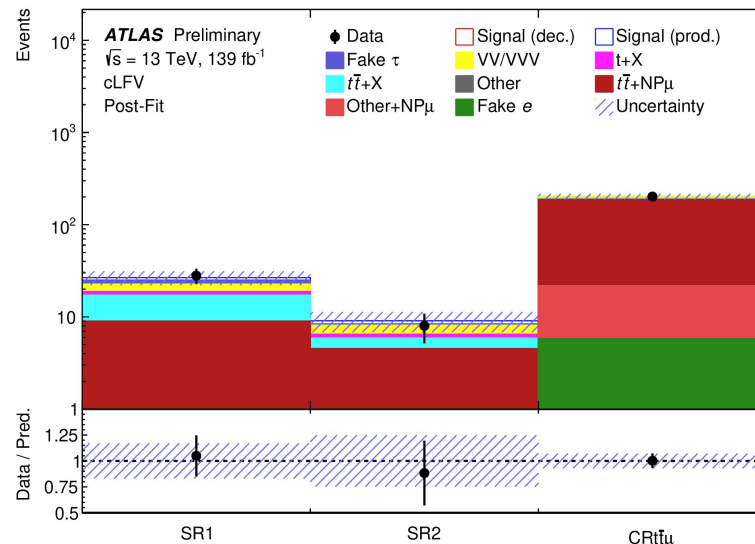
Fake τ_{had} control region



Non-prompt μ control region

- Profile likelihood fit across two SRs and non-prompt muon CR
- Good agreement between data and background-only model
- Statistically limited

	Exclusion limit $B(t \rightarrow \mu\tau q)$	
	Stat. only	All systematics
Expected	7.57×10^{-7}	9.82×10^{-7}
Observed	9.43×10^{-7}	10.8×10^{-7}



- Stringent limits on Wilson coefficients corresponding to 2Q2L operators
 - Improve upon the previous results by up to a factor of 51

$$\Gamma(t \rightarrow \ell_i^+ \ell_j^- qk) = \frac{m_t}{6144\pi^3} \left(\frac{m_t}{\Lambda}\right)^4 \left\{ 4|c_{lq}^{-(ijk3)}|^2 + 4|c_{eq}^{(ijk3)}|^2 + 4|c_{lu}^{(ijk3)}|^2 + 4|c_{eu}^{(ijk3)}|^2 + |c_{lequ}^{1(jik3)}|^2 + |c_{lequ}^{1(ij3k)}|^2 + 48|c_{lequ}^{3(jik3)}|^2 + 48|c_{lequ}^{3(ij3k)}|^2 \right\}$$

	95% CL upper limits on Wilson coefficients c/Λ^2 [TeV ⁻²]							
	$c_{lq}^{-(ijk3)}$	$c_{eq}^{(ijk3)}$	$c_{lu}^{(ijk3)}$	$c_{eu}^{(ijk3)}$	$c_{lequ}^{1(ij3k)}$	$c_{lequ}^{1(ij3k)}$	$c_{lequ}^{3(ij3k)}$	$c_{lequ}^{3(ij3k)}$
Previous (u)	12	12	12	12	26	26	3.4	3.4
ATLAS expected (u)	0.47	0.44	0.43	0.46	0.49	0.49	0.11	0.11
ATLAS observed (u)	0.49	0.47	0.46	0.48	0.51	0.51	0.11	0.11
Previous (c)	14	14	14	14	29	29	3.7	3.7
ATLAS expected (c)	1.6	1.6	1.5	1.6	1.8	1.8	0.35	0.35
ATLAS observed (c)	1.7	1.6	1.6	1.6	1.9	1.9	0.37	0.37

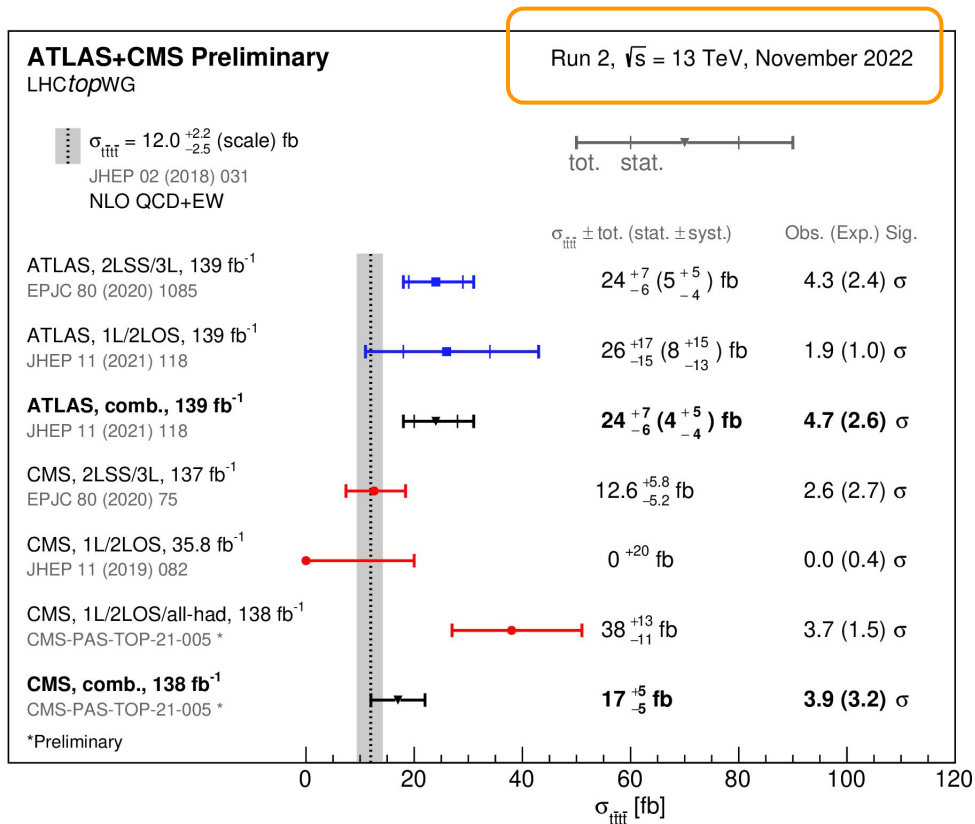
Previous limits and equation from [JHEP04 \(2019\) 014](#) (reinterpretation of [JHEP07 \(2018\) 176](#))

Concluding remarks

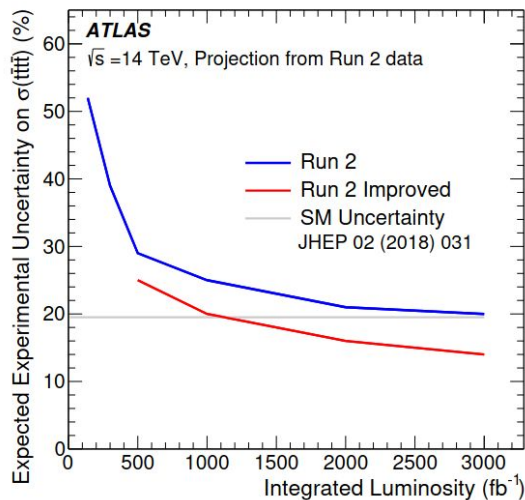
- Many exciting Run 2 rare top results!
 - Observation of four top production
 - Diverse BSM couplings programme
- No evidence for new physics as of yet...
 - In many cases setting most stringent limits on these branching ratios to date
- Many measurements statistically limited → significant improvements with Run 3 and beyond
- Modelling of signal and background is frequently a limiting systematic
 - Much work is going into improving modelling of generators and theoretical predictions

BACKUP

History of $4t$ production measurements at the LHC



Both ATLAS and CMS now report observation of this process

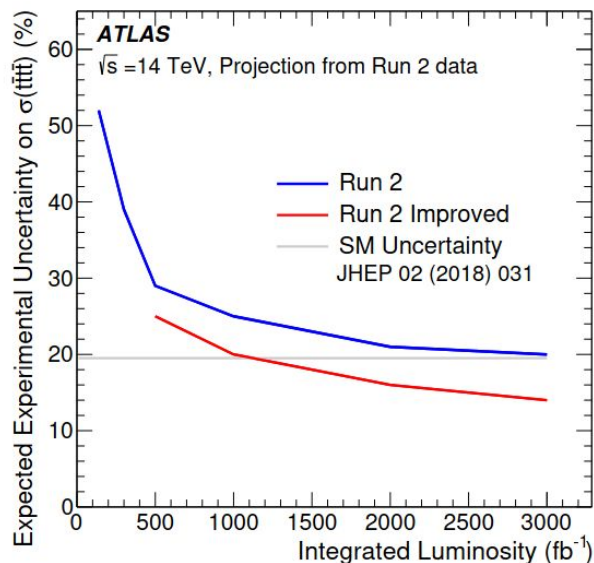


Study into HL-LHC sensitivity - [ATL-PHYS-PUB-2022-004](#)

Consider conservative/optimistic systematic reductions with 3000 ifb at 14 TeV in 2 ℓ SS/3 ℓ channel

Expected significance (wrt B-only hypothesis): 4.2-6.4 σ

Expected uncertainty on cross section: 14%-20%



Integrated luminosity (fb^{-1})	“Run 2”	“Run 2 Improved”
500	3.5	4.1
1000	3.9	4.9
2000	4.0	5.9
3000	4.2	6.4

Uncertainty source	Treatment in the “Run 2 Improved” model
Signal modelling	
$t\bar{t}t\bar{t}$ cross section	Half of Run 2
$t\bar{t}t\bar{t}$ modelling	Half of Run 2
Background modelling	
$t\bar{t}W$ +jets modelling	
Renormalisation and factorisation scales	Half of Run 2
Generator	Half of Run 2
Jets multiplicity modelling	Scaled by Run 2 pulls
Additional heavy flavour jets	Scaled by luminosity
$t\bar{t}t\bar{t}$ modelling	
Cross section	Half of Run 2
Additional heavy flavour jets	Scaled by luminosity
Non-prompt leptons modelling	Scaled by luminosity
$t\bar{t}H$ +jets and $t\bar{t}Z$ +jets modelling	
Cross section	Half of Run 2
Renormalisation and factorisation scales	Half of Run 2
Generator	Half of Run 2
PDF	Half of Run 2
Additional heavy flavour jets	Scaled by luminosity
Other background modelling	
Cross section	Half of Run 2
Additional heavy flavour jets	Scaled by luminosity
Charge misassignment	Same as Run 2
Template fit shape uncertainties	
Mat. Conv., γ^* , and HF non-prompt leptons	Scaled by luminosity
Other fake leptons	Half of Run 2
Additional heavy flavour jets	Half of Run 2
Instrumental	
Jet uncertainties	Same as Run 2
Jet flavour tagging (light-flavour jets)	Half of Run 2
Luminosity	Same as Run 2
Jet flavour tagging (b -jets)	Half of Run 2
Jet flavour tagging (c -jets)	Half of Run 2
Other experimental uncertainties	Same as Run 2

Four top production - background estimation

Fake/non-prompt background	NF _{Mat. Conv.}	NF _{Low m_{γ^*}}	NF _{HF e}	NF _{HF μ}
Value	$1.80^{+0.47}_{-0.41}$	$1.08^{+0.37}_{-0.31}$	$0.66^{+0.75}_{-0.46}$	$1.27^{+0.53}_{-0.46}$

$$\text{NF}_{t\bar{t}W(j)} = \text{NF}_{t\bar{t}W^+(4\text{jet})} \times \prod_{j'=4}^{j'-1} \left[a_0 + \frac{a_1}{1 + (j' - 4)} \right] + \text{NF}_{t\bar{t}W^-(4\text{jet})} \times \prod_{j'=4}^{j'-1} \left[a_0 + \frac{a_1}{1 + (j' - 4)} \right]$$

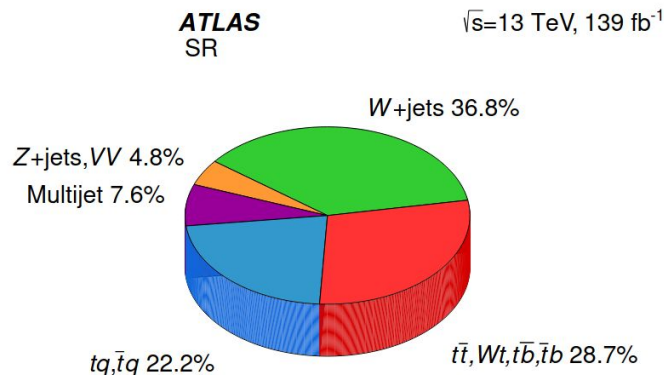
$t\bar{t}W$ background	a_0	a_1	NF _{$t\bar{t}W^+(4\text{jet})$}	NF _{$t\bar{t}W^-(4\text{jet})$}
Value	0.51 ± 0.10	$0.22^{+0.25}_{-0.22}$	$1.27^{+0.25}_{-0.22}$	$1.11^{+0.31}_{-0.28}$

Observable	Common requirements
$n_{\text{Tight}}(e) + n_{\text{Medium}}(\mu)$	= 1
$n_{\text{Loose}}(e) + n_{\text{Loose}}(\mu)$	= 1
$E_{\text{T}}^{\text{miss}}$	> 30 GeV
$m_{\text{T}}(W)$	> 50 GeV
$n(j)$	≥ 1
$p_{\text{T}}(\ell)$	$> 50 \text{ GeV} \cdot \left(1 - \frac{\pi - \Delta\phi(j_1, \ell) }{\pi - 1}\right)$

	Analysis regions			
	SR	W+jets VR	$t\bar{t}$ VR	tq VR
$n(\eta(j) < 2.5)$	= 1	= 1	= 2	= 1
$n(b)$	= 1	= 1	= 2	= 1
ϵ_b	30%	60% (veto 30%)	30%	30%
$n(\eta(j) > 2.5)$	≥ 0	≥ 0	≥ 0	= 1
$D_{1(2)}$	-	$0.3 < D_{1(2)} < 0.6$	-	$0.2 < D_{1(2)} < 0.4$

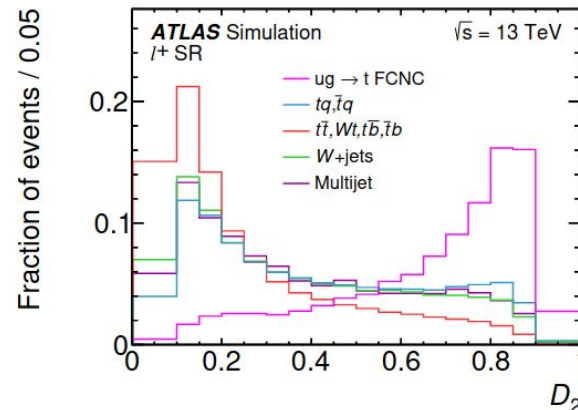
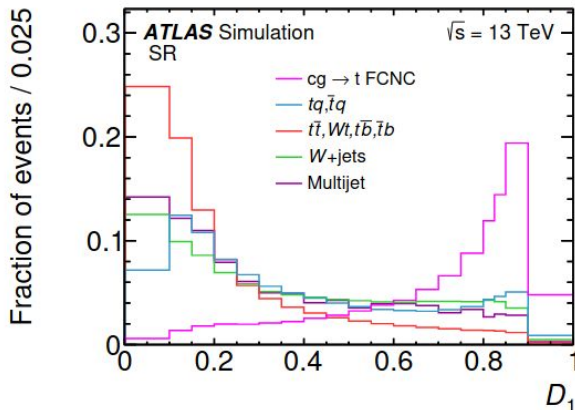
Fake estimation for events with fake leptons from multi-jet background

- e: shape from dijet MC ([jet electron method](#))
- μ : shape from data enriched in non-prompt muons
- Maximum likelihood fit to $E_{\text{miss}}^{\text{T}}(m_{\text{T}})$ distribution in e (μ) channel to correct normalisation



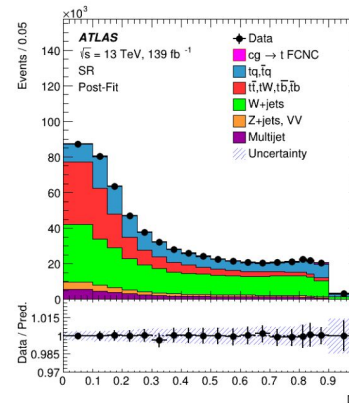
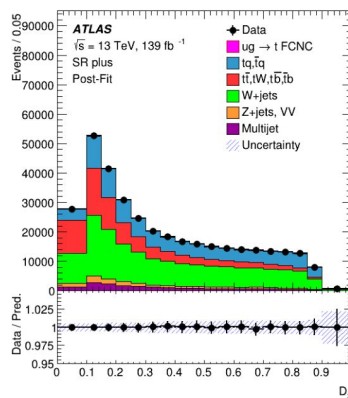
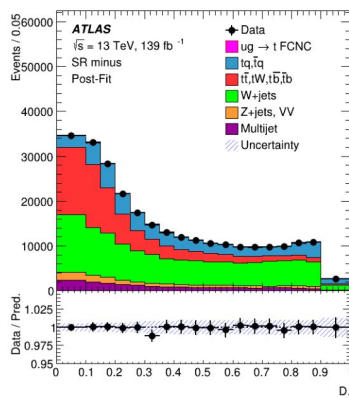
- Two NNs to discriminate S/B
 - D_1 trained only on $c+g \rightarrow t$ (incl. $\bar{c}+g \rightarrow \bar{t}$) - optimised for sea quark production
 - D_2 trained only on $u+g \rightarrow t$ (excl. $\bar{u}+g \rightarrow \bar{t}$) - optimised for valence quark production
 - Multijet background excluded from NN training
- Use D_1 in $cg\bar{t}$ analysis and ℓ^- channel of ugt analysis
- Use D_2 in ℓ^+ channel of ugt analysis

NN output discriminant distribution for $cg\bar{t}$ analysis



NN output discriminant distribution for ugt analysis

NN
discriminant
distributions
in SRs



Scenario	Description	$\mathcal{B}_{95}^{\text{exp}}(t \rightarrow u + g)$	$\mathcal{B}_{95}^{\text{exp}}(t \rightarrow c + g)$
(1)	Data statistical only	1.1×10^{-5}	2.4×10^{-5}
(2)	Experimental uncertainties also	3.1×10^{-5}	12×10^{-5}
(3)	All uncertainties except MC statistical	3.9×10^{-5}	18×10^{-5}
(4)	All uncertainties	4.9×10^{-5}	20×10^{-5}

Object	SR	CR $t\bar{t}\gamma$	CR $W\gamma$ +jets
Photon ($p_T > 20$ GeV)		= 1	
Lepton ($p_T > 27$ GeV)		= 1	
E_T^{miss}		> 30 GeV	
Jets ($p_T > 25$ GeV)	≥ 1	≥ 4	≥ 1
b -tagged jets (60% WP)	= 1	–	= 0
b -tagged jets (70% WP)	= 1	≥ 1	= 0
b -tagged jets (77% WP)	= 1	≥ 2	= 1
$m(e, \gamma)$	–	–	$\notin [80, 100]$ GeV

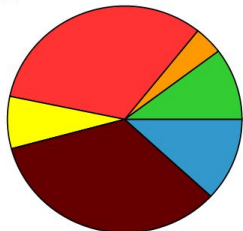
Data-driven corrections to rate of $e/h \rightarrow \gamma$ fakes

- $e \rightarrow \gamma$: correct rate of $Z \rightarrow e\gamma$ to $Z \rightarrow ee$ in bins of photon η and reconstruction type
- $h \rightarrow \gamma$: ABCD method using modified photon ID & isolation; binning in photon p_T , η and reconstruction type

ATLAS Simulation
 $\sqrt{s} = 13$ TeV



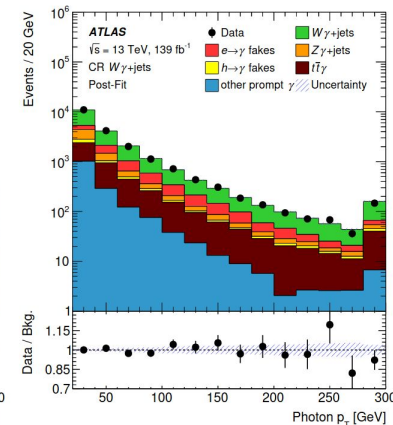
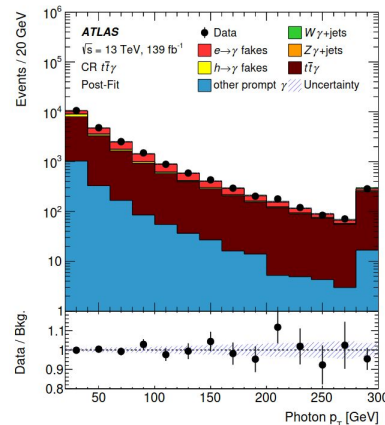
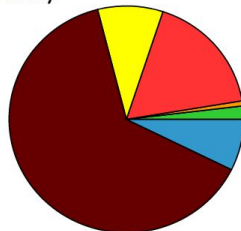
SR



CR $W\gamma$ +jets



CR $t\bar{t}\gamma$

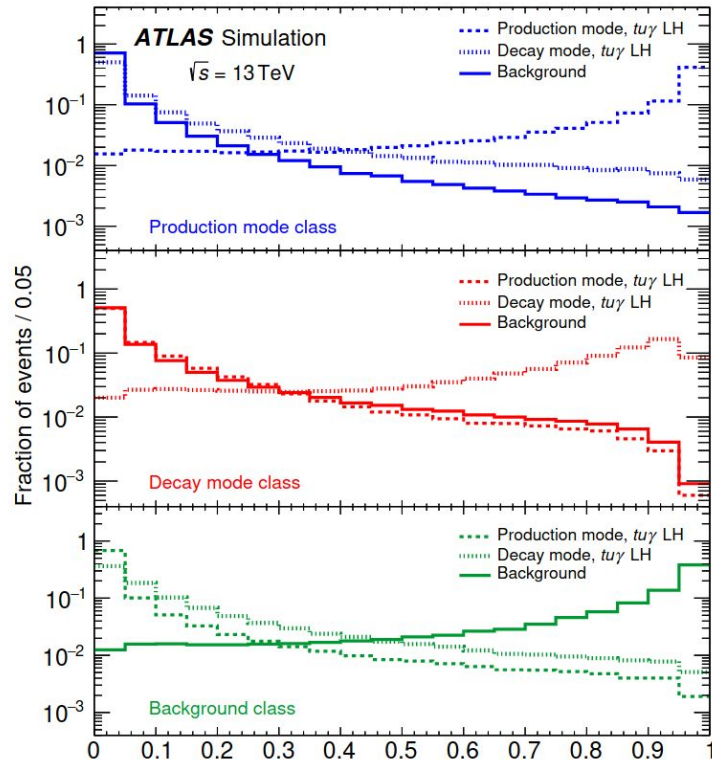
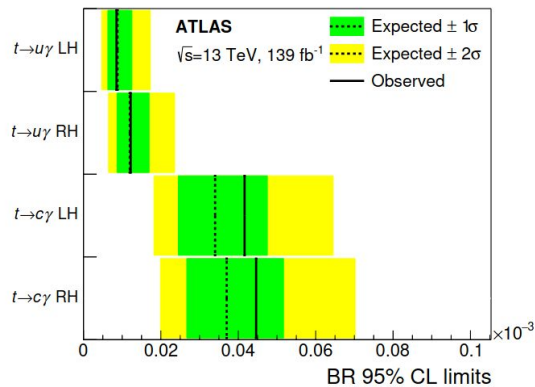
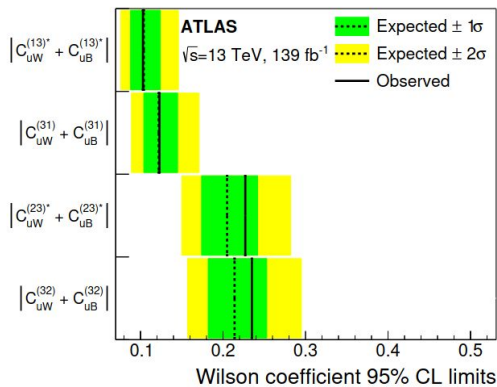


Data / Bkg.

Data / Bkg.

Photon p_T [GeV]

Photon p_T [GeV]



Effective coupling	Coefficient limits		Coupling	BR limits [10^{-5}]	
	Expected	Observed		Expected	Observed
$ C_{uW}^{(13)*} + C_{uB}^{(13)*} $	$0.104^{+0.020}_{-0.016}$	0.103	$t \rightarrow u\gamma$ LH	$0.88^{+0.37}_{-0.25}$	0.85
$ C_{uW}^{(31)} + C_{uB}^{(31)} $	$0.122^{+0.023}_{-0.018}$	0.123	$t \rightarrow u\gamma$ RH	$1.20^{+0.50}_{-0.33}$	1.22
$ C_{uW}^{(23)*} + C_{uB}^{(23)*} $	$0.205^{+0.037}_{-0.031}$	0.227	$t \rightarrow c\gamma$ LH	$3.40^{+1.35}_{-0.95}$	4.16
$ C_{uW}^{(32)} + C_{uB}^{(32)} $	$0.214^{+0.039}_{-0.032}$	0.235	$t \rightarrow c\gamma$ RH	$3.70^{+1.47}_{-1.03}$	4.46

Common selections		
Exactly 3 leptons with $p_T(\ell_1) > 27$ GeV		
≥ 1 OSSF pair, with $ m_{\ell\ell} - m_Z < 15$ GeV		
SR1	SR2	
≥ 2 jets	1 jet	2 jets
1 b -jet	1 b -jet	1 b -jet
-	$m_T(\ell_W, \nu) > 40$ GeV	$m_T(\ell_W, \nu) > 40$ GeV
$ m_{j_a^{\text{reco}}^{\ell\ell}} - m_t < 2\sigma_{t_{\text{FCNC}}}$	-	$ m_{j_a^{\text{reco}}^{\ell\ell}} - m_t > 2\sigma_{t_{\text{FCNC}}}$
-	$ m_{j_b^{\text{reco}}^{\ell_W\nu}} - m_t < 2\sigma_{t_{\text{SM}}}$	$ m_{j_b^{\text{reco}}^{\ell_W\nu}} - m_t < 2\sigma_{t_{\text{SM}}}$

- GBDTs used for S/B discrimination
 - Reconstructed top kinematics provide key inputs
 - Separate training for each SR based on dominant FCNC process

Common selections			
Exactly 3 leptons with $p_T(\ell_1) > 27$ GeV			
$t\bar{t}$ CR	$t\bar{t}Z$ CR	Side-band CR1	Side-band CR2
≥ 1 OS pair, no OSSF	≥ 1 OSSF pair	≥ 1 OSSF pair	≥ 1 OSSF pair
-	with $ m_{\ell\ell} - m_Z < 15$ GeV	with $ m_{\ell\ell} - m_Z < 15$ GeV	with $ m_{\ell\ell} - m_Z < 15$ GeV
-	-	-	$m_T(\ell_W, \nu) > 40$ GeV
≥ 1 jet	≥ 4 jets	≥ 2 jets	1 jet
1 b -jet	2 b -jets	1 b -jet	1 b -jet
-	-	$ m_{j_a^{\text{reco}}^{\ell\ell}} - m_t > 2\sigma_{t_{\text{FCNC}}}$	-
-	-	$ m_{j_b^{\text{reco}}^{\ell_W\nu}} - m_t > 2\sigma_{t_{\text{SM}}}$	$ m_{j_b^{\text{reco}}^{\ell_W\nu}} - m_t > 2\sigma_{t_{\text{SM}}}$

Requirement	Leptonic channels			Hadronic channel
	$t_h \tau_{lep} \tau_{had}$	$t_\ell \tau_{had} \tau_{had}$	$t_\ell \tau_{had}$	$t_h \tau_{had} \tau_{had}$
Trigger		single-lepton trigger		di- τ trigger
Leptons		=1 isolated e or μ		=0 isolated e or μ
τ_{had}	=1 τ_{had}	=2 τ_{had}	=1 τ_{had}	=2 τ_{had}
Electric charge (Q)	$Q_\ell \times Q_{\tau_{had1}} = -1$	$Q_{\tau_{had1}} \times Q_{\tau_{had2}} = -1$	$Q_\ell \times Q_{\tau_{had1}} = 1$	$Q_{\tau_{had1}} \times Q_{\tau_{had2}} = -1$
Jets	≥ 3 jets	≥ 1 jets	≥ 2 jets	≥ 3 jets
b -tagging		=1 b -jets		=1 b -jets

	Regions	b -jets	Light-flavour jets	Leptons	Hadronic τ decays	Charge
SR	$t_\ell \tau_{had} \tau_{had}$	1	≥ 0	1	2	$\tau_{had} \tau_{had}$ OS
	$t_\ell \tau_{had} 1j$	1	1	1	1	$t_\ell \tau_{had}$ SS
	$t_\ell \tau_{had} 2j$	1	2	1	1	$t_\ell \tau_{had}$ SS
	$t_h \tau_{lep} \tau_{had} 2j$	1	2	1	1	$\tau_{lep} \tau_{had}$ OS
	$t_h \tau_{lep} \tau_{had} 3j$	1	≥ 3	1	1	$\tau_{lep} \tau_{had}$ OS
	$t_h \tau_{had} \tau_{had} 2j$	1	2	0	2	$\tau_{had} \tau_{had}$ OS
VR	$t_h \tau_{had} \tau_{had} 3j$	1	≥ 3	0	2	$\tau_{had} \tau_{had}$ OS
	$t_\ell \tau_{had} \tau_{had} SS$	1	≥ 0	1	2	$\tau_{had} \tau_{had}$ SS
CRtt	$t_h \tau_{had} \tau_{had} 3j SS$	1	≥ 3	0	2	$\tau_{had} \tau_{had}$ SS
	$t_\ell t_\ell 1b \tau_{had}$	1	≥ 0	2	1	$t_\ell t_\ell$ OS
	$t_\ell t_\ell 2b \tau_{had}$	2	≥ 0	2	1	$t_\ell t_\ell$ OS
	$t_\ell t_h 2b \tau_{had} 2j SS$	2	2	1	1	$t_\ell \tau_{had}$ SS
	$t_\ell t_h 2b \tau_{had} 2j OS$	2	2	1	1	$t_\ell \tau_{had}$ OS
	$t_\ell t_h 2b \tau_{had} 3j SS$	2	≥ 3	1	1	$t_\ell \tau_{had}$ SS
	$t_\ell t_h 2b \tau_{had} 3j OS$	2	≥ 3	1	1	$t_\ell \tau_{had}$ OS

Signal Region	$t \rightarrow cH$			$t \rightarrow uH$		
	95% CL upper limit [10^{-3}]	Significance	\mathcal{B} [10^{-3}]	95% CL upper limit [10^{-3}]	Significance	\mathcal{B} [10^{-3}]
	Observed (Expected)			Observed (Expected)		
$t_h \tau_{\text{had}} \tau_{\text{had}}^{-2j}$	1.80 (2.72 ^{+1.18} _{-0.76})	-0.96 (0.78)	-1.03 ^{+1.03} _{-1.03}	1.07 (1.60 ^{+0.71} _{-0.45})	-0.90 (1.31)	-0.55 ^{+0.58} _{-0.58}
$t_h \tau_{\text{had}} \tau_{\text{had}}^{-3j}$	1.14 (1.02 ^{+0.45} _{-0.29})	0.34 (1.87)	0.16 ^{+0.47} _{-0.47}	0.97 (0.86 ^{+0.38} _{-0.24})	0.36 (2.25)	0.14 ^{+0.40} _{-0.40}
Hadronic combination	1.00 (0.95 ^{+0.42} _{-0.27})	0.26 (1.99)	0.11 ^{+0.43} _{-0.43}	0.76 (0.76 ^{+0.33} _{-0.21})	0.12 (2.52)	0.04 ^{+0.34} _{-0.34}
$t_\ell \tau_{\text{had}}^{-2j}$	4.77 (4.23 ^{+1.72} _{-1.18})	0.41 (0.47)	0.85 ^{+2.06} _{-2.06}	3.84 (3.48 ^{+1.42} _{-0.97})	0.36 (0.58)	0.61 ^{+1.68} _{-1.68}
$t_\ell \tau_{\text{had}}^{-1j}$	3.80 (3.56 ^{+1.51} _{-0.99})	0.22 (0.58)	0.36 ^{+1.70} _{-1.70}	2.98 (2.78 ^{+1.17} _{-0.78})	0.22 (0.73)	0.29 ^{+1.33} _{-1.33}
$t_h \tau_{\text{lep}} \tau_{\text{had}}^{-2j}$	4.71 (5.71 ^{+2.68} _{-1.60})	-0.52 (0.38)	-1.36 ^{+2.56} _{-2.56}	2.50 (2.97 ^{+1.25} _{-0.83})	-0.47 (0.70)	-0.66 ^{+1.38} _{-1.38}
$t_h \tau_{\text{lep}} \tau_{\text{had}}^{-3j}$	2.71 (2.71 ^{+1.25} _{-0.76})	-0.03 (0.77)	-0.03 ^{+1.26} _{-1.26}	2.02 (2.03 ^{+0.86} _{-0.57})	-0.05 (0.99)	-0.03 ^{+0.98} _{-0.98}
$t_\ell \tau_{\text{had}} \tau_{\text{had}}$	1.35 (0.61 ^{+0.27} _{-0.17})	2.64 (3.31)	0.74 ^{+0.33} _{-0.33}	0.97 (0.44 ^{+0.19} _{-0.12})	2.64 (4.38)	0.53 ^{+0.24} _{-0.24}
Leptonic combination	1.25 (0.58 ^{+0.25} _{-0.16})	2.61 (3.46)	0.69 ^{+0.31} _{-0.31}	0.88 (0.41 ^{+0.18} _{-0.11})	2.60 (4.62)	0.49 ^{+0.22} _{-0.22}
Combination	0.94 (0.48 ^{+0.20} _{-0.14})	2.34 (4.02)	0.51 ^{+0.24} _{-0.24}	0.69 (0.35 ^{+0.15} _{-0.10})	2.31 (5.18)	0.37 ^{+0.18} _{-0.18}

Preselection:	
Number of leptons	$N_\ell = 3, p_T > 10 \text{ GeV}, \eta < 2.5$
Leading muon / electron p_T	$p_T > 27 \text{ GeV}$
Trigger matching	≥ 1 trigger-matched muon / electron
Sum of lepton charges	$\sum q_i = \pm 1$

	SR1	SR2	CRτ	CR$t\bar{t}\mu$
Lepton flavour		$2\mu 1\tau_{\text{had-vis}}$		$2\mu 1e (\ell_3 = \mu)$
N_{jets}	≥ 2	1	≥ 2	≥ 2
$N_{b\text{-tags}}$	1	1	1	≤ 2
Muon p_T cut	$> 15 \text{ GeV}$	$> 15 \text{ GeV}$	$> 15 \text{ GeV}$	$> 10 \text{ GeV}$
Lowest p_T muon selection	<i>Tight</i>	<i>Tight</i>	<i>Tight</i>	<i>Loose</i>
Muon charges	SS	SS	OS	-
$ m_{\mu\mu}^{OS} - M_Z $	-	-	$< 10 \text{ GeV}$	$> 10 \text{ GeV}$

Operator	Lorentz Structure	
$O_{lq}^{1(ijkl)}$	$(\bar{l}_i \gamma^\mu l_j)(\bar{q}_k \gamma_\mu q_l)$	Vector
$O_{lq}^{3(ijkl)}$	$(\bar{l}_i \gamma^\mu \sigma^I l_j)(\bar{q}_k \gamma_\mu \sigma^I q_l)$	Vector
$O_{eq}^{(ijkl)}$	$(\bar{e}_i \gamma^\mu e_j)(\bar{q}_k \gamma_\mu q_l)$	Vector
$O_{lu}^{(ijkl)}$	$(\bar{l}_i \gamma^\mu l_j)(\bar{u}_k \gamma_\mu u_l)$	Vector
$O_{eu}^{(ijkl)}$	$(\bar{e}_i \gamma^\mu e_j)(\bar{u}_k \gamma_\mu u_l)$	Vector
$\ddagger O_{lequ}^{1(ijkl)}$	$(\bar{l}_i e_j) \varepsilon(\bar{q}_k u_l)$	Scalar
$\ddagger O_{lequ}^{3(ijkl)}$	$(\bar{l}_i \sigma^{\mu\nu} e_j) \varepsilon(\bar{q}_k \sigma_{\mu\nu} u_l)$	Tensor

$$\Gamma(t \rightarrow \ell_i^+ \ell_j^- qk) = \frac{m_t}{6144\pi^3} \left(\frac{m_t}{\Lambda}\right)^4 \left\{ 4|c_{lq}^{-(ijk3)}|^2 + 4|c_{eq}^{(ijk3)}|^2 + 4|c_{lu}^{(ijk3)}|^2 + 4|c_{eu}^{(ijk3)}|^2 \right. \\ \left. + |c_{lequ}^{1(jik3)}|^2 + |c_{lequ}^{1(ij3k)}|^2 + 48|c_{lequ}^{3(jik3)}|^2 + 48|c_{lequ}^{3(ij3k)}|^2 \right\}$$