



A network of clocks for measuring  
the stability of fundamental constants



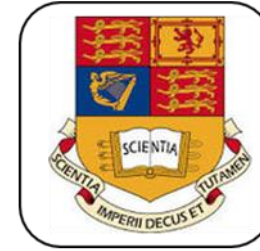
Birmingham



NPL



Sussex



Imperial

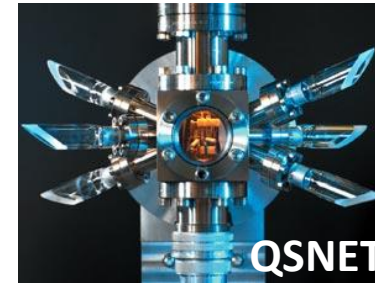
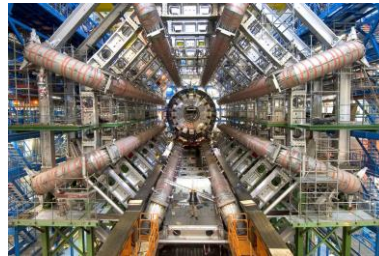
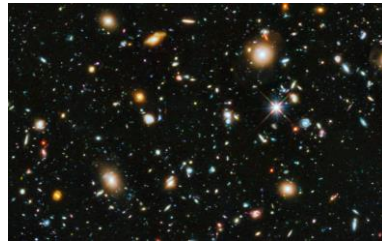
# QTFP

- QSNET is one of the 7 projects funded within the QTFP programme of STFC&EPSRC  
<https://www.ukri.org/news/quantum-projects-launched-to-solve-the-universes-mysteries/>
- QTFP aims at **building a community** at the interface of quantum physics and fundamental physics

# Background

- Searches for physics beyond the SM

Energy



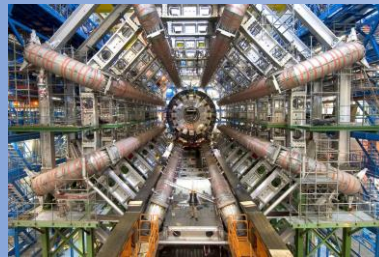
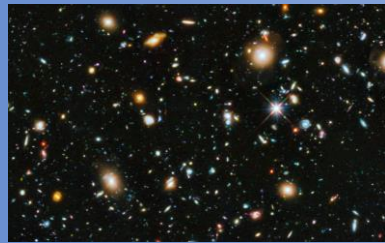
Precision



# Background

- Searches for physics beyond the SM

Energy

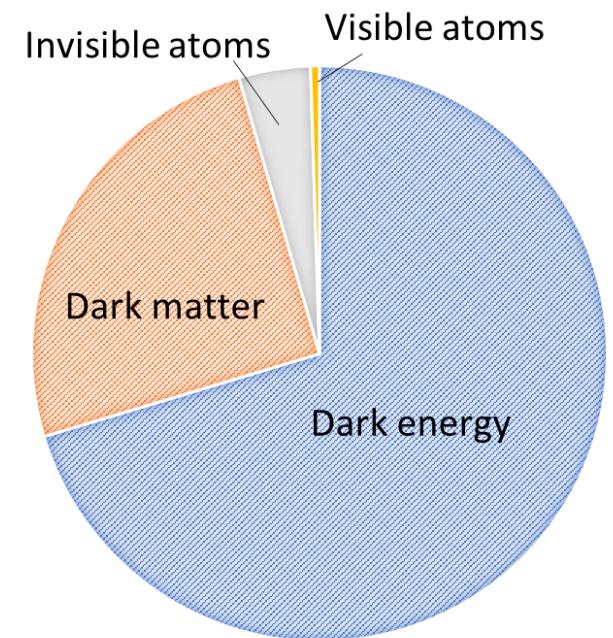
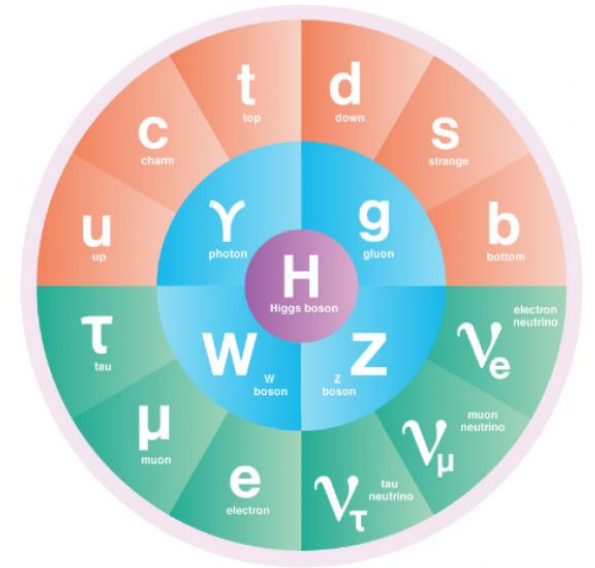


Precision



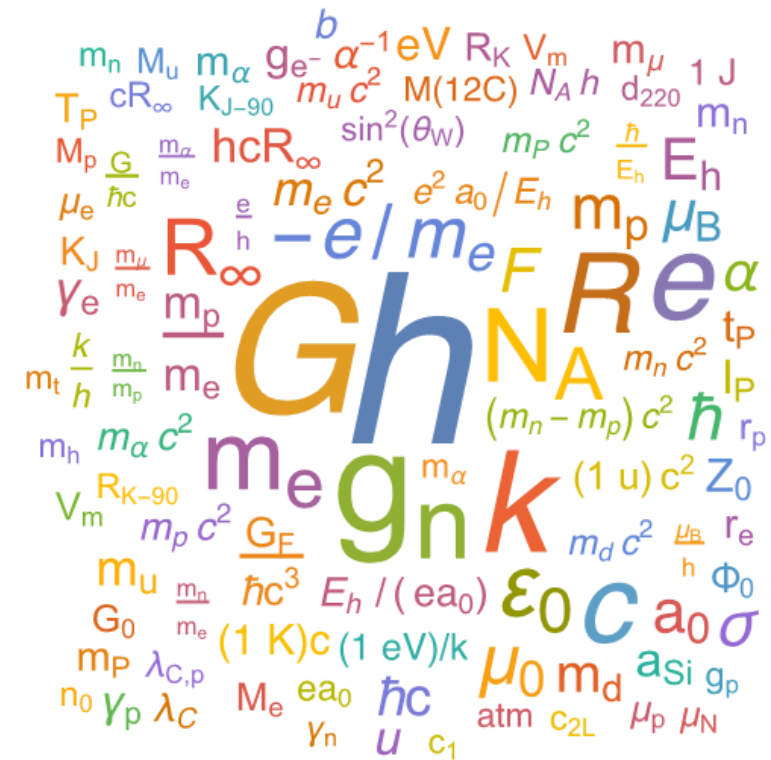
# Background

- The Standard Model and  $\Lambda$ CDM are very successful theories but...
- The  $\Lambda$ CDM model postulates that 95% of the energy content of the universe is **dark matter and dark energy**. Their exact nature is unknown. Only the remaining 5% is described by the SM.



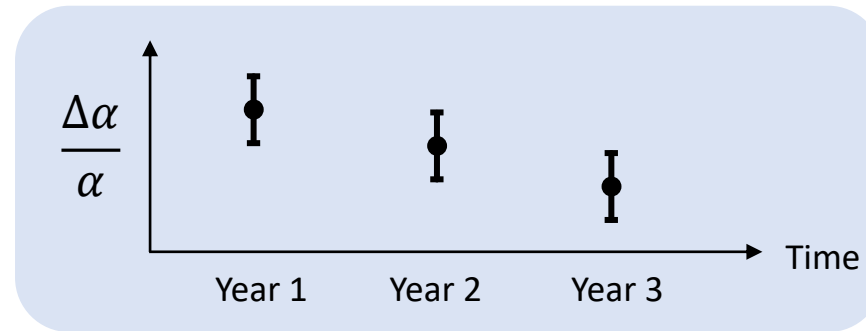
# Background

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- The  $\Lambda$ CDM model postulates that 95% of the energy content of the universe is **dark matter and dark energy**. Their exact nature is unknown. Only the remaining 5% is described by the SM.
- Both models have **several parameters**, supposed to be immutable, called **fundamental constants**.
- Challenging this central assumption could be the key to solving the dark matter and dark energy enigmas
- **Any variations** of fundamental constants would give us evidence of **revolutionary new physics**

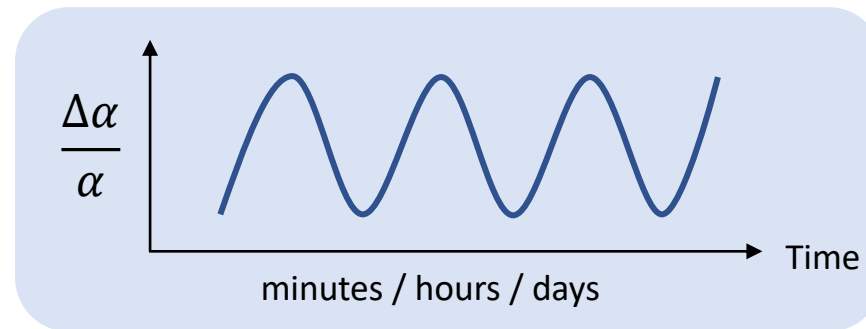


# Look for variation on different timescales

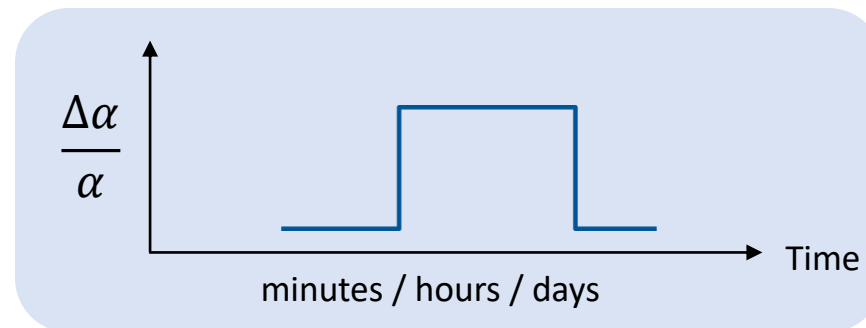
- Slow drifts



- Oscillations



- Fast transients



And any combination...

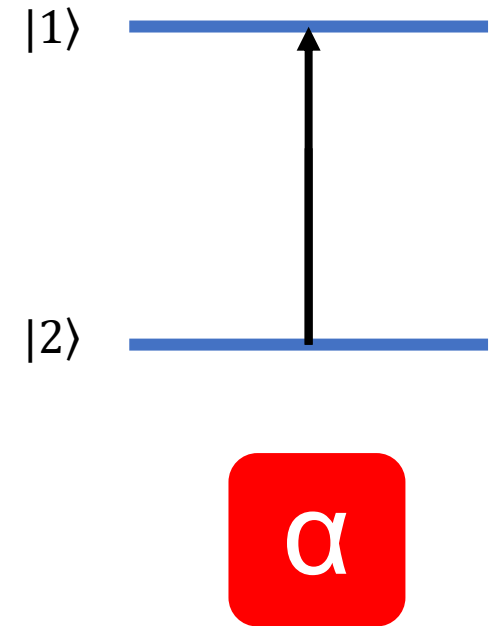
# Why clocks?

- All atomic and molecular energy spectra depend on the fundamental constants of the Standard Model
- Spectroscopy lends itself to measure variations of:

$$\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c}$$

$$\mu = \frac{m_p}{m_e}$$

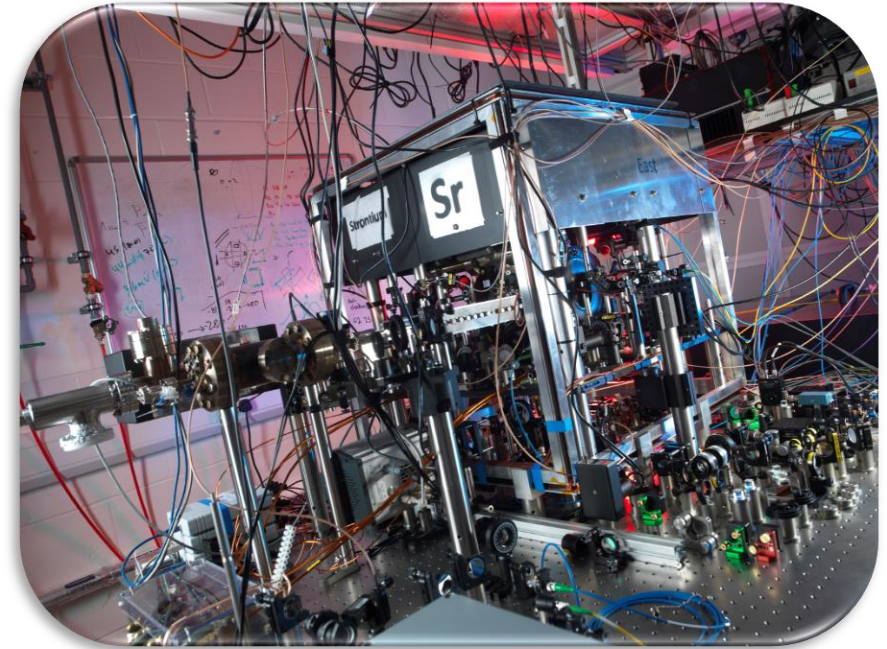
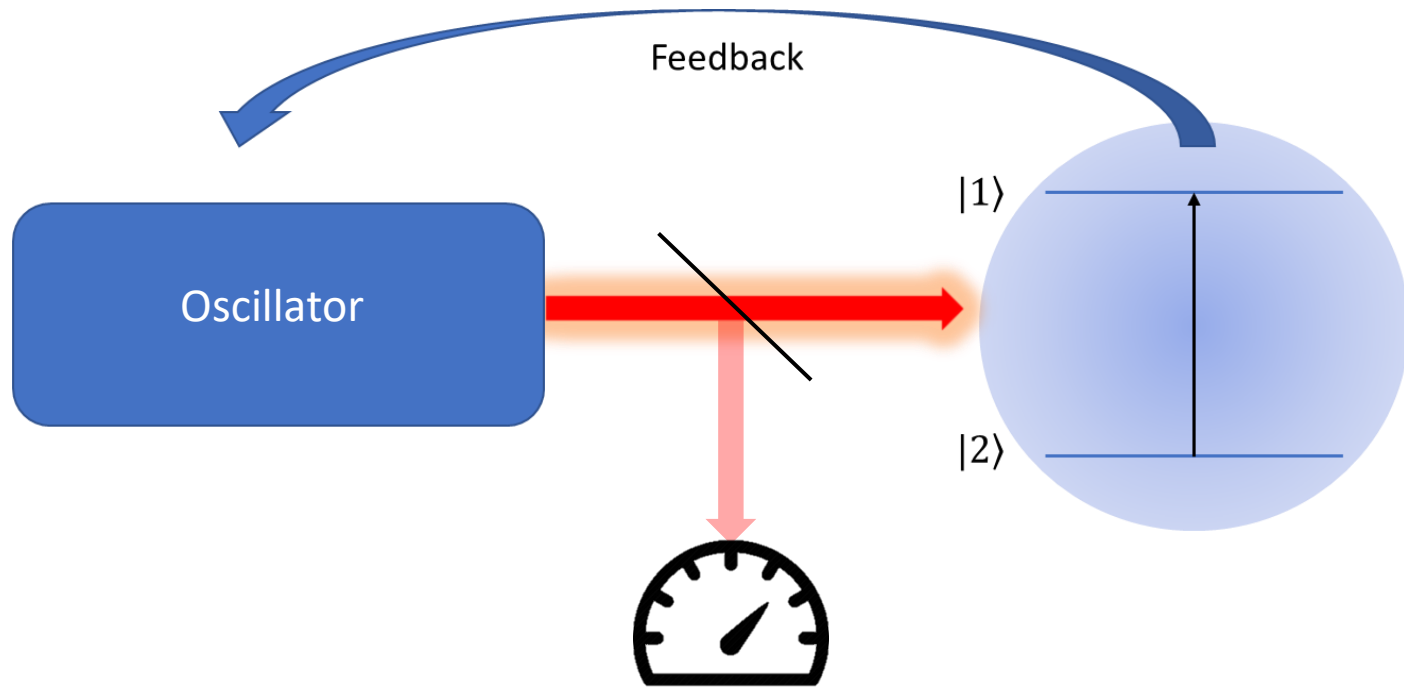
- Atomic and molecular spectra can be measured with extreme precision using **atomic clocks**
- Grand unification physics fixes relations between fundamental constants (if one changes with time, others will as well)





# Atomic clocks

- Extremely high-precision spectroscopy



- Stability and accuracy at the  $10^{-18}$  level

# How to measure variations of fundamental constants

- Different clock transitions have different sensitivities to fundamental constants

- Hyperfine transitions

$$\nu_{Hf} = A\mu\alpha^2 F_{Hf}(\alpha)R_\infty$$

- Optical transitions

$$\nu_{opt} = BF_{opt}(\alpha)R_\infty$$

- Vibrational transitions

$$\nu_{vib} = C\mu^{1/2}R_\infty$$

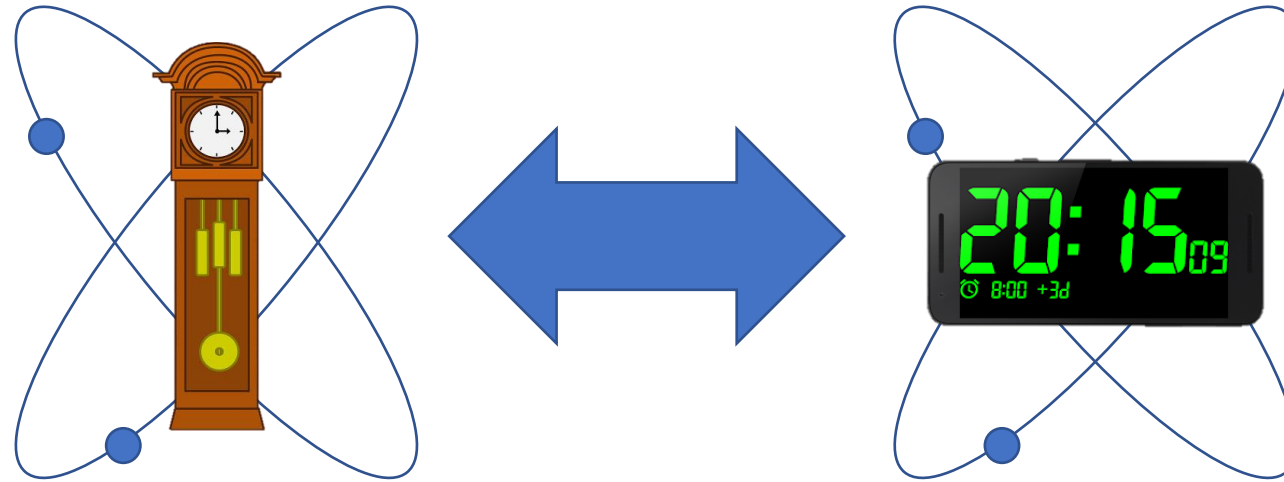
$$\frac{dE}{E_0} = K_X \frac{dX}{X_0}$$



Clock	$K_\alpha$	$K_\mu$
Sr	0.06	0
Yb+	-5.95	0
Cs	2.83	1
CaF	0	0.5

# How to measure variations of fundamental constants

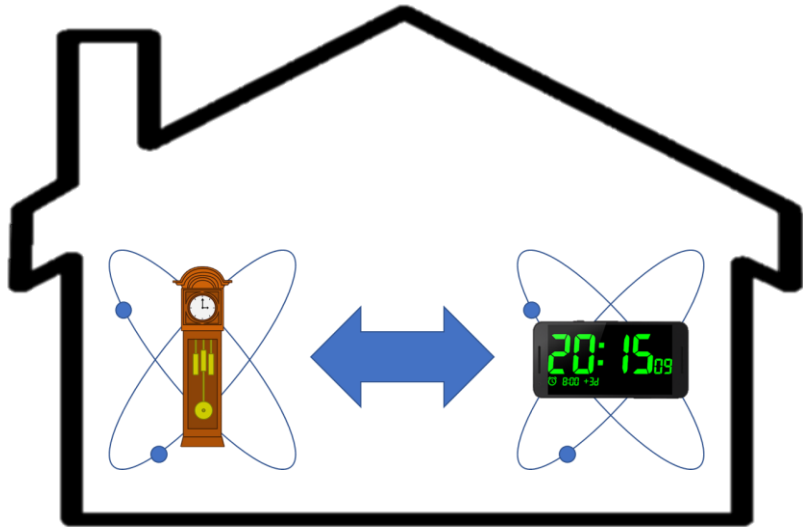
- Comparing clocks with different sensitivities to fundamental constants



- Measure ratio  $f_1 / f_2$
- Look for changes over time

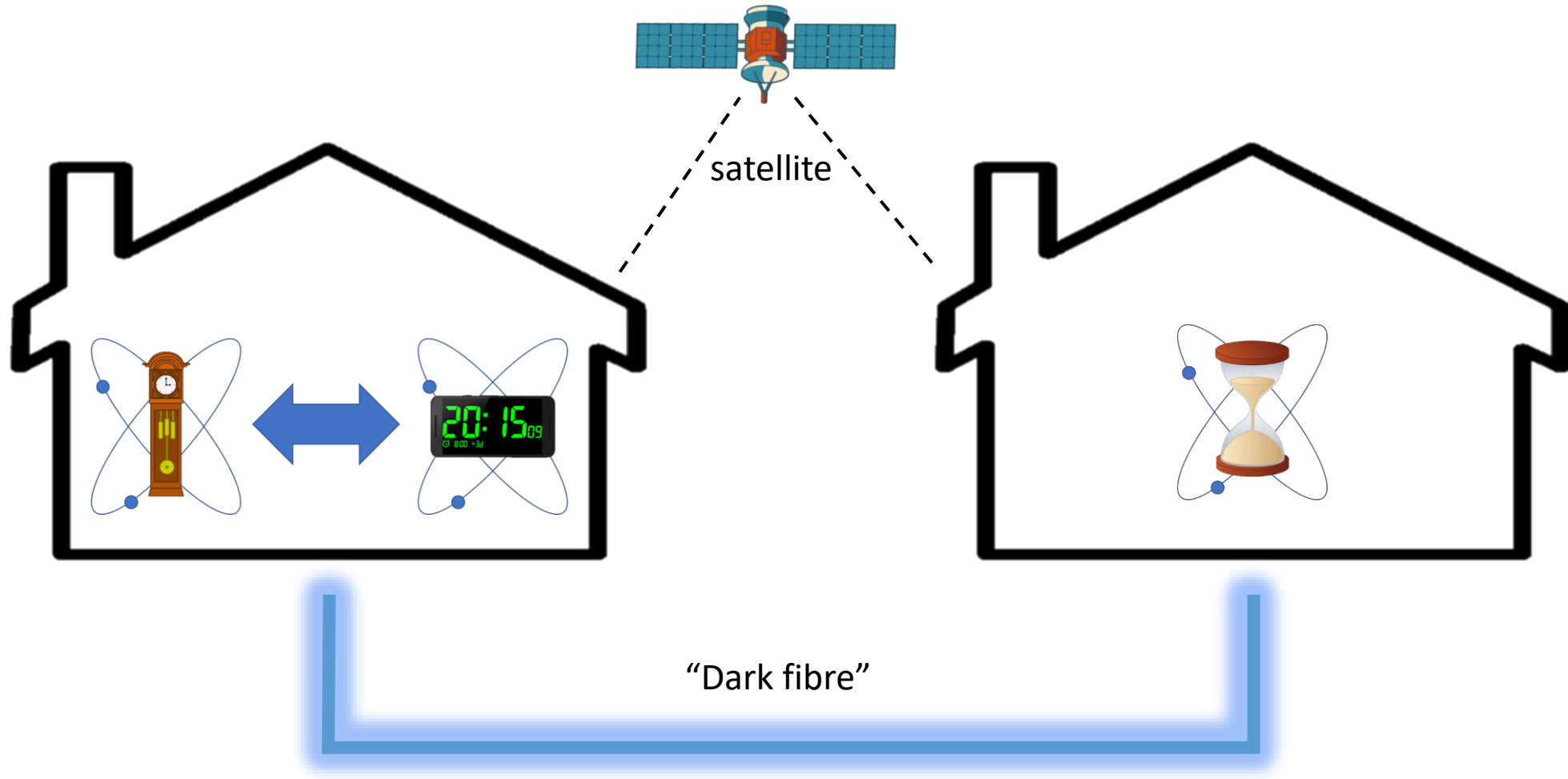
$$\frac{\Delta f_1}{\Delta f_2} = |K_{1x} - K_{2x}| \frac{\Delta x}{x} \quad x = \alpha, \mu$$

# How to measure variations of fundamental constants



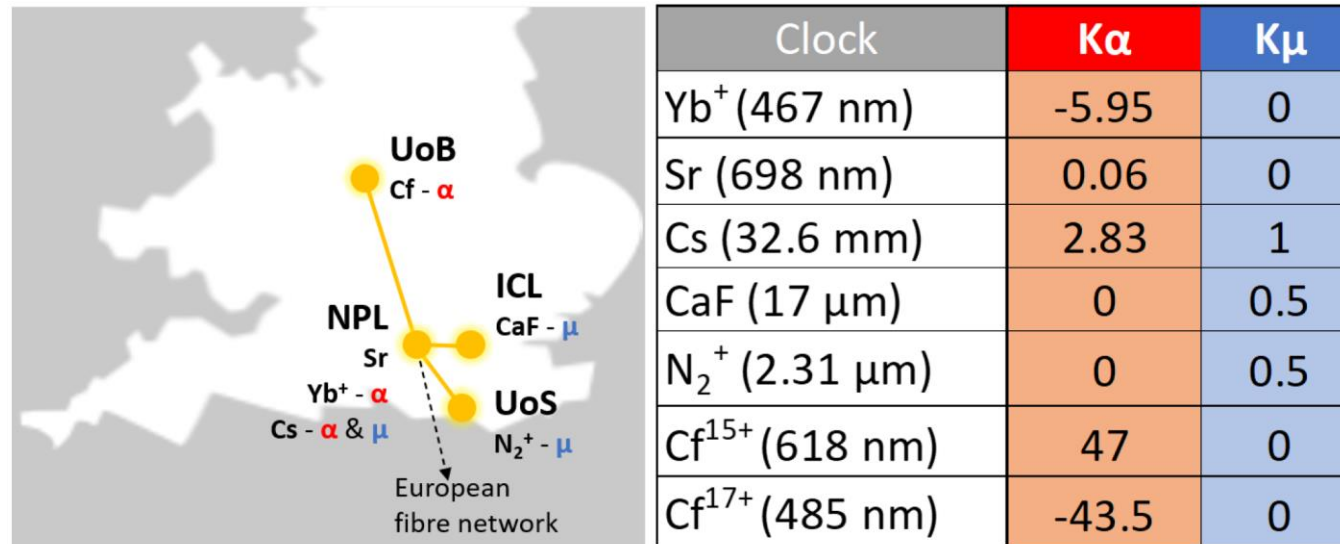
"in house" comparison

# How to measure variations of fundamental constants



# The QSNET project

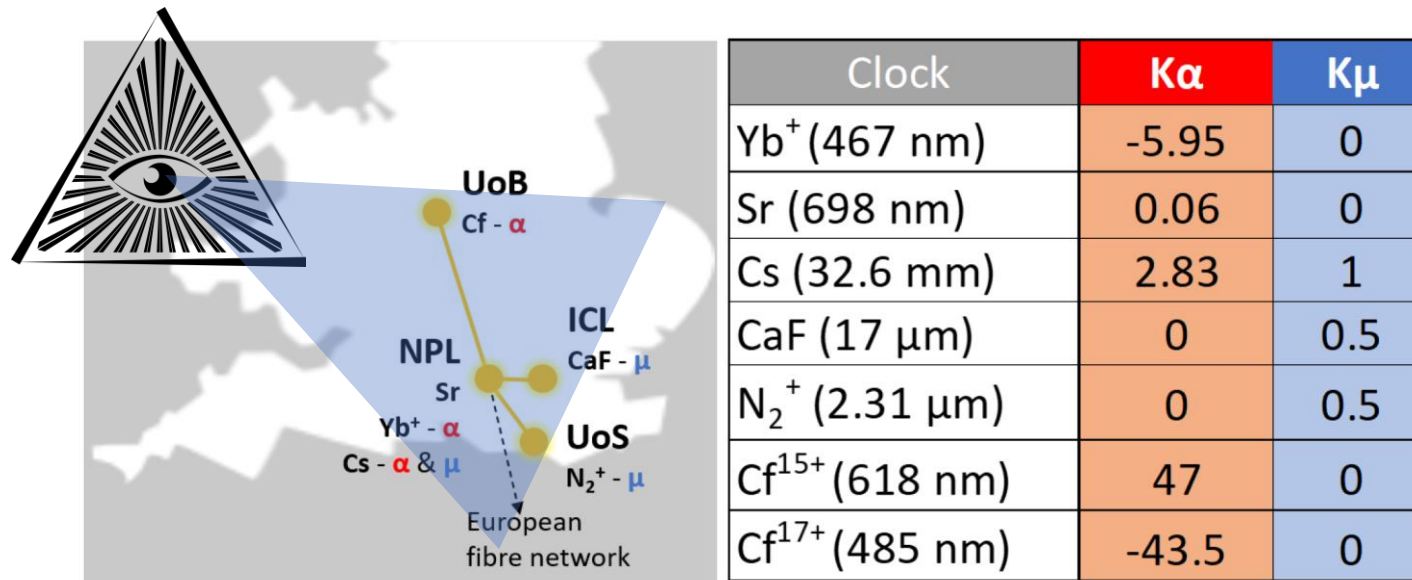
- Search for variations of fundamental constants of the Standard Model, using a network of clocks
- A **unique** network of clocks chosen for their **different sensitivities** to variations of  $\alpha$  and  $\mu$



- The clocks **will be linked**, essential to do clock-clock comparisons

# The QSNET project

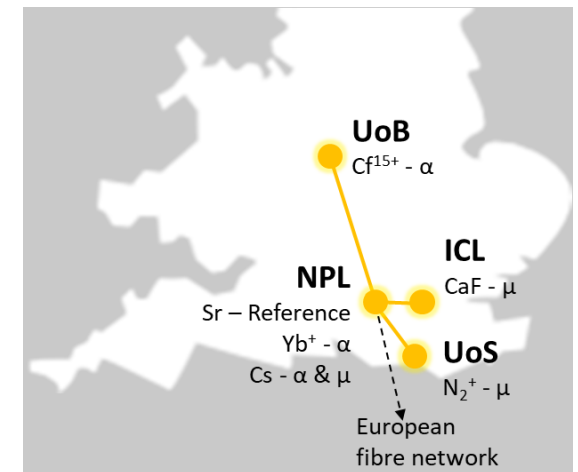
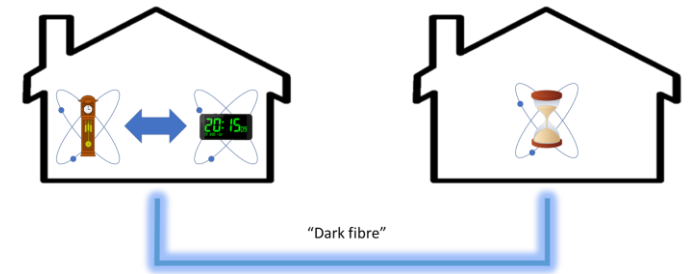
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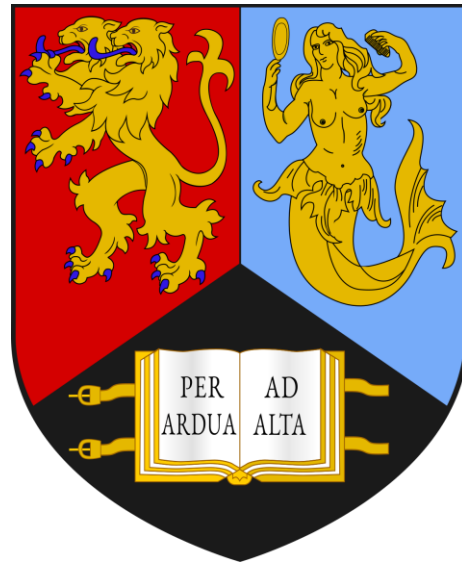
# The network approach

- **Optimally exploit existing expertise.** No single institution has the range of expertise required to run a sufficiently large and diverse set of clocks
- Sensors with **similar sensitivities and different systematics** are necessary to confirm any measurements and reject false positives
- Networks enable probing of **space-time correlations**
- The possibility of detecting transient events such as **topological defects in dark matter fields or oscillations of dark matter**
- A new versatile and expandable **national infrastructure** with possible further applications in and beyond fundamental physics.



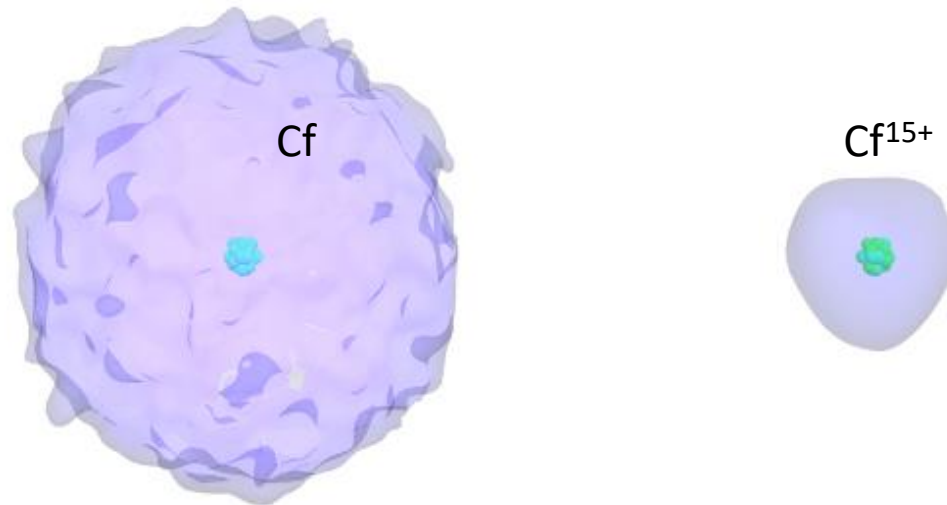


# The Bham node



# The Bham node: Highly-charged ions

Strip neutral atoms of several electrons



“Compressed” electronic cloud

Low sensitivity to external perturbations (hopefully!) -> good for clocks

Large relativistic corrections -> high sensitivities to variations of  $\alpha$  ( $K_\alpha \sim 10 - 100$ )<sub>18</sub>

# Highly-charged ions

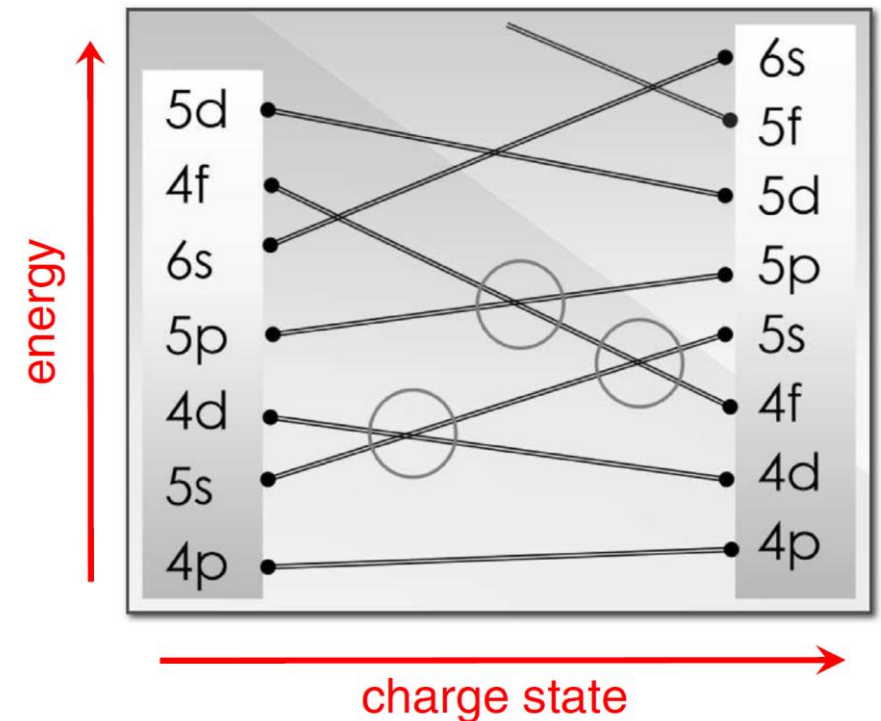
The energy scale for electronic transitions scales as

$$E \propto (q + 1)^2 R_{\infty}$$

So HCIs normally feature transitions in the XUV and x-ray regions

However there are some level crossings going from the Madelung ordering to the hydrogen-like ordering

Some HCIs feature **ground-state transitions in the visible range** -> good for clocks



Phys. Rev. Lett. 109, 070802 (2012)

# HClIs and variations of $\alpha$

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Nd <sup>13+</sup>	5s <sub>1/2</sub>	0				
	4f <sub>5/2</sub>	55 706	104 229	3.7	179	1.3 × 10 <sup>6a</sup>
	4f <sub>7/2</sub>	60 134	108 243	3.6	166	0.996
Sm <sup>15+</sup>	4f <sub>5/2</sub>	0				
	4f <sub>7/2</sub>	6 444	5 910	1.8	1526	0.308
	5s <sub>1/2</sub>	60 517	-134 148	-4.4	166	3.1 × 10 <sup>5</sup>
*Cf <sup>17+</sup>	5f <sub>5/2</sub>	0				
	6p <sub>1/2</sub>	18 686	-449 750	-48	535	
	5f <sub>7/2</sub>	21 848	17 900	1.6	458	
Nd <sup>12+</sup>	5s <sup>2</sup> 1S <sub>0</sub>	0				
	5s4f <sup>3</sup> F <sub>2</sub>	79 469	101 461	2.6	126	8.5 × 10 <sup>10</sup>
	5s4f <sup>3</sup> F <sub>3</sub>	80 769	102 325	2.4	124	19.7
Sm <sup>14+</sup>	4f <sup>2</sup> 3H <sub>4</sub>	0				
	5s4f <sup>3</sup> F <sub>2</sub>	2 172	-127 720	-118	4600	5.6 × 10 <sup>13b</sup>
	5s4f <sup>3</sup> F <sub>3</sub>	3 826	-126 746	-66	2614	8.51
*Es <sup>17+</sup>	5f <sup>2</sup> 3H <sub>4</sub>	0				
	5f6p <sup>3</sup> F <sub>2</sub>	7 445	-46 600	-13	1343	11 000

Ion	Level	Energy	$q$	$K$	$\lambda$
Ir <sup>16+</sup>	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>7/2</sub>	0			
	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>5/2</sub>	25 898	23 652	1.8	386
	4f <sup>14</sup> 5s 2S <sub>1/2</sub>	37 460	367 315	20	267
Ir <sup>17+</sup>	4f <sup>13</sup> 5s 3F <sub>4</sub>	0			
	4f <sup>13</sup> 5s 3F <sub>3</sub>	4 838	2 065	0.9	2067
	4f <sup>13</sup> 5s 3F <sub>2</sub>	26 272	24 183	1.8	381
	4f <sup>14</sup> 1S <sub>0</sub>	5 055	367 161	145	1978
	4f <sup>12</sup> 5s <sup>2</sup> 3H <sub>6</sub>	35 285	-385 367	-22	283
Ho <sup>14+</sup>	4f <sup>6</sup> 5s 8F <sub>1/2</sub>	45 214	-387 086	-17	221
	4f <sup>5</sup> 5s <sup>2</sup> 6H <sub>5/2</sub>	23 823	-186 000	-16	420

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Ce <sup>9+</sup>	5s <sup>2</sup> 5p <sub>1/2</sub>	0				
	5s <sup>2</sup> 5p <sub>3/2</sub>	33 450	37 544	2.2	299	0.0030
	5s <sup>2</sup> 4f <sub>5/2</sub>	54 683	62 873	2.3	182	0.0812
	5s <sup>2</sup> 4f <sub>7/2</sub>	57 235	65 150	2.3	174	2.18
Pr <sup>10+</sup>	5s <sup>2</sup> 5p <sub>1/2</sub>	0				
	5s <sup>2</sup> 4f <sub>5/2</sub>	3 702	73 849	40	2700	8.5 × 10 <sup>4</sup>
	5s <sup>2</sup> 4f <sub>7/2</sub>	7 031	76 833	22	1422	2.35
	5s <sup>2</sup> 5p <sub>3/2</sub>	39 141	44 098	2.3	256	0.0018
Nd <sup>11+</sup>	5s <sup>2</sup> 4f <sub>5/2</sub>	0				
	5s <sup>2</sup> 4f <sub>7/2</sub>	4 180	3 785	1.8	2392	1.19
	5s <sup>2</sup> 5p <sub>1/2</sub>	53 684	-85 692	-3.2	186	0.061
Sm <sup>13+</sup>	5s <sup>2</sup> 4f <sup>2</sup> F <sub>5/2</sub>	0				
	5s <sup>2</sup> 4f <sup>2</sup> F <sub>7/2</sub>	6 203	5 654	1.8	1612	0.367
	4f <sup>2</sup> 5s <sup>4</sup> H <sub>7/2</sub>	20 254	123 621	12	494	0.133
Eu <sup>14+</sup>	4f <sup>2</sup> 5s J = 7/2	0				
	4f <sup>3</sup> J = 9/2	1 262	137 437	218	7924	
	4f <sup>2</sup> 5s J = 9/2	2 594	1 942	1.5	3855	
	4f <sup>3</sup> J = 11/2	5 388	141 771	53	1856	
*Cf <sup>15+</sup>	5f6p <sup>2</sup> 2F <sub>5/2</sub>	0				
	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	12 898	380 000	59	775	6900
	5f6p <sup>2</sup> 2F <sub>7/2</sub>	22 018			454	0.012
*Es <sup>16+</sup>	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	0				
	5f <sup>2</sup> 6p <sup>2</sup> F <sub>5/2</sub>	6 994	-184 000	-53	1430	16 000
	5f <sup>3</sup> 2H <sub>9/2</sub>	10 591			944	3.4
Pr <sup>9+</sup>	5s <sup>2</sup> 5p <sup>2</sup> 3P <sub>0</sub>	0				
	5s <sup>2</sup> 5p4f <sup>3</sup> G <sub>3</sub>	20 216	42 721	4.2	475	6.6 × 10 <sup>14</sup>
	5s <sup>2</sup> 5p4f <sup>3</sup> F <sub>2</sub>	22 772	42 865	3.8	426	59.0
	5s <sup>2</sup> 5p4f <sup>3</sup> F <sub>3</sub>	25 362	47 076	3.7	382	5.33
Nd <sup>10+</sup>	5s <sup>2</sup> 4f <sup>2</sup> J = 4	0				
	5s <sup>2</sup> 5p4f J = 3	1 564	-81 052	-104		16 000
	5s <sup>2</sup> 4f <sup>2</sup> J = 5	3 059	3 113	2.0		1.4
	5s <sup>2</sup> 5p4f J = 2	5 060	-60 350	-24	2200	25

# HCI and variations of $\alpha$

✓ Visible range

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Nd <sup>13+</sup>	5s <sub>1/2</sub>	0				
	<del>4f<sub>5/2</sub></del>	<del>55 706</del>	<del>104 229</del>	<del>3.7</del>	<del>179</del>	<del>1.3 × 10<sup>6a</sup></del>
	<del>4f<sub>7/2</sub></del>	<del>60 134</del>	<del>108 243</del>	<del>3.6</del>	<del>166</del>	<del>0.996</del>
Sm <sup>15+</sup>	4f <sub>5/2</sub>	0				
	<del>4f<sub>7/2</sub></del>	<del>6 444</del>	<del>5 910</del>	<del>1.8</del>	<del>1526</del>	<del>0.308</del>
	<del>5s<sub>1/2</sub></del>	<del>60 517</del>	<del>134 148</del>	<del>4.4</del>	<del>166</del>	<del>3.1 × 10<sup>5</sup></del>
*Cf <sup>17+</sup>	5f <sub>5/2</sub>	0				
	6p <sub>1/2</sub>	18 686	-449 750	-48	535	
	5f <sub>7/2</sub>	21 848	17 900	1.6	458	
Nd <sup>12+</sup>	5s <sup>2</sup> 1S <sub>0</sub>	0				
	<del>5s4f<sup>3</sup>F<sub>2</sub></del>	<del>79 469</del>	<del>101 461</del>	<del>2.6</del>	<del>126</del>	<del>8.5 × 10<sup>10</sup></del>
	<del>5s4f<sup>3</sup>F<sub>3</sub></del>	<del>80 769</del>	<del>102 323</del>	<del>2.4</del>	<del>124</del>	<del>19.7</del>
Sm <sup>14+</sup>	4f <sup>2</sup> 3H <sub>4</sub>	0				
	<del>5s4f<sup>3</sup>F<sub>2</sub></del>	<del>2 172</del>	<del>127 720</del>	<del>118</del>	<del>4600</del>	<del>5.6 × 10<sup>13b</sup></del>
	<del>5s4f<sup>3</sup>F<sub>3</sub></del>	<del>3 826</del>	<del>-126 746</del>	<del>-66</del>	<del>2614</del>	<del>8.51</del>
*Es <sup>17+</sup>	5f <sup>2</sup> 3H <sub>4</sub>	0				
	5f6p <sup>3</sup> F <sub>2</sub>	7 445	-46 600	-13	1343	11 000

Ion	Level	Energy	$q$	$K$	$\lambda$
Ir <sup>16+</sup>	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>7/2</sub>	0			
	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>5/2</sub>	25 898	23 652	1.8	386
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Ir <sup>17+</sup>	4f <sup>13</sup> 5s 3F <sub>4</sub>	0			
	<del>4f<sup>13</sup>5s 3F<sub>3</sub></del>	<del>4 838</del>	<del>2 065</del>	<del>0.9</del>	<del>2067</del>
	4f <sup>13</sup> 5s 3F <sub>2</sub>	26 272	24 183	1.8	381
	<del>4f<sup>14</sup> 1S<sub>0</sub></del>	<del>5 055</del>	<del>367 161</del>	<del>145</del>	<del>1978</del>
	4f <sup>12</sup> 5s <sup>2</sup> 3H <sub>6</sub>	35 285	-385 367	-22	283
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Ho <sup>14+</sup>	4f <sup>6</sup> 5s 8F <sub>1/2</sub>	0			
	4f <sup>5</sup> 5s <sup>2</sup> 6H <sub>5/2</sub>	23 823	-186 000	-16	420

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Ce <sup>9+</sup>	5s <sup>2</sup> 5p <sub>1/2</sub>	0				
	5s <sup>2</sup> 5p <sub>3/2</sub>	33 450	37 544	2.2	299	0.0030
	<del>5s<sup>2</sup>4f<sub>5/2</sub></del>	<del>54 683</del>	<del>62 873</del>	<del>2.3</del>	<del>182</del>	<del>0.0812</del>
	<del>5s<sup>2</sup>4f<sub>7/2</sub></del>	<del>57 235</del>	<del>65 150</del>	<del>2.3</del>	<del>174</del>	<del>2.18</del>
Pr <sup>10+</sup>	5s <sup>2</sup> 5p <sub>1/2</sub>	0				
	<del>5s<sup>2</sup>4f<sub>5/2</sub></del>	<del>3 702</del>	<del>73 849</del>	<del>40</del>	<del>2700</del>	<del>8.5 × 10<sup>4</sup></del>
	<del>5s<sup>2</sup>4f<sub>7/2</sub></del>	<del>7 031</del>	<del>76 833</del>	<del>22</del>	<del>1422</del>	<del>2.35</del>
	5s <sup>2</sup> 5p <sub>3/2</sub>	39 141	44 098	2.3	256	0.0018
Nd <sup>11+</sup>	5s <sup>2</sup> 4f <sub>5/2</sub>	0				
	<del>5s<sup>2</sup>4f<sub>7/2</sub></del>	<del>4 180</del>	<del>3 785</del>	<del>1.8</del>	<del>2392</del>	<del>1.19</del>
	5s <sup>2</sup> 5p <sub>1/2</sub>	53 684	-85 692	-3.2	186	0.061
Sm <sup>13+</sup>	5s <sup>2</sup> 4f <sup>2</sup> F <sub>5/2</sub>	0				
	<del>5s<sup>2</sup>4f<sup>2</sup>F<sub>7/2</sub></del>	<del>6 203</del>	<del>5 654</del>	<del>1.8</del>	<del>1612</del>	<del>0.367</del>
	4f <sup>2</sup> 5s <sup>4</sup> H <sub>7/2</sub>	20 254	123 621	12	494	0.133
Eu <sup>14+</sup>	4f <sup>2</sup> 5s J = 7/2	0				
	<del>4f<sup>3</sup> J = 9/2</del>	<del>1 262</del>	<del>137 437</del>	<del>218</del>	<del>7924</del>	
	<del>4f<sup>2</sup>5s J = 9/2</del>	<del>2 594</del>	<del>1 942</del>	<del>1.5</del>	<del>3855</del>	
	<del>4f<sup>2</sup> J = 11/2</del>	<del>5 388</del>	<del>141 771</del>	<del>53</del>	<del>1856</del>	
*Cf <sup>15+</sup>	5f6p <sup>2</sup> 2F <sub>5/2</sub>	0				
	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	12 898	380 000	59	775	6900
	5f6p <sup>2</sup> 2F <sub>7/2</sub>	22 018			454	0.012
*Es <sup>16+</sup>	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	0				
	<del>5f<sup>2</sup>6p<sup>2</sup>F<sub>5/2</sub></del>	<del>6 994</del>	<del>-184 000</del>	<del>-53</del>	<del>1430</del>	<del>16 000</del>
	5f <sup>3</sup> 2H <sub>9/2</sub>	10 591			944	3.4
Pr <sup>9+</sup>	5s <sup>2</sup> 5p <sup>2</sup> 3P <sub>0</sub>	0				
	5s <sup>2</sup> 5p4f <sup>3</sup> G <sub>3</sub>	20 216	42 721	4.2	475	6.6 × 10 <sup>14</sup>
	5s <sup>2</sup> 5p4f <sup>3</sup> F <sub>2</sub>	22 772	42 865	3.8	426	59.0
	5s <sup>2</sup> 5p4f <sup>3</sup> F <sub>3</sub>	25 362	47 076	3.7	382	5.33
Nd <sup>10+</sup>	5s <sup>2</sup> 4f <sup>2</sup> J = 4	0				
	5s <sup>2</sup> 5p4f J = 3	1 564	-81 052	-104		16 000
	5s <sup>2</sup> 4f <sup>2</sup> J = 5	3 059	3 113	2.0		1.4
	<del>5s<sup>2</sup>5p4f J = 2</del>	<del>5 060</del>	<del>-60 350</del>	<del>24</del>	<del>2200</del>	<del>25</del>

# HClIs and variations of $\alpha$

✓ Visible range

✓ High values of K



Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Nd <sup>13+</sup>	5s <sub>1/2</sub>	0				
	<del>4f<sub>5/2</sub></del>	<del>55 706</del>	<del>104 229</del>	<del>3.7</del>	<del>179</del>	<del>1.3 × 10<sup>6a</sup></del>
	<del>4f<sub>7/2</sub></del>	<del>60 134</del>	<del>108 243</del>	<del>3.6</del>	<del>166</del>	<del>0.996</del>
Sm <sup>15+</sup>	4f <sub>5/2</sub>	0				
	<del>4f<sub>7/2</sub></del>	<del>6 444</del>	<del>5 910</del>	<del>1.8</del>	<del>1526</del>	<del>0.308</del>
	<del>5s<sub>1/2</sub></del>	<del>60 517</del>	<del>134 148</del>	<del>4.4</del>	<del>166</del>	<del>3.1 × 10<sup>5</sup></del>
*Cf <sup>17+</sup>	5f <sub>5/2</sub>	0				
	6p <sub>1/2</sub>	18 686	-449 750	-48	535	
	5f <sub>7/2</sub>	21 848	17 900	1.6	458	
Nd <sup>12+</sup>	5s <sup>2</sup> 1s <sub>0</sub>	0				
	<del>5s4f<sup>3</sup>F<sub>2</sub></del>	<del>79 469</del>	<del>101 461</del>	<del>2.6</del>	<del>126</del>	<del>8.5 × 10<sup>10</sup></del>
	<del>5s4f<sup>3</sup>F<sub>3</sub></del>	<del>80 769</del>	<del>102 323</del>	<del>2.4</del>	<del>124</del>	<del>19.7</del>
Sm <sup>14+</sup>	4f <sup>2</sup> 3H <sub>4</sub>	0				
	<del>5s4f<sup>3</sup>F<sub>2</sub></del>	<del>2 172</del>	<del>127 720</del>	<del>118</del>	<del>4600</del>	<del>5.6 × 10<sup>13b</sup></del>
	<del>5s4f<sup>3</sup>F<sub>3</sub></del>	<del>3 826</del>	<del>-126 746</del>	<del>-66</del>	<del>2614</del>	<del>8.51</del>
*Es <sup>17+</sup>	5f <sup>2</sup> 3H <sub>4</sub>	0				
	5f6p <sup>3</sup> F <sub>2</sub>	7 445	-46 600	-13	1343	11 000



Ion	Level	Energy	$q$	$K$	$\lambda$
Ir <sup>16+</sup>	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>7/2</sub>	0			
	<del>4f<sup>13</sup>5s<sup>2</sup> 2F<sub>5/2</sub></del>	<del>25 898</del>	<del>23 652</del>	<del>1.8</del>	<del>386</del>
	4f <sup>14</sup> 5s	37 460	367 315	20	267
Ir <sup>17+</sup>	4f <sup>13</sup> 5s 3F <sub>4</sub>	0			
	<del>4f<sup>13</sup>5s 3F<sub>3</sub></del>	<del>4 838</del>	<del>2 065</del>	<del>0.9</del>	<del>2067</del>
	<del>4f<sup>13</sup>5s 3F<sub>2</sub></del>	<del>26 272</del>	<del>24 183</del>	<del>1.8</del>	<del>381</del>
	4f <sup>14</sup> 1s <sub>0</sub>	5 055	367 161	145	1978
	<del>4f<sup>12</sup>5s<sup>2</sup> 3H<sub>6</sub></del>	<del>35 285</del>	<del>-385 367</del>	<del>-22</del>	<del>283</del>
	<del>4f<sup>12</sup>5s<sup>2</sup> 3F<sub>4</sub></del>	<del>45 214</del>	<del>-387 086</del>	<del>-17</del>	<del>221</del>
Ho <sup>14+</sup>	4f <sup>6</sup> 5s 8F <sub>1/2</sub>				
	4f <sup>5</sup> 5s <sup>2</sup> 6H <sub>5/2</sub>	23 823	-186 000	-16	420

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Ce <sup>9+</sup>	5s <sup>2</sup> 5p <sub>1/2</sub>	0				
	<del>5s<sup>2</sup>5p<sub>3/2</sub></del>	<del>33 450</del>	<del>37 544</del>	<del>2.2</del>	<del>299</del>	<del>0.0030</del>
	<del>5s<sup>2</sup>4f<sub>5/2</sub></del>	<del>54 683</del>	<del>62 873</del>	<del>2.3</del>	<del>182</del>	<del>0.0812</del>
	<del>5s<sup>2</sup>4f<sub>7/2</sub></del>	<del>57 235</del>	<del>65 150</del>	<del>2.3</del>	<del>174</del>	<del>2.18</del>
Pr <sup>10+</sup>	5s <sup>2</sup> 5p <sub>1/2</sub>	0				
	<del>5s<sup>2</sup>4f<sub>5/2</sub></del>	<del>3 702</del>	<del>73 849</del>	<del>40</del>	<del>2700</del>	<del>8.5 × 10<sup>4</sup></del>
	<del>5s<sup>2</sup>4f<sub>7/2</sub></del>	<del>7 031</del>	<del>76 833</del>	<del>22</del>	<del>1422</del>	<del>2.35</del>
	5s <sup>2</sup> 5p <sub>3/2</sub>	39 141	44 098	2.3	256	0.0018
Nd <sup>11+</sup>	5s <sup>2</sup> 4f <sub>5/2</sub>	0				
	<del>5s<sup>2</sup>4f<sub>7/2</sub></del>	<del>4 180</del>	<del>3 785</del>	<del>1.8</del>	<del>2392</del>	<del>1.19</del>
	5s <sup>2</sup> 5p <sub>1/2</sub>	53 684	-85 692	-3.2	186	0.061
Sm <sup>13+</sup>	5s <sup>2</sup> 4f <sup>2</sup> F <sub>5/2</sub>	0				
	<del>5s<sup>2</sup>4f<sup>2</sup>F<sub>7/2</sub></del>	<del>6 203</del>	<del>5 654</del>	<del>1.8</del>	<del>1612</del>	<del>0.367</del>
	4f <sup>2</sup> 5s <sup>4</sup> H <sub>7/2</sub>	20 254	123 621	12	494	0.133
Eu <sup>14+</sup>	4f <sup>2</sup> 5s J = 7/2	0				
	<del>4f<sup>3</sup> J = 9/2</del>	<del>1 262</del>	<del>137 437</del>	<del>218</del>	<del>7924</del>	
	<del>4f<sup>2</sup>5s J = 9/2</del>	<del>2 594</del>	<del>1 942</del>	<del>1.5</del>	<del>3855</del>	
	<del>4f<sup>2</sup> J = 11/2</del>	<del>5 388</del>	<del>141 771</del>	<del>53</del>	<del>1856</del>	
*Cf <sup>15+</sup>	5f6p <sup>2</sup> 2F <sub>5/2</sub>	0				
	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	12 898	380 000	59	775	6900
	5f6p <sup>2</sup> 2F <sub>7/2</sub>	22 018			454	0.012
*Es <sup>16+</sup>	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	0				
	<del>5f<sup>2</sup>6p<sup>2</sup>F<sub>5/2</sub></del>	<del>6 994</del>	<del>-184 000</del>	<del>-53</del>	<del>1430</del>	<del>16 000</del>
	5f <sup>3</sup> 2H <sub>9/2</sub>	10 591			944	3.4
Pr <sup>9+</sup>	5s <sup>2</sup> 5p <sup>2</sup> 3P <sub>0</sub>	0				
	<del>5s<sup>2</sup>5p4f<sup>3</sup>G<sub>3</sub></del>	<del>20 216</del>	<del>42 721</del>	<del>4.2</del>	<del>475</del>	<del>6.6 × 10<sup>14</sup></del>
	<del>5s<sup>2</sup>5p4f<sup>3</sup>F<sub>2</sub></del>	<del>22 772</del>	<del>42 865</del>	<del>3.8</del>	<del>426</del>	<del>59.0</del>
	<del>5s<sup>2</sup>5p4f<sup>3</sup>F<sub>3</sub></del>	<del>25 362</del>	<del>47 076</del>	<del>3.7</del>	<del>382</del>	<del>5.33</del>
Nd <sup>10+</sup>	5s <sup>2</sup> 4f <sup>2</sup> J = 4	0				
	5s <sup>2</sup> 5p4f J = 3	1 564	-81 052	-104		16 000
	5s <sup>2</sup> 4f <sup>2</sup> J = 5	3 059	3 113	2.0		1.4
	<del>5s<sup>2</sup>5p4f J = 2</del>	<del>5 060</del>	<del>60 350</del>	<del>24</del>	<del>2200</del>	<del>25</del>

# HClIs and variations of $\alpha$

✓ Visible range

✓ High values of K

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
*Cf <sup>17+</sup>	$5f_{5/2}$	0				
	$6p_{1/2}$	18 686	-449 750	-48	535	
	$5f_{7/2}$	21 848	17 900	1.6	458	
*Es <sup>17+</sup>	$5f^2\ ^3H_4$	0				
	$5f6p\ ^3F_2$	7 445	-46 600	-13	1343	11 000

Ion	Level	Energy	$q$	$K$	$\lambda$
Ir <sup>16+</sup>	$4f^{13}5s^2\ ^2F_{7/2}$	0			
	$4f^{13}5s^2\ ^2F_{5/2}$	25 898	23 652	1.8	386
	$4f^{14}5s\ ^2S_{1/2}$	37 460	367 315	20	267
Ir <sup>17+</sup>	$4f^{13}5s\ ^3F_4$	0			
	$4f^{13}5s\ ^3F_3$	4 838	2 065	0.9	2067
	$4f^{13}5s\ ^3F_2$	26 272	24 183	1.8	381
	$4f^{14}\ ^1S_0$	5 055	367 161	145	1978
	$4f^{12}5s^2\ ^3H_6$	35 285	-385 367	-22	283
	$4f^{12}5s^2\ ^3F_4$	45 214	-387 086	-17	221
Ho <sup>14+</sup>	$4f^65s\ ^8F_{1/2}$				
	$4f^55s^2\ ^6H_{5/2}$	23 823	-186 000	-16	420

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
Sm <sup>13+</sup>	$5s^24f^2F_{5/2}$	0				
	$5s^24f^2F_{7/2}$	6 203	5 654	1.8	1612	0.367
	$4f^25s\ ^4H_{7/2}$	20 254	123 621	12	494	0.133
*Cf <sup>15+</sup>	$5f6p^2\ ^2F_{5/2}$	0				
	$5f^26p\ ^4I_{9/2}$	12 898	380 000	59	775	6900
	$5f6p^2\ ^2F_{7/2}$	22 018			454	0.012
*Es <sup>16+</sup>	$5f^26p\ ^4I_{9/2}$	0				
	$5f^26p\ ^2F_{5/2}$	6 994	-184 000	-53	1430	16 000
	$5f^3\ ^2H_{9/2}$	10 591			944	3.4

# HClIs and variations of $\alpha$

- ✓ Visible range
- ✓ High values of K
- ❖ Other groups
- ❖ Too unstable

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
-----	-------	--------	-----	-----	-----------	--------

*Cf <sup>17+</sup>	5f <sub>5/2</sub>	0				
	6p <sub>1/2</sub>	18 686	-449 750	-48	535	
	5f <sub>7/2</sub>	21 848	17 900	1.6	458	
*Es <sup>17+</sup>	5f <sup>2</sup> 3H <sub>4</sub>					
	5f6p <sup>3</sup> F <sub>2</sub>					

Ion	Level	Energy	$q$	$K$	$\lambda$
Ir <sup>16+</sup>	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>7/2</sub>	0			
	4f <sup>13</sup> 5s <sup>2</sup> 2F <sub>5/2</sub>	25 898	23 652	1.8	386
	2S <sub>1/2</sub>	37 460	367 315		267
Ir <sup>17+</sup>	4f <sup>13</sup> 5s				
	4f <sup>13</sup> 5s				
	4f <sup>14</sup>				
		55 285			
		45 214	-36		
Ho <sup>14+</sup>	4f <sup>9</sup> 5s 8F <sub>1/2</sub>	23 823	-186 000	-16	420
	4f <sup>9</sup> 5s <sup>2</sup> 6H <sub>5/2</sub>				

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
-----	-------	--------	-----	-----	-----------	--------

Sm <sup>13+</sup>	5s <sup>2</sup> 4f <sup>2</sup> F <sub>5/2</sub>	0				
	5s <sup>2</sup> 4f <sup>2</sup> F <sub>7/2</sub>	6 203	5 654	1.8	1612	0.367
	4f <sup>2</sup> 5s <sup>4</sup> H <sub>7/2</sub>	20 254	123 621	12	494	0.133

*Cf <sup>15+</sup>	5f6p <sup>2</sup> F <sub>5/2</sub>	0				
	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	12 898	380 000	59	775	6900
	5f6p <sup>2</sup> F <sub>7/2</sub>	22 018			454	0.012
*Es <sup>16+</sup>	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>					
	5f <sup>2</sup> 6p <sup>2</sup> F <sub>5/2</sub>				-53	1430
	5f <sup>3</sup> 2H <sub>9/2</sub>					944



# HClIs and variations of $\alpha$

- ✓ Visible range
- ✓ High values of K
- ❖ Other groups
- ❖ Too unstable

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
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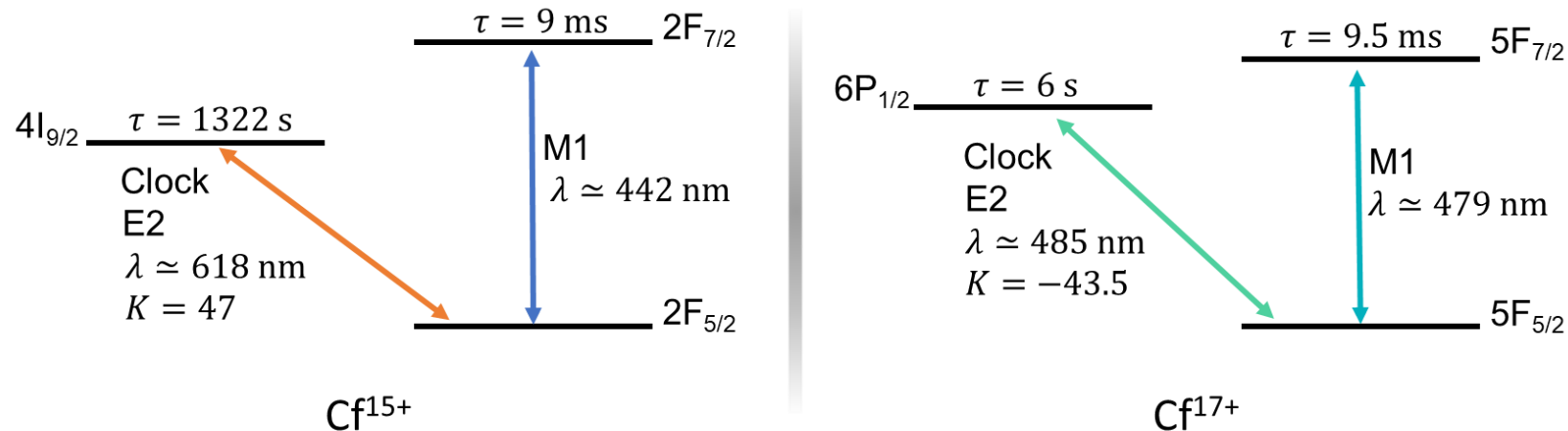
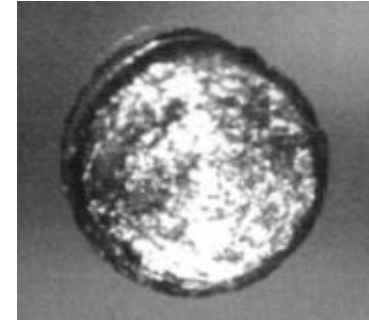
*Cf <sup>17+</sup>	5f <sub>5/2</sub>	0				
	6p <sub>1/2</sub>	18 686	-449 750	-48	535	
	5f <sub>7/2</sub>	21 848	17 900	1.6	458	

Ion	Level	Energy	$q$	$K$	$\lambda$	$\tau$
-----	-------	--------	-----	-----	-----------	--------

*Cf <sup>15+</sup>	5f6p <sup>2</sup> 2F <sub>5/2</sub>	0				
	5f <sup>2</sup> 6p <sup>4</sup> I <sub>9/2</sub>	12 898	380 000	59	775	6900
	5f6p <sup>2</sup> 2F <sub>7/2</sub>	22 018			454	0.012

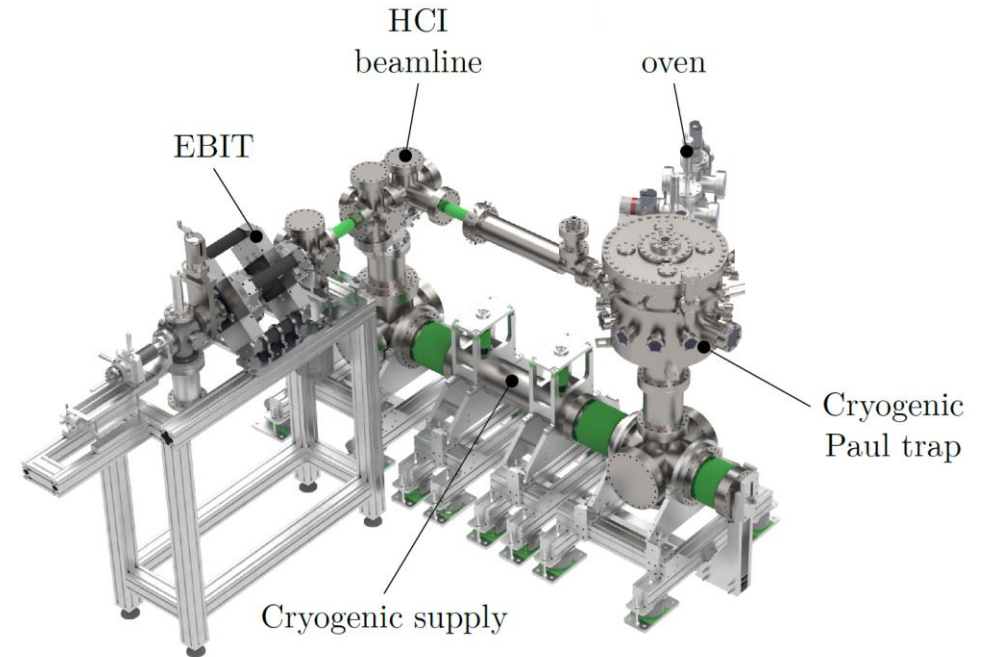
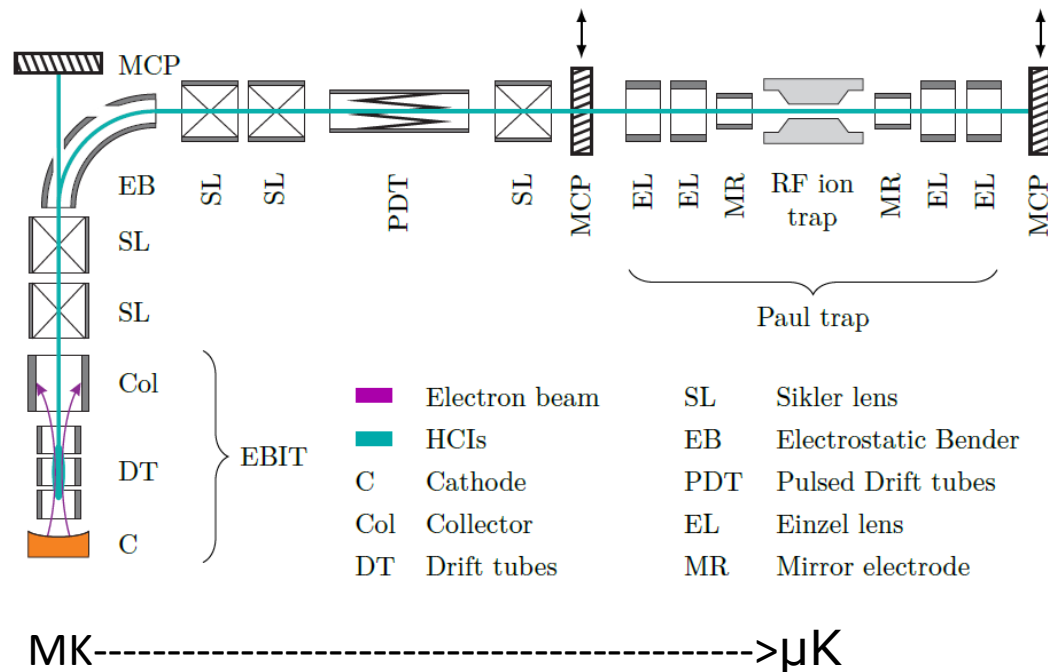
# Cf HCIs

- Cf is a synthetic element produced in reactors
- $^{249}\text{Cf}$  has a half-life of 350 y,  $^{252}\text{Cf}$  of 2650 y
- It costs  $\sim \$7,350,000 / \text{g}$  (!)

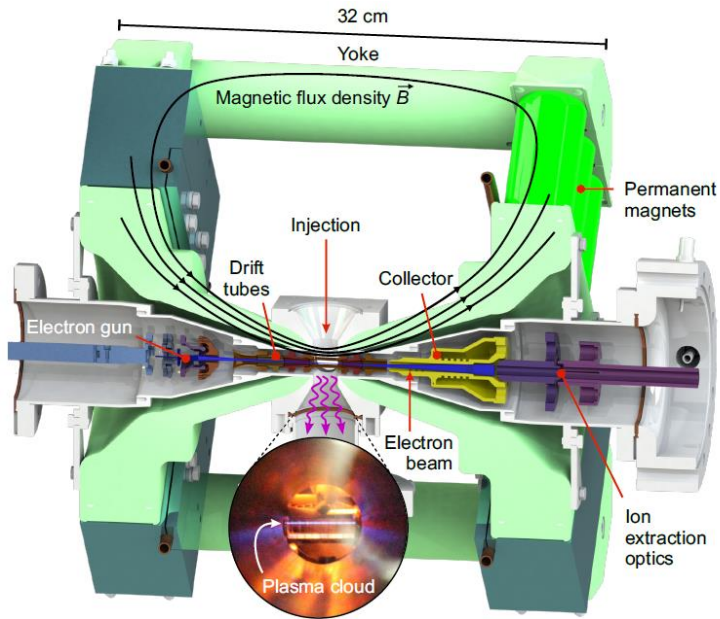


- Both ionisation states feature a clock transition in the visible range and a strong-ish transition also in the visible range
- The two clock transitions have **large Ks with opposite sign**

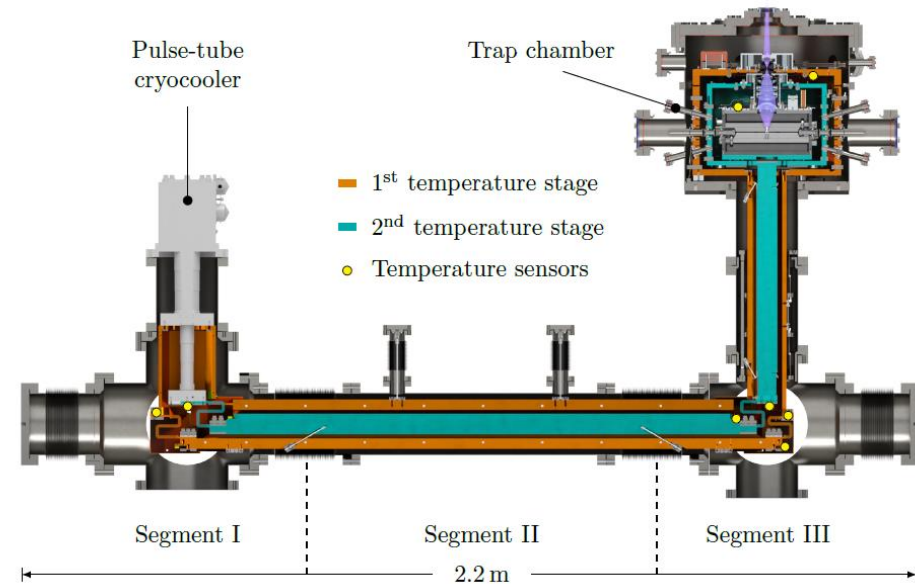
# Production, cooling and trapping of HCl<sup>-</sup>



# Production, cooling and trapping of HCs

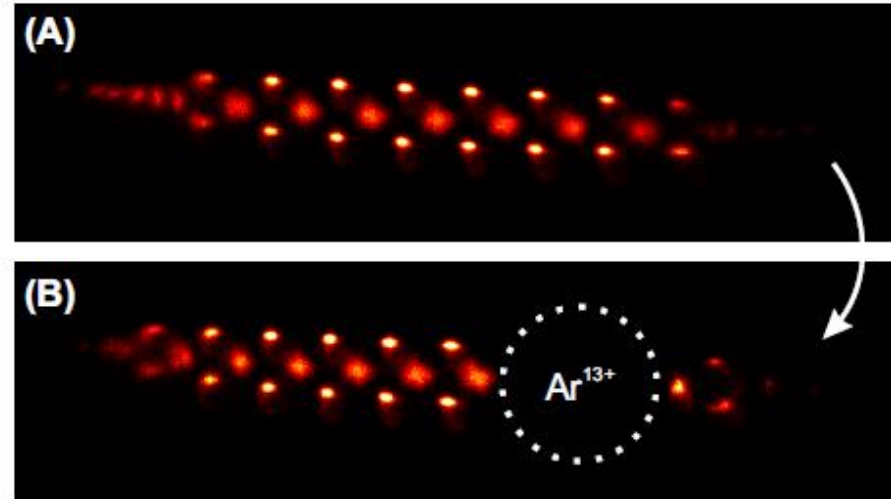


Compact EBIT  
@ MPI Heidelberg



Ultra-low vibration  
cryogenic vacuum

# Production, cooling and trapping of HCl ions



- Once produced and pre-cooled, the ions are implanted into a Coulomb crystal of singly-charged ions
- Sympathetic cooling with the crystal [Science 347 (6227), 1233-1236 (2015)]
- QLS using the co-trapped ions [Nature 578 (7793), 60-65 (2020)]

# QSNET Phenomenology



# Phenomenology

- Coupling of scalar fields with standard matter [EPJ QT 9, 12 (2022)]:

$$\mathcal{L}_{scalar} \supset \frac{\phi^n}{\Lambda_\gamma^n} F_{\mu\nu} F^{\mu\nu} - \sum_f \frac{\phi^n}{\Lambda_f^n} m_f \bar{f} f$$

$\Lambda_\gamma^n$  alter the fine structure constant  $\alpha$ ,  $\Lambda_f^n$  the fermionic masses  $\rightarrow$  manifest as **effective variations of fundamental constants**

- Scalar dark matter models
- Quintessence-like models
- A generic hidden sector scalar field
- Kaluza-Klein models/moduli models
- Dilaton field models
- Soliton models, transient phenomena, cosmic strings, domain walls, and kink solutions

# Scalar dark matter

**Low-mass** spinless bosons may form a coherently oscillating classical field, which in the rest frame is given by:

$$\phi(t) \approx \phi_0 \cos(m_\phi c^2 t / \hbar)$$

This would induce **apparent oscillations** of the fine structure constant and electron mass

$$\frac{d\alpha}{\alpha} \approx \frac{\phi_0 \cos(m_\phi t)}{\Lambda_\gamma}, \quad \frac{dm_e}{m_e} \approx \frac{\phi_0 \cos(m_\phi t)}{\Lambda_e}$$

$$\frac{d\alpha}{\alpha} \approx \frac{\phi_0^2 \cos^2(m_\phi t)}{(\Lambda'_\gamma)^2}, \quad \frac{dm_e}{m_e} \approx \frac{\phi_0^2 \cos^2(m_\phi t)}{(\Lambda'_e)^2}$$

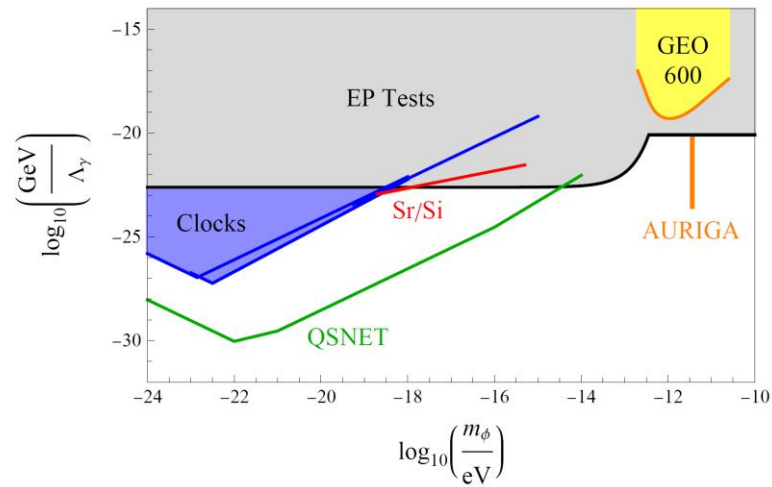
Therefore we would observe atomic frequencies undergoing small oscillations in time around their mean value:

$$\frac{dR}{R} = (K_{X,1} - K_{X,2}) \frac{dX}{X} \propto (K_{X,1} - K_{X,2}) \cos(2\pi f_{\text{signal}} t)$$

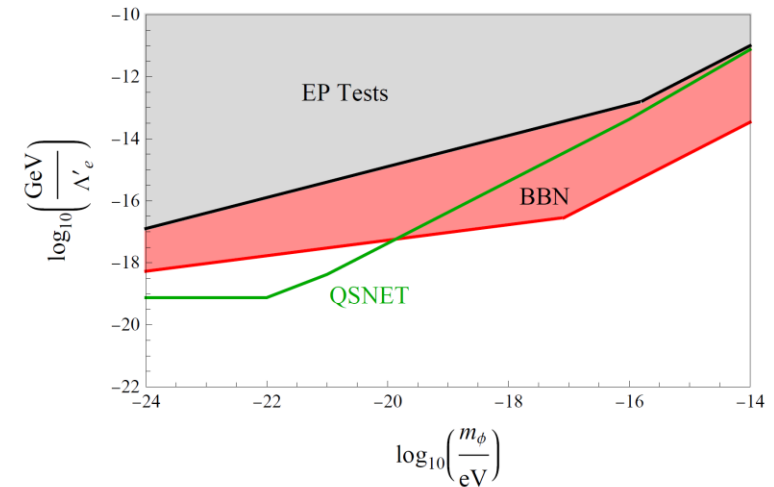
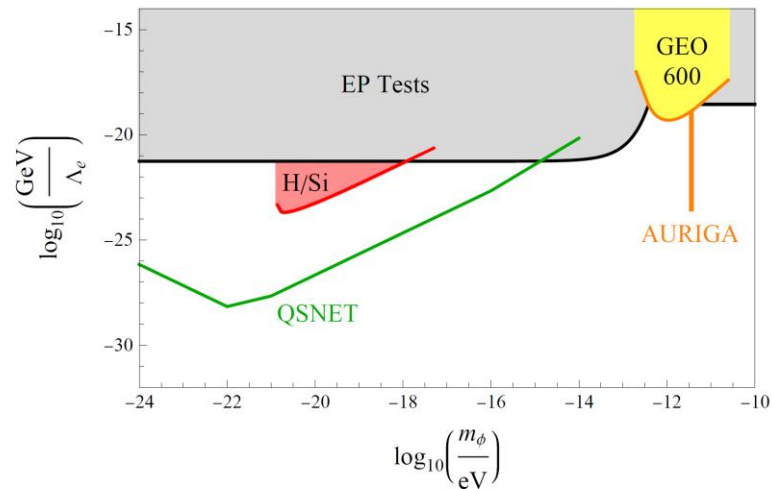
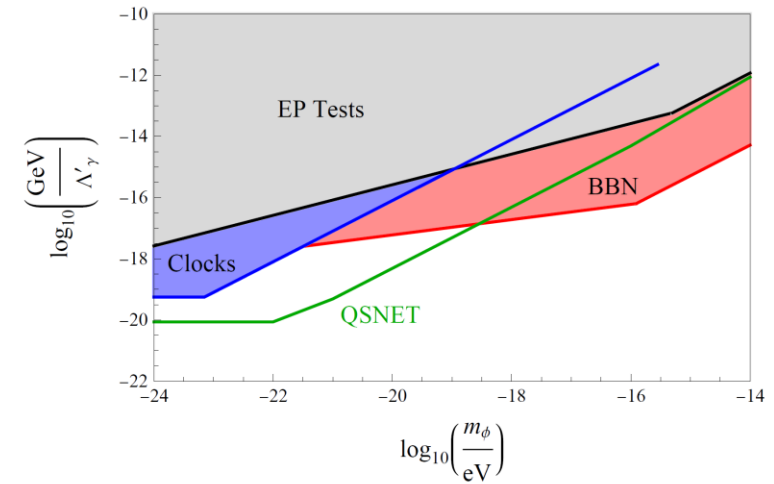


# Scalar dark matter

Linear



Quadratic



# Dark energy

Dark energy, usually in the form of a cosmological constant, is postulated to explain the observed accelerated expansion of the universe.

In **quintessence** models, the matter content of the universe consists of radiation, dark matter, visible matter and quintessence, which is a scalar field that evolves on a cosmological time scale.

$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V}{\partial\phi} = \frac{\partial\mathcal{L}_{\text{int}}}{\partial\phi} \longrightarrow \ddot{\phi} + 3H\dot{\phi} + m_{\phi}^2\phi \approx 0$$

- Overdamped regime, very low masses, no appreciable change
- Underdamped regime, large masses, oscillations similar to DM
- Appreciable changes in the scalar field compatible with dark energy occur when  $m_{\phi} \sim H_0 \sim 10^{-33} \text{ eV}$

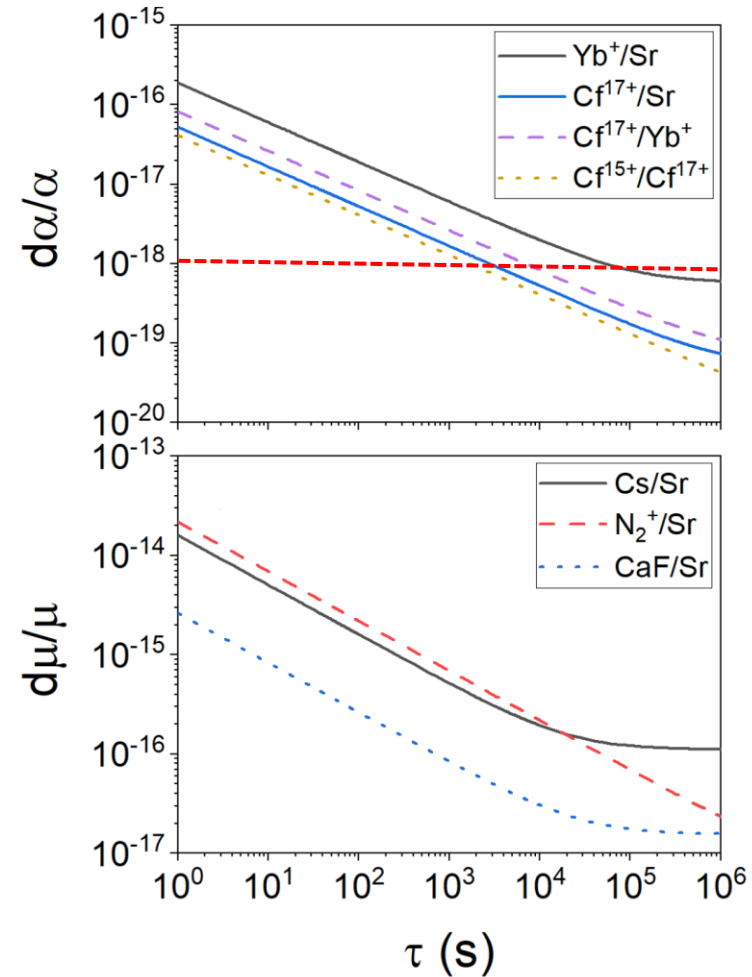
If the quintessence field couples to visible matter, **fundamental constants could be slowly evolving with cosmological time**

# Dark energy

Linear drifts in  $\alpha$

Current limits:

Measurement type	$ d \ln(\alpha)/dt /\text{yr}$
Yb <sup>+</sup> clocks	$\sim 10^{-18}$
Oklo phenomenon	$\sim 10^{-17}$
Meteorite dating	$\sim 10^{-16}$
MICROSCOPE (indirect limits)	$\sim 10^{-17} - 10^{-23}$

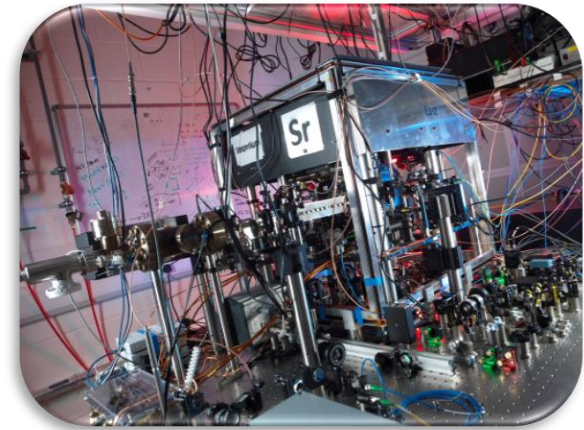
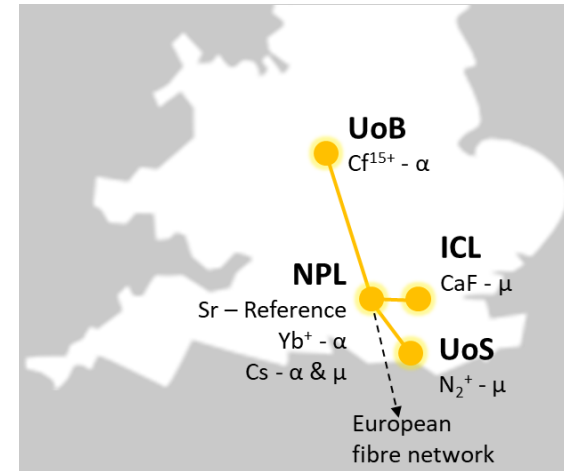


# Other tests [EPJ QT 9, 12 (2022) ]

- Solitons
  - Topological solitons are made up of one or more fields that acquire stability due to the presence of two or more vacua
  - transient events, network is needed
- Violation of fundamental symmetries (Lorentz invariance)
  - Space-time symmetries have been studied in a number of new-physics scenarios, some of these works suggest Lorentz-violating effects may exist and be detectable in experiments with exceptional sensitivity (Cf)
- Grand unification theories
  - QSNET is sensitive both to variations of  $\alpha$  and  $\mu$ , can discriminate between GUTs:  
 $\dot{\mu}/\mu = R \dot{\alpha}/\alpha$ , with  $R$  strongly model dependent
- Quantum gravity
  - If light scalar field is detected, coupling operators between dark and standard matter are not generated by quantum gravity

# Summary

- A new **inter-disciplinary community** gathered around a new (expandable) national infrastructure
- Extending and exploiting **world-class expertise and capabilities** developed in NQTP
- A **unique opportunity for discovery**, improving current limits on variations of  $\alpha$  and  $\mu$  by **orders of magnitude**
  - **Cosmology**
  - **Astrophysics**
  - **High-energy theory**
  - **Fundamental symmetries**
  - ...



# Thanks

- White paper: [EPJ Quantum Technology 9, 12 \(2022\)](#)  
[arXiv:2112.10618]
- Website: [qsnet.org.uk](https://qsnet.org.uk)



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- Quantum systems: [quantumsystemsbrham.wixsite.com](https://quantumsystemsbrham.wixsite.com)
    - Quantum simulations [arXiv:2112.10648]
    - Quantum thermodynamics [arXiv:2204.11816, PRX Quantum tbp]
    - Quantum sensors for neuroscience [NeuroImage tbp]

