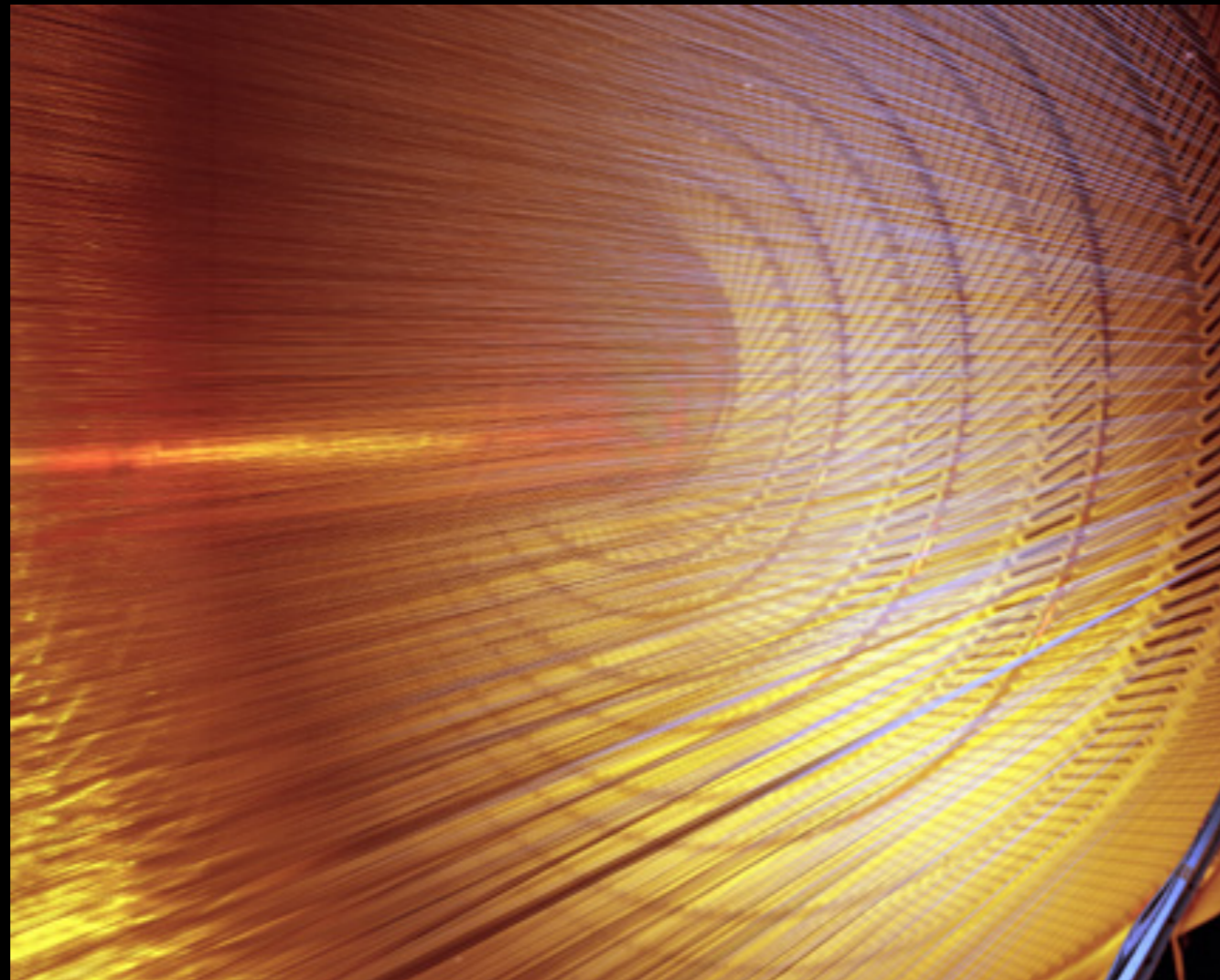


High-precision measurement of the W boson mass with the CDF II detector



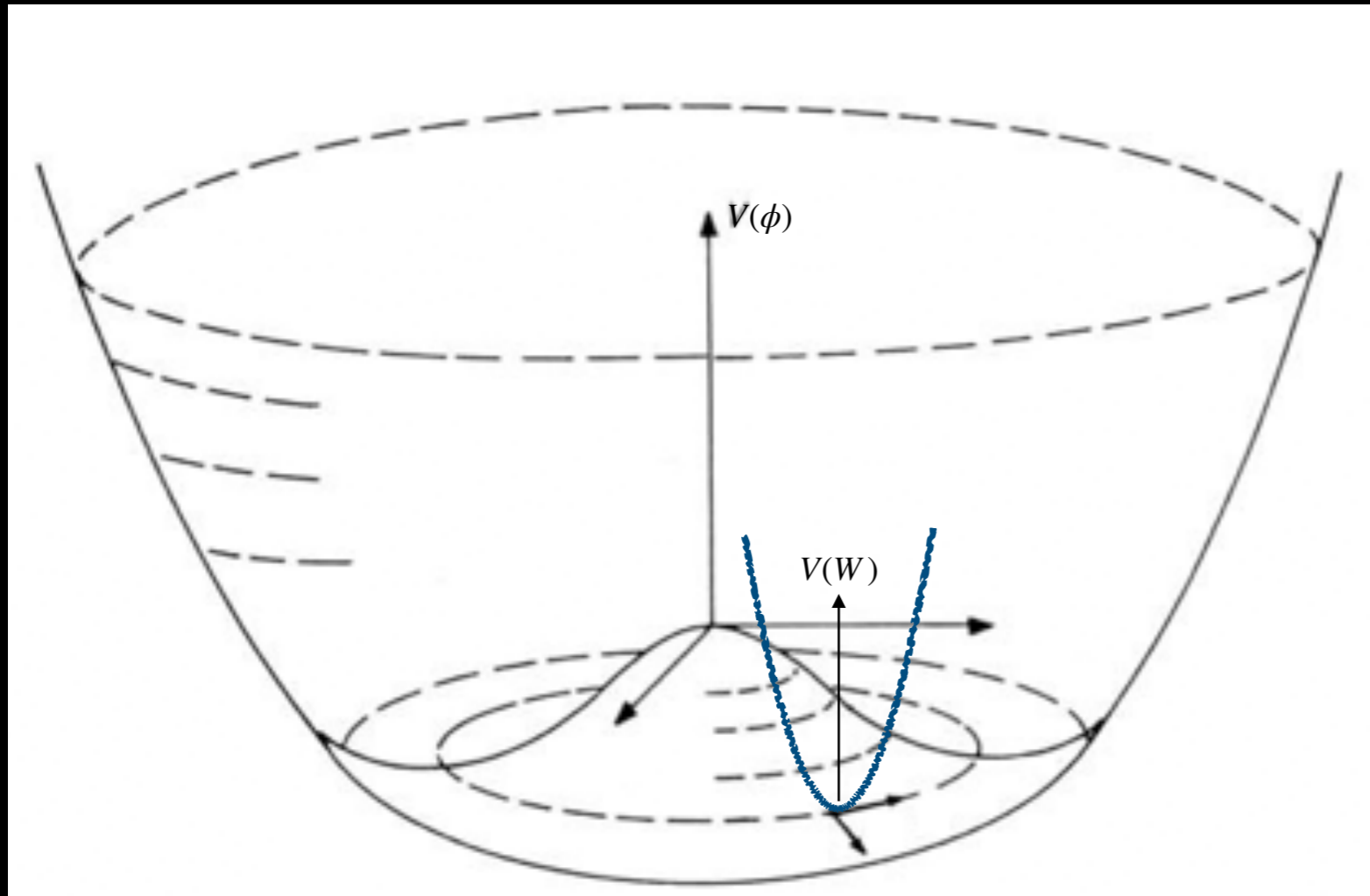
Chris Hays, Oxford University

University of Birmingham seminar
21 September, 2022



Boson masses

Higgs field potential



$$m_H = v\sqrt{2\lambda} = 125 \text{ GeV}$$

$$\lambda \approx 0.1$$

Gauge field potential

$$V = -\frac{g^2 v^2}{8} [(W_\mu^+)^2 + (W_\mu^-)^2] - \frac{v^2 (g^2 + g'^2)}{8} Z^\mu Z_\mu$$

$$m_W = \frac{v}{2} g$$

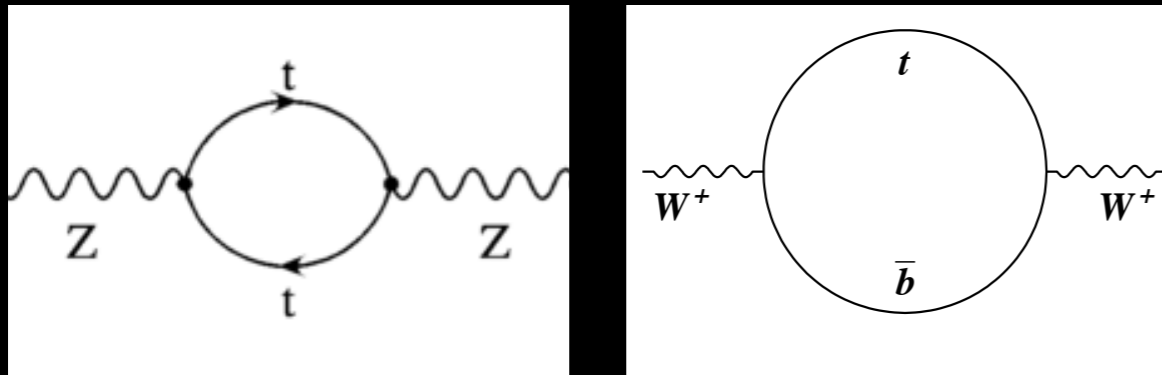
$$m_Z = \frac{v}{2} \sqrt{g^2 + g'^2}$$

$$v = 246 \text{ GeV and } g = 0.64:$$

$$m_W = 78.7 \text{ GeV}$$

Quantum corrections

Gauge quantum corrections



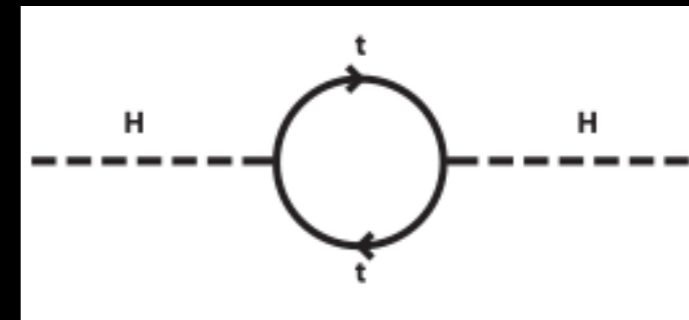
$$m_W^2 = \frac{\hbar^3}{c} \frac{\pi \alpha_{EM}}{\sqrt{2} G_F (1 - m_W^2/m_Z^2) (1 - \Delta r)}$$

$$\Delta r_{tb} = \frac{c}{\hbar^3} \frac{-3G_F m_W^2}{8\sqrt{2}\pi^2(m_Z^2 - m_W^2)} \times \left[m_t^2 + m_b^2 - \frac{2m_t^2 m_b^2}{m_t^2 - m_b^2} \ln(m_t^2/m_b^2) \right]$$

SM calculation of W boson mass yields
81358 ± 4 MeV

Erlar & Freitas
 PDG (2022)

Higgs quantum corrections



Naively integrating to a cutoff scale Λ :

$$\Delta m_H = \frac{3g^2 m_t^2}{16\pi^2 m_W^2} \Lambda^2$$

If there is no new physics up to scale Λ
 then we need 'fine-tuning' to cancel the
 quantum corrections

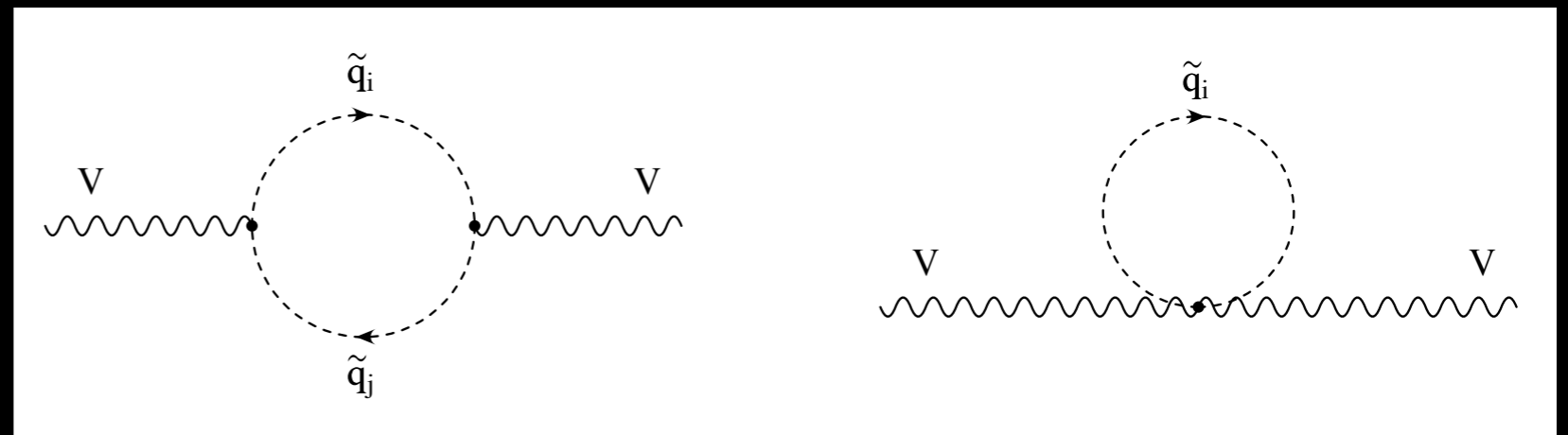
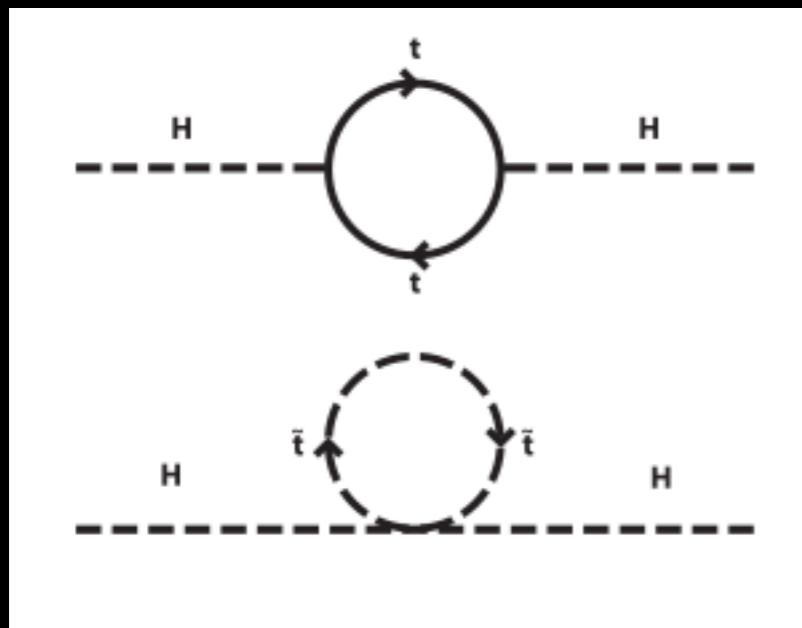
1% fine tuning: $\Lambda = 6.6 \text{ TeV}$

Motivates TeV-scale new physics

W boson mass

The W boson mass is the most sensitive observable to sources of ‘naturalness’

Classic example: **Supersymmetry**



Mass splittings in supersymmetric isospin doublets: **different mass shifts for W & Z bosons**

W boson mass

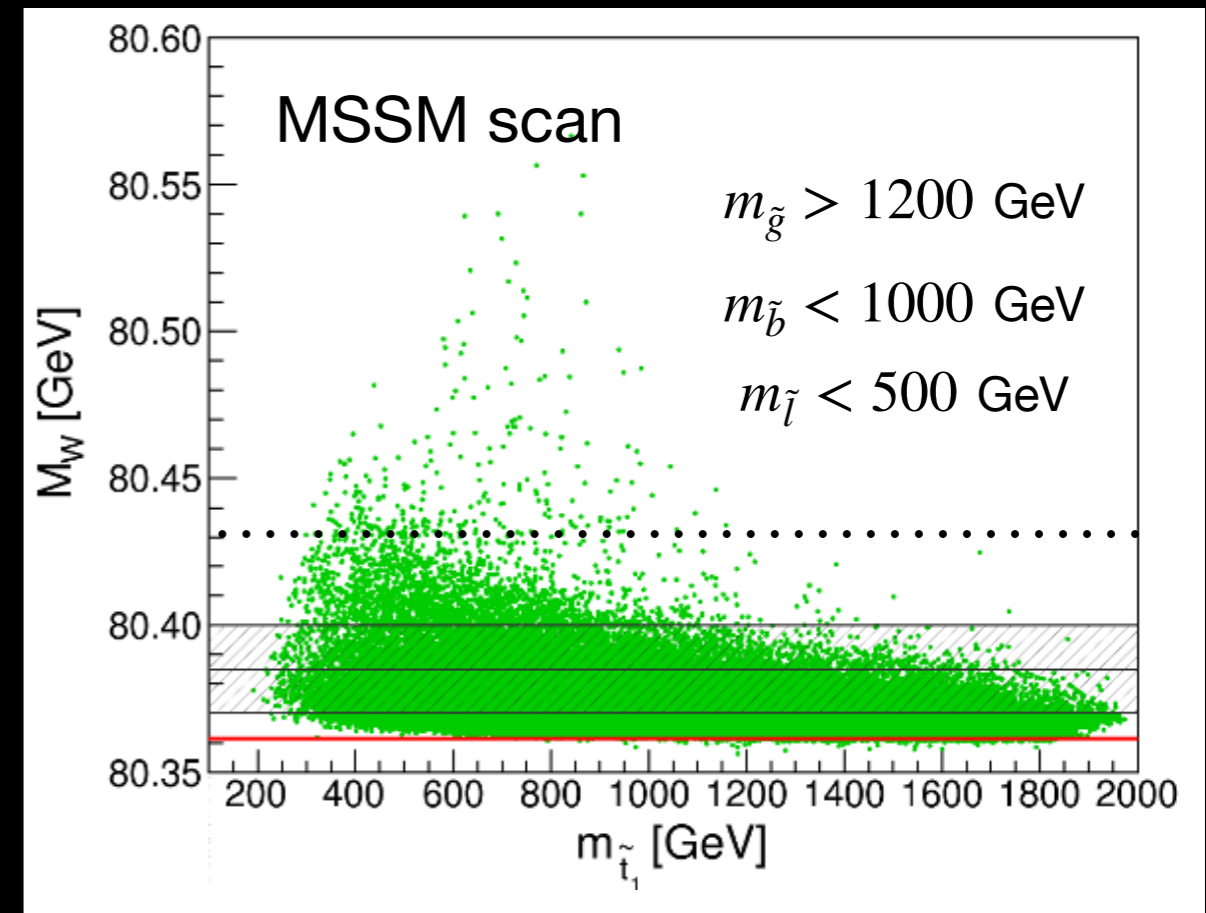
Difference in corrections to W and Z propagators encapsulated by ρ parameter

$$\Delta\rho = \frac{\Sigma^Z(0)}{M_Z^2} - \frac{\Sigma^W(0)}{M_W^2}$$

$$\Delta\rho_0^{\text{SUSY}} = \frac{3G_\mu}{8\sqrt{2}\pi^2} \left[-\sin^2\theta_{\tilde{t}} \cos^2\theta_{\tilde{t}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2) - \sin^2\theta_{\tilde{b}} \cos^2\theta_{\tilde{b}} F_0(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2) \right. \\ \left. + \cos^2\theta_{\tilde{t}} \cos^2\theta_{\tilde{b}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{b}_1}^2) + \cos^2\theta_{\tilde{t}} \sin^2\theta_{\tilde{b}} F_0(m_{\tilde{t}_1}^2, m_{\tilde{b}_2}^2) \right. \\ \left. + \sin^2\theta_{\tilde{t}} \cos^2\theta_{\tilde{b}} F_0(m_{\tilde{t}_2}^2, m_{\tilde{b}_1}^2) + \sin^2\theta_{\tilde{t}} \sin^2\theta_{\tilde{b}} F_0(m_{\tilde{t}_2}^2, m_{\tilde{b}_2}^2) \right].$$

$$\delta M_W \approx \frac{M_W}{2} \frac{c_W^2}{c_W^2 - s_W^2} \Delta\rho$$

Heinemeyer, Hollik, Weiglein
Phys Rep 425, 265 (2006)



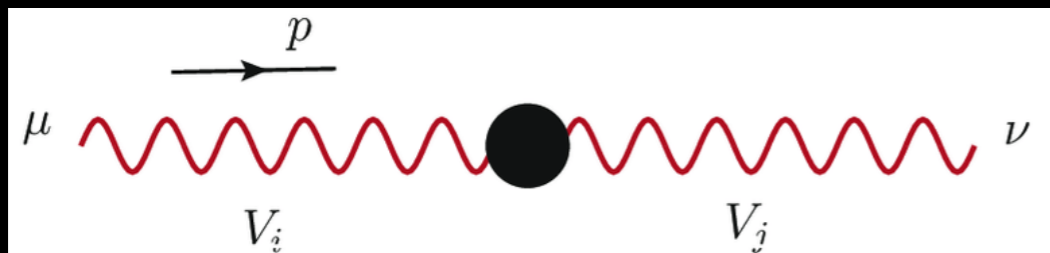
Heinemeyer, Hollik, Weiglein, Zeune
JHEP 12 (2013) 084

W boson mass

More generally the SM effective field theory parameterizes high-scale effects

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \mathcal{L}^{(5)} + \mathcal{L}^{(6)} + \mathcal{L}^{(7)} + \dots, \quad \mathcal{L}^{(d)} = \sum_{i=1}^{n_d} \frac{C_i^{(d)}}{\Lambda^{d-4}} Q_i^{(d)} \quad \text{for } d > 4.$$

I. Brivio and M. Trott,
Phys. Rep. 793 (2019) 1



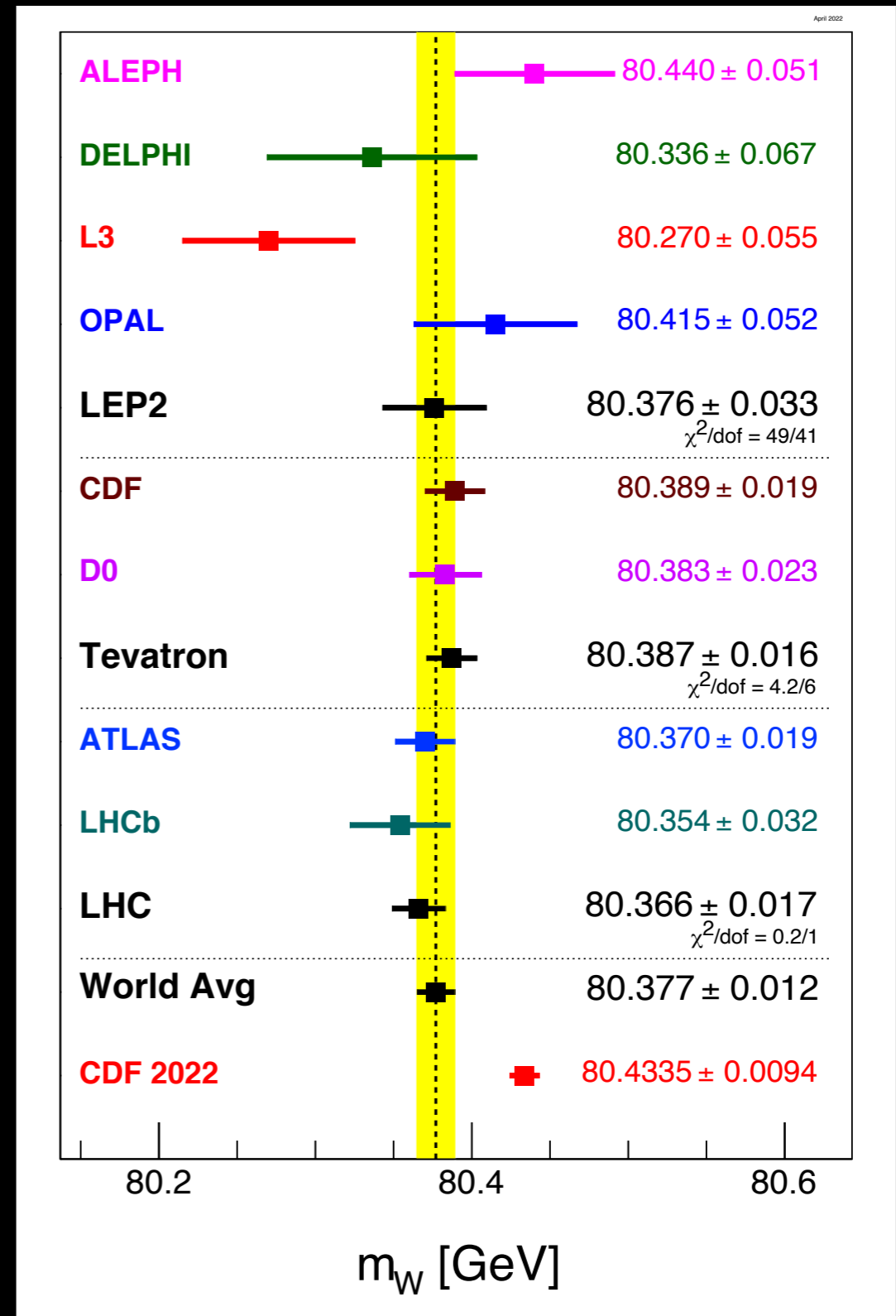
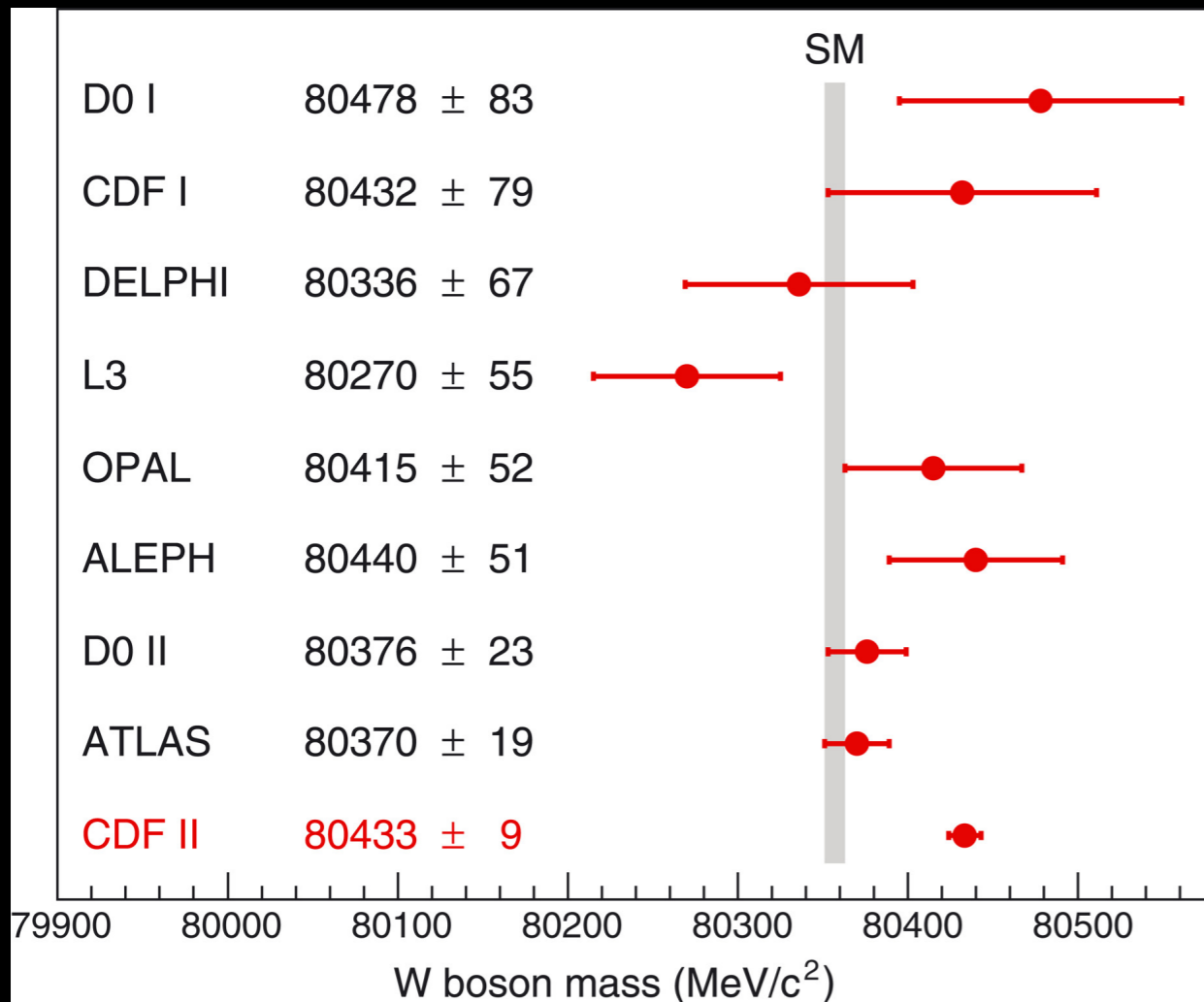
$$\frac{\delta m_W}{m_W} = (0.34c_{HD} + 0.72c_{HWB} + 0.37c_{Hl3} - 0.19c_{ll1}) \frac{v^2}{\Lambda^2}$$

For $\delta m_W/m_W = 0.1\%$ and $c_{HD}=1$, $\Lambda = 4.5$ TeV
e.g. Z' boson

For $\delta m_W/m_W = 0.1\%$ and $c_{HWB}=1$, $\Lambda = 6.6$ TeV
e.g. compositeness

Smaller $c_i \rightarrow$ smaller Λ

W boson mass measurements



CDF II measurement of the W boson mass



$\sqrt{s} = 1.96$ TeV proton-antiproton collisions from the Fermilab Tevatron

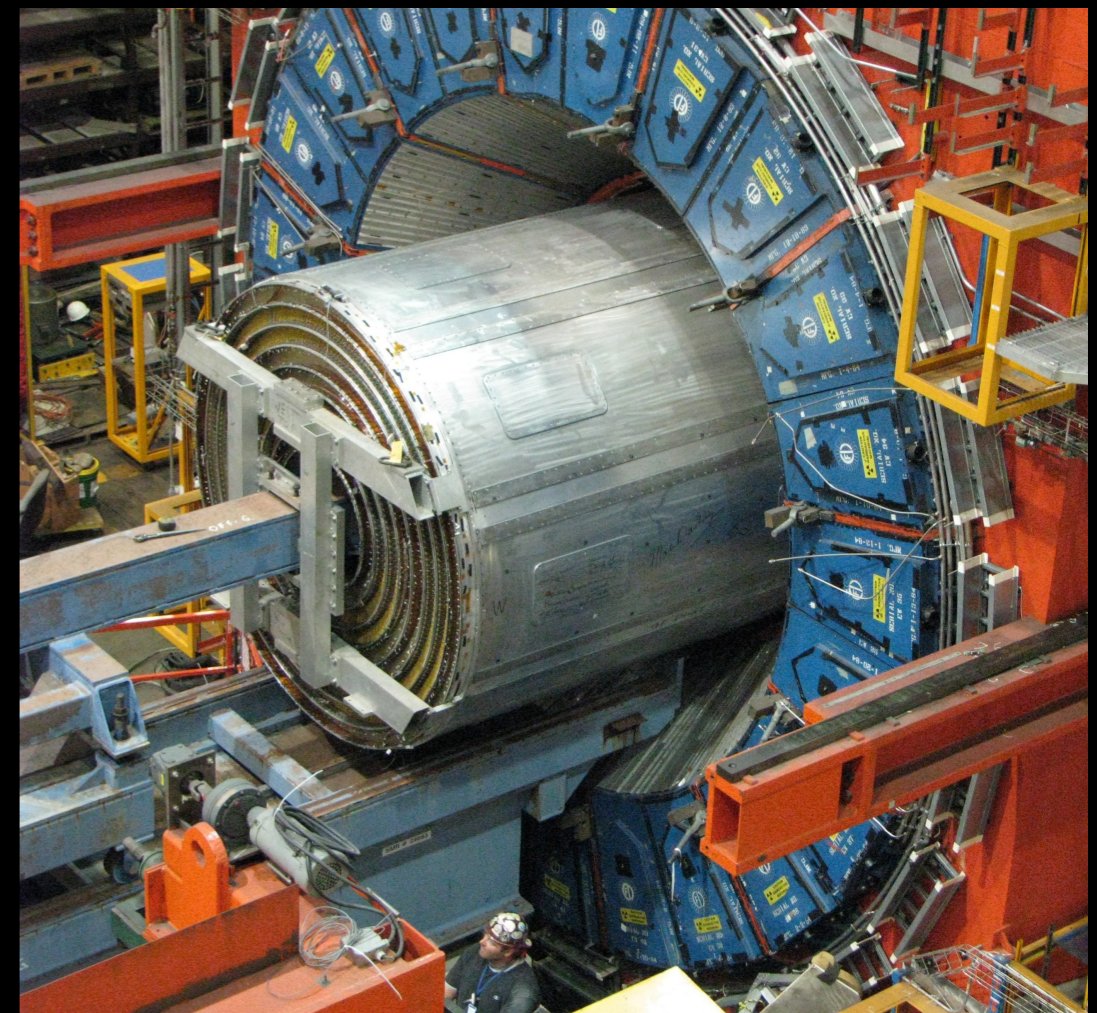
CDF II detector consists of

silicon vertex detector

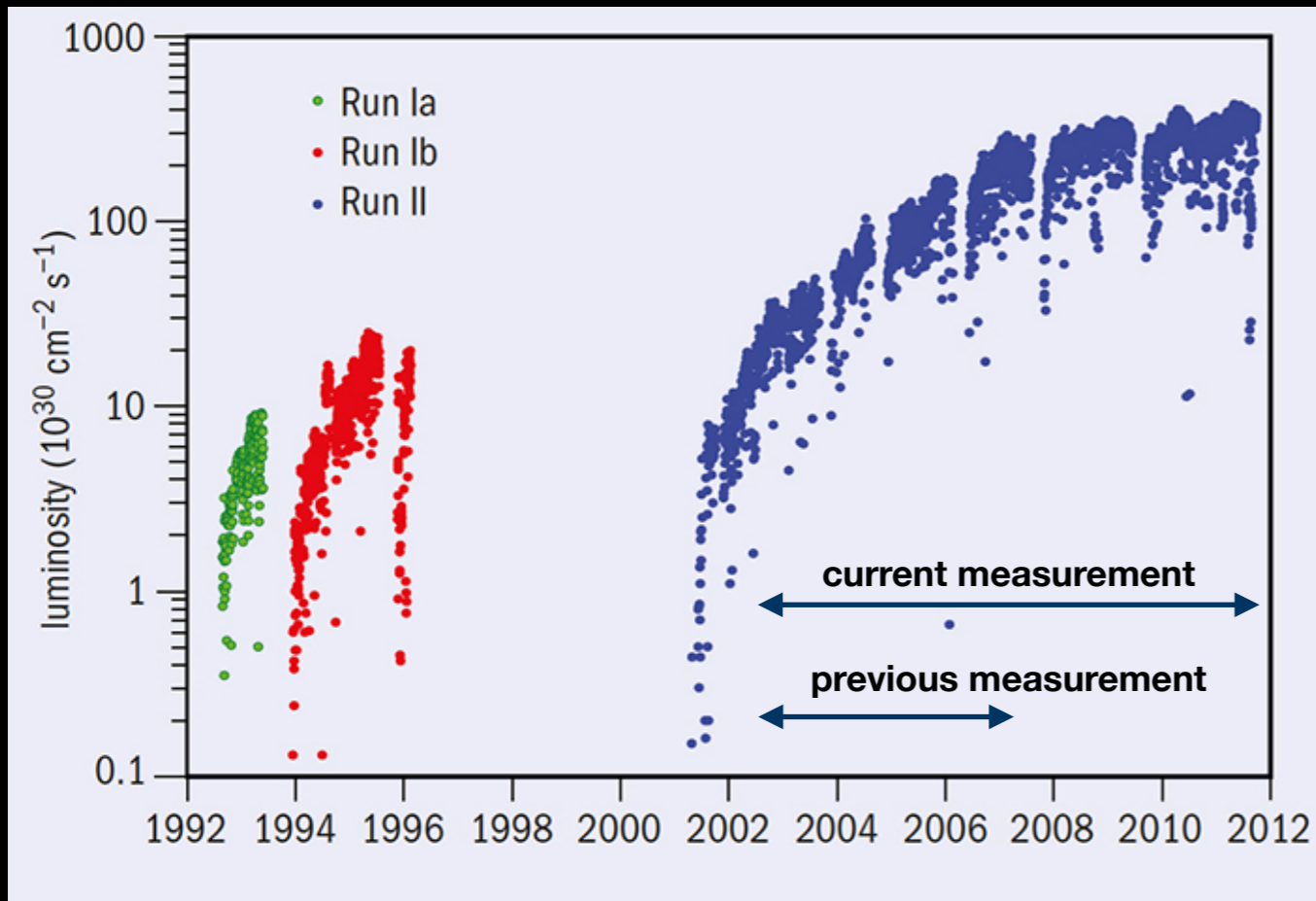
large drift chamber

coarse calorimeter towers

outer muon chambers



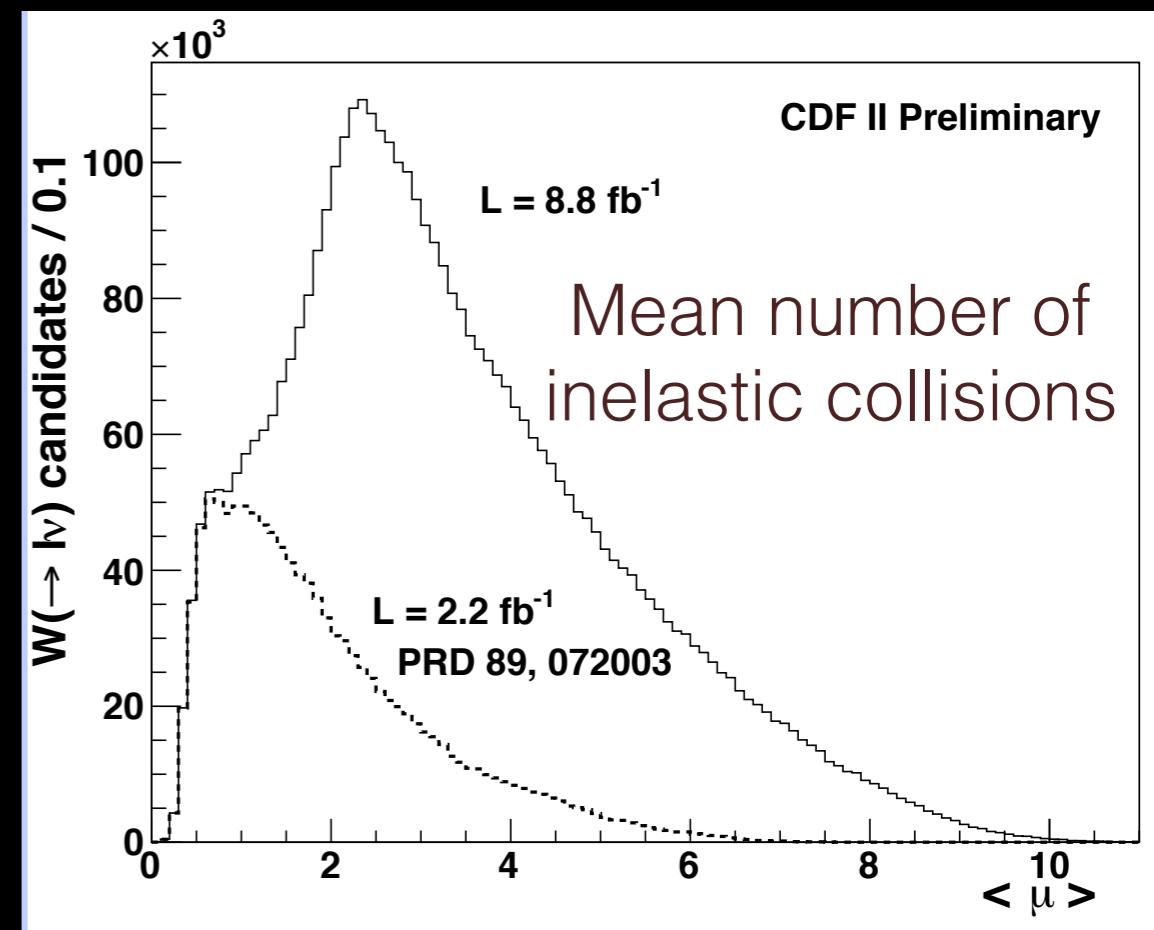
CDF II measurement of the W boson mass



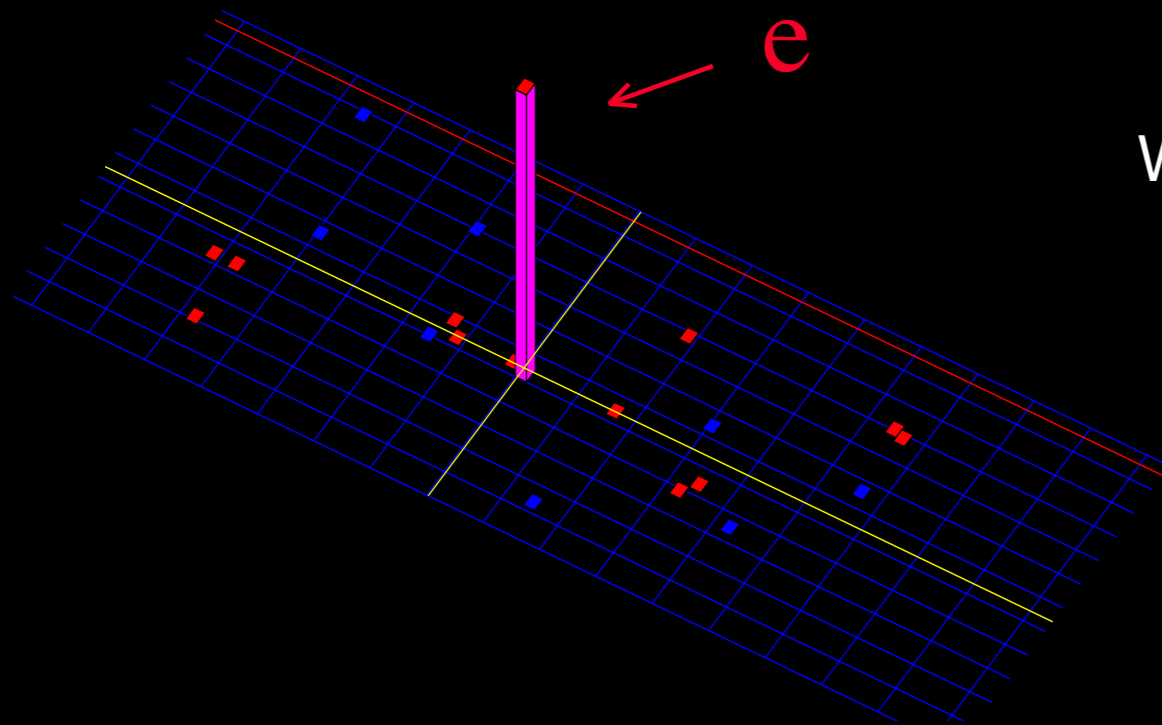
4x the integrated luminosity of the previous measurement

Higher $\langle \mu \rangle$: peaks at 3

Measurement uses complete Tevatron Run II data set



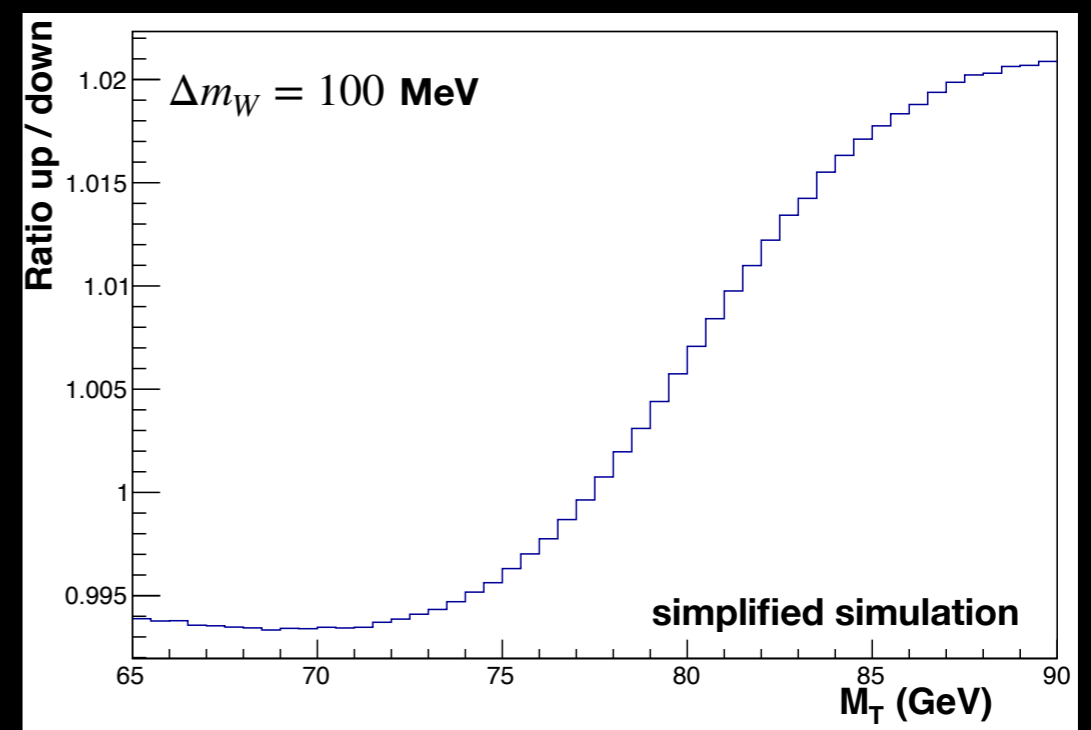
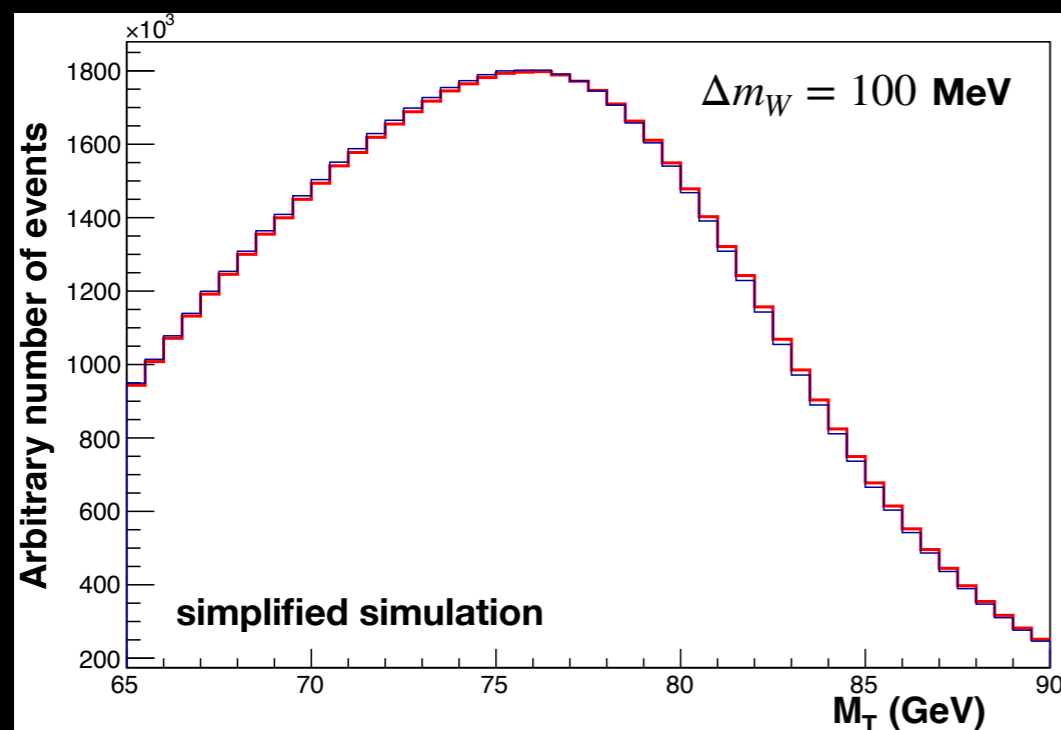
CDF II measurement of the W boson mass



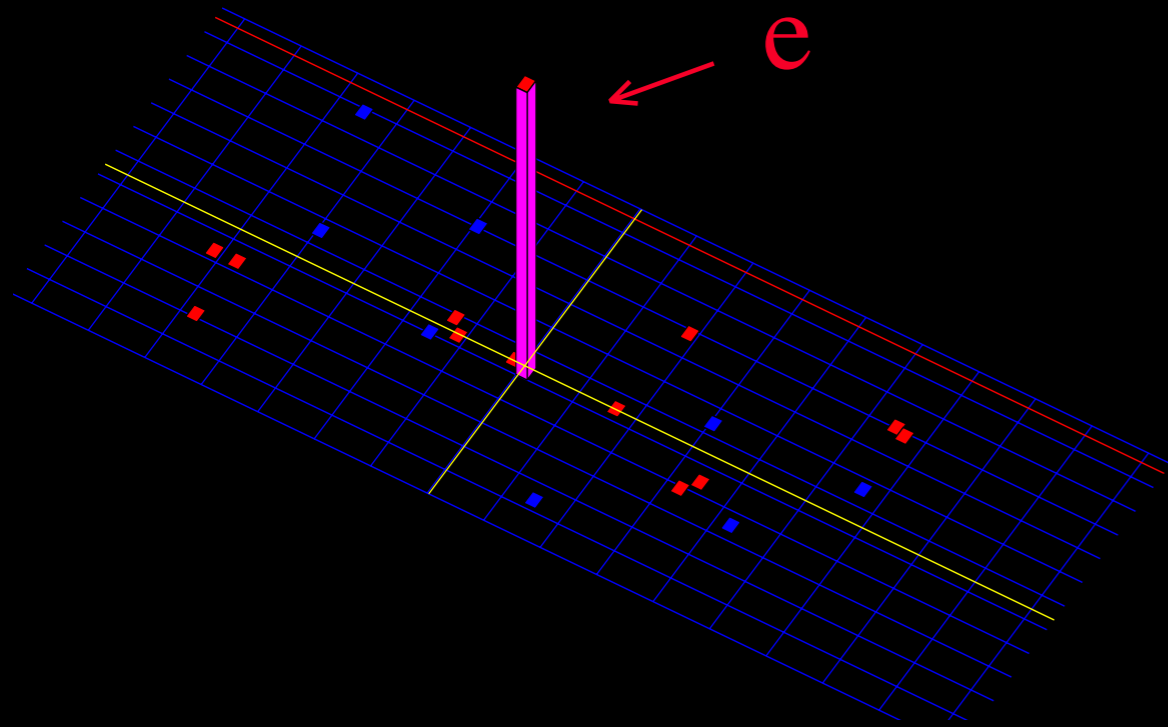
W bosons identified from their decays to $e\nu$ and $\mu\nu$

Mass measured by fitting template distributions of transverse momentum and mass

$$m_T = \sqrt{2p_T^l p_T (1 - \cos \Delta\phi)}$$

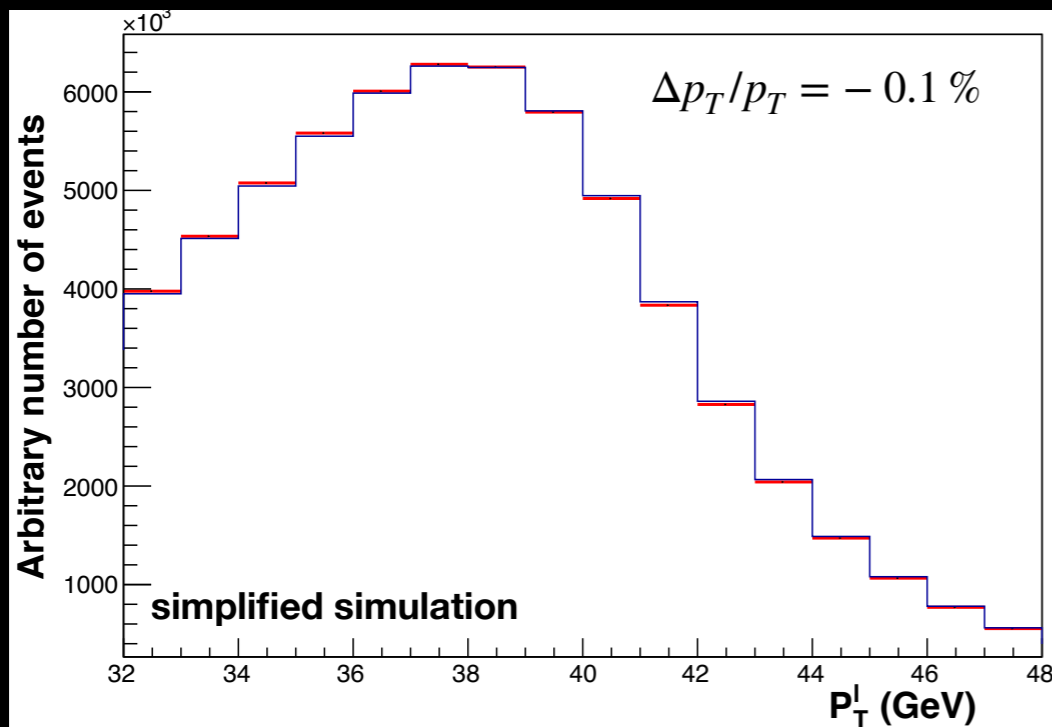


Calibrations

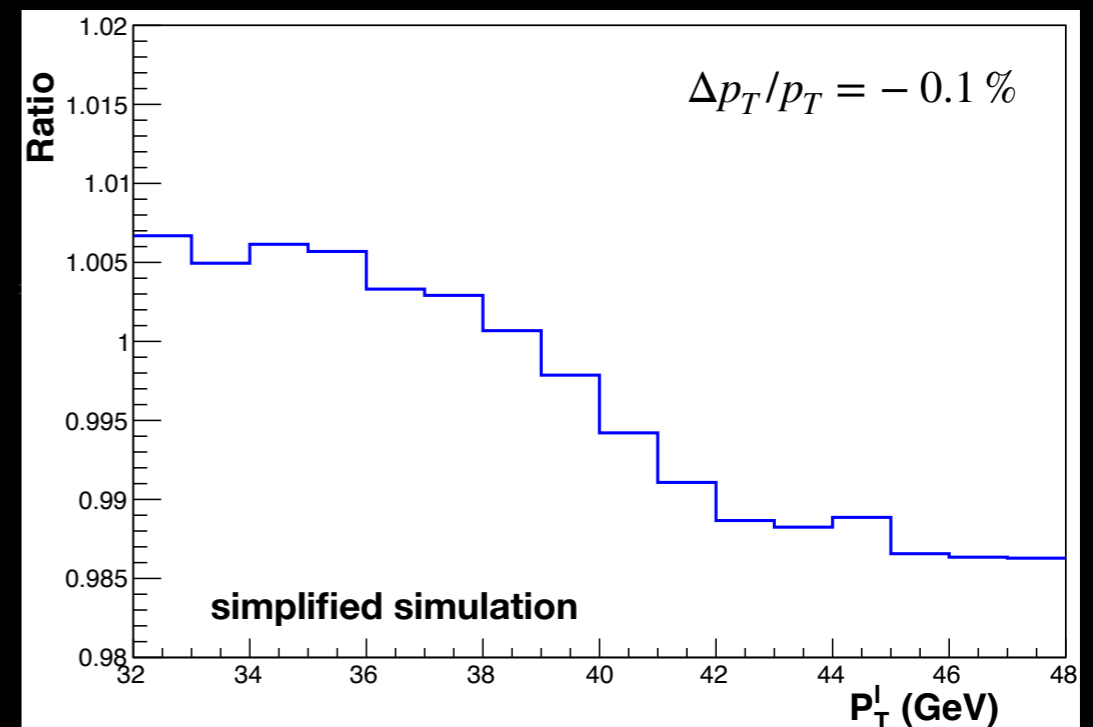


Measurement requires precise calibrations and momentum scale and resolution

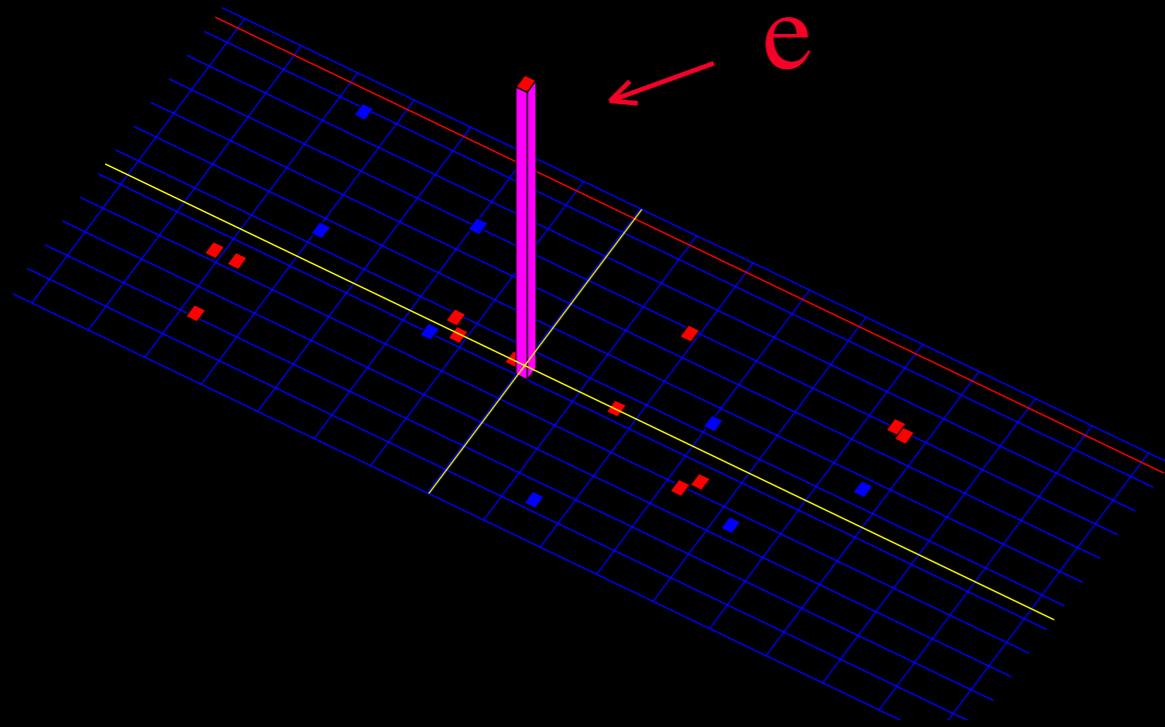
Charged lepton scale



$|m_{\beta\beta}|$



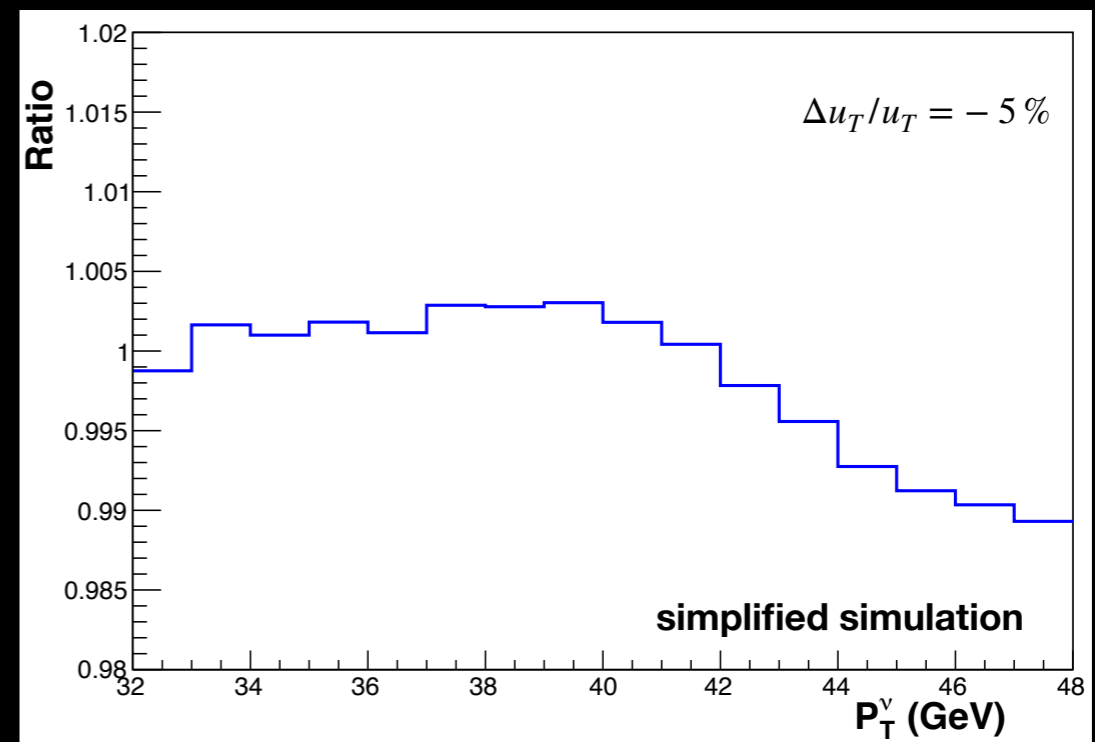
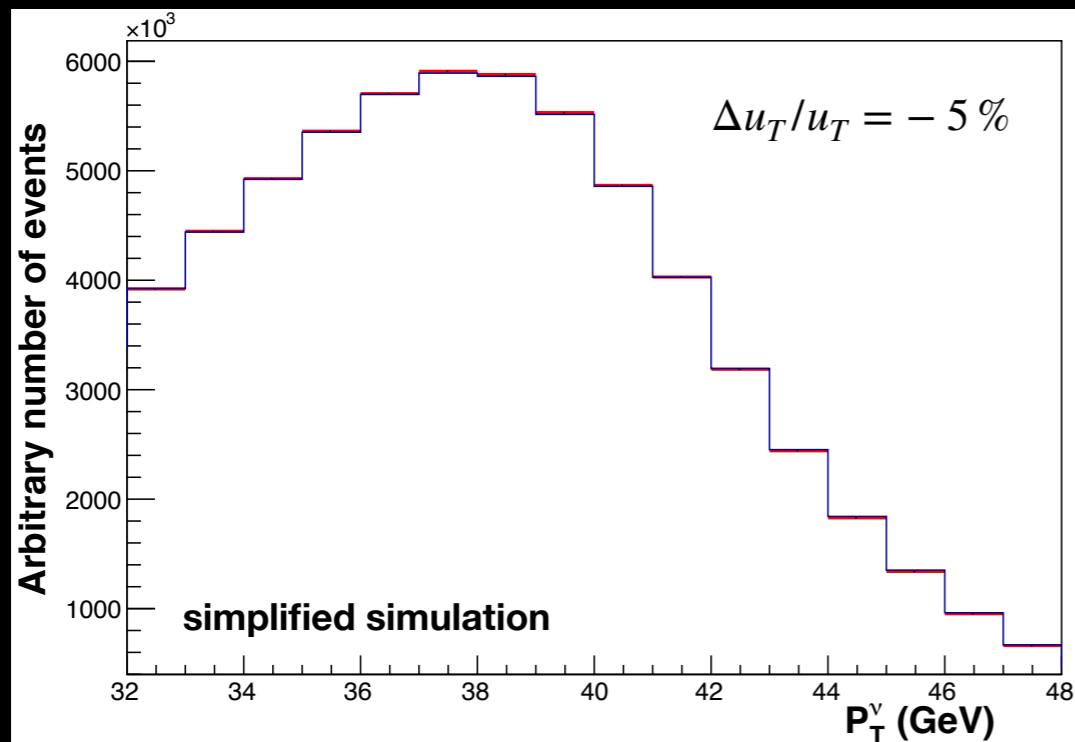
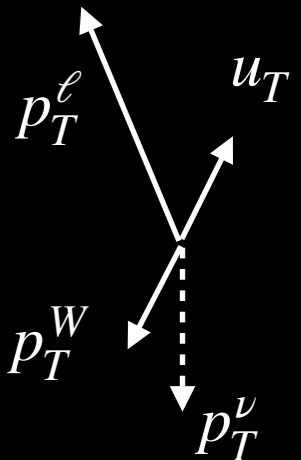
Calibrations



Measurement requires precise calibrations and momentum scale and resolution

$$\vec{p}_T = -(\vec{p}_T^l + \vec{u}_T)$$

Recoil scale



Detector simulation

Developed custom simulation for analysis

Models ionization energy loss, multiple scattering, bremsstrahlung, photon conversion, Compton scattering

Acceptance map for muon detectors

Parameterized GEANT4 model of electromagnetic calorimeter showers

Includes shower losses due to finite calorimeter thickness

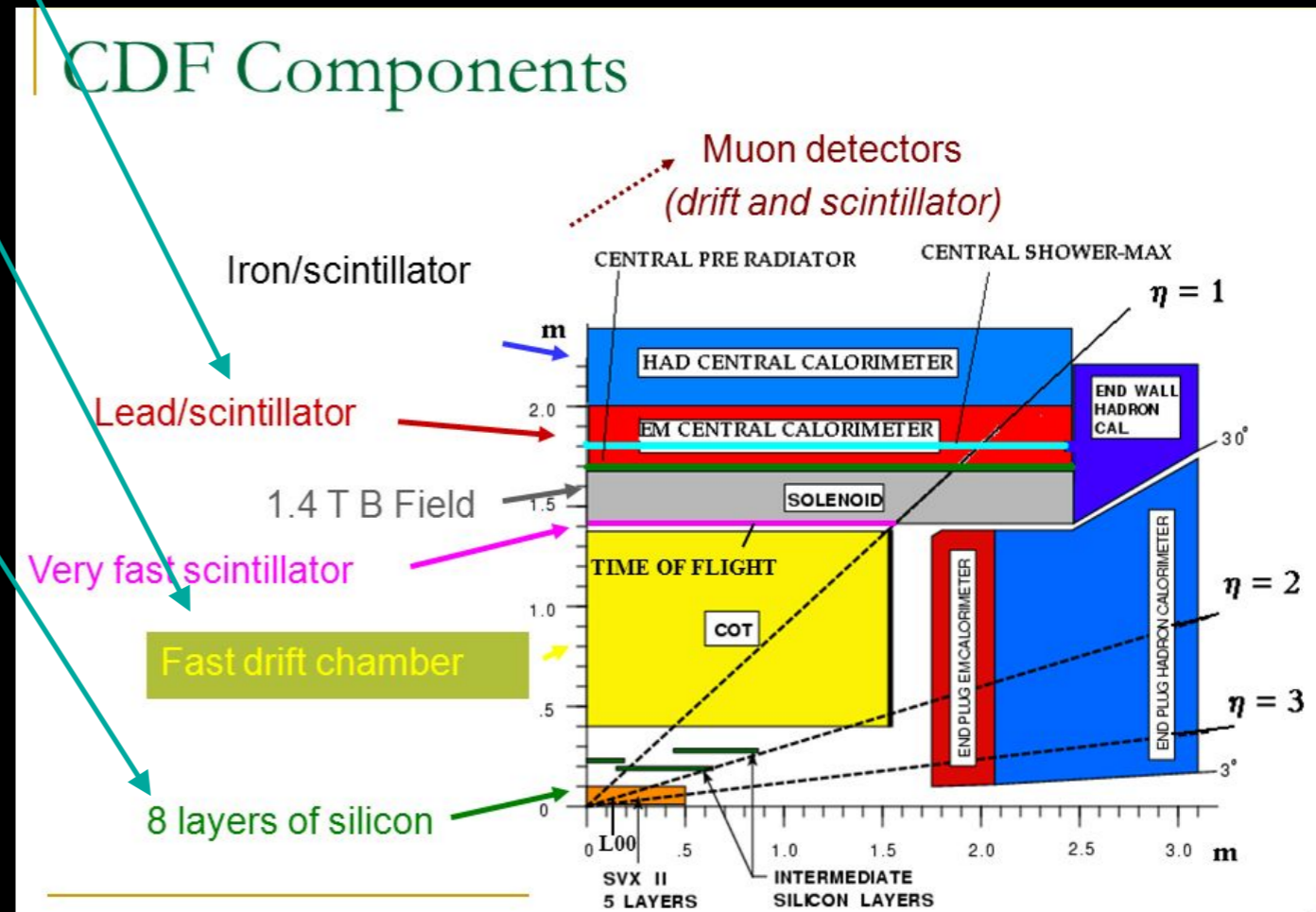
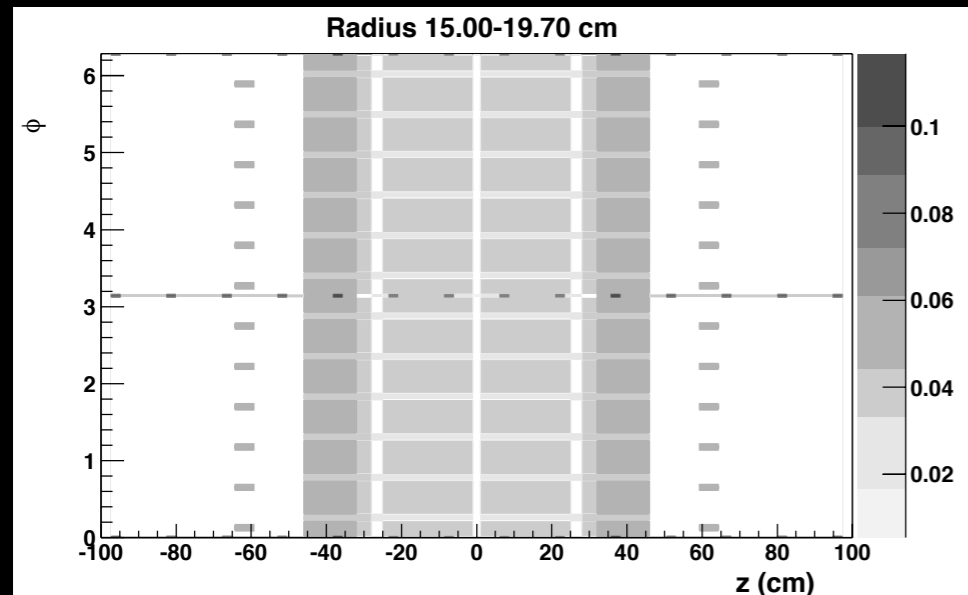
Hit-level model of central outer tracker

Layer-by-layer resolution functions and efficiencies

Material map of inner silicon detector

Includes radiation lengths and Bethe-Bloch terms

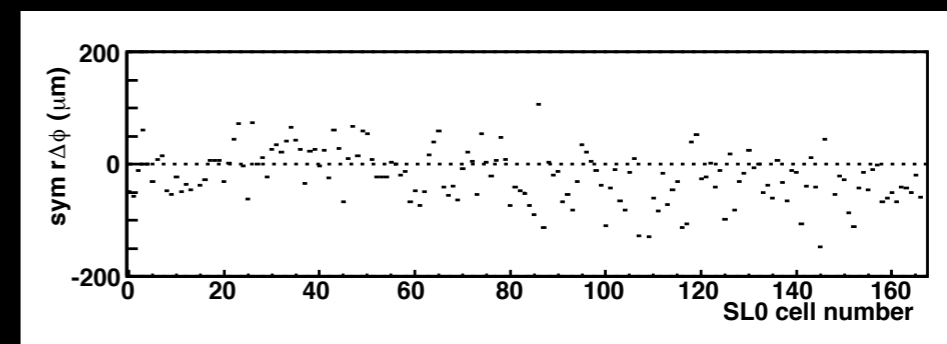
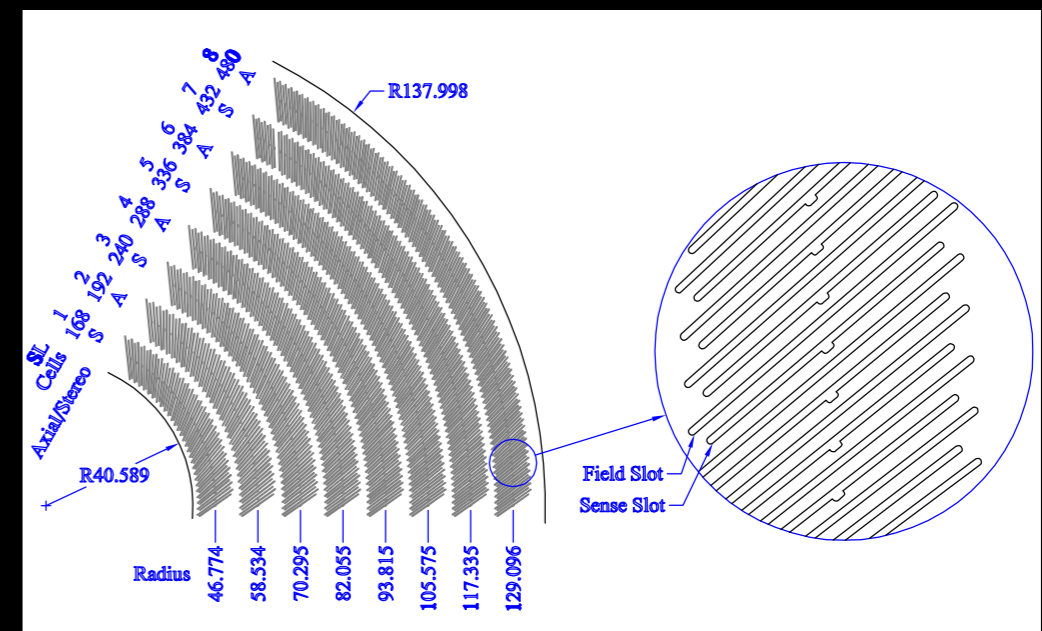
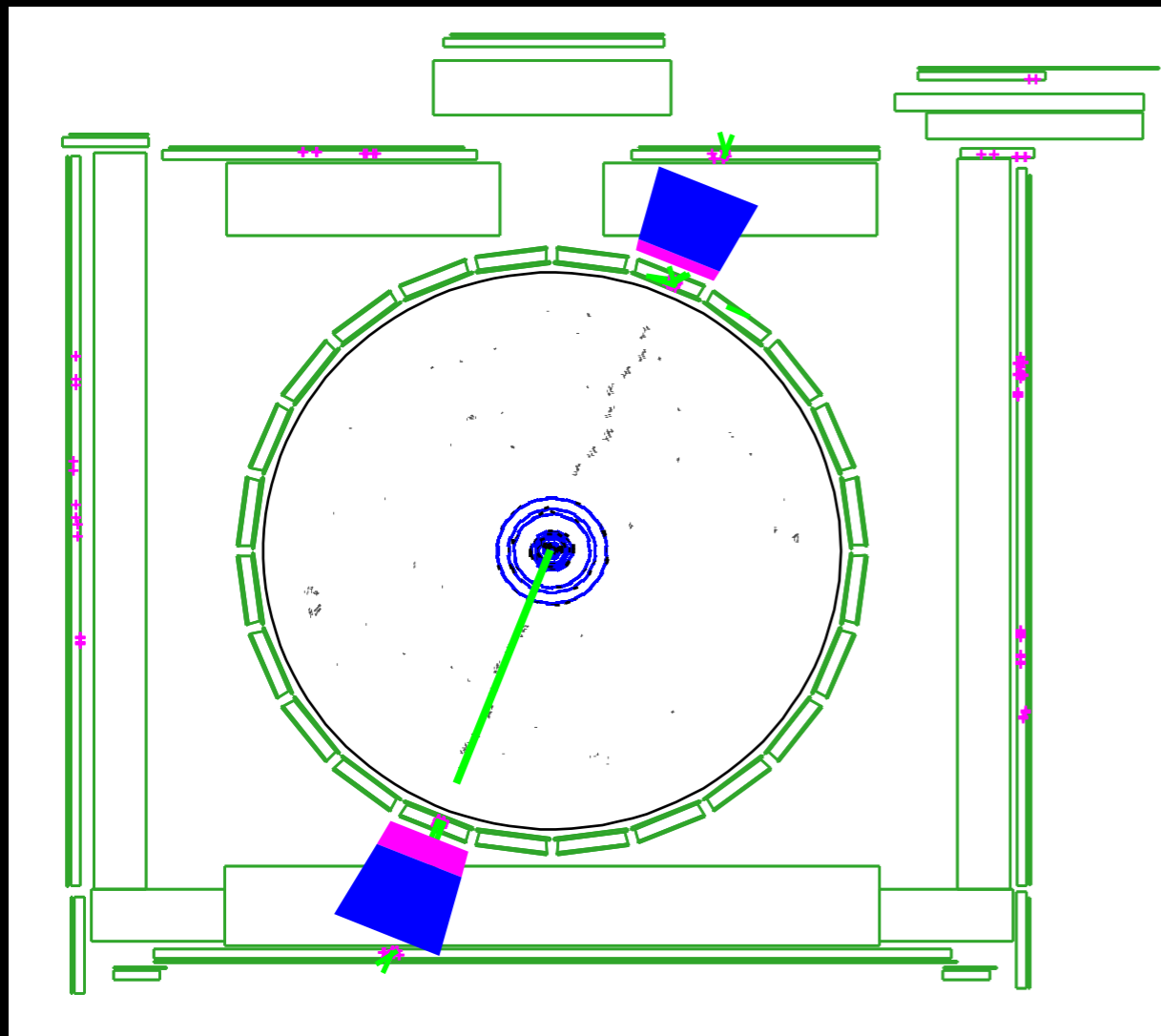
Kotwal & CH, NIMA 729, 25 (2013)



Muon momentum calibration

First step is to align the drift chamber (the “central outer tracker” or COT)

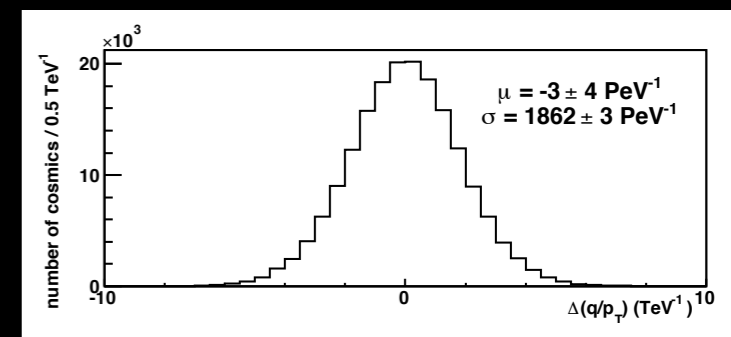
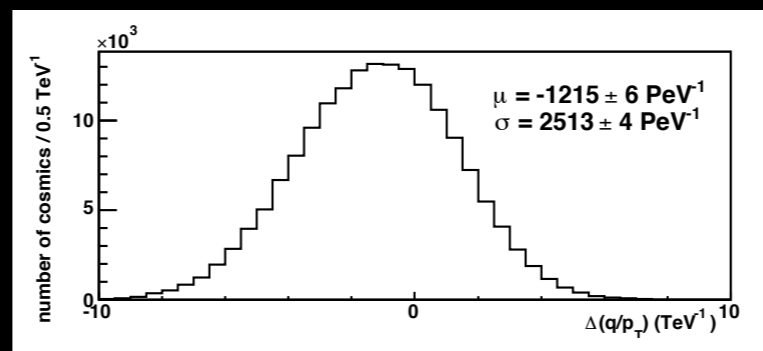
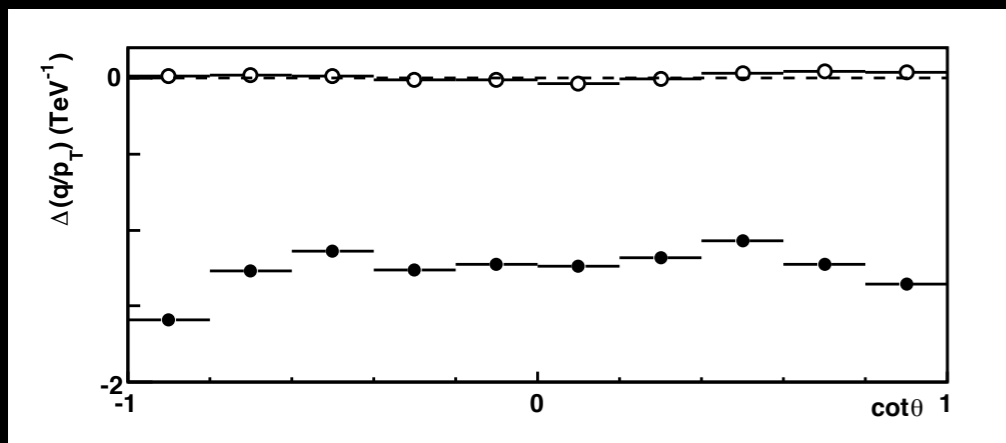
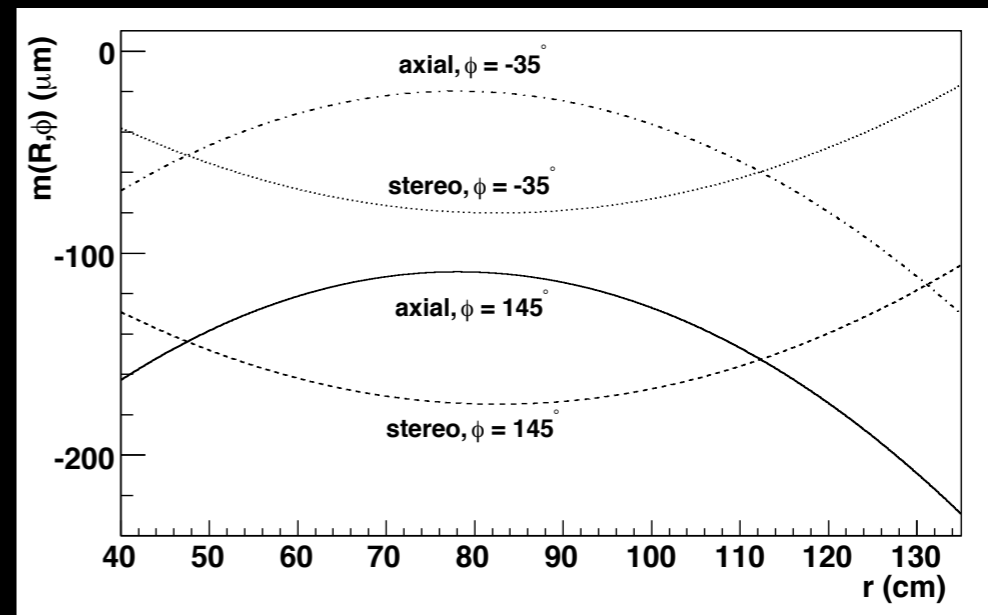
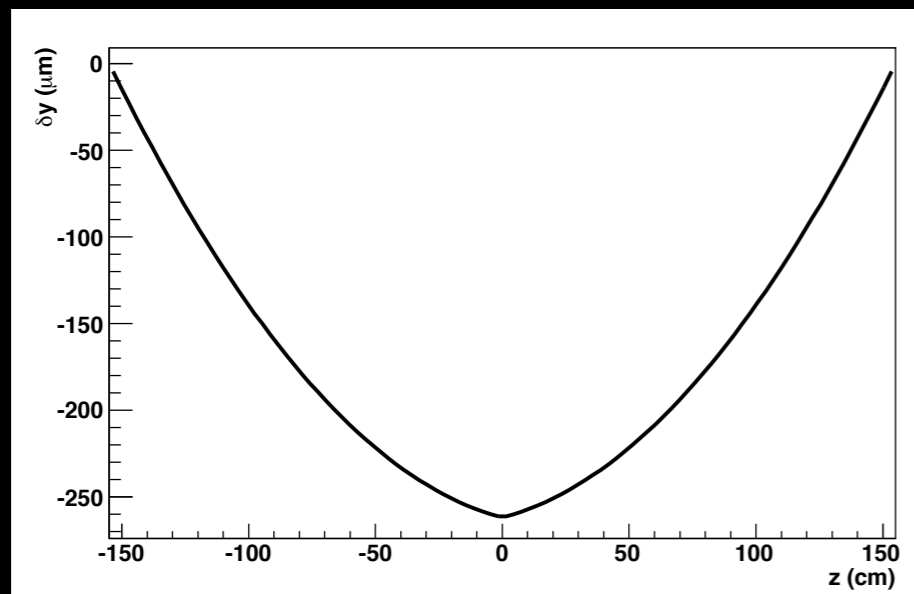
Two degrees of freedom (shift & rotation) for each of 2520 cells made up of twelve sense wires constrained using hit residuals from cosmic-ray tracks



Muon momentum calibration

First step is to align the drift chamber (the “central outer tracker” or COT)

Two parameters for the electrostatic deflection of the wire within the chamber constrained using difference between fit parameters of incoming and outgoing cosmic-ray tracks



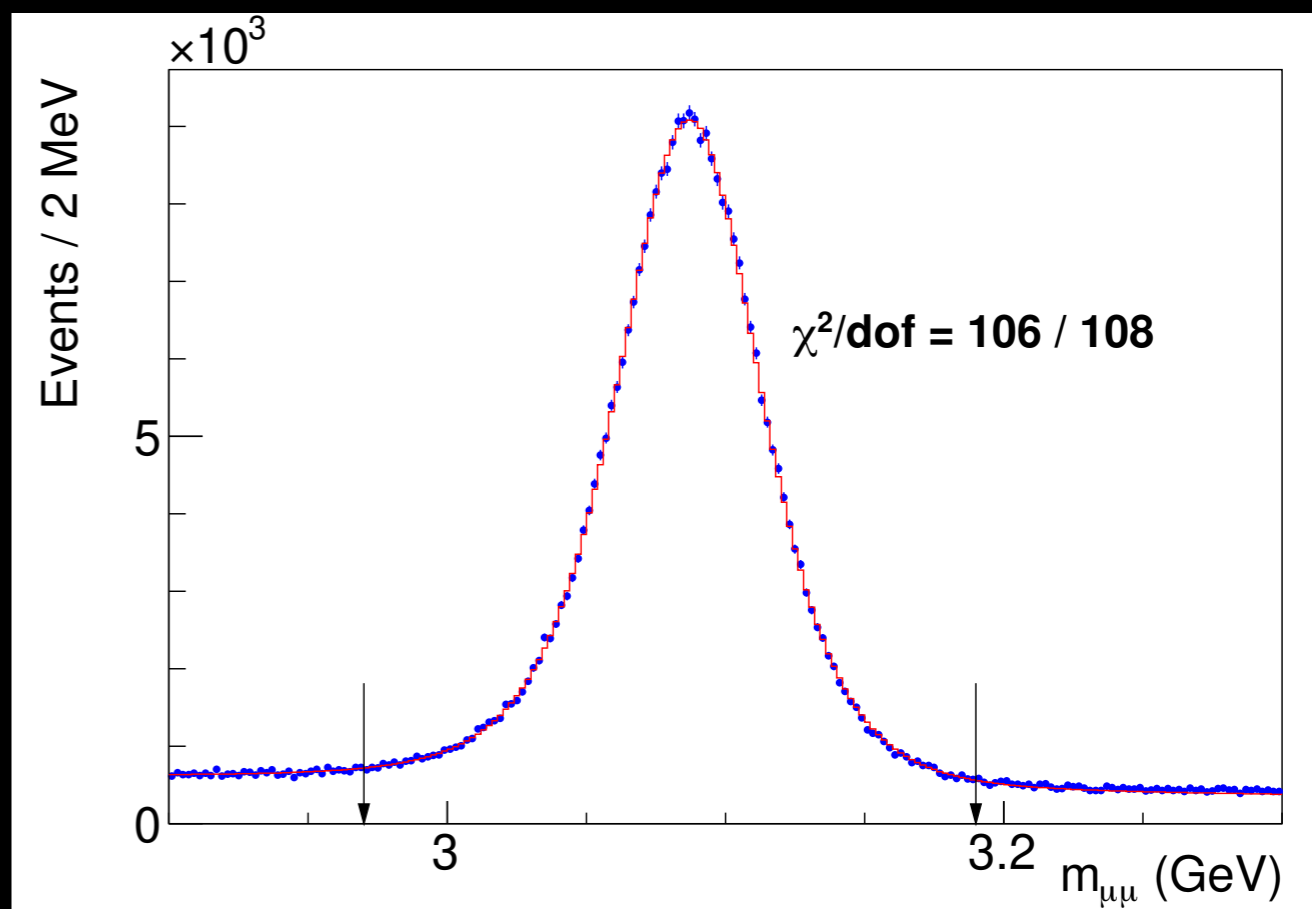
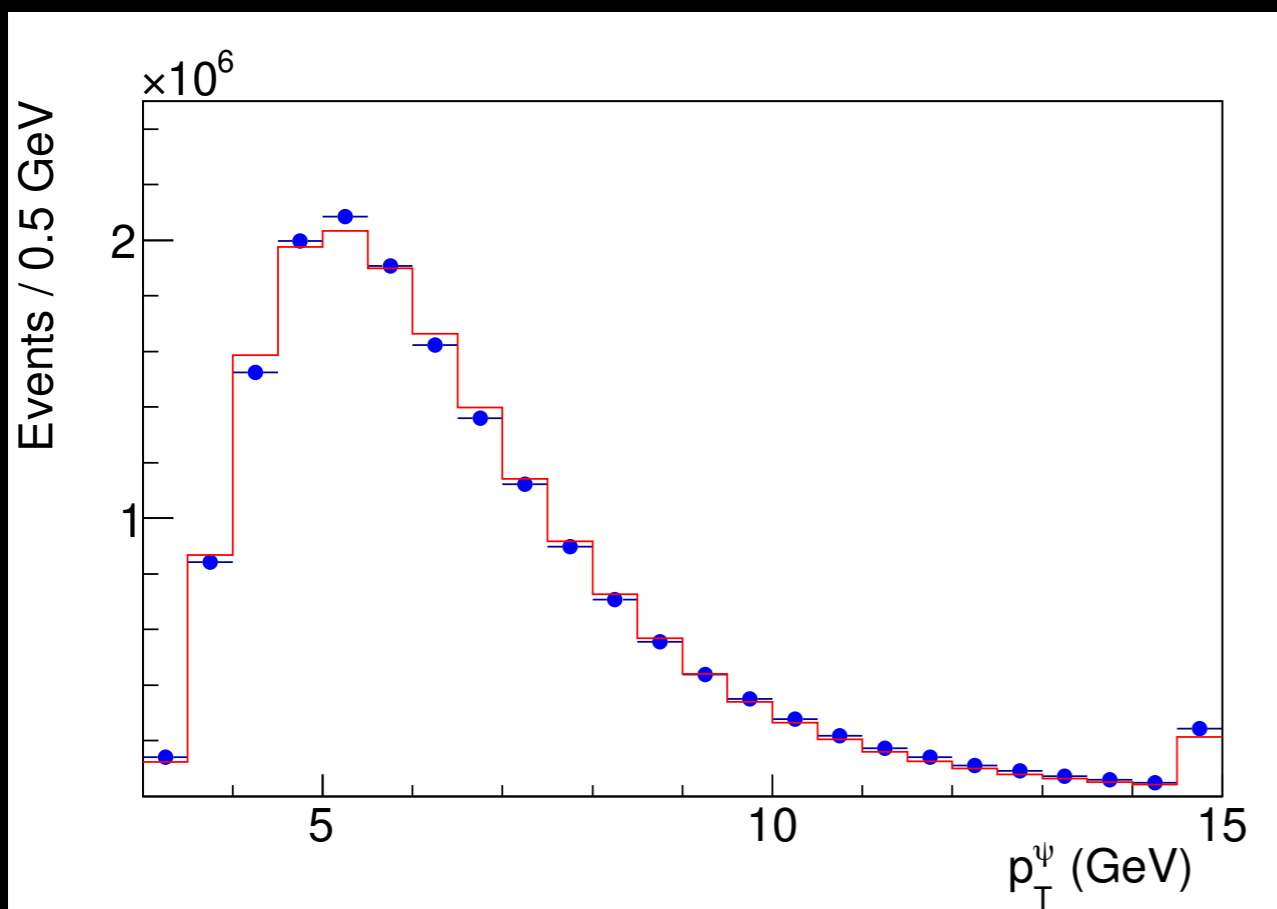
Muon momentum calibration

Second step is to calibrate the momentum scale using J/ψ decays to muons

Simulation:

Adjust kinematics to match the data

Model resonance shape using hit-level simulation and NLO form factor for QED radiation



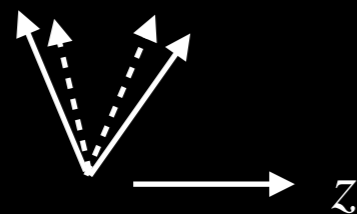
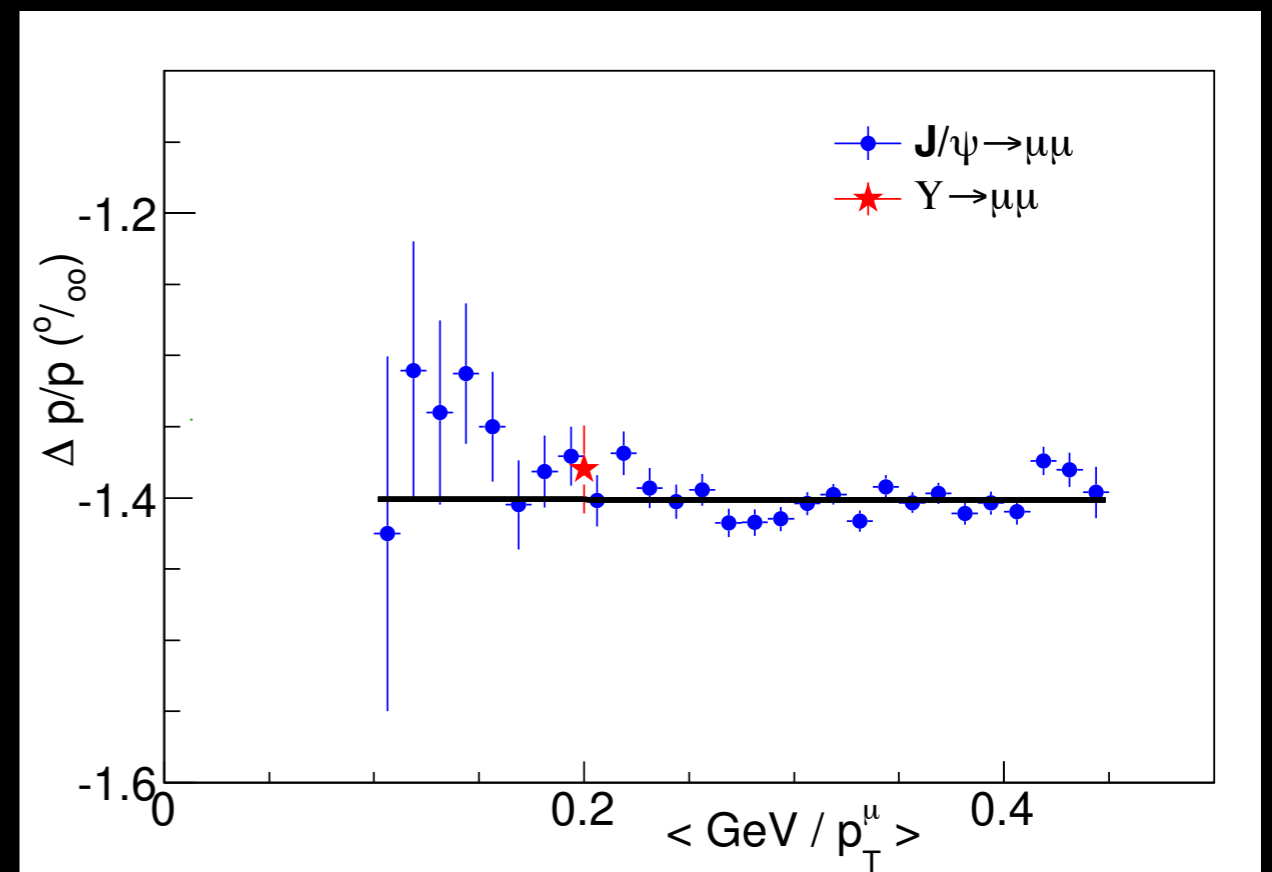
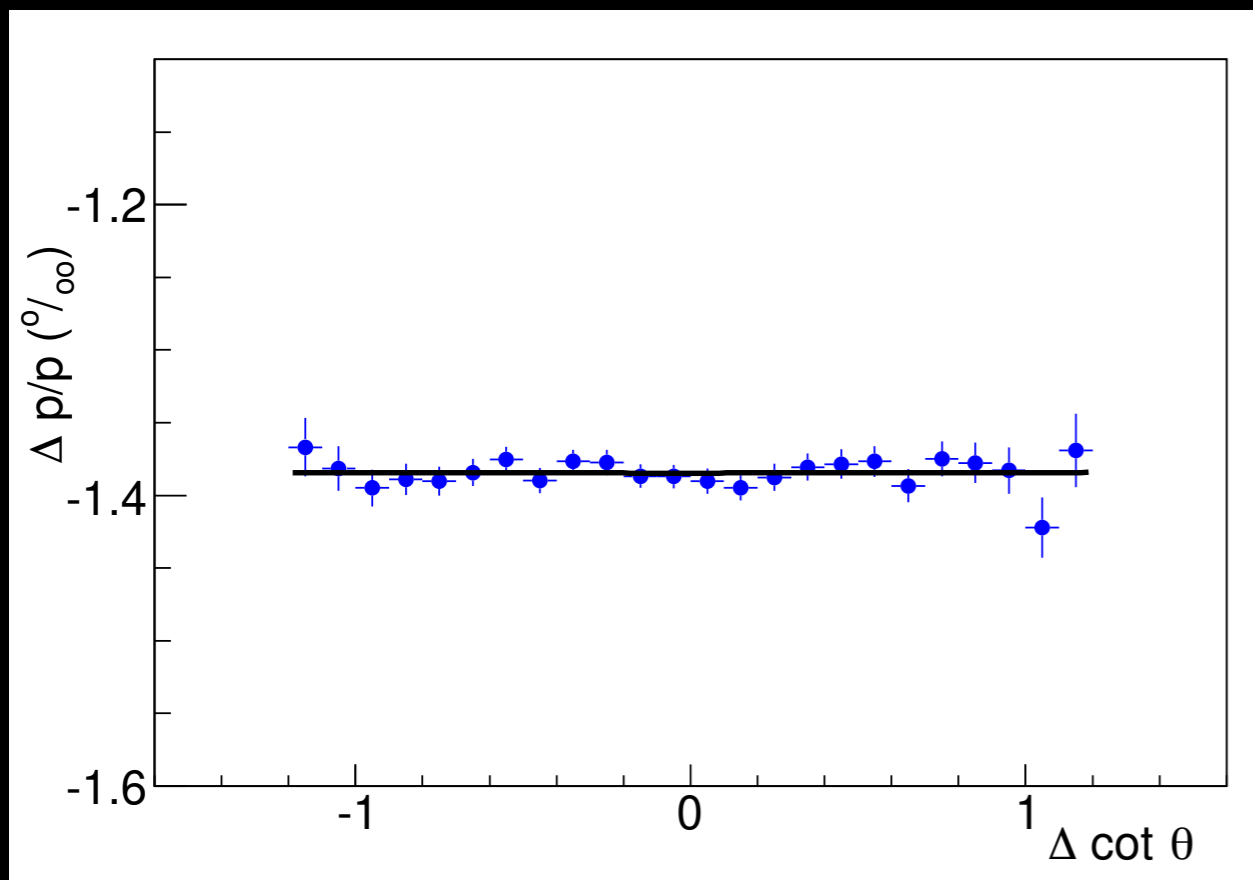
Muon momentum calibration

Second step is to calibrate the momentum scale using J/ψ decays to muons

Simulation corrections:

Correct the length scale of the tracker with mass measurement as a function of $\Delta \cot \theta$

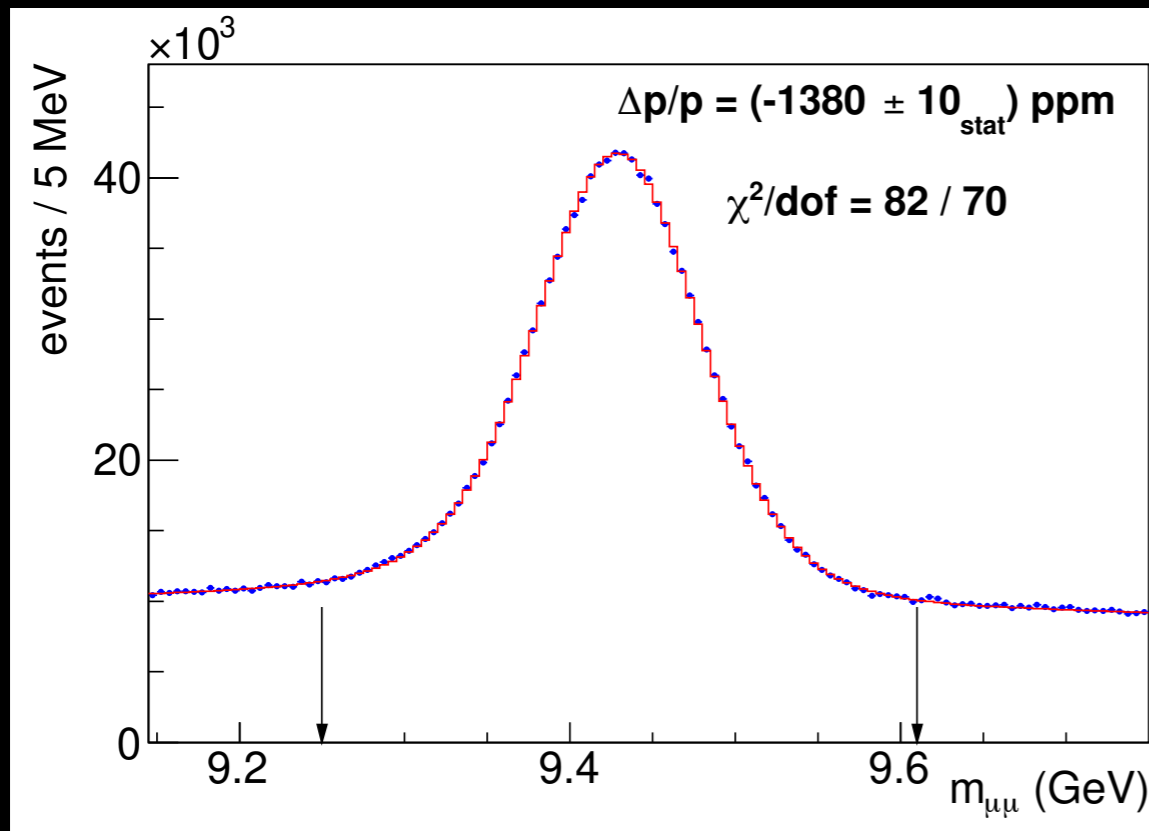
Correct the amount of upstream material with mass measurement as a function of p_T^{-1}



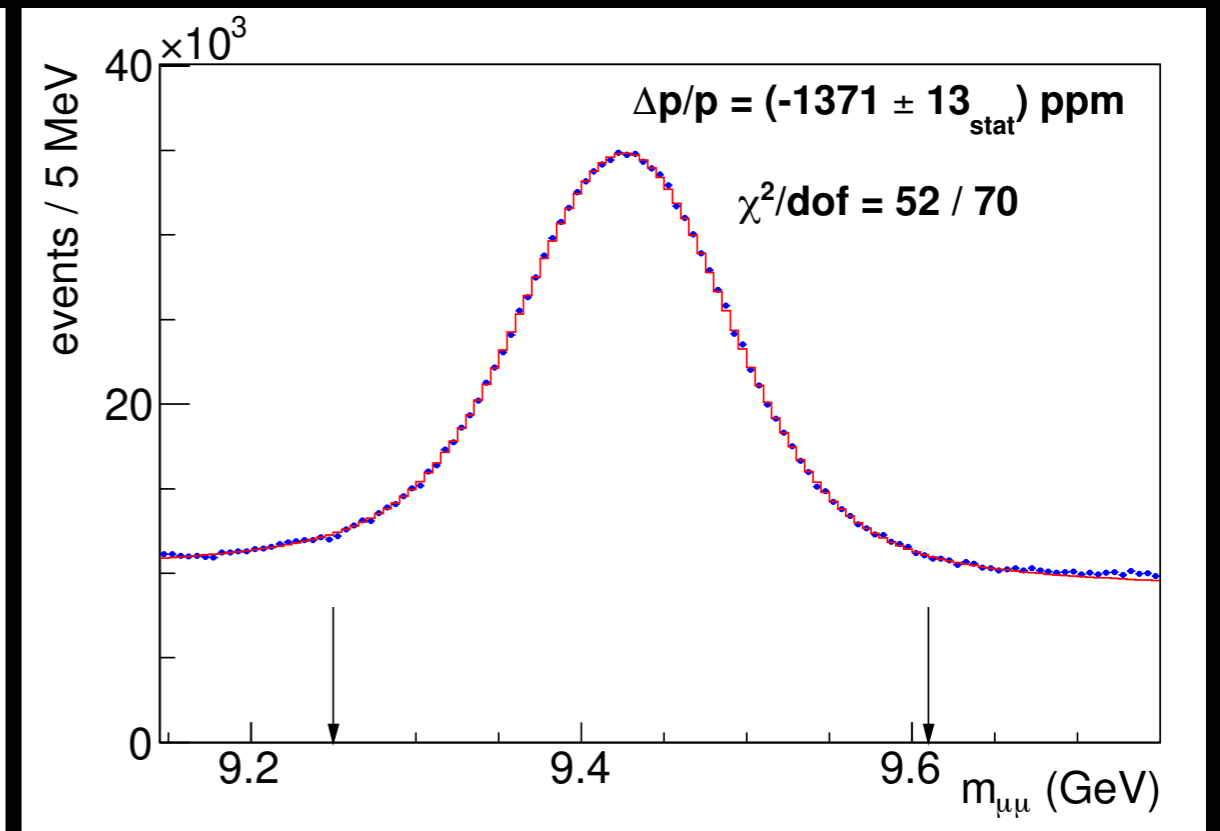
Muon momentum calibration

Third step is to calibrate the scale using Υ decays to muons

Compare fit results with and without constraining the track to the collision point



with constraint



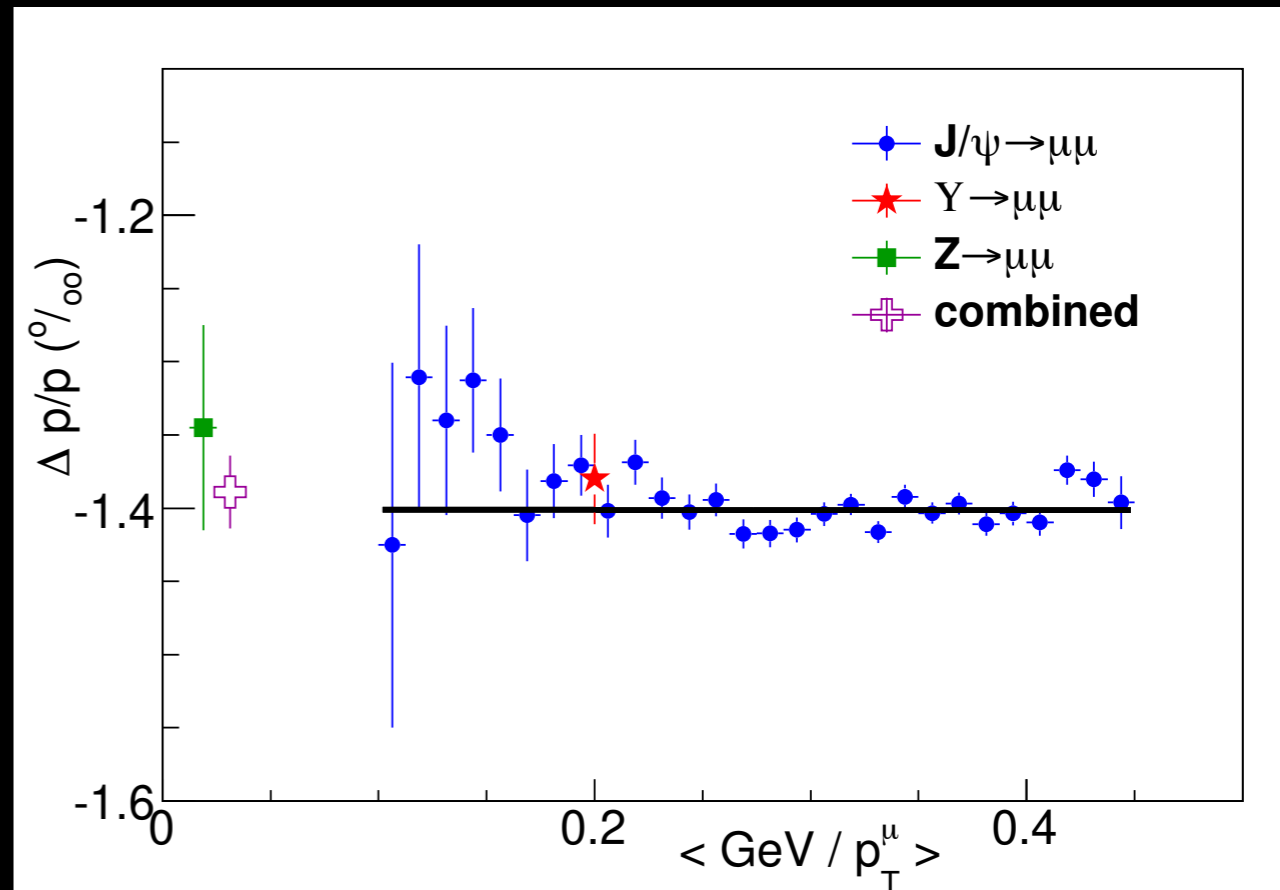
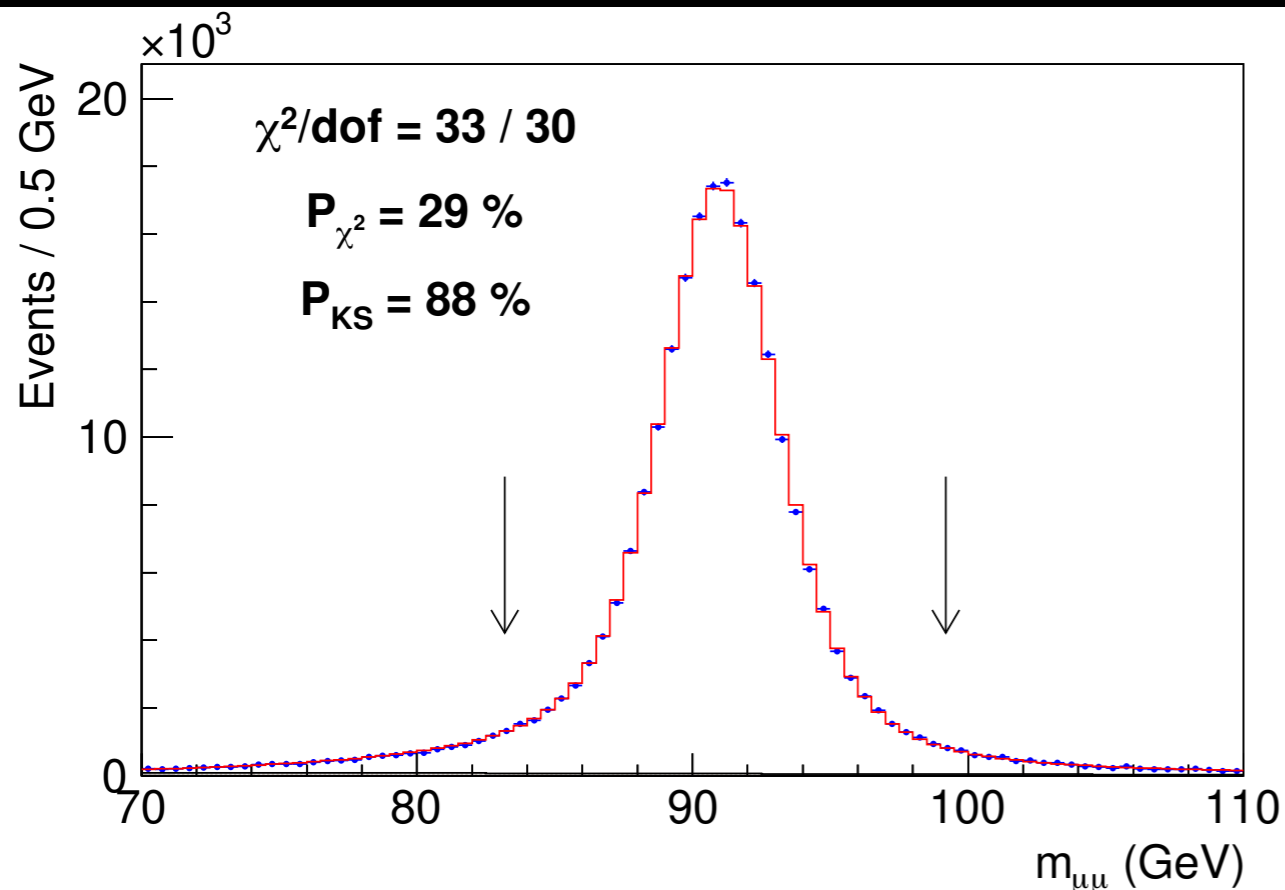
without constraint

Muon momentum calibration

Final step is to measure the Z boson mass

$$M_Z = 91\,192.0 \pm 6.4_{stat} \pm 4.0_{sys} \text{ MeV}$$

Result blinded with $[-50,50]$ MeV offset until previous steps were complete
Combine all measurements into a final charged-track momentum scale



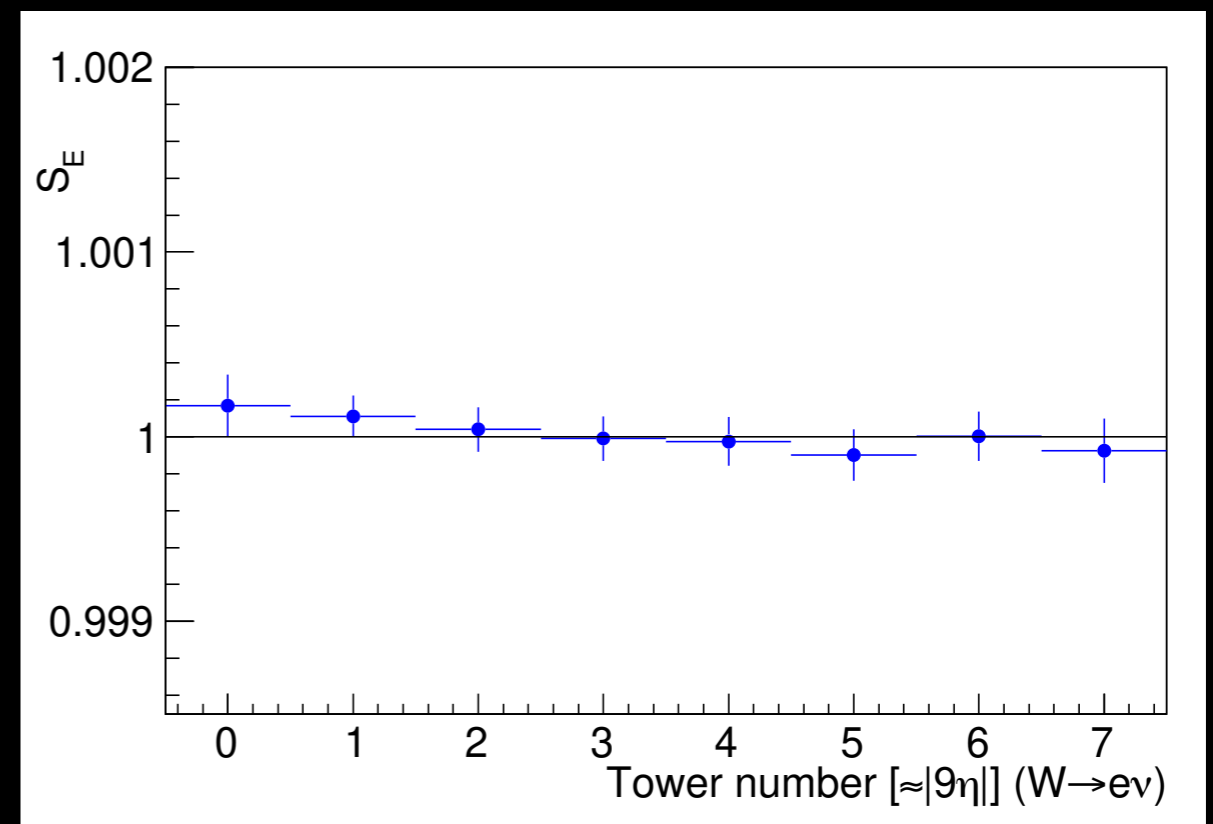
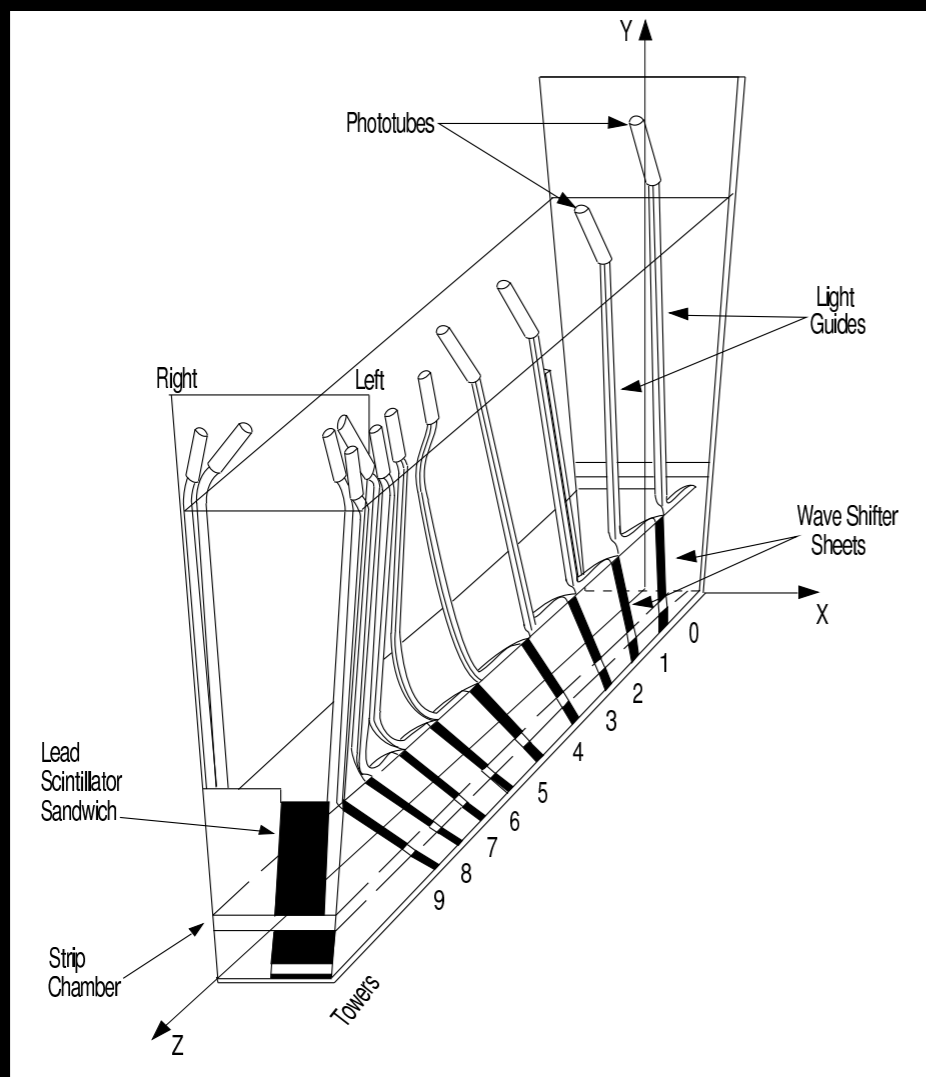
Electron momentum calibration

First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Data corrections:

Use mean E/p to remove time dependence & response variations in tower

Fit ratio of calorimeter energy to track momentum to correct each tower in η



Electron momentum calibration

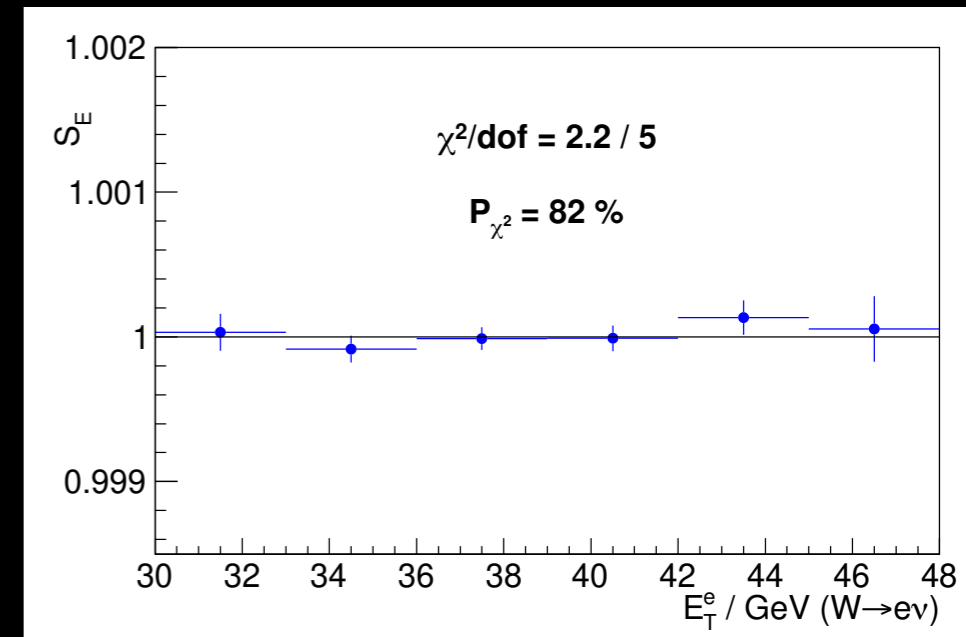
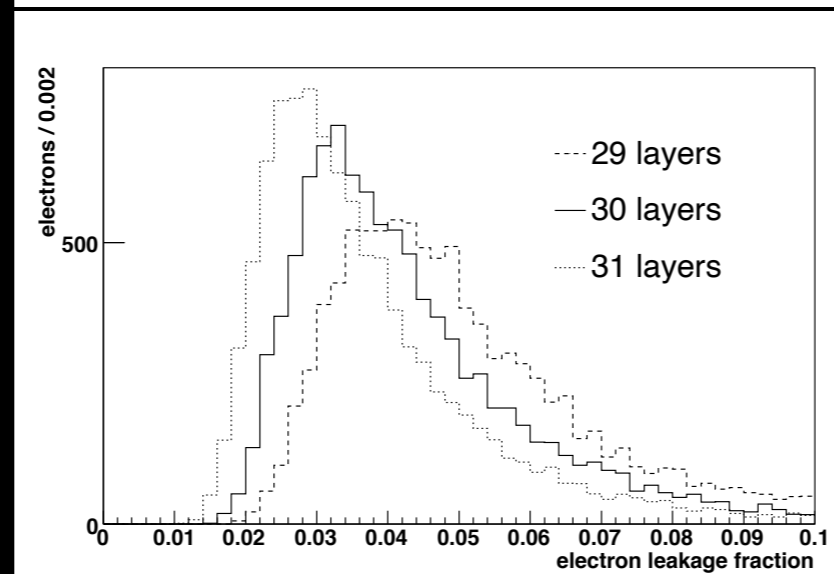
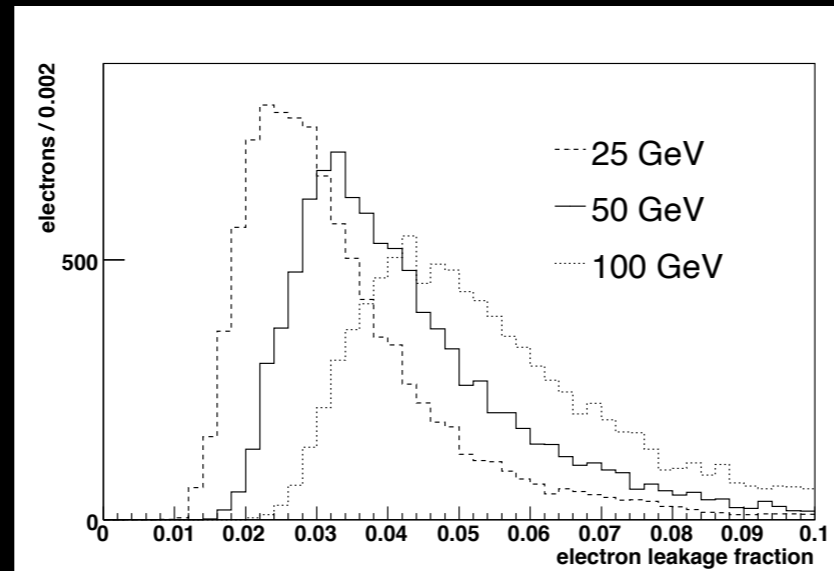
First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Parameterize calorimeter shower deposition and leakage based on GEANT4

Determine small calorimeter thickness corrections using region of low E/p in data

Fit calorimeter scale as a function of E_T to correct for any remaining energy dependence

Tower	Thickness (x_0)	Number of lead sheets
0	17.9	30
1	18.2	30
2	18.2	29
3	17.8	27
4	18.0	26
5	17.7	24
6	18.1	23
7	17.7	21
8	18.0	20



Kotwal & CH, NIMA 729, 25 (2013)

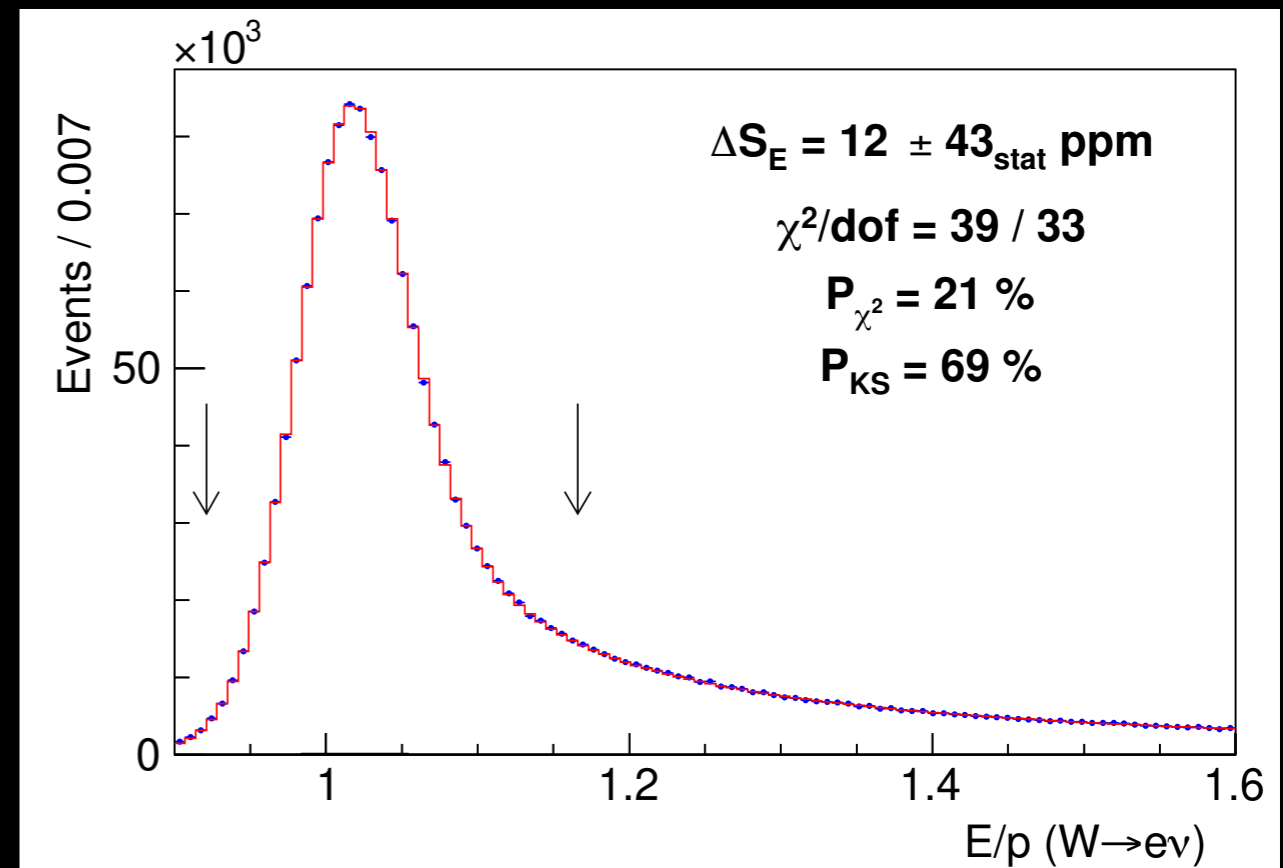
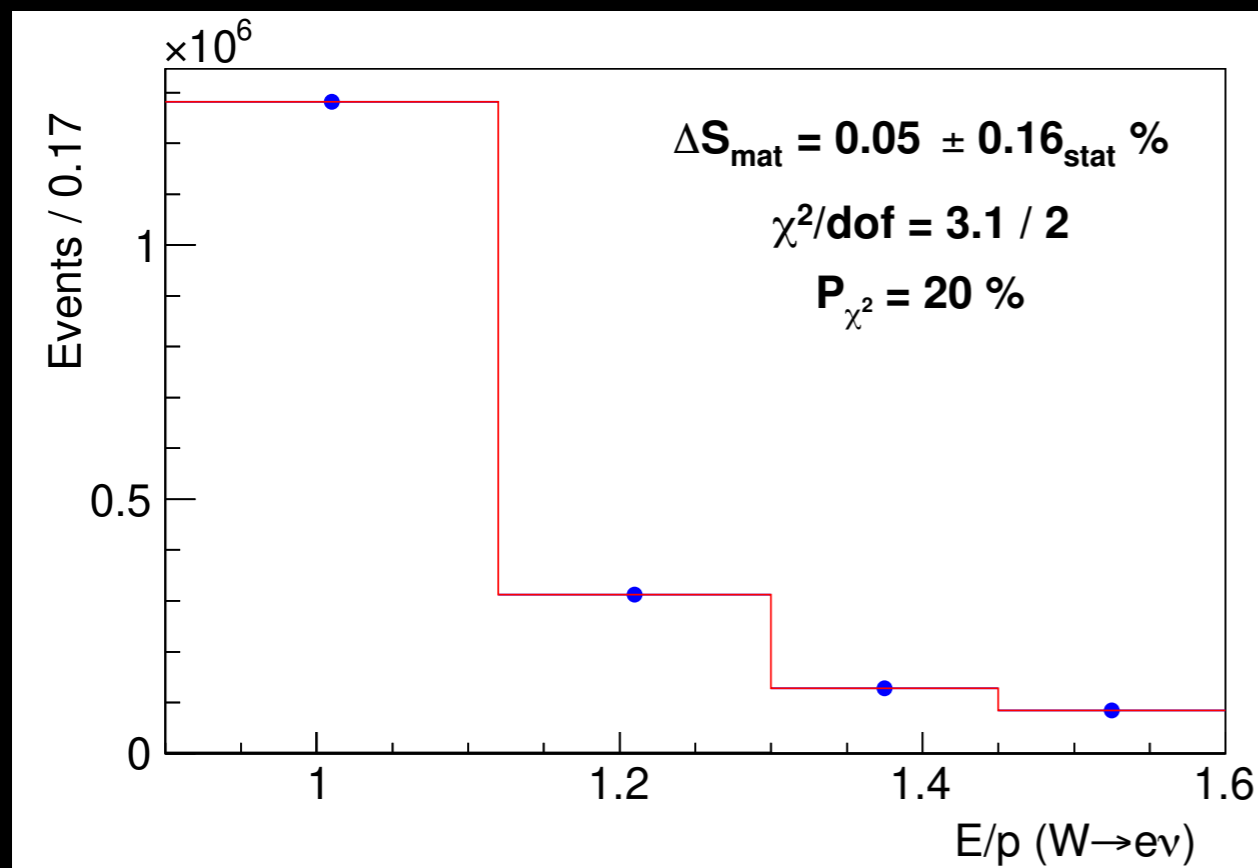
Electron momentum calibration

First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Model bremsstrahlung and pair production upstream of the drift chamber

Tune energy loss due to material upstream of the tracker (high E/p)

Sampling resolution given by $\sigma_E/E = \sqrt{\frac{12.6\%}{E_T} + \kappa^2}$ with $\kappa = 0.7 - 1.1\%$ increasing with tower η



Electron momentum calibration

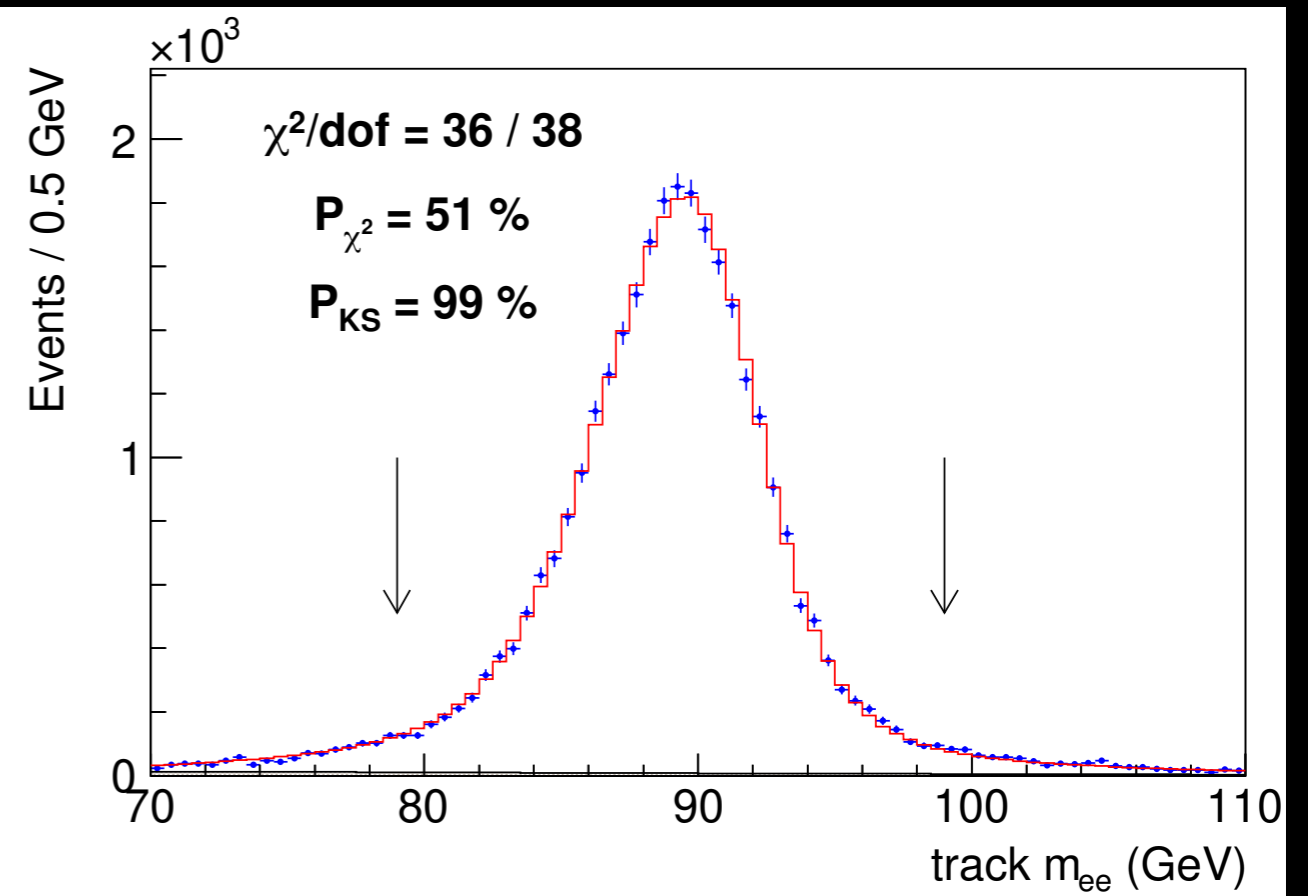
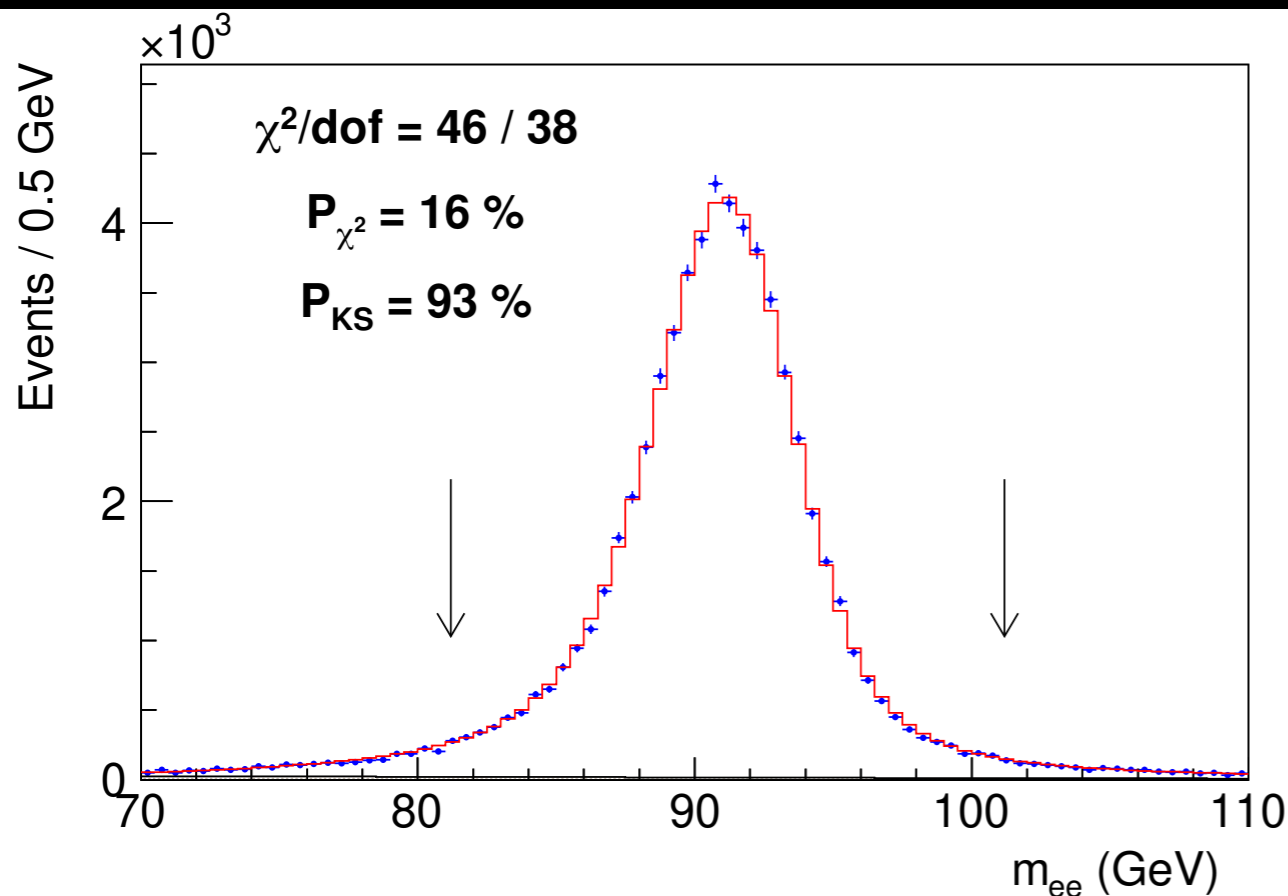
Second step is the measurement of the Z boson mass

$$M_Z = 91\,194.3 \pm 13.8_{stat} \pm 7.6_{sys} \text{ MeV}$$

As a consistency check measure mass using only track information

e.g. $M_Z = 91\,215.2 \pm 22.4 \text{ MeV}$ for non-radiative electrons ($E/p < 1.1$)

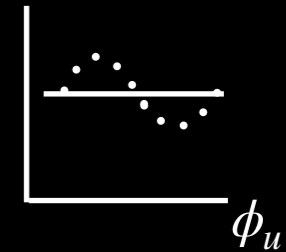
Same blinding as for muon channel



Recoil momentum calibration

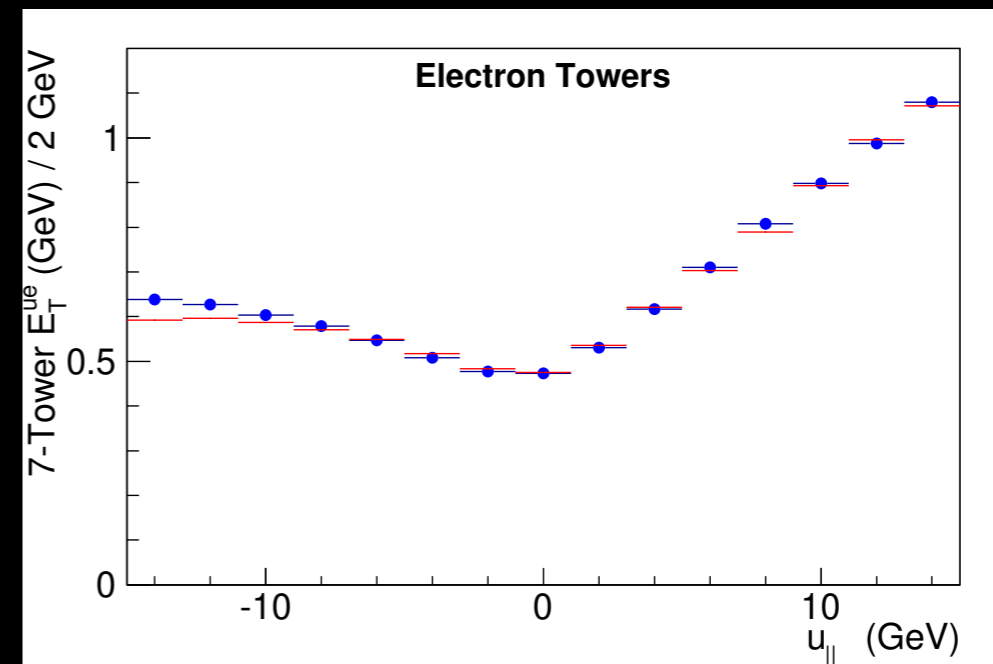
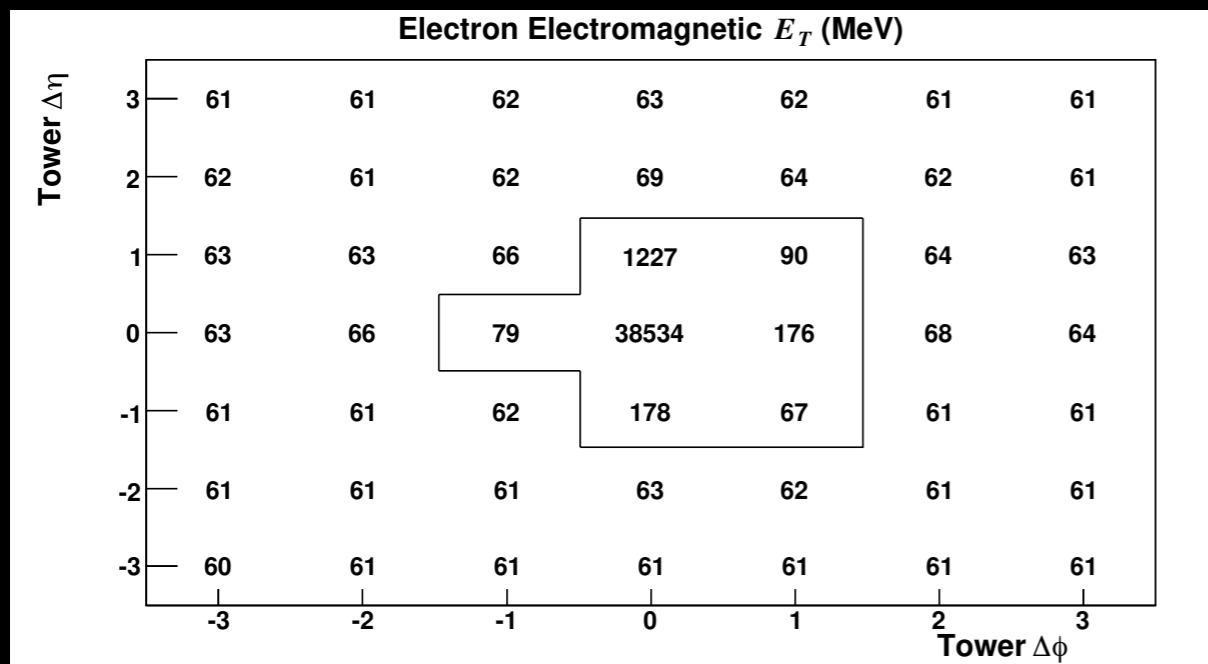
First step is the alignment of the calorimeters

Misalignments relative to the beam axis cause a modulation in the recoil direction
 Alignment performed separately for each run period using minimum-bias data



Second step is the reconstruction of the recoil

Remove towers traversed by identified leptons
 Remove corresponding recoil energy in simulation using towers rotated by 90°
validate using towers rotated by 180°

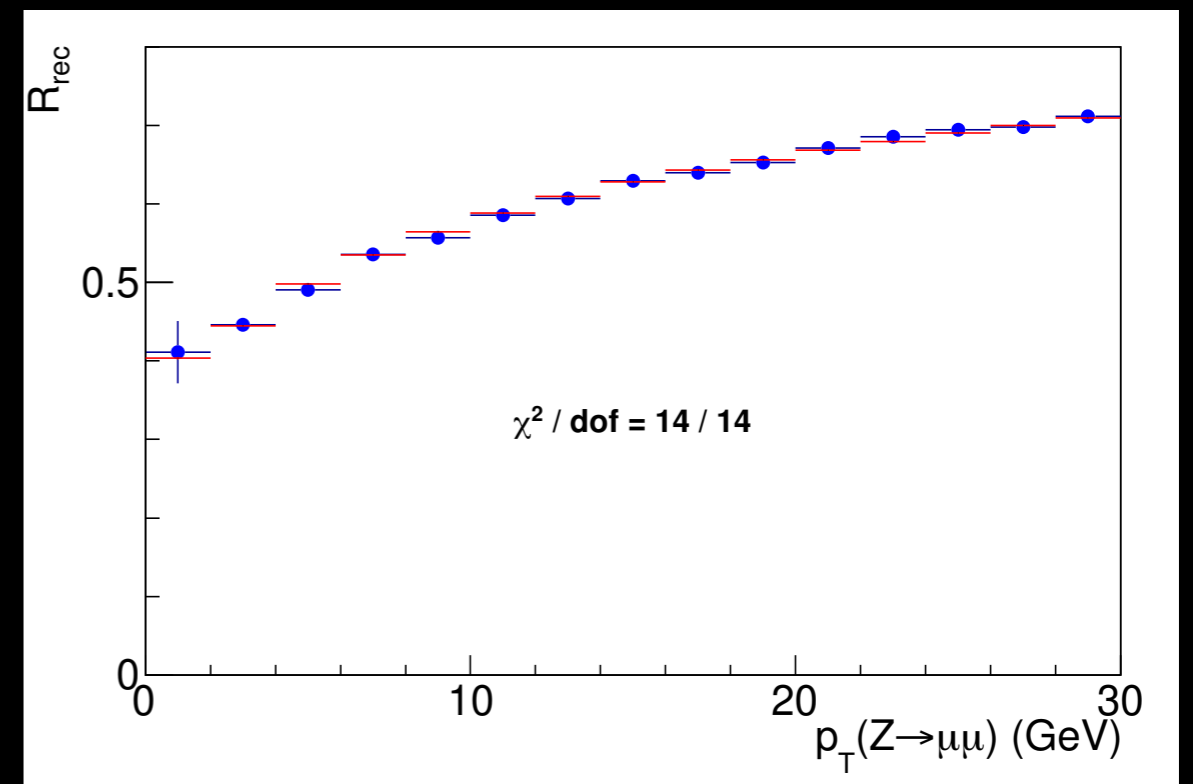
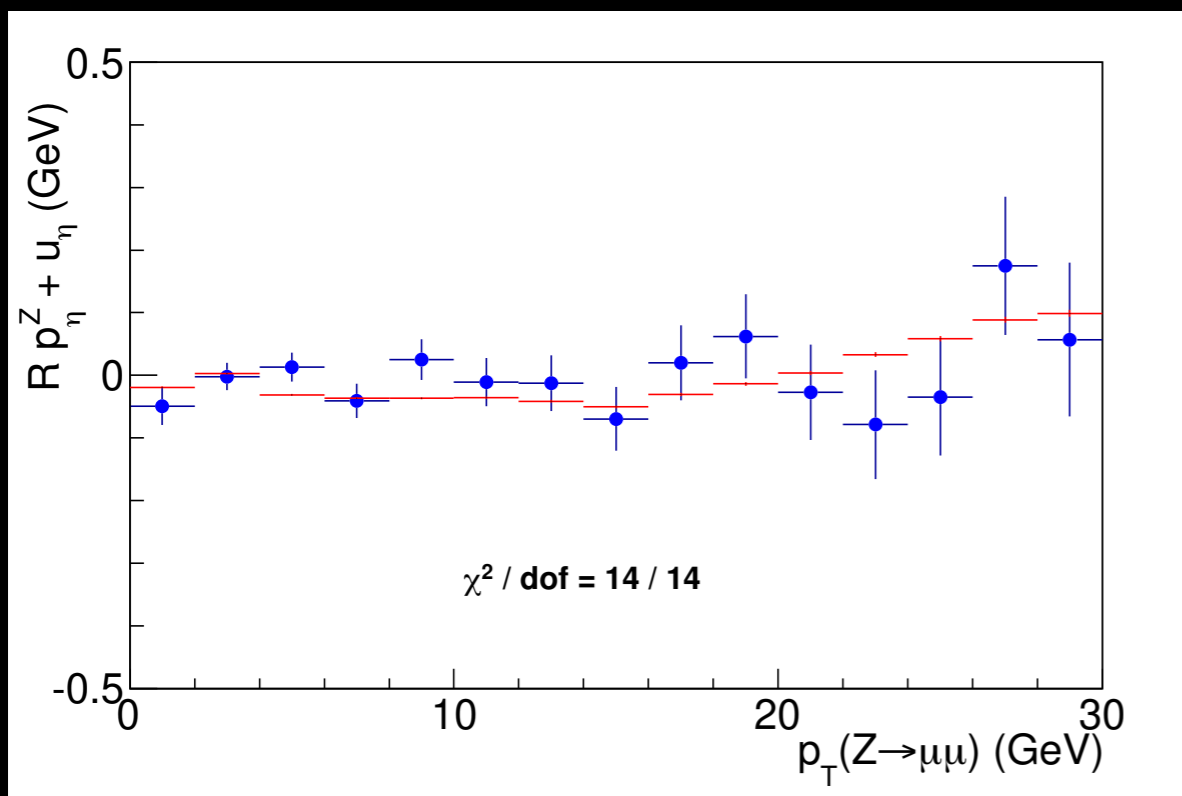
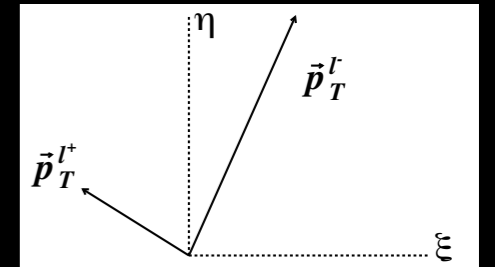


Recoil momentum calibration

Third step is the calibration of the recoil response

Balance recoil against direction of p_T^Z

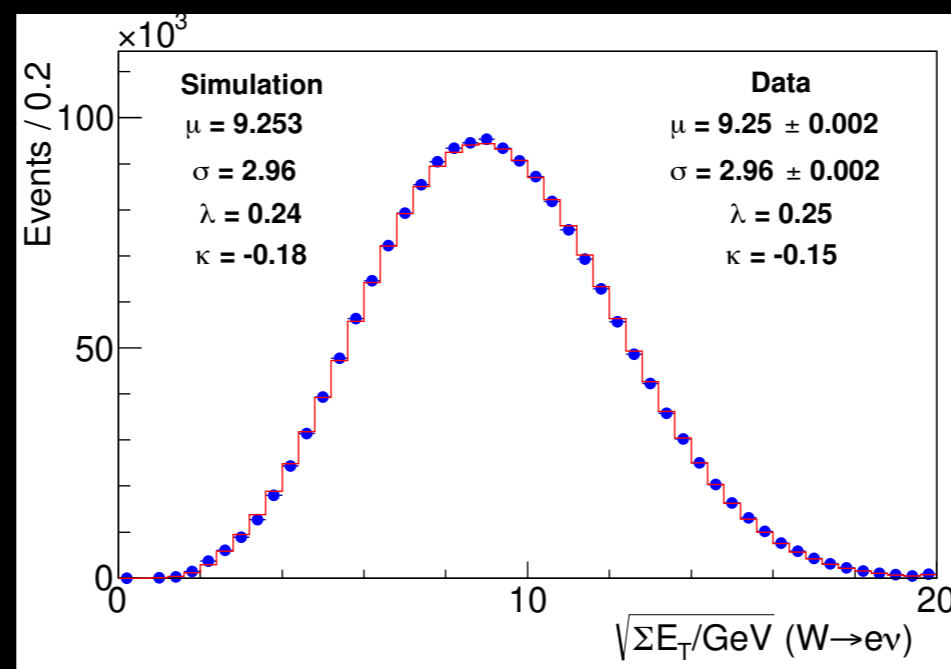
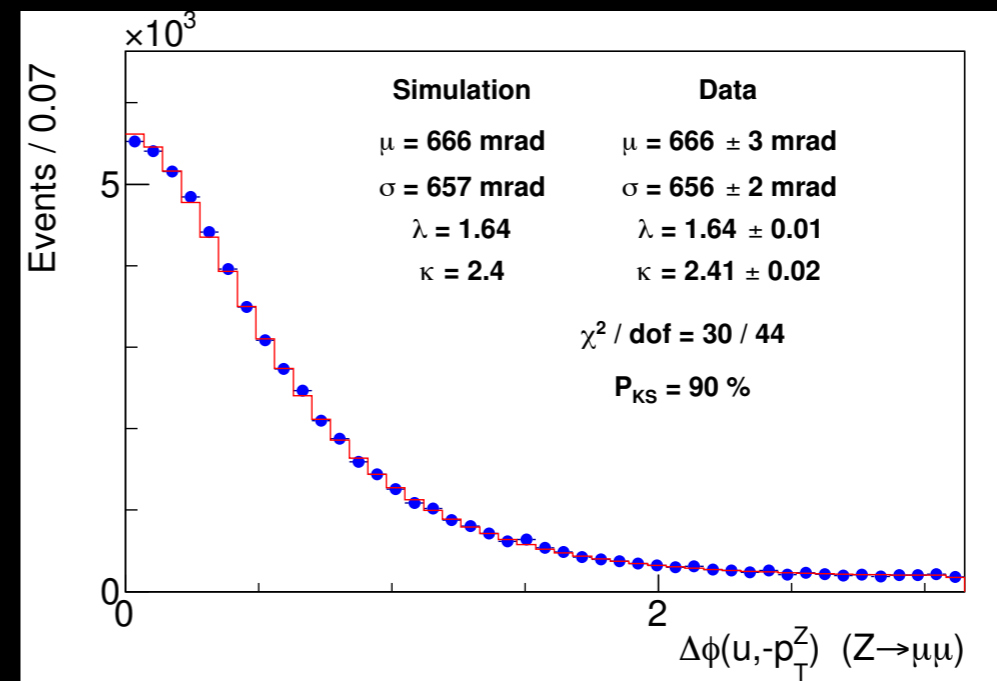
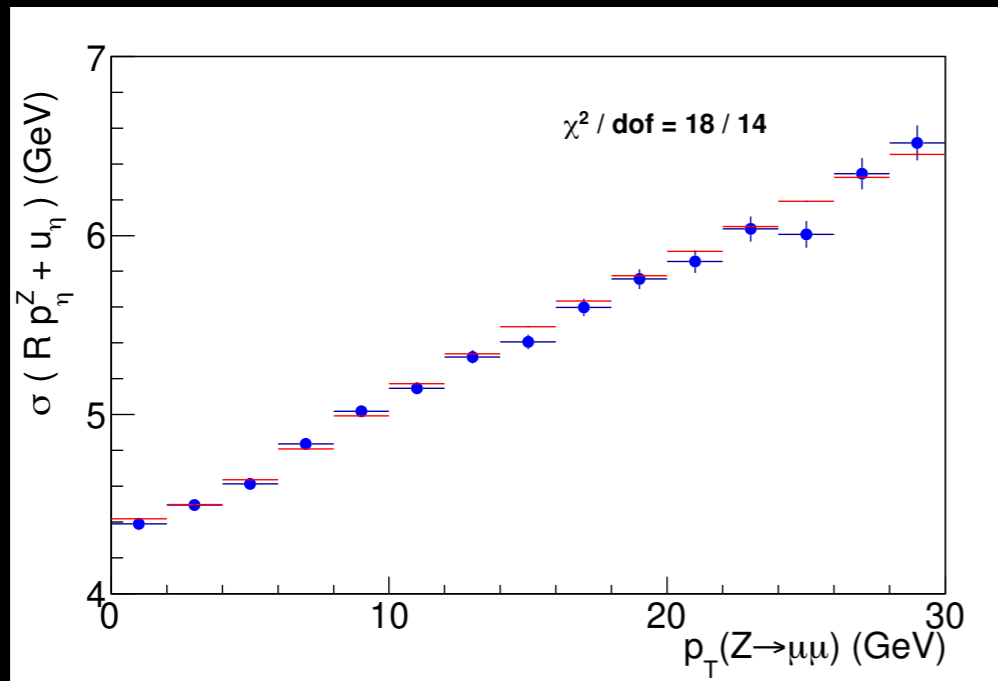
Check calibration using ratio of recoil magnitude to p_T^Z along direction of p_T^Z (R_{rec})



Recoil momentum calibration

Fourth step is the calibration of the recoil resolution

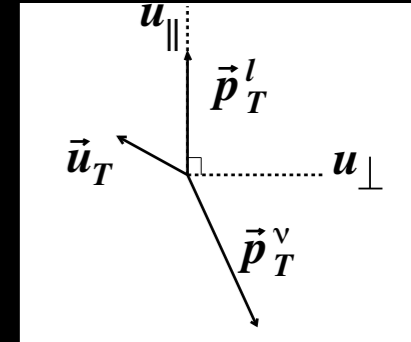
Includes jet-like energy and angular resolution, additional dijet fraction term, and pileup



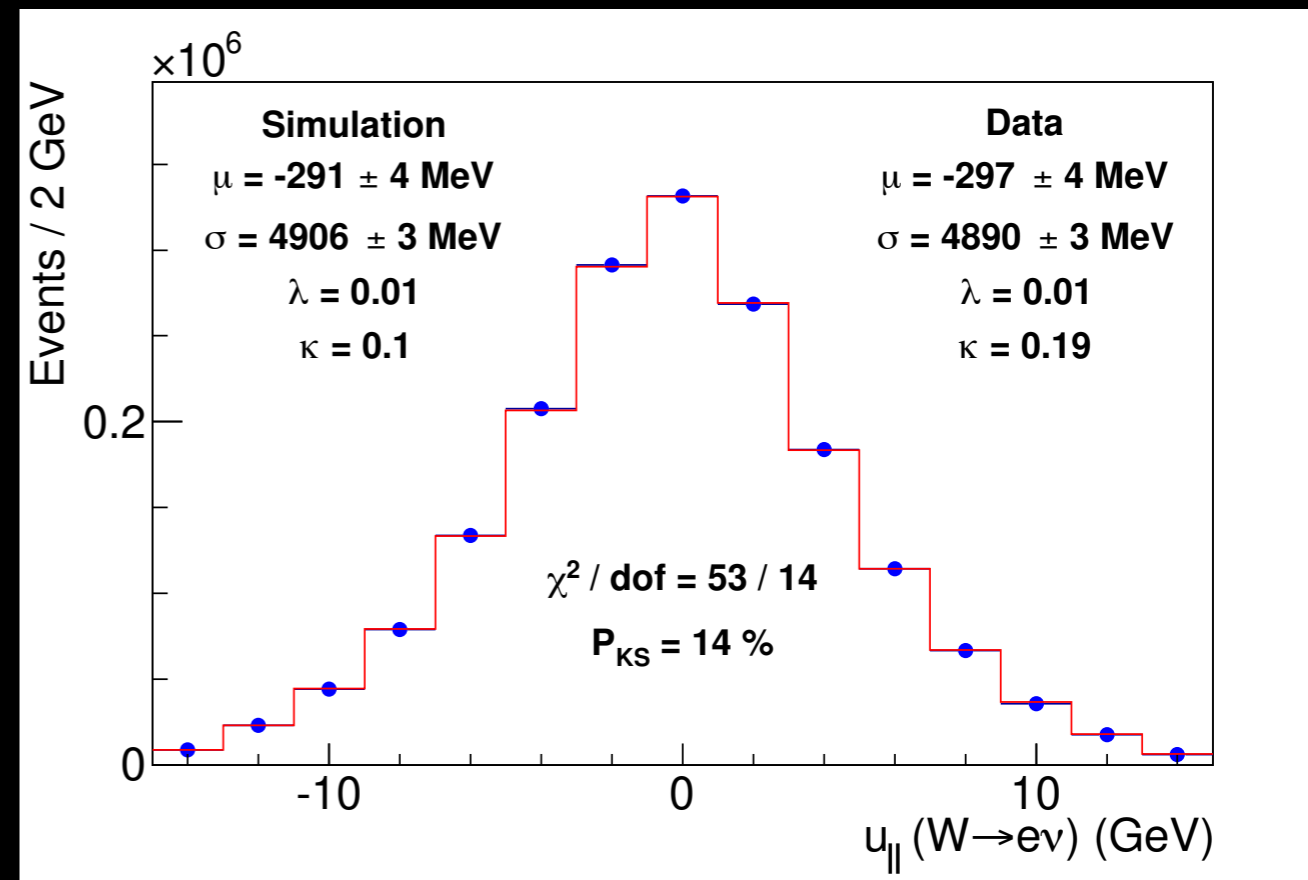
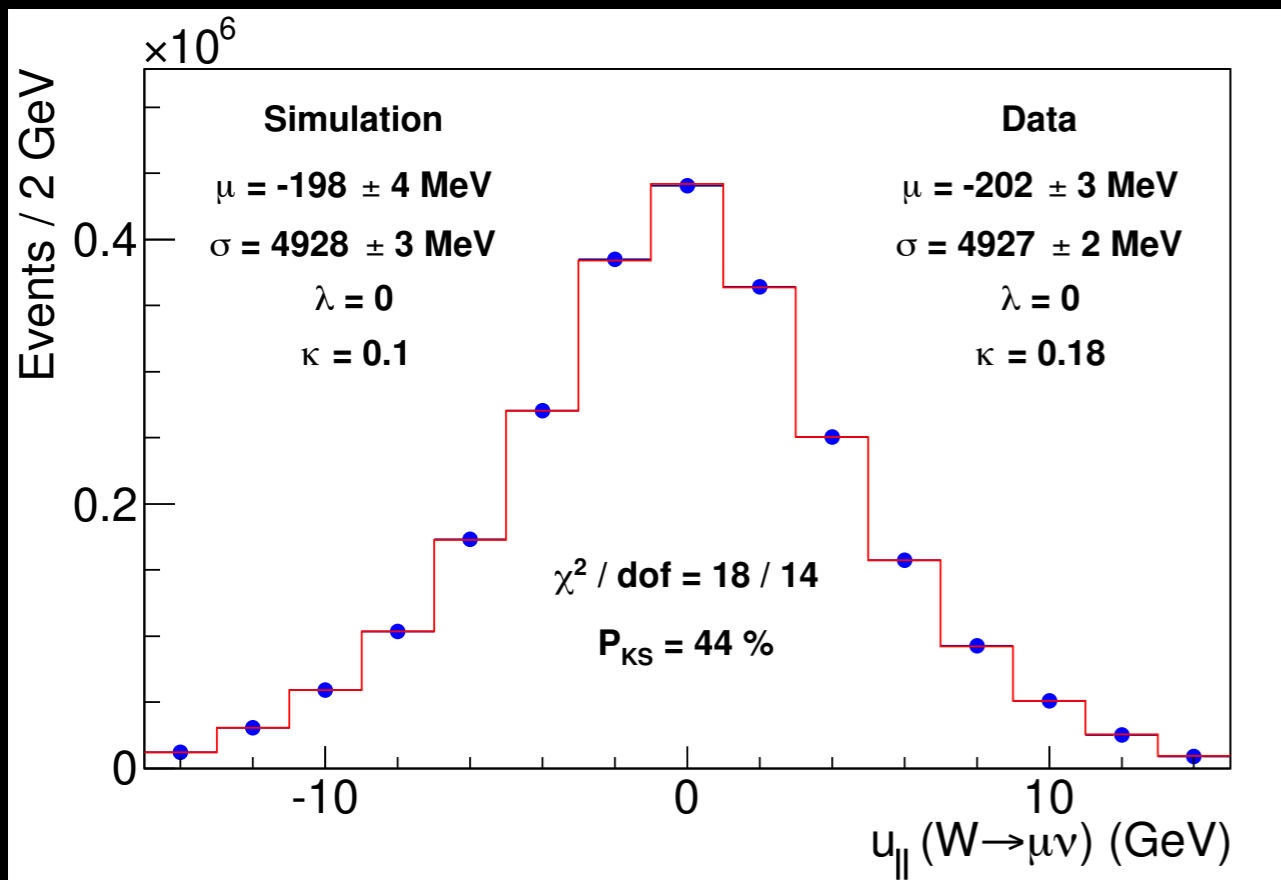
Recoil momentum validation

W boson recoil distributions validate the model

Most important is the recoil projected along the charged-lepton's momentum ($u_{||}$)



$$m_T \approx 2p_T \sqrt{1 + u_{||}/p_T} \approx 2p_T + u_{||}$$



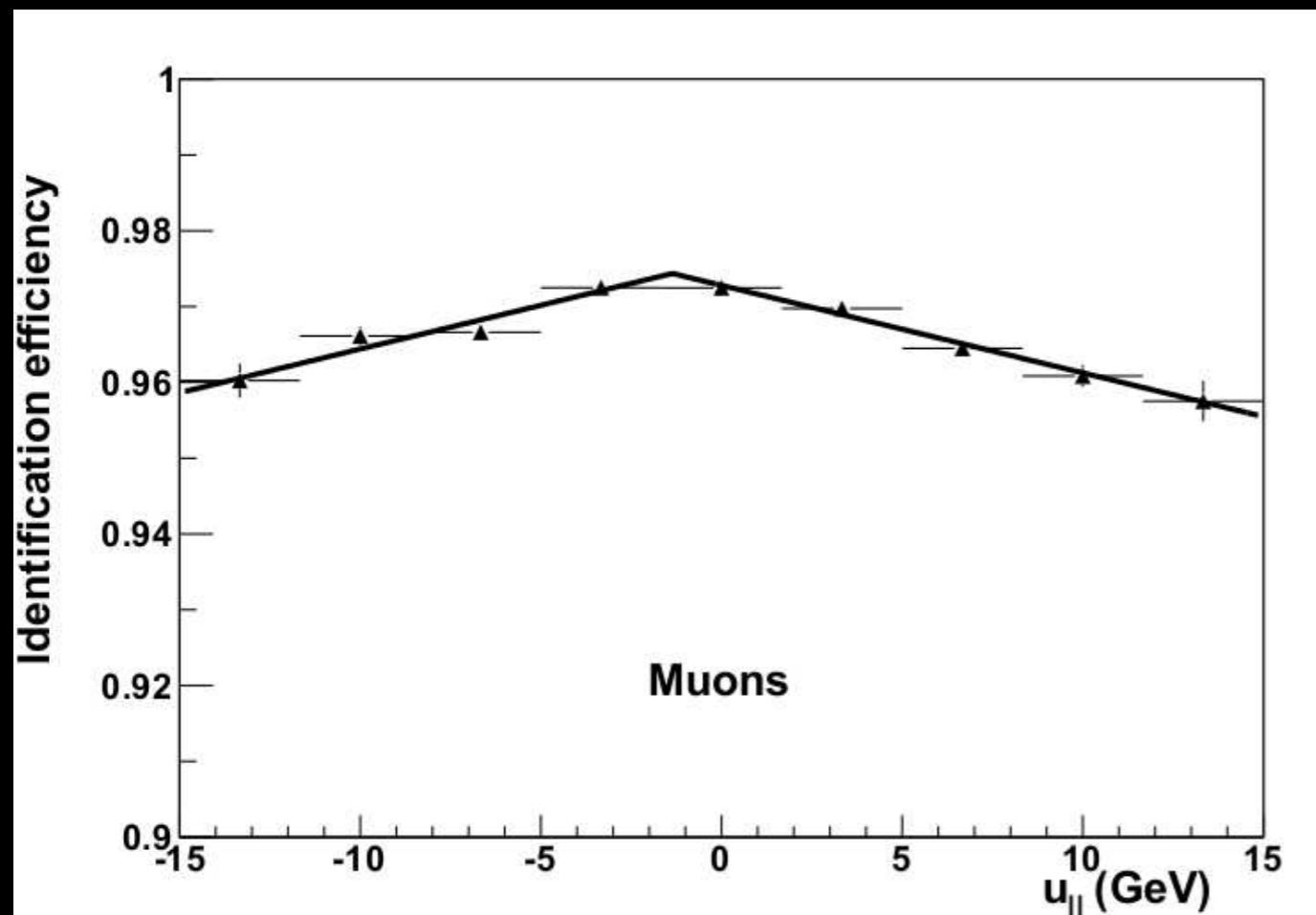
W boson candidates

W boson event selection

Triggers with low momentum thresholds (18 GeV) and very loose lepton id

Offline id also loose, efficiencies vary by 2% as hadronic recoil direction changes

No lepton isolation requirement in trigger or offline selection



Background suppressed by stringent hadronic recoil requirement

$$u_{\perp} < 15 \text{ GeV}$$

Other kinematic requirements

Lepton and missing p_{\perp} in the range 30-55 GeV

Transverse mass in the range 60-100 GeV

2.4 M $W \rightarrow \mu\nu$ candidates

1.8 M $W \rightarrow e\nu$ candidates

Backgrounds

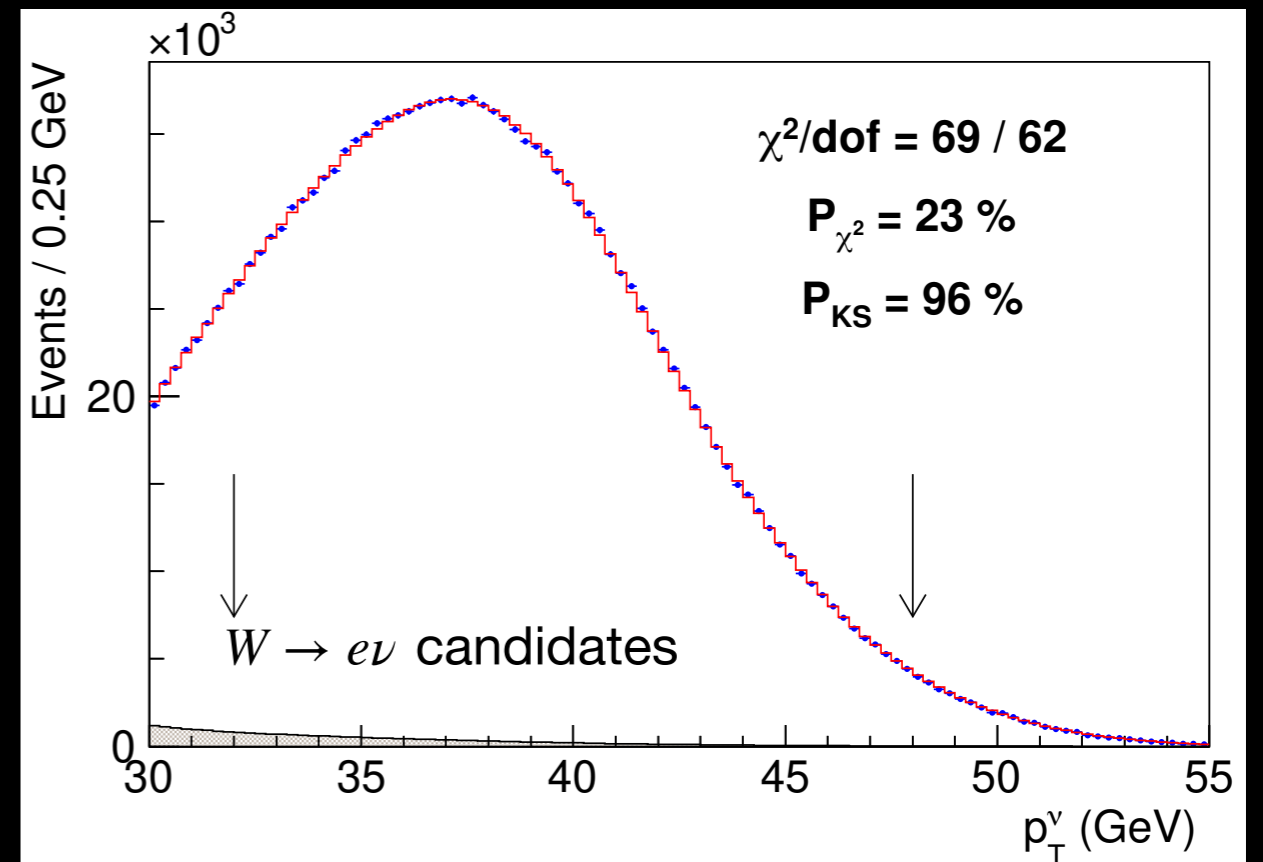
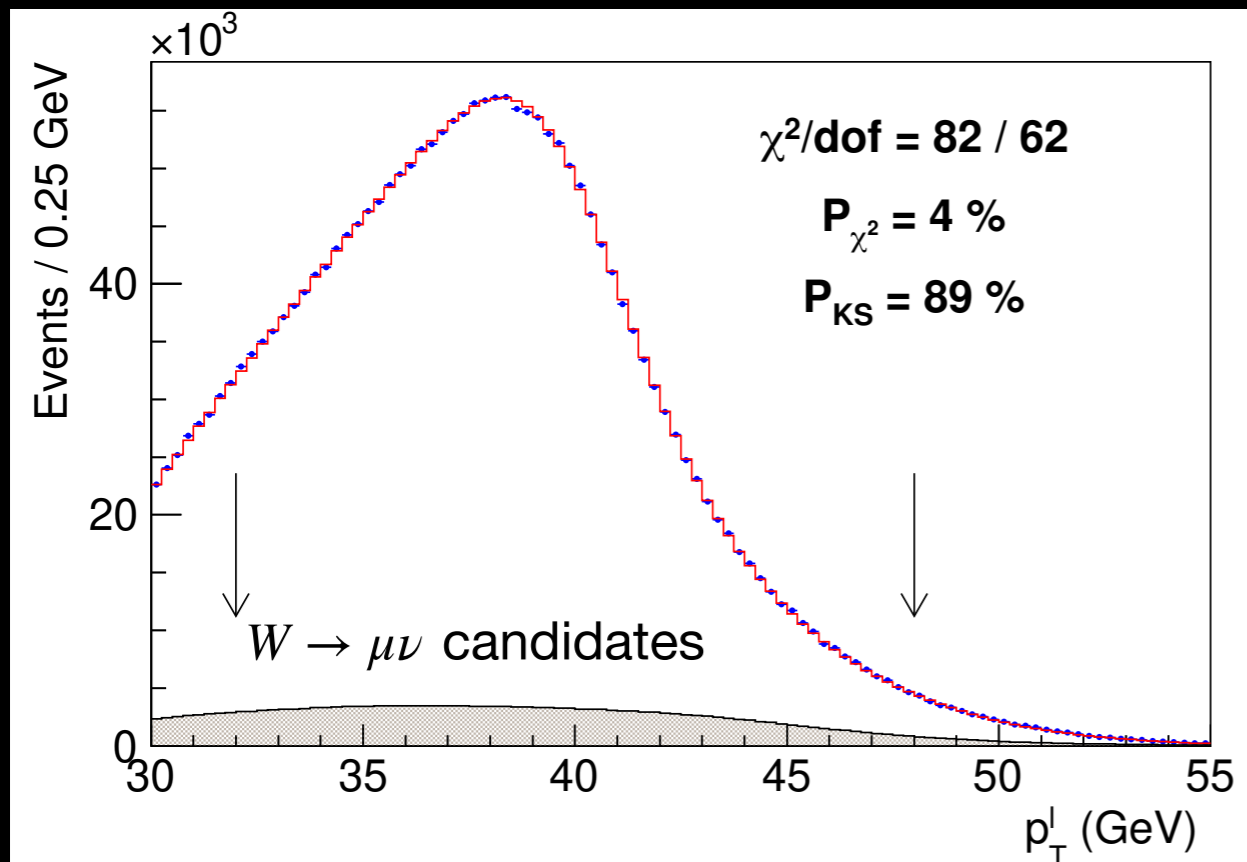
Electroweak backgrounds modelled with fast simulation tuned with data and full simulation

Cross-checked with full simulation tuned to data

Largest background is $Z \rightarrow \mu\mu$ with one unreconstructed muon: **7.4% of data sample**

$W \rightarrow \tau\nu$ background is $\sim 1\%$ in each channel: largest background in electron sample

Background from hadrons misreconstructed as leptons estimated using data: 0.2-0.3%



W boson transverse momentum

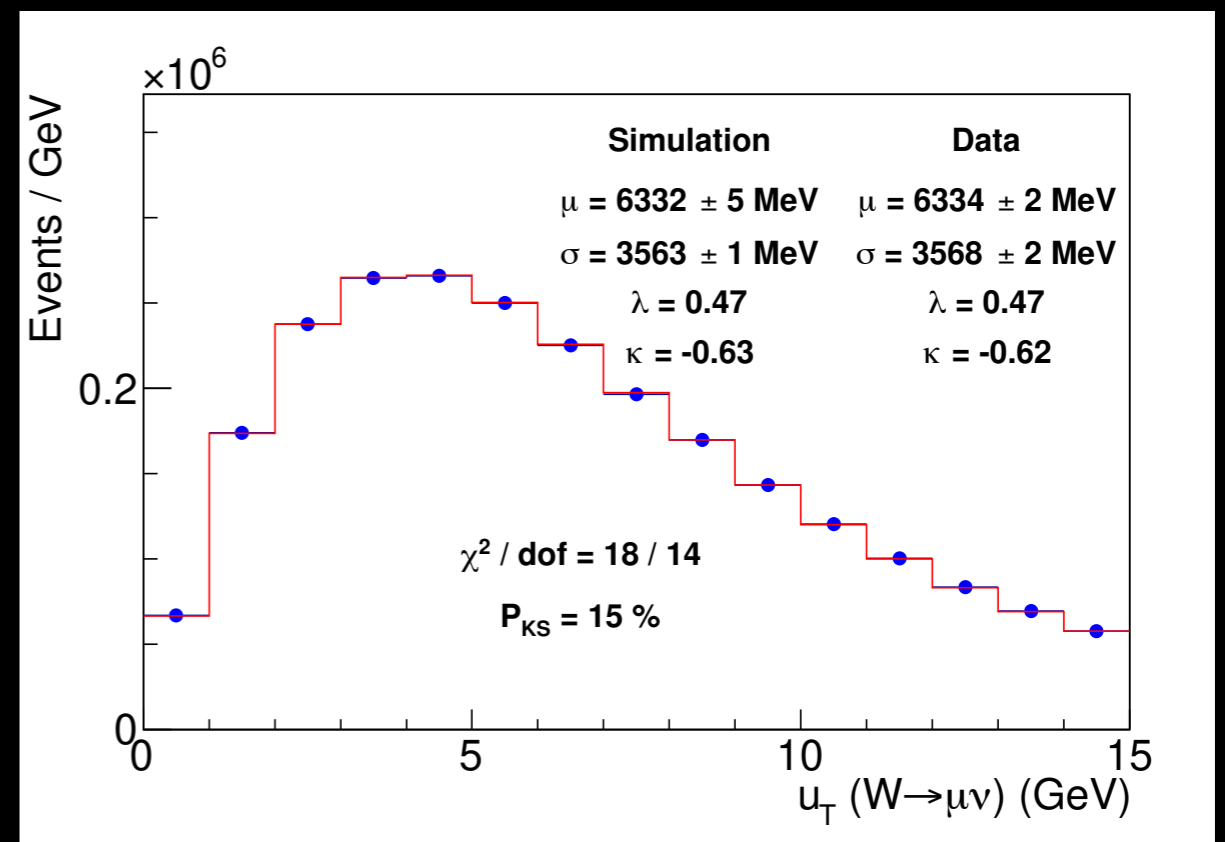
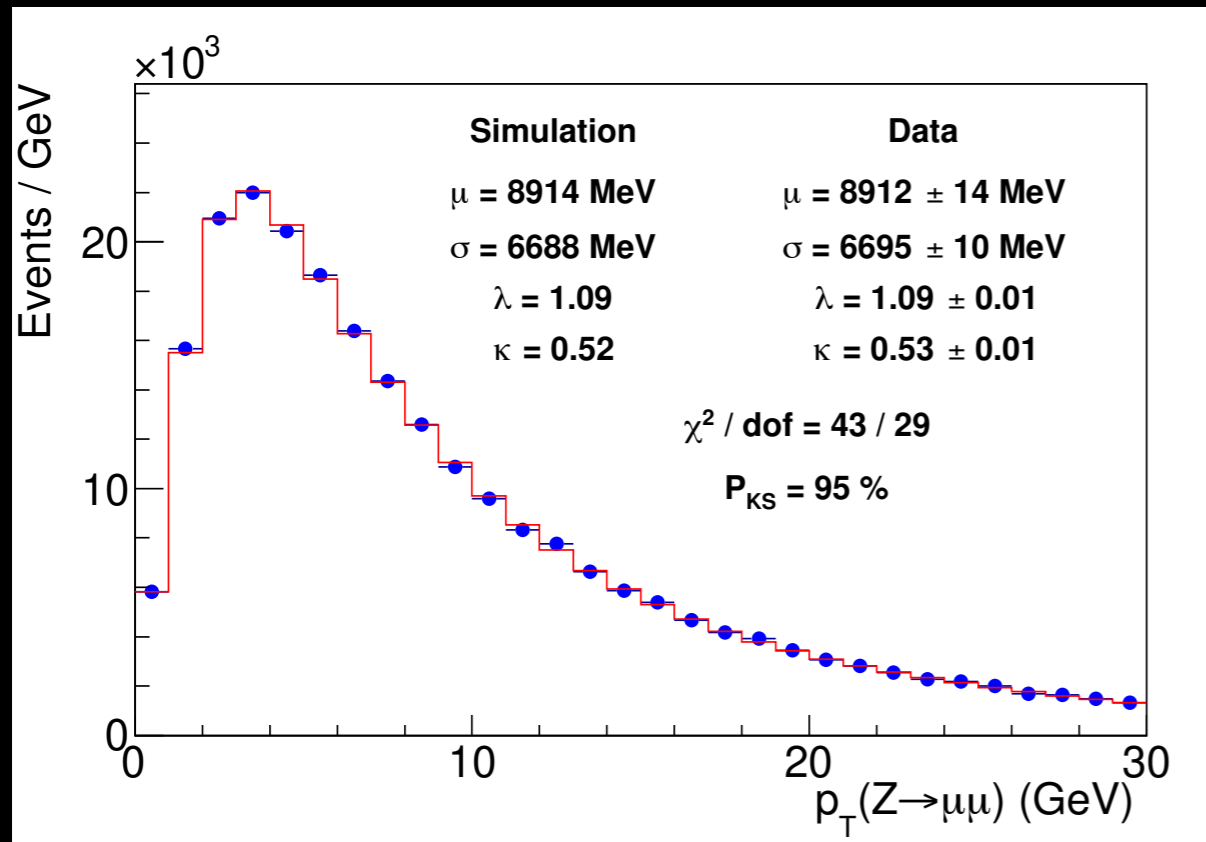
Boson p_T impacts the p_T distributions of the decay leptons

Resbos used to generate events with non-perturbative parameters and NNLL resummation to model the region of low boson p_T

Z boson p_T used to constrain the non-perturbative parameter g_2 and the perturbative coupling α_s

Resbos models W boson p_T well

uncertainty estimated using DYQT and constrained with data



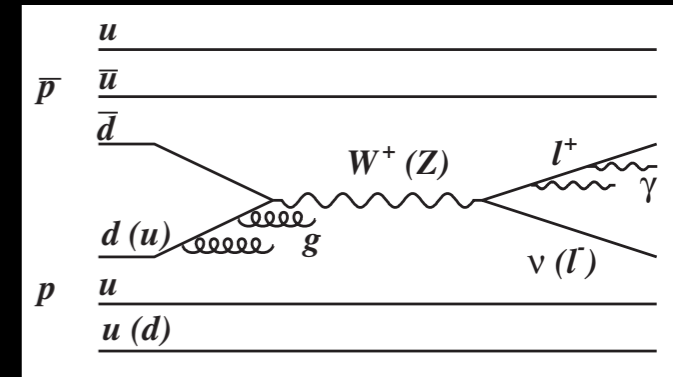
W boson production and decay

Parton distributions impact the measurement through lepton acceptance

Restriction in η reduces the fraction of low- p_T leptons

Small correction applied to update to NNPDF3.1 NNLO PDF

The set with the most W charge asymmetry measurements at the time



Uncertainty determined using a principal component analysis on the replica set

Measurement sensitive to ~15 eigenvectors

Leading 25 eigenvectors used to estimate uncertainty (3.9 MeV)

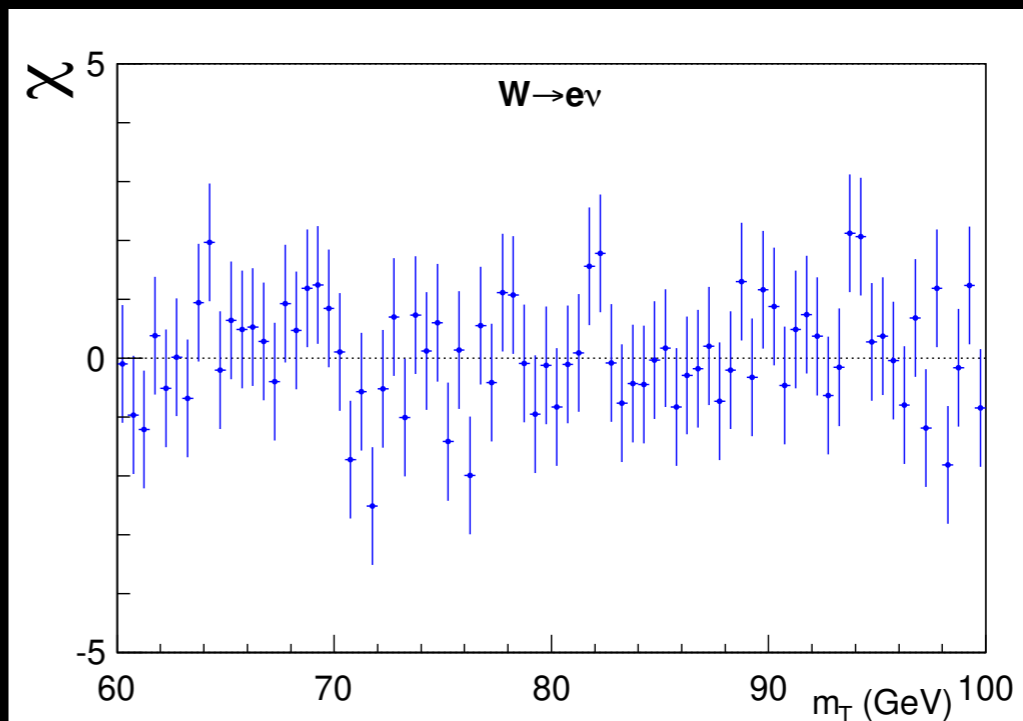
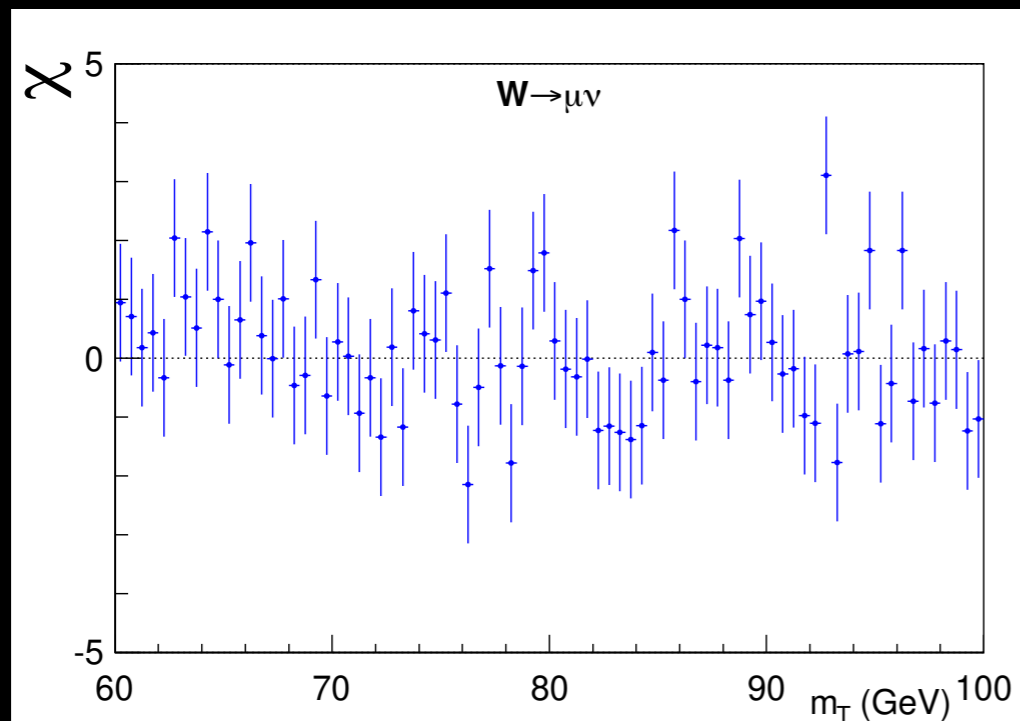
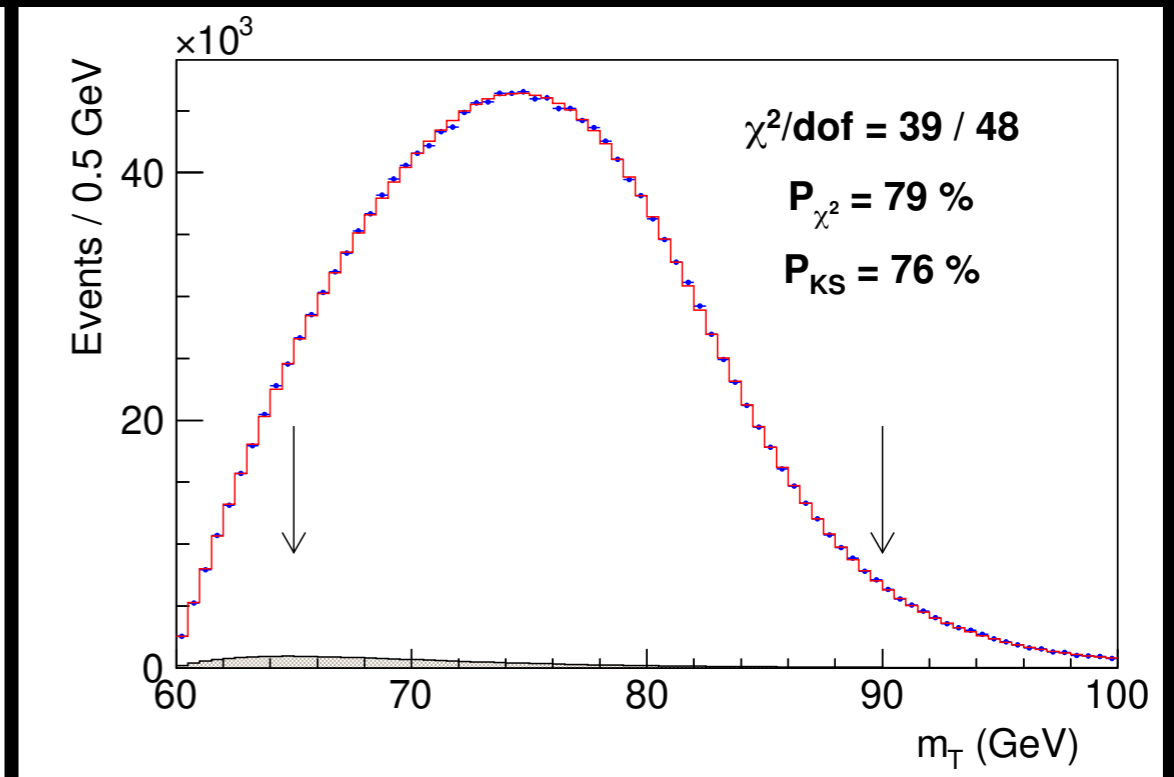
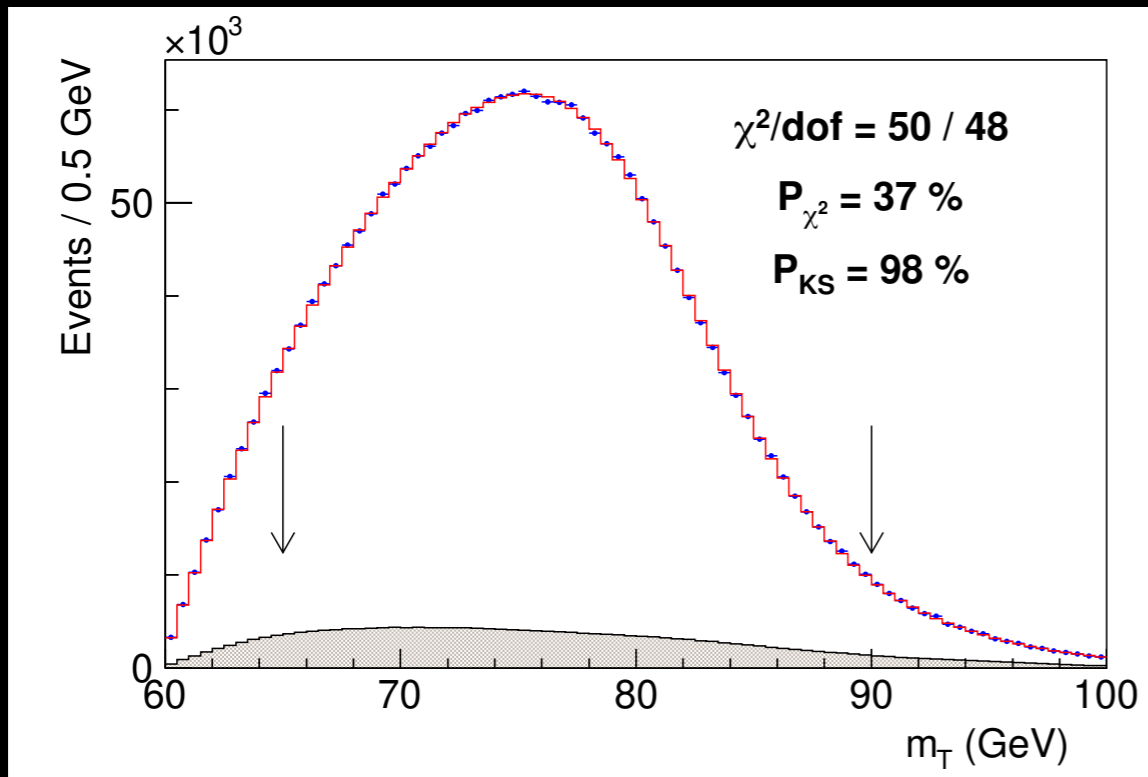
Three general NNLO PDF sets (NNPDF3.1, CT18, and MMHT14) have a range of ± 2.1 MeV from mean

Photos resummation with ME corrections used to model final-state photon radiation

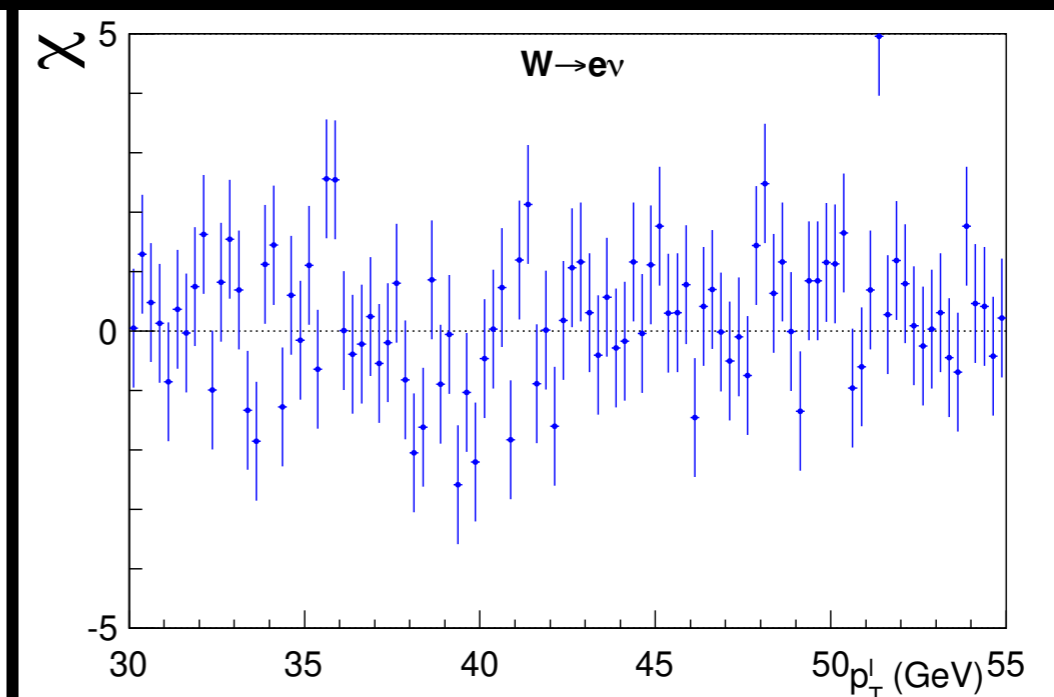
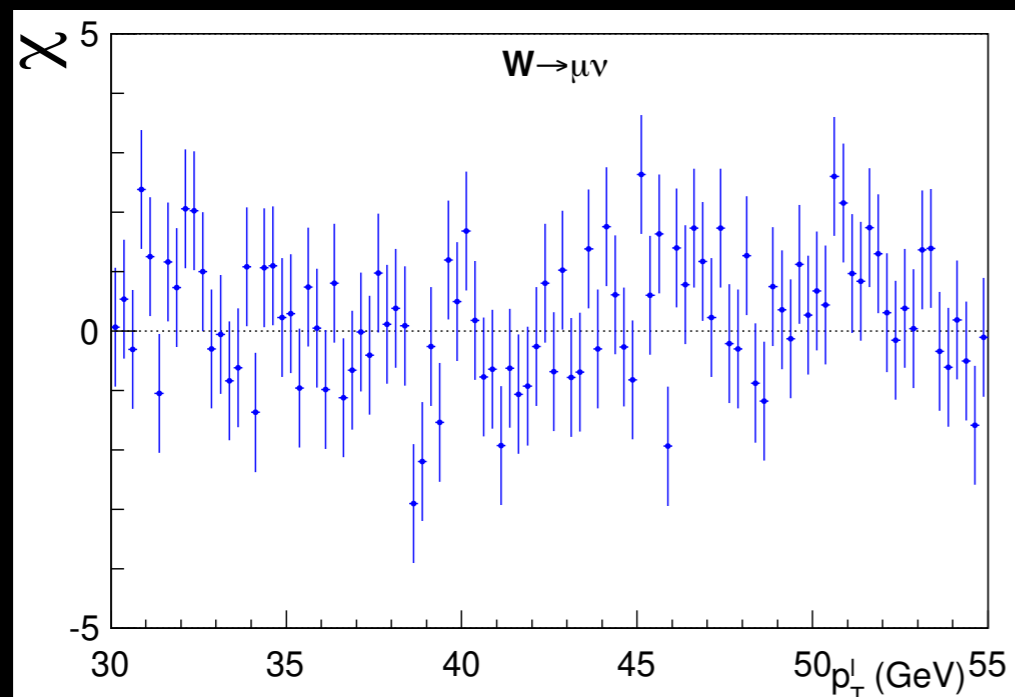
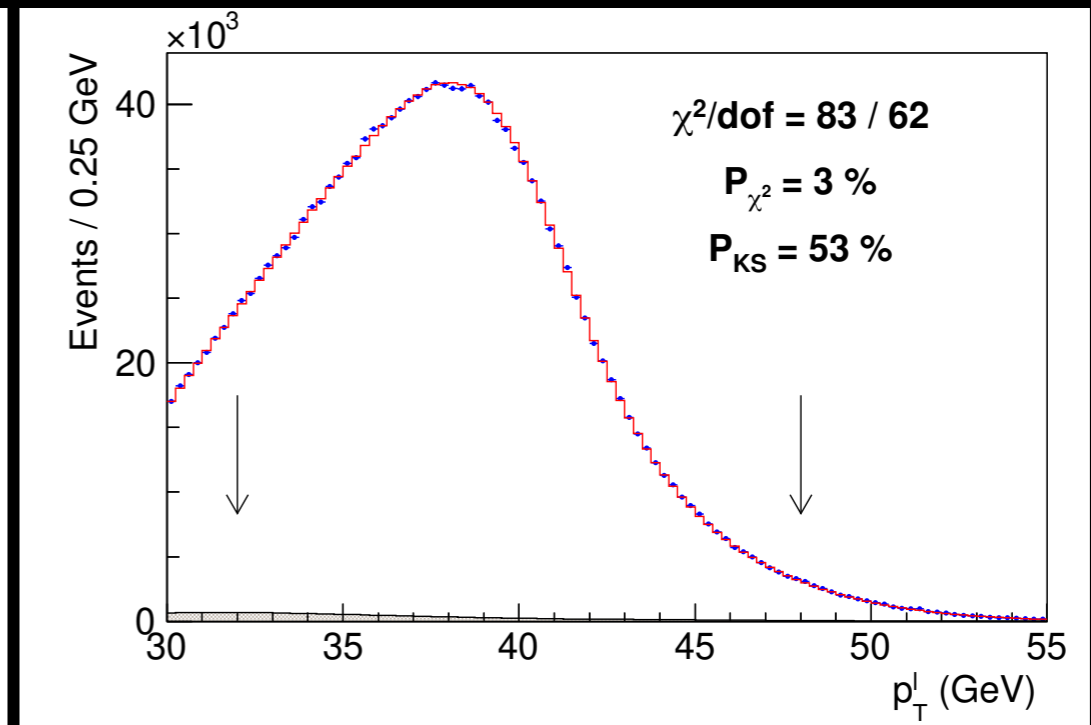
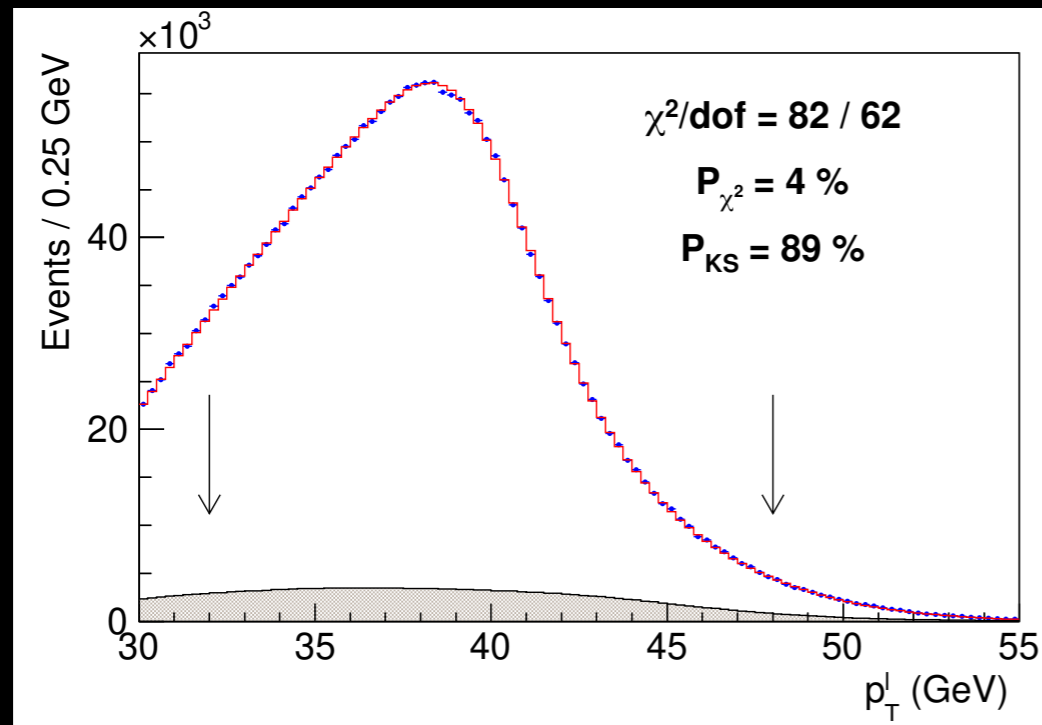
*validated by studying the average radiation in EM towers around the charged lepton,
and with the Z mass measurement*

W boson mass measurement

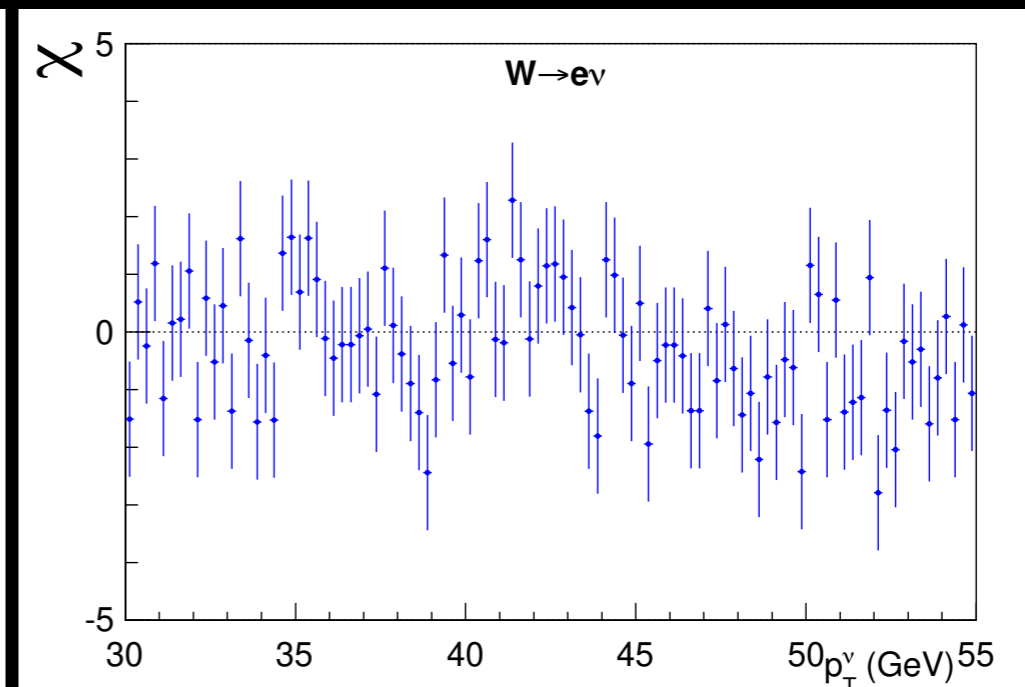
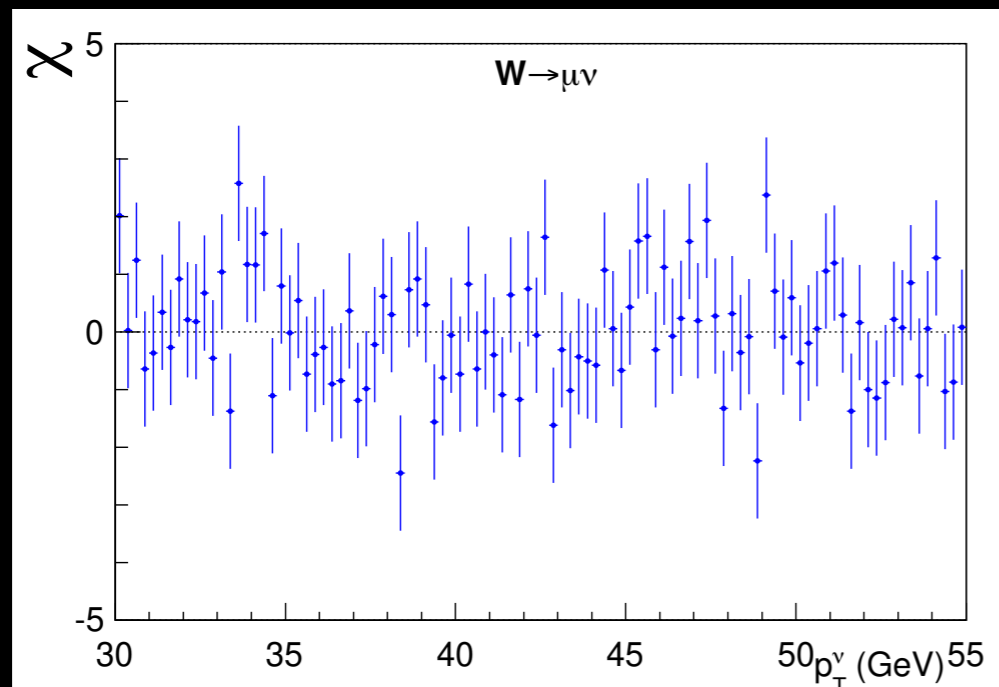
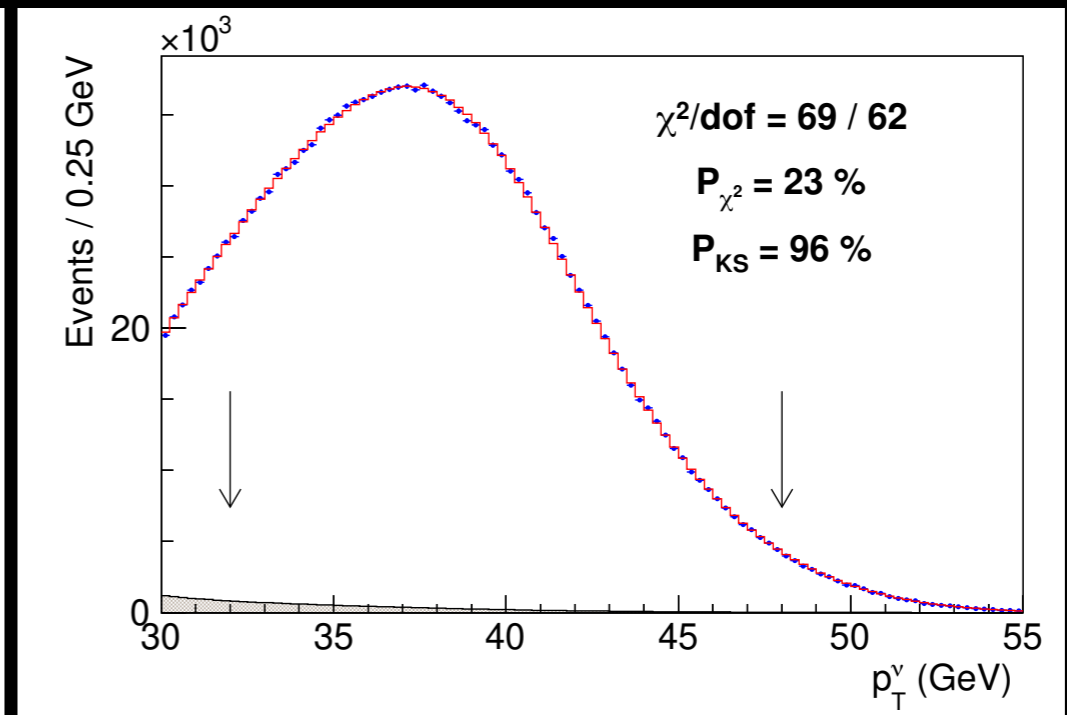
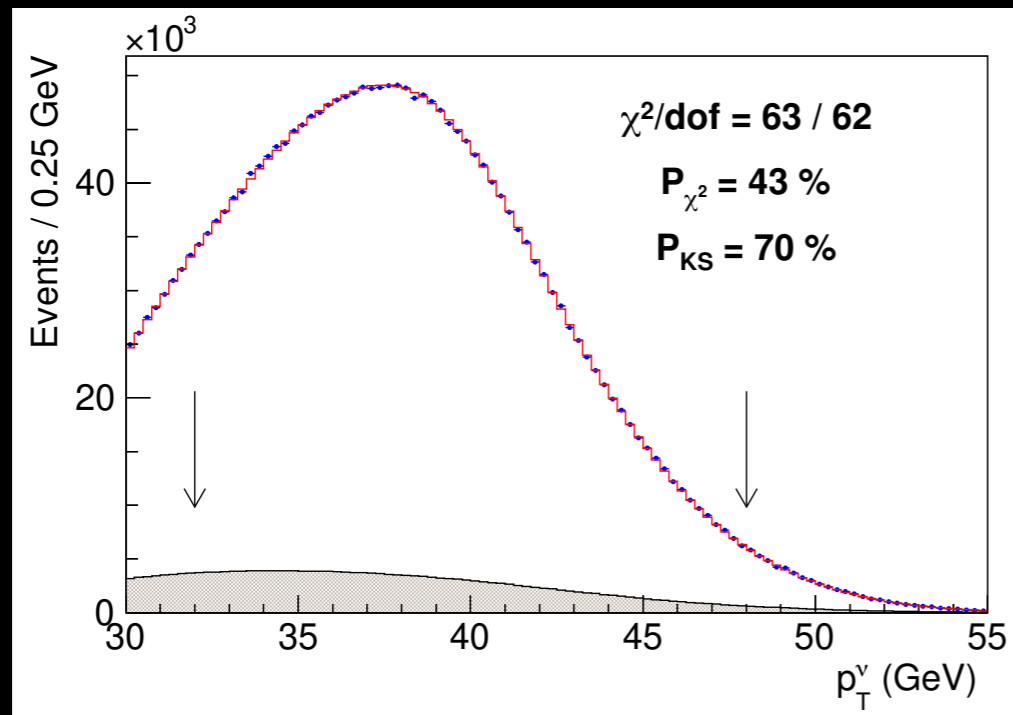
Result blinded by [-50,50] MeV offset until all previous steps complete



Mass measurement with p_T^ℓ distribution



Mass measurement with p_T^ν distribution



W boson mass measurement

Combination	m_T fit		p_T^ℓ fit		p_T^ν fit		Value (MeV)	χ^2/dof	Probability (%)
	Electrons	Muons	Electrons	Muons	Electrons	Muons			
m_T	✓	✓					80 439.0 ± 9.8	1.2 / 1	28
p_T^ℓ			✓	✓			80 421.2 ± 11.9	0.9 / 1	36
p_T^ν					✓	✓	80 427.7 ± 13.8	0.0 / 1	91
m_T & p_T^ℓ	✓	✓	✓	✓			80 435.4 ± 9.5	4.8 / 3	19
m_T & p_T^ν	✓	✓			✓	✓	80 437.9 ± 9.7	2.2 / 3	53
p_T^ℓ & p_T^ν			✓	✓	✓	✓	80 424.1 ± 10.1	1.1 / 3	78
Electrons	✓		✓		✓		80 424.6 ± 13.2	3.3 / 2	19
Muons		✓		✓		✓	80 437.9 ± 11.0	3.6 / 2	17
All	✓	✓	✓	✓	✓	✓	80 433.5 ± 9.4	7.4 / 5	20

Fit difference	Muon channel	Electron channel
$M_W(\ell^+) - M_W(\ell^-)$	$-7.8 \pm 18.5_{\text{stat}} \pm 12.7_{\text{COT}}$	$14.7 \pm 21.3_{\text{stat}} \pm 7.7_{\text{stat}}^{\text{E/P}} (0.4 \pm 21.3_{\text{stat}})$
$M_W(\phi_e > 0) - M_W(\phi_e < 0)$	$24.4 \pm 18.5_{\text{stat}}$	$9.9 \pm 21.3_{\text{stat}} \pm 7.5_{\text{stat}}^{\text{E/P}} (-0.8 \pm 21.3_{\text{stat}})$
$M_Z(\text{run} > 271100) - M_Z(\text{run} < 271100)$	$5.2 \pm 12.2_{\text{stat}}$	$63.2 \pm 29.9_{\text{stat}} \pm 8.2_{\text{stat}}^{\text{E/P}} (-16.0 \pm 29.9_{\text{stat}})$

Summary

The W boson mass is an important parameter in particle physics

Measurement of W boson mass with <10 MeV precision achieved with complete CDF data set

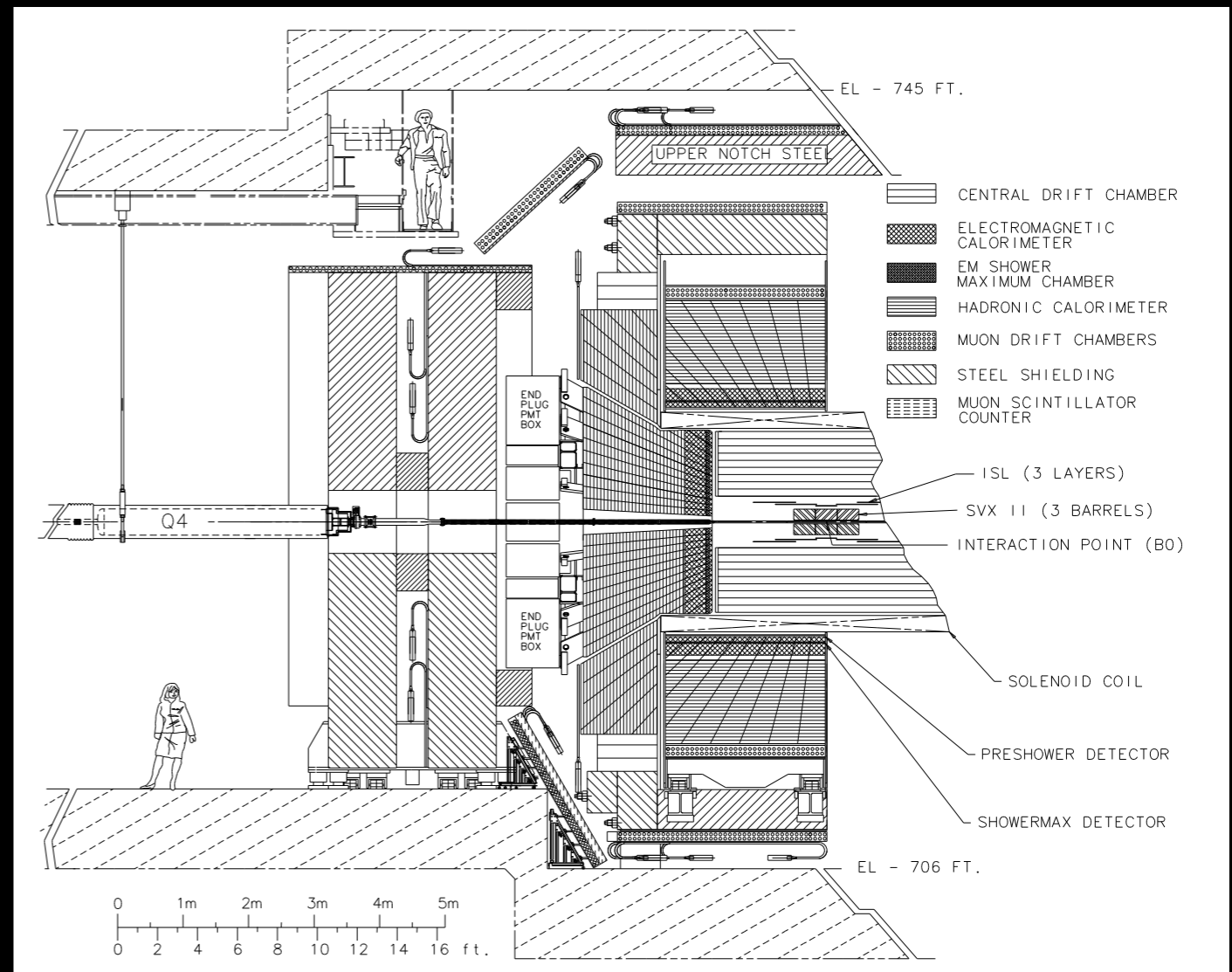
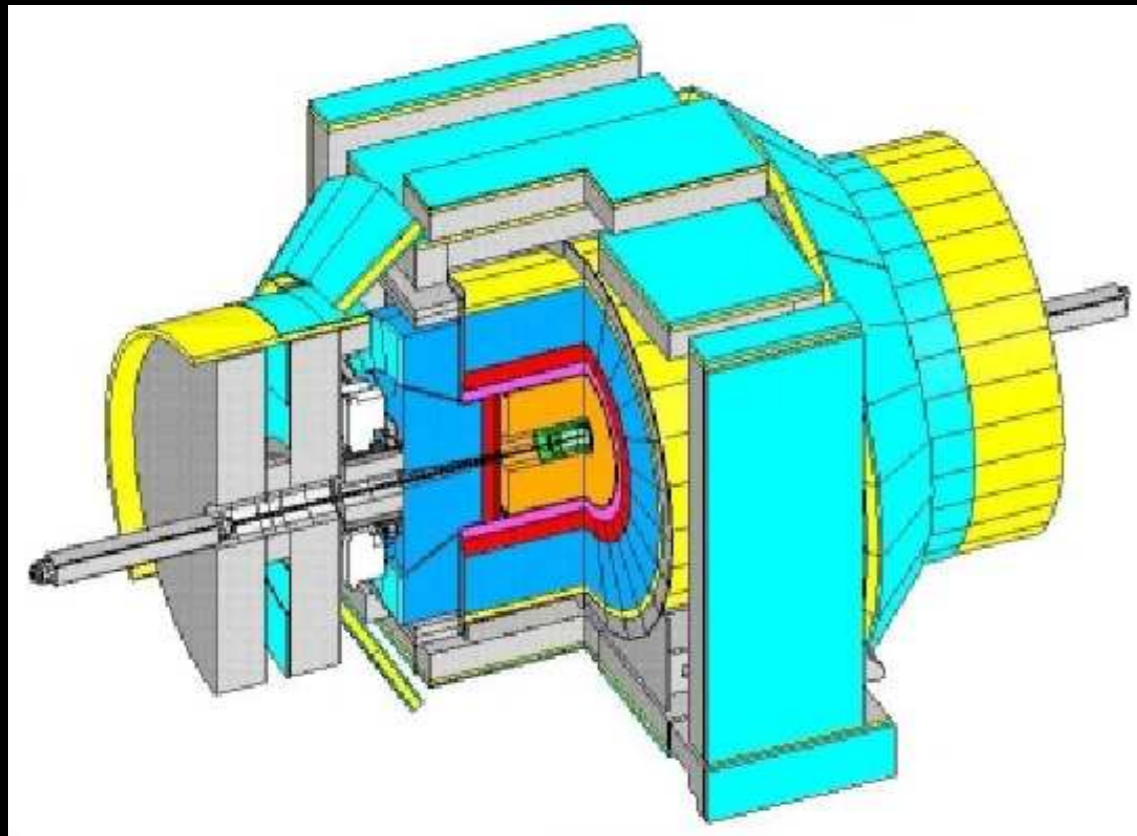
Result of >20 years of experience with the CDF II detector

0.01% precision required flexibility: all experimental aspects controlled by the analysis team
Reconstruction, alignment, calibration, simulation, analysis

Analysis procedures approved pre-unblinding and frozen

Surprising 0.1% deviation from SM motivates expanded study of m_W measurements and procedures

Backup



Uncertainties

Source of systematic uncertainty	m_T fit			p_T^ℓ fit			p_T^ν fit		
	Electrons	Muons	Common	Electrons	Muons	Common	Electrons	Muons	Common
Lepton energy scale	5.8	2.1	1.8	5.8	2.1	1.8	5.8	2.1	1.8
Lepton energy resolution	0.9	0.3	-0.3	0.9	0.3	-0.3	0.9	0.3	-0.3
Recoil energy scale	1.8	1.8	1.8	3.5	3.5	3.5	0.7	0.7	0.7
Recoil energy resolution	1.8	1.8	1.8	3.6	3.6	3.6	5.2	5.2	5.2
Lepton $u_{ }$ efficiency	0.5	0.5	0	1.3	1.0	0	2.6	2.1	0
Lepton removal	1.0	1.7	0	0	0	0	2.0	3.4	0
Backgrounds	2.6	3.9	0	6.6	6.4	0	6.4	6.8	0
p_T^Z model	0.7	0.7	0.7	2.3	2.3	2.3	0.9	0.9	0.9
p_T^W / p_T^Z model	0.8	0.8	0.8	2.3	2.3	2.3	0.9	0.9	0.9
Parton distributions	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9
QED radiation	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7
Statistical	10.3	9.2	0	10.7	9.6	0	14.5	13.1	0
Total	13.5	11.8	5.8	16.0	14.1	7.9	18.8	17.1	7.4

Background fractions

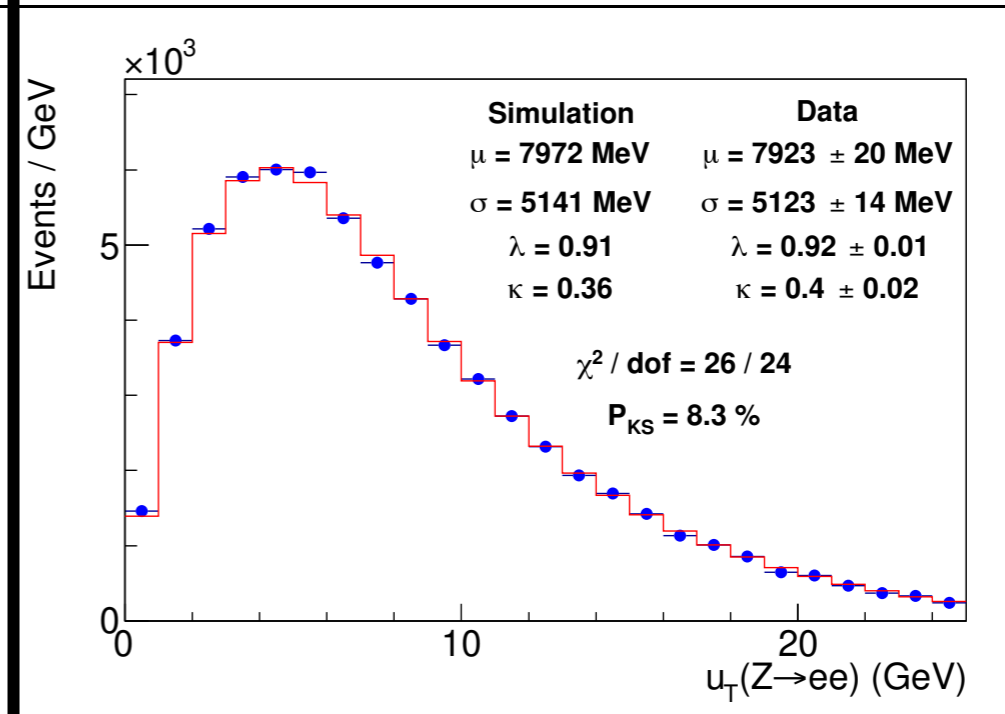
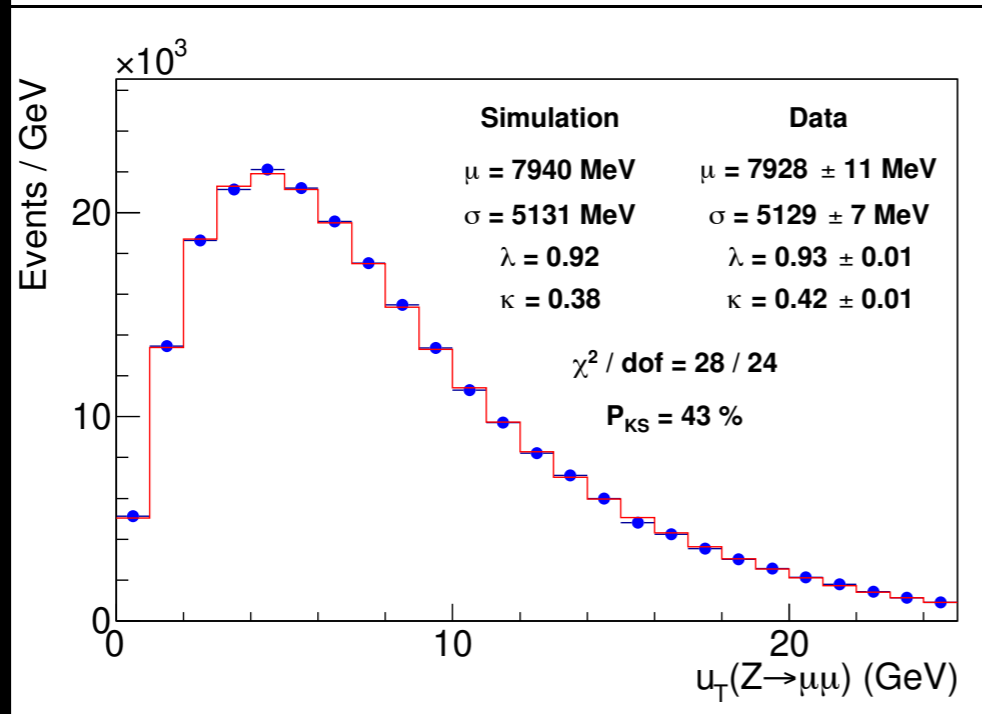
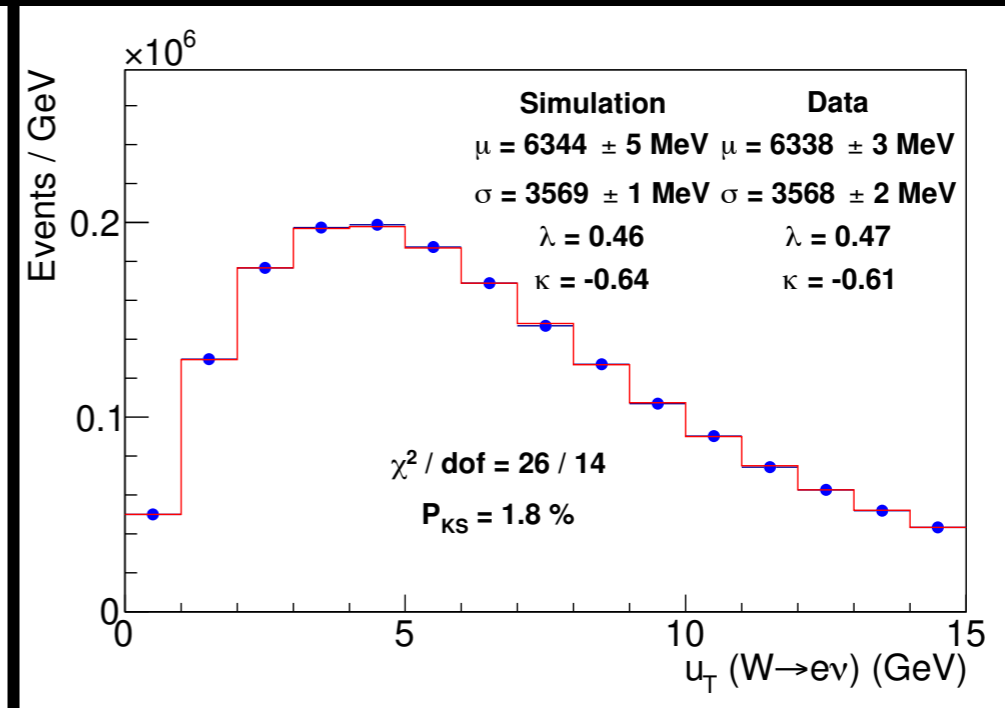
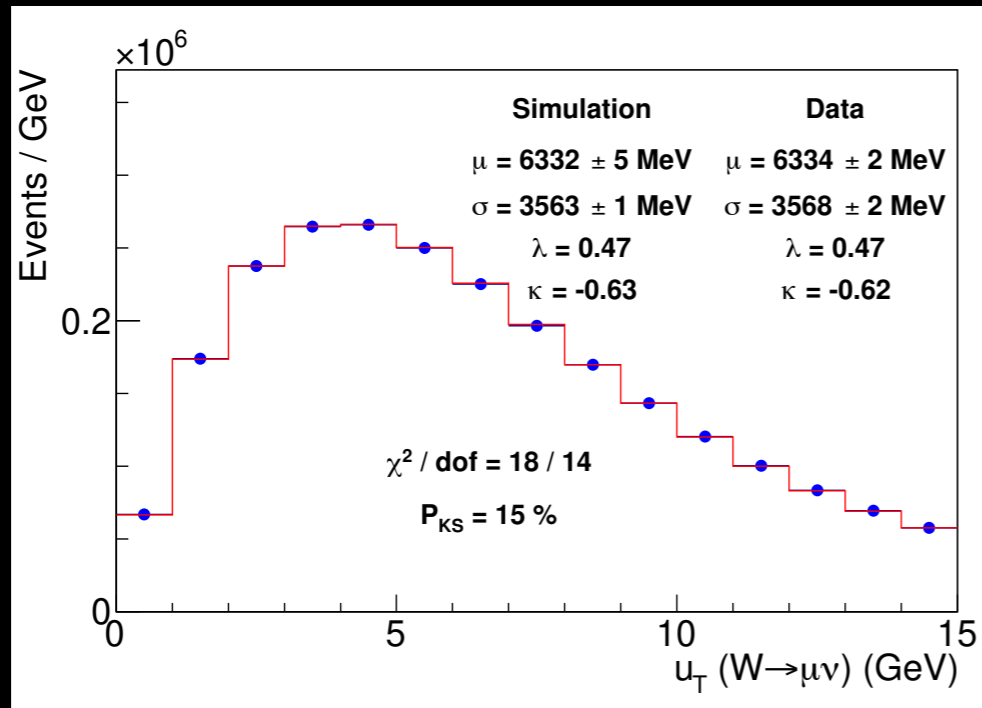
Source	Fraction (%)	δM_W (MeV)		
		m_T fit	p_T^μ fit	p_T^ν fit
$Z/\gamma^* \rightarrow \mu\mu$	7.37 ± 0.10	1.6 (0.7)	3.6 (0.3)	0.1 (1.5)
$W \rightarrow \tau\nu$	0.880 ± 0.004	0.1 (0.0)	0.1 (0.0)	0.1 (0.0)
Hadronic jets	0.01 ± 0.04	0.1 (0.8)	-0.6 (0.8)	2.4 (0.5)
Decays in flight	0.20 ± 0.14	1.3 (3.1)	1.3 (5.0)	-5.2 (3.2)
Cosmic rays	0.01 ± 0.01	0.3 (0.0)	0.5 (0.0)	0.3 (0.3)
Total	8.47 ± 0.18	2.1 (3.3)	3.9 (5.1)	5.7 (3.6)

Source	Fraction (%)	δM_W (MeV)		
		m_T fit	p_T^e fit	p_T^ν fit
$Z/\gamma^* \rightarrow ee$	0.134 ± 0.003	0.2 (0.3)	0.3 (0.0)	0.0 (0.6)
$W \rightarrow \tau\nu$	0.94 ± 0.01	0.6 (0.0)	0.6 (0.0)	0.6 (0.0)
Hadronic jets	0.34 ± 0.08	2.2 (1.2)	0.9 (6.5)	6.2 (-1.1)
Total	1.41 ± 0.08	2.3 (1.2)	1.1 (6.5)	6.2 (1.3)

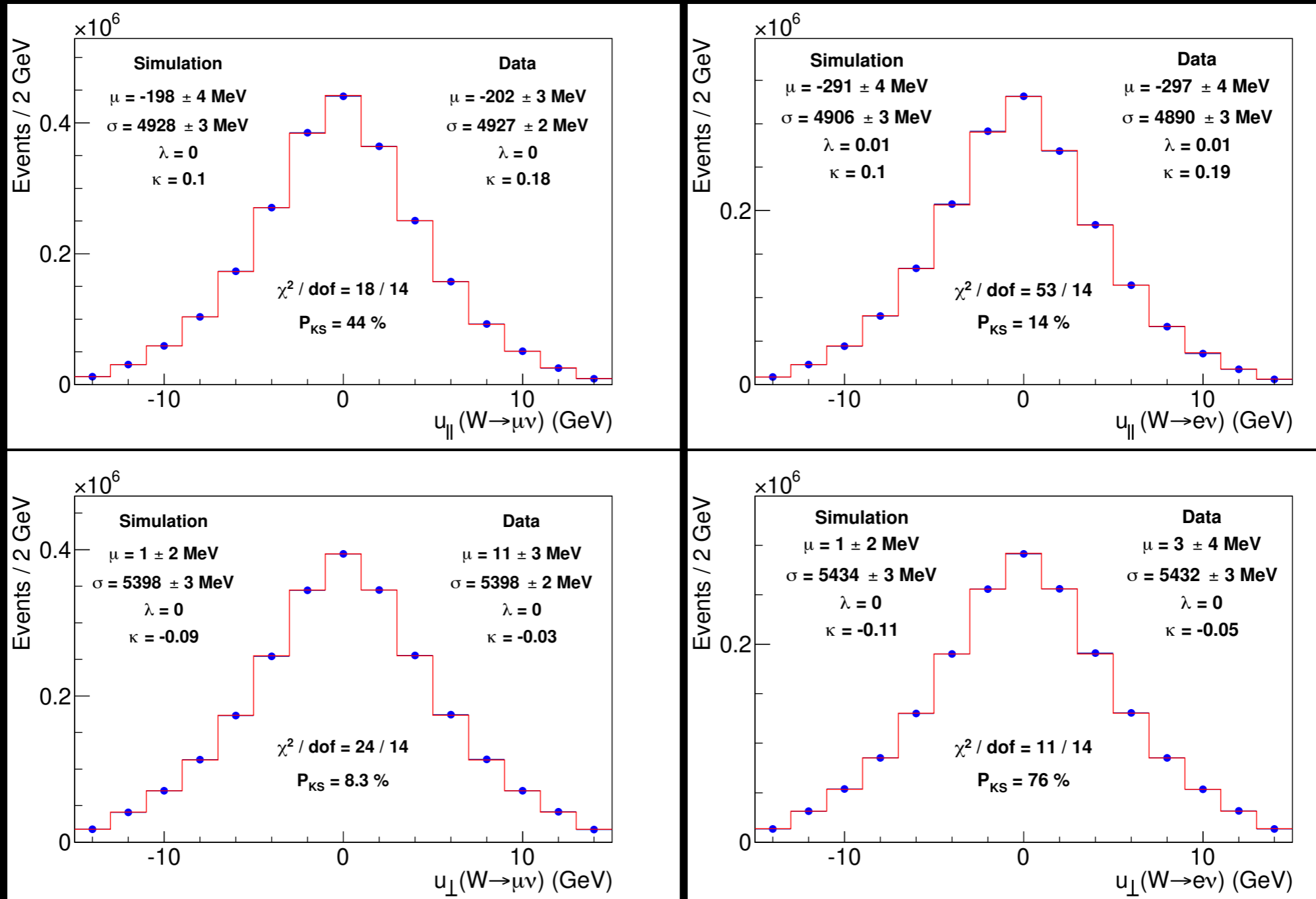
Initial state LO & NLO

W ⁺ initial	Type	Pythia LO	Madgraph LO	Madgraph NLO
u dbar	v-v	81.7%	82.0%	82.7%
dbar u	s-s	8.9%	9.0%	8.8%
u sbar	v-s	1.6%	1.9%	1.8%
sbar u	s-s	0.3%	0.3%	0.3%
c sbar	s-s	2.9%	2.9%	-
sbar c	s-s	2.9%	2.9%	-
c dbar	s-v	0.7%	0.7%	-
dbar c	s-s	0.2%	0.2%	-
u g	v-g	-	-	3.7%
g dbar	g-v	-	-	1.8%
g u	g-s	-	-	0.4%
dbar g	s-g	-	-	0.5%
g sbar	g-s	-	-	0.02%
sbar g	s-g	-	-	0.02%

Recoil in W & Z events



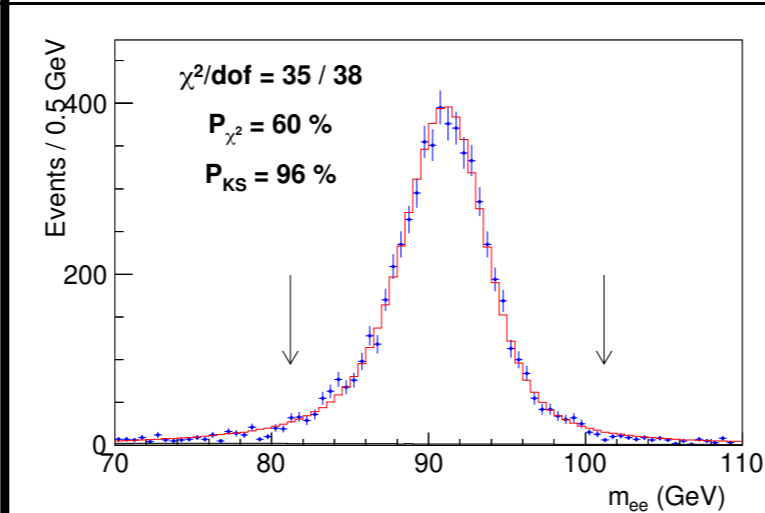
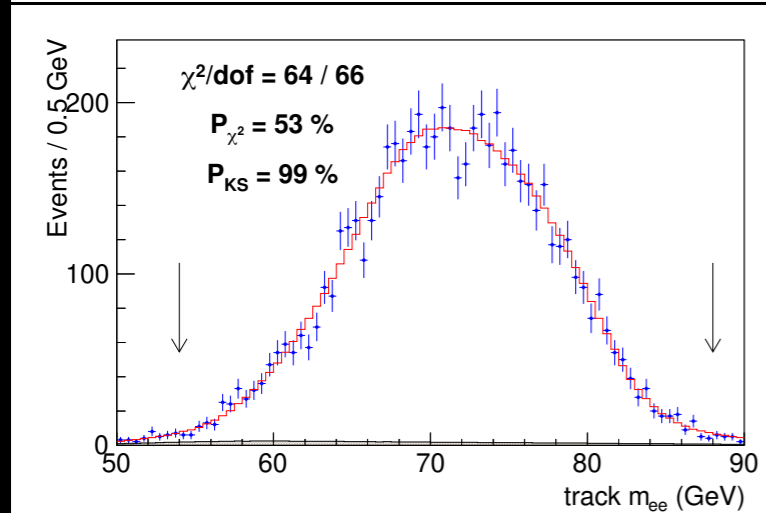
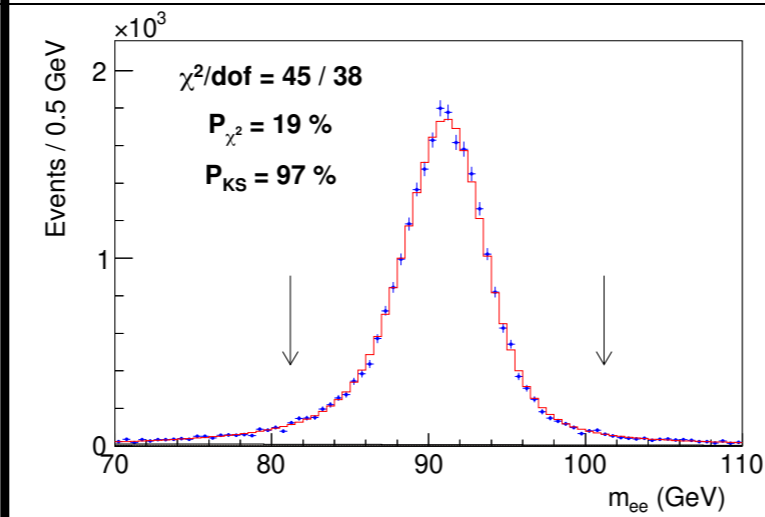
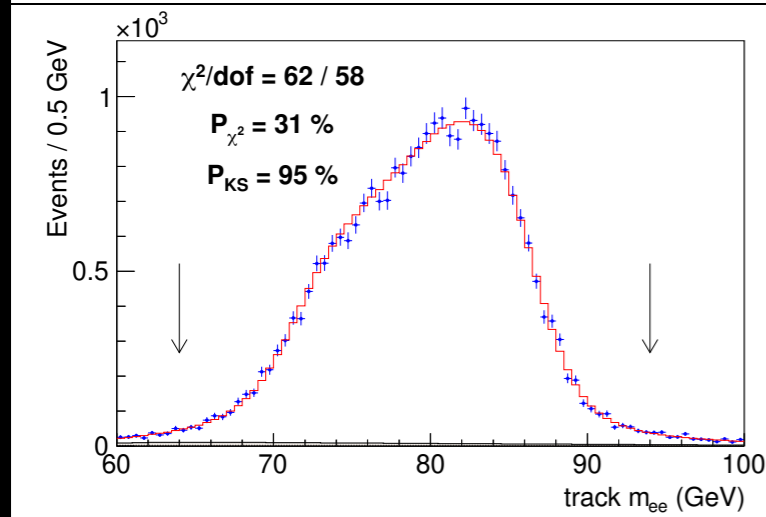
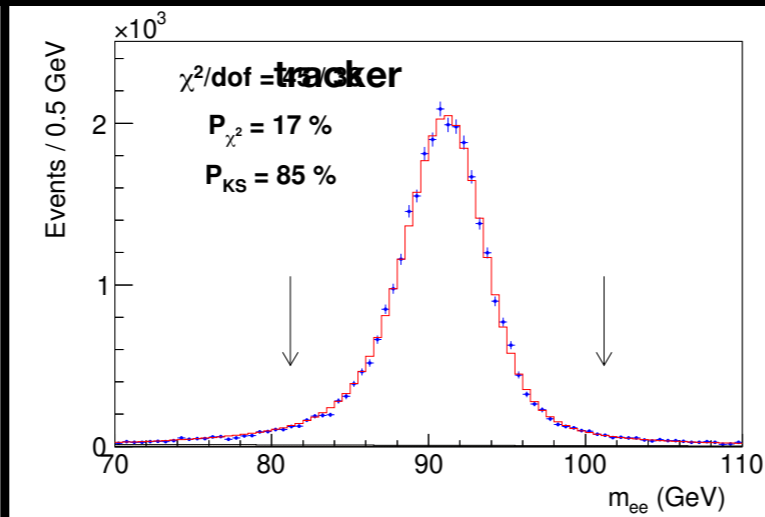
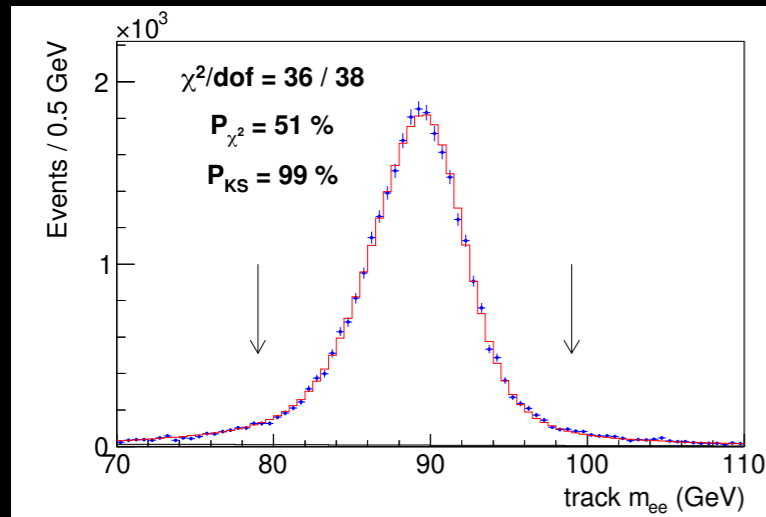
Recoil projections in W events



Recoil model parameters

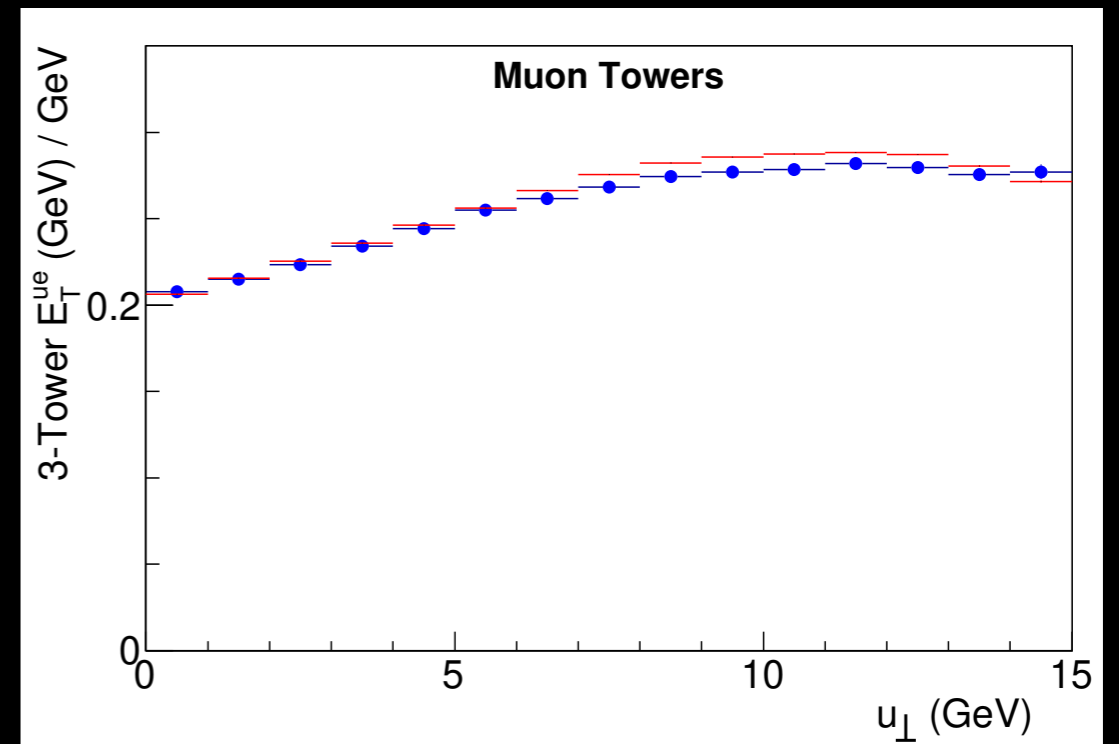
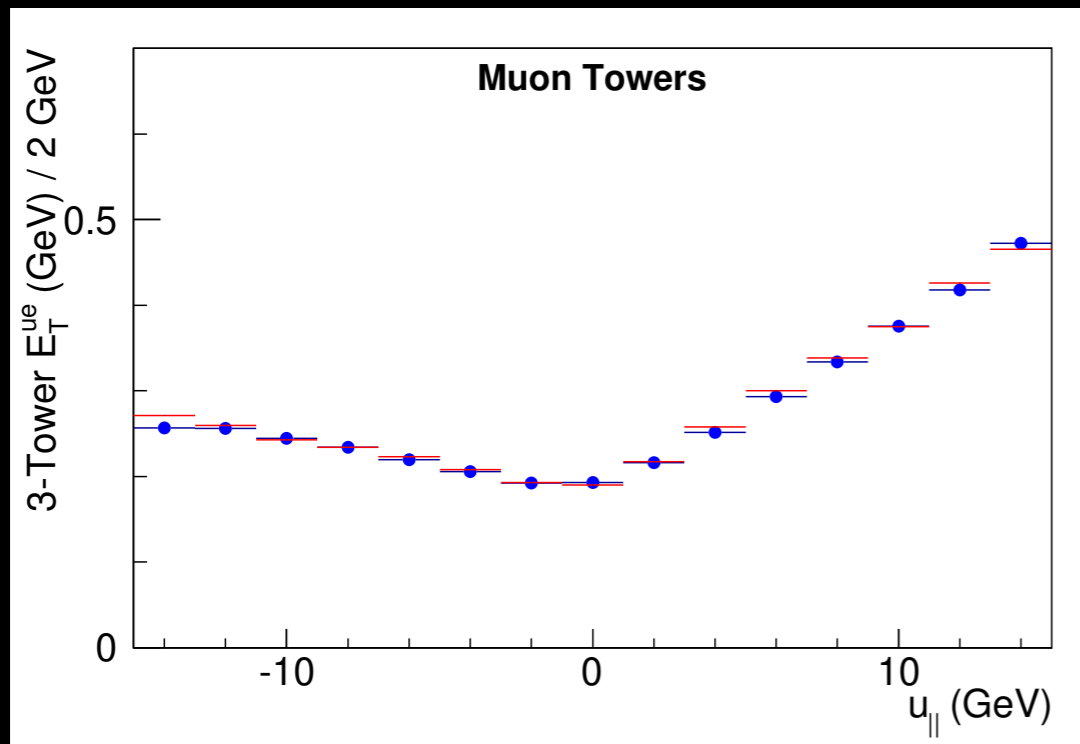
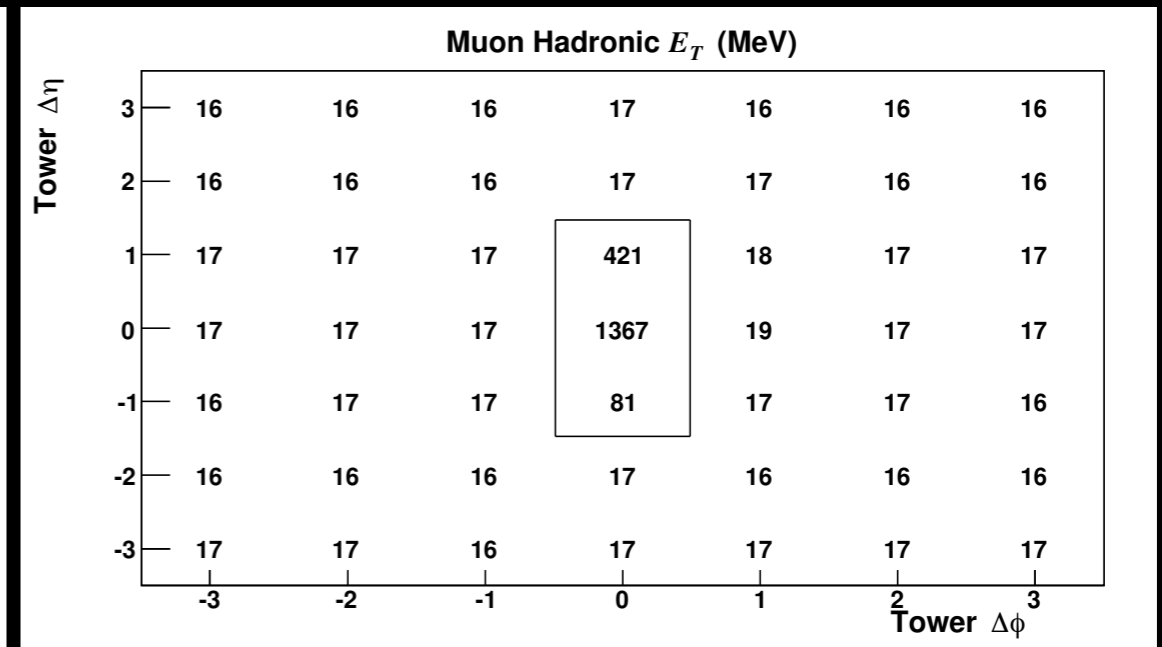
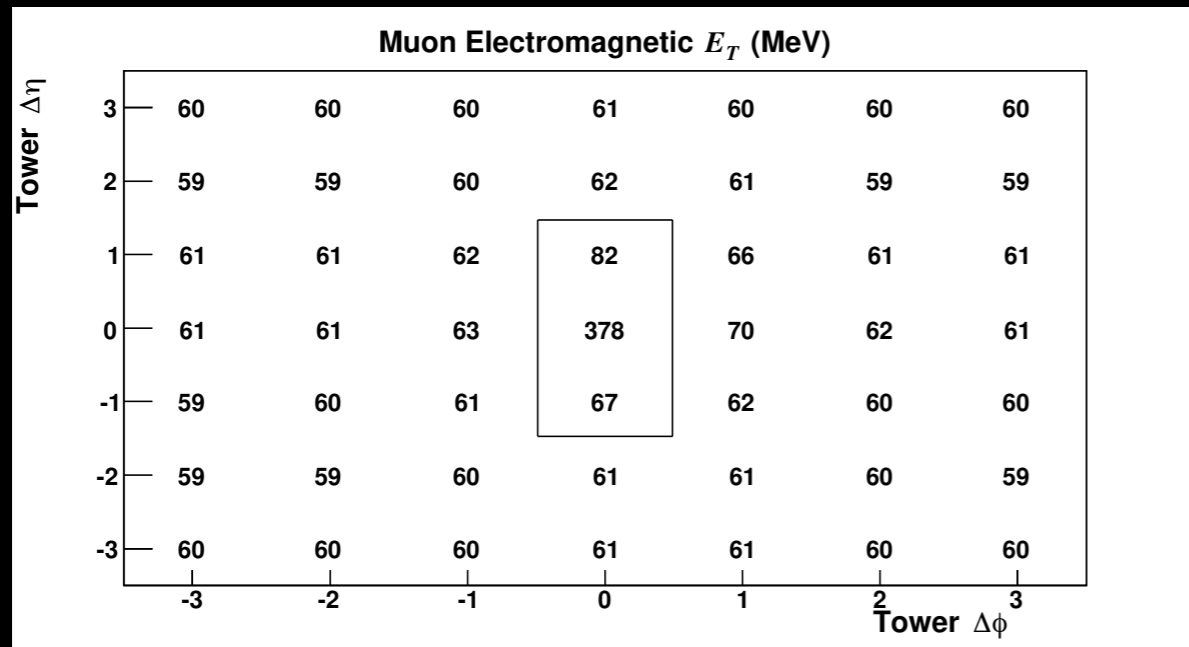
Parameter	Description	Source	m_T	p_T^ℓ	p_T^ν
a	average response	Fig. S23	-1.6	-2.9	-0.2
b	response non-linearity	Fig. S23	-0.8	-2.0	0.7
Response			1.8	3.5	0.7
N_V	spectator interactions	Fig. S24	0.5	-3.2	3.6
s_{had}	sampling resolution	Fig. S24	0.3	0.3	0.8
$f_{\pi^0}^4$	EM fluctuations at low u_T	Fig. S25	-0.3	-0.2	-1.0
$f_{\pi^0}^{15}$	EM fluctuations at high u_T	Fig. S25	-0.3	-0.3	-0.2
α	angular resolution at low u_T	Fig. S26	1.4	0.1	2.5
β	angular resolution at intermediate u_T	Fig. S26	0.2	0.1	0.7
γ	angular resolution at high u_T	Fig. S26	0.3	0.3	0.7
f_2^a	average dijet component	Fig. S27	0.1	-1.1	0.8
f_2^s	variation of dijet component with u_T	Fig. S27	-0.1	-0.2	-0.1
k_ξ	average dijet resolution	Fig. S28	-0.1	0.1	-0.3
δ_ξ	fluctuations in dijet resolution	Fig. S28	-0.2	0.2	-1.1
A_ξ	higher-order term in dijet resolution	Fig. S28	0.1	-1.0	0.7
μ_ξ	—"—	Fig. S28	-0.5	-0.4	-0.9
ϵ_ξ	—"—	Fig. S28	0.1	-0.2	0.4
S_ξ^+	—"—	Fig. S28	0.5	-0.4	1.4
S_ξ^-	—"—	Fig. S28	-0.3	-0.2	-0.5
q_ξ	—"—	Fig. S28	-0.2	0.0	0.2
Resolution			1.8	3.6	5.2

Z mass fits using tracker or calorimeter



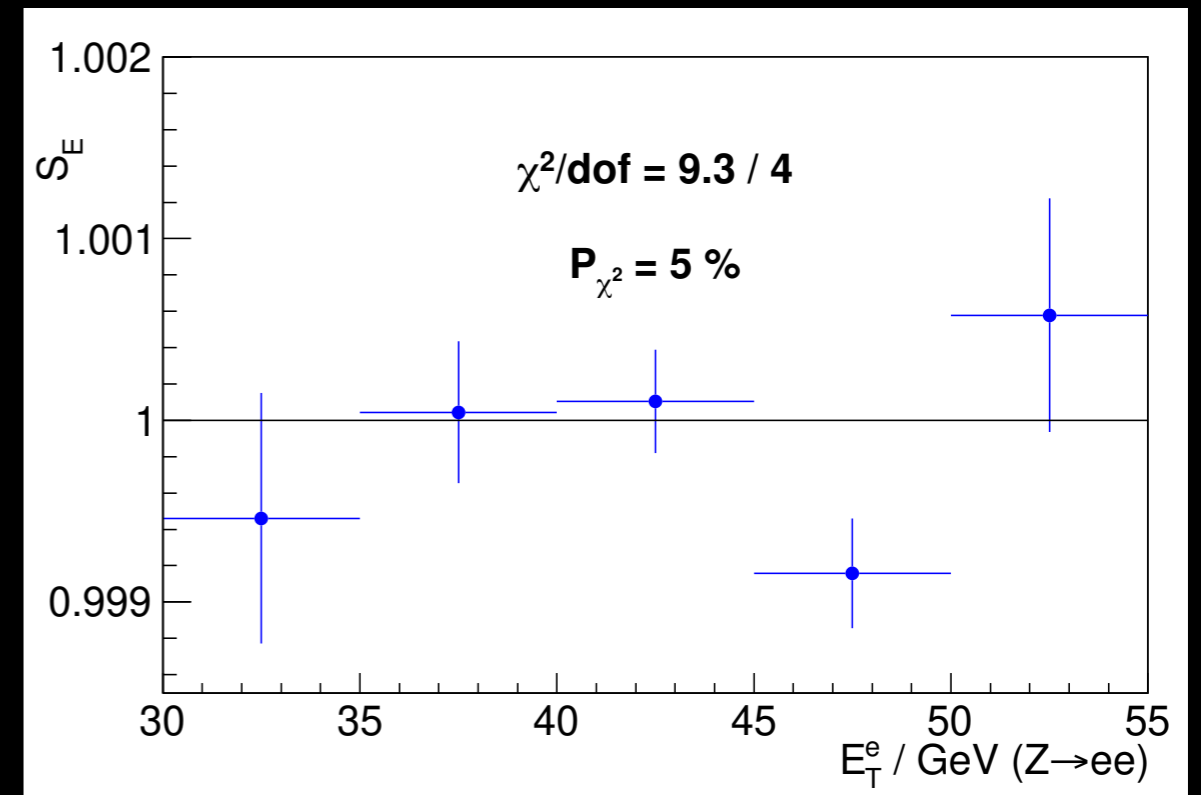
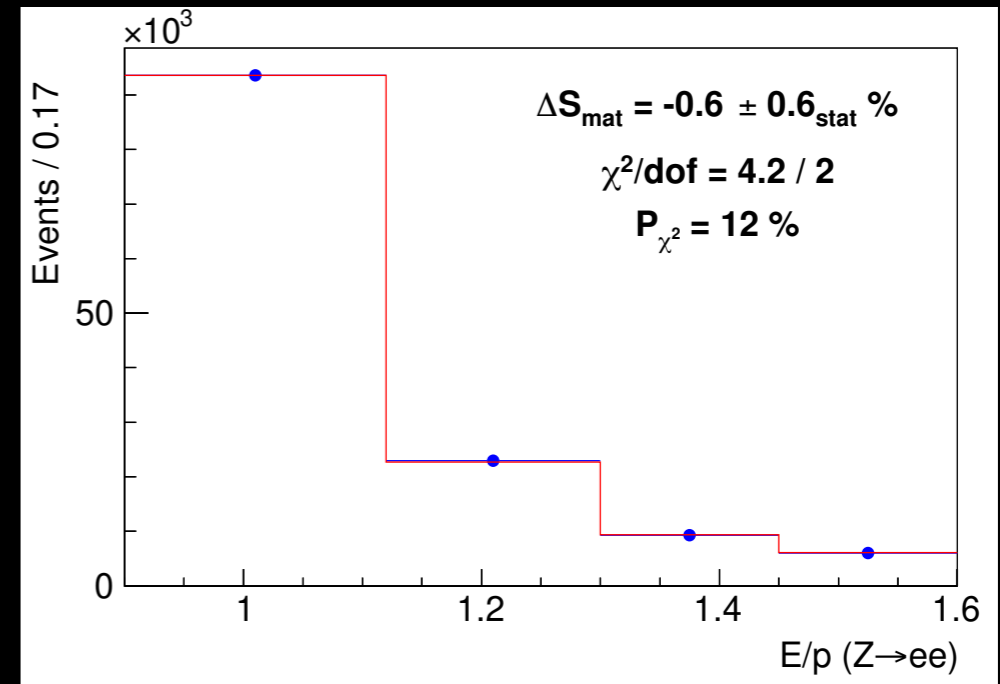
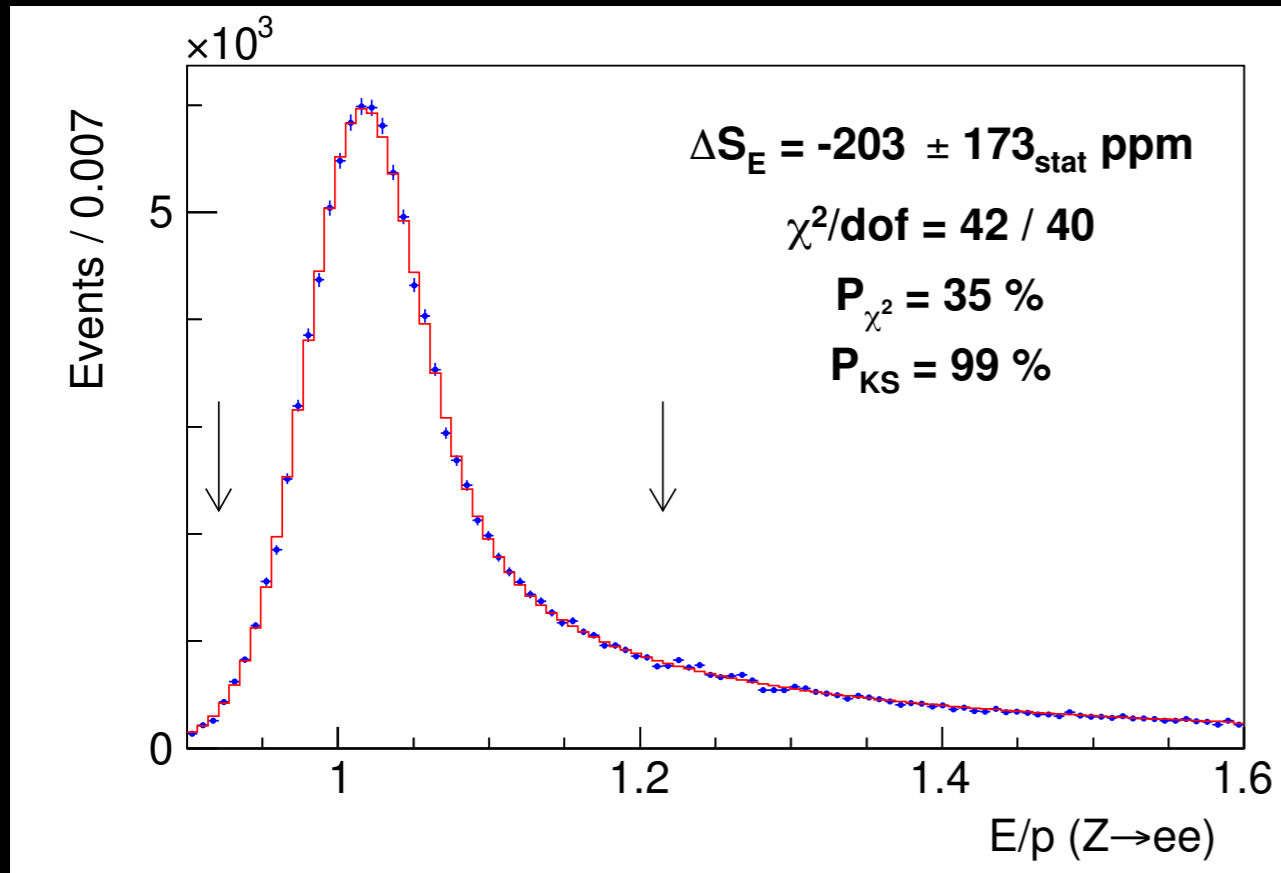
Electrons	Calorimeter	Track
$E/p < 1.1$ only	$91\,190.9 \pm 19.7$	$91\,215.2 \pm 22.4$
$E/p > 1.1$ and $E/p < 1.1$	$91\,201.1 \pm 21.5$	$91\,259.9 \pm 39.0$
$E/p > 1.1$ only	$91\,184.5 \pm 46.4$	$91\,167.7 \pm 109.9$

Recoil reconstruction in muon channel

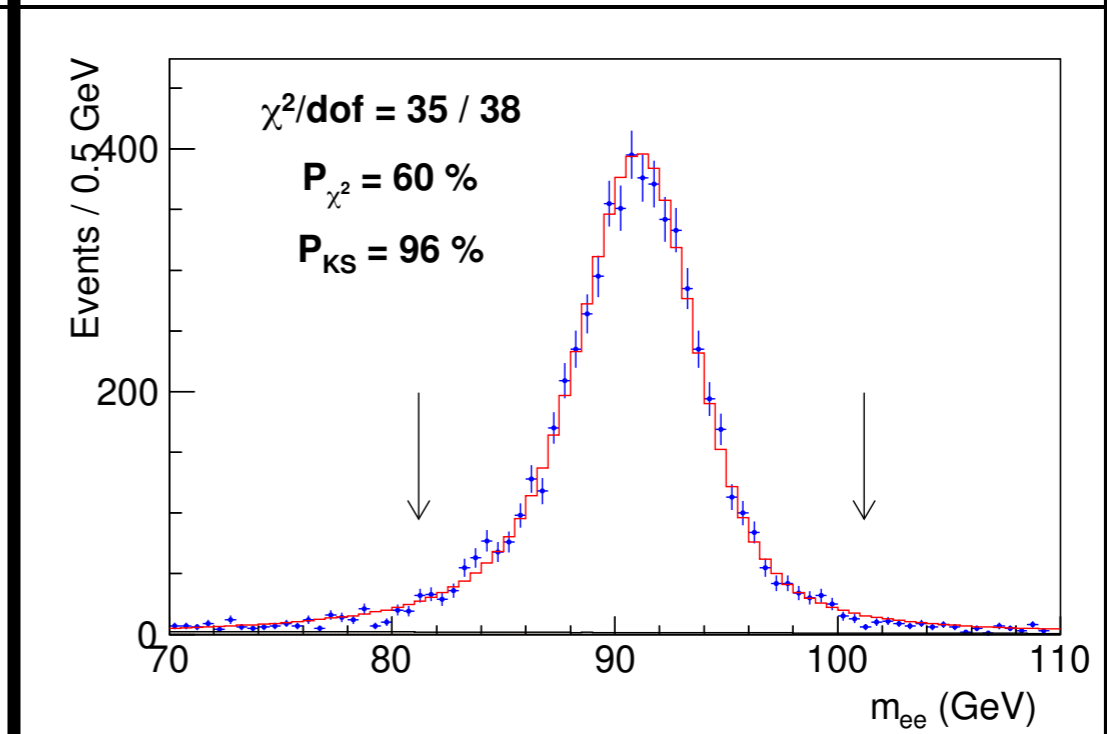
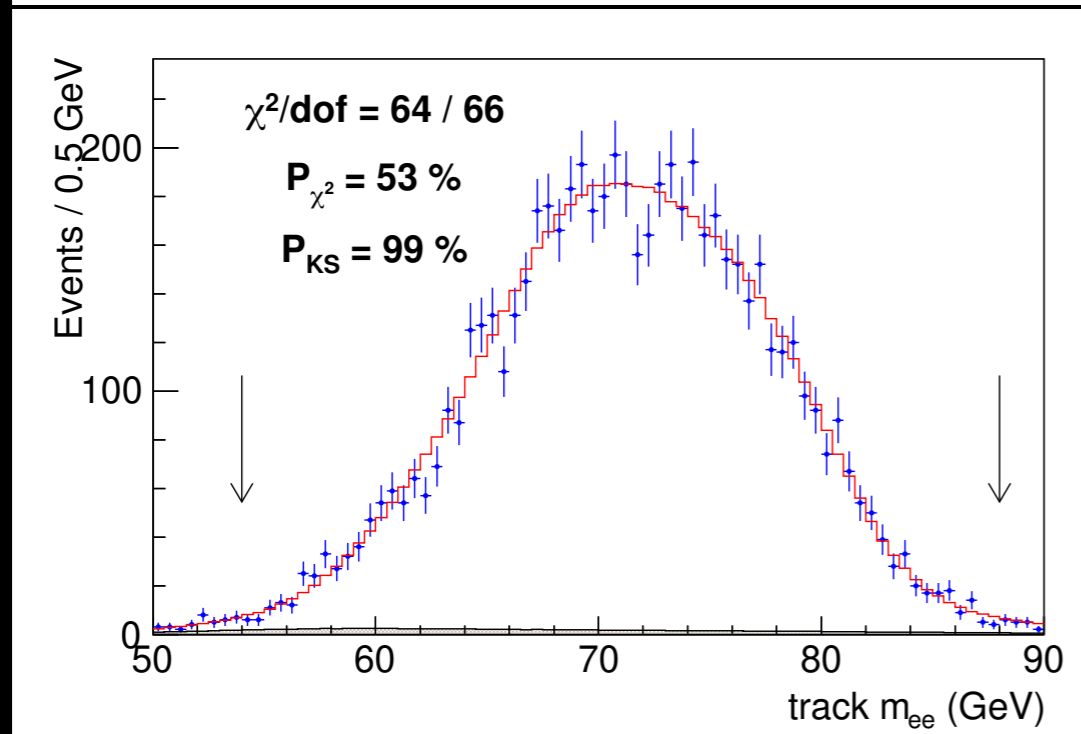
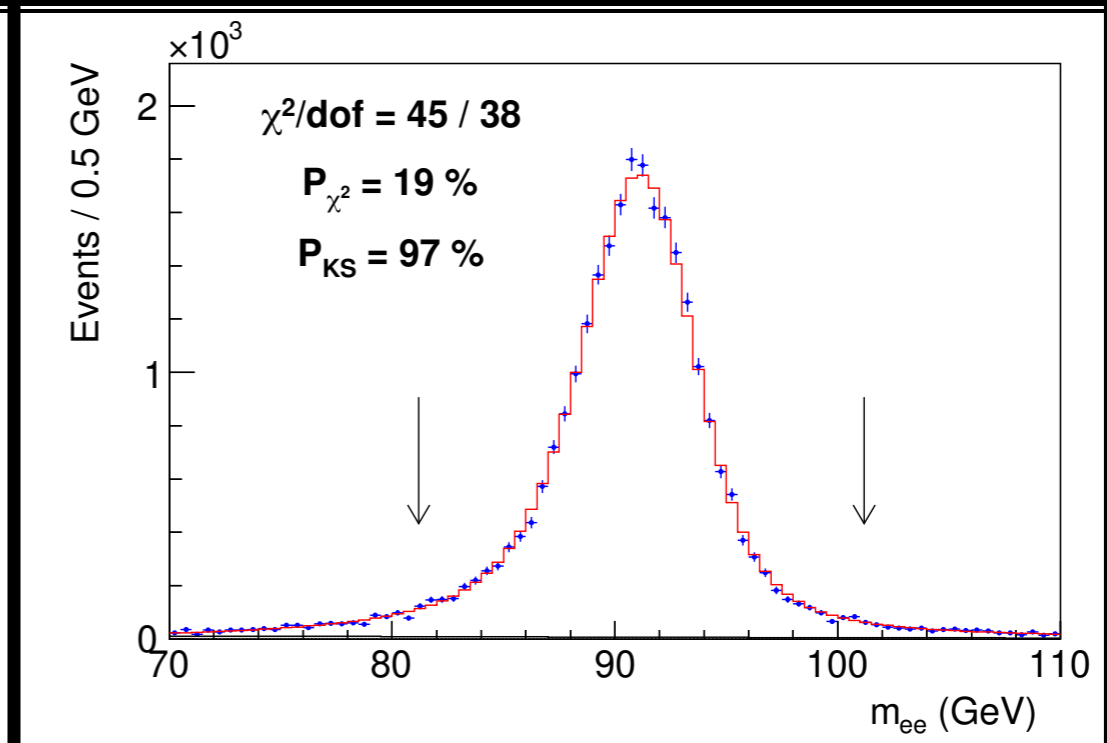
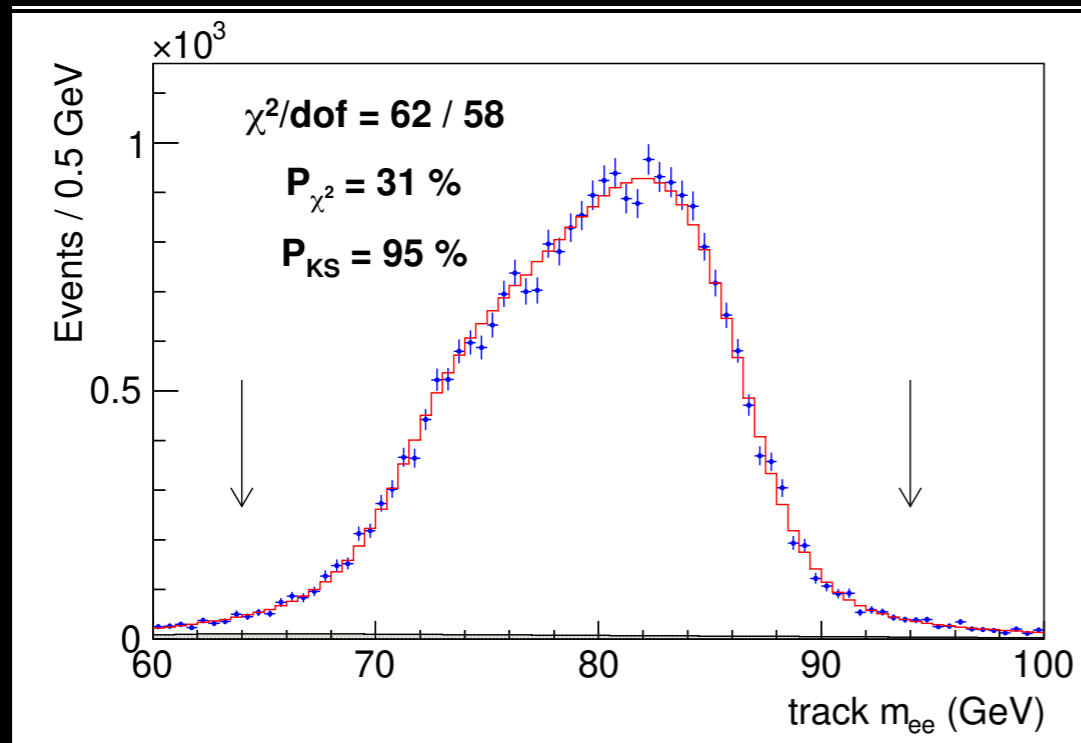


Electron momentum calibration

Gauge field potential



Electron momentum calibration



Muon momentum calibration

Source	J/ψ (ppm)	Υ (ppm)	Correlation (%)
QED	1	1	100
Magnetic field non-uniformity	13	13	100
Ionizing material correction	11	8	100
Resolution model	10	1	100
Background model	7	6	0
COT alignment correction	4	8	0
Trigger efficiency	18	9	100
Fit range	2	1	100
$\Delta p/p$ step size	2	2	0
World-average mass value	4	27	0
Total systematic	29	34	16 ppm
Statistical NBC (BC)	2	13(10)	0
Total	29	36	16 ppm

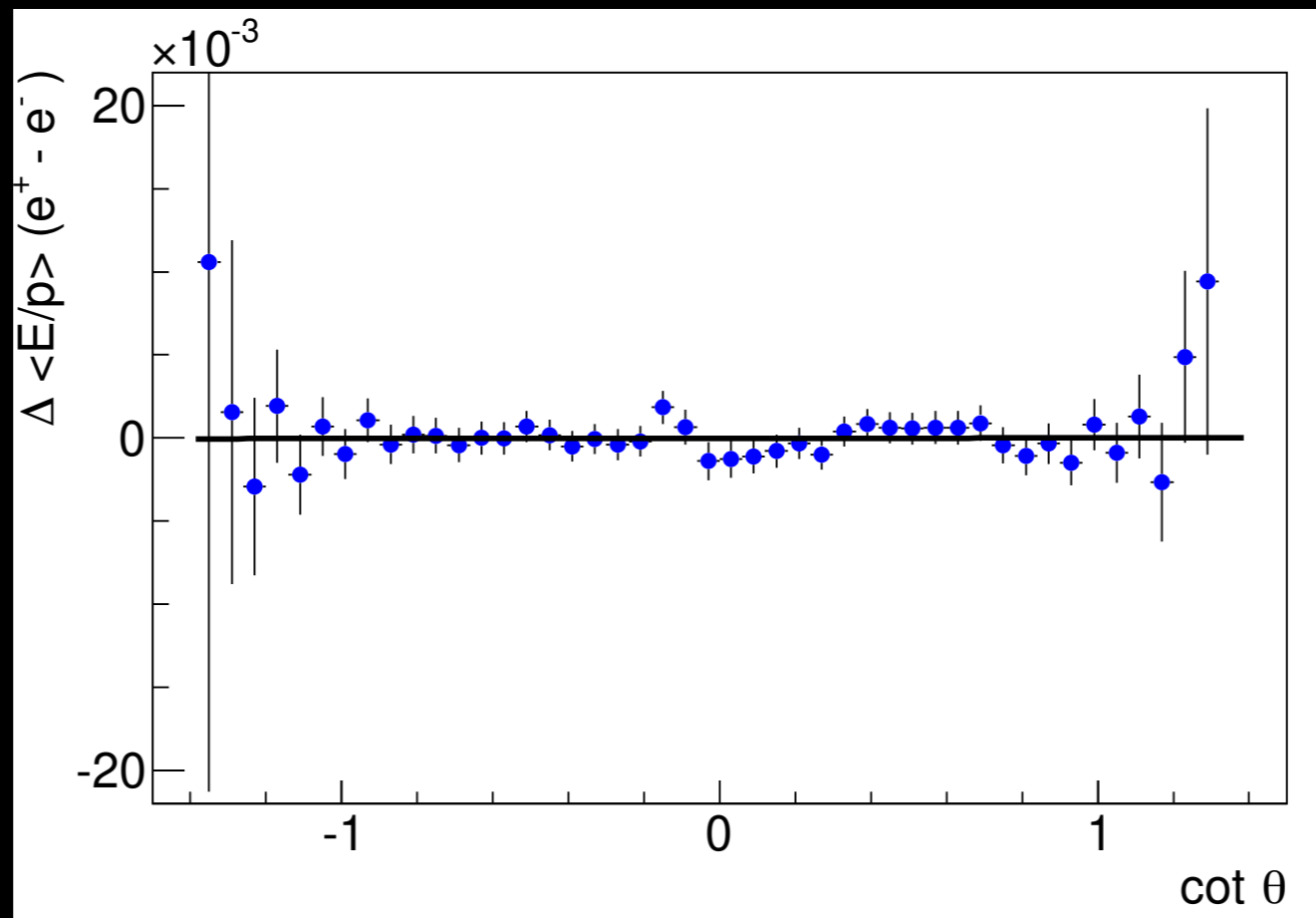
Track momentum calibration

Residual tracker misalignments studied using difference in E/p between electrons and positrons

Correction as a function of polar angle applied to measured tracks from W and Z decays

Linear dependence on cot theta would cause a bias in the m_W mass fit

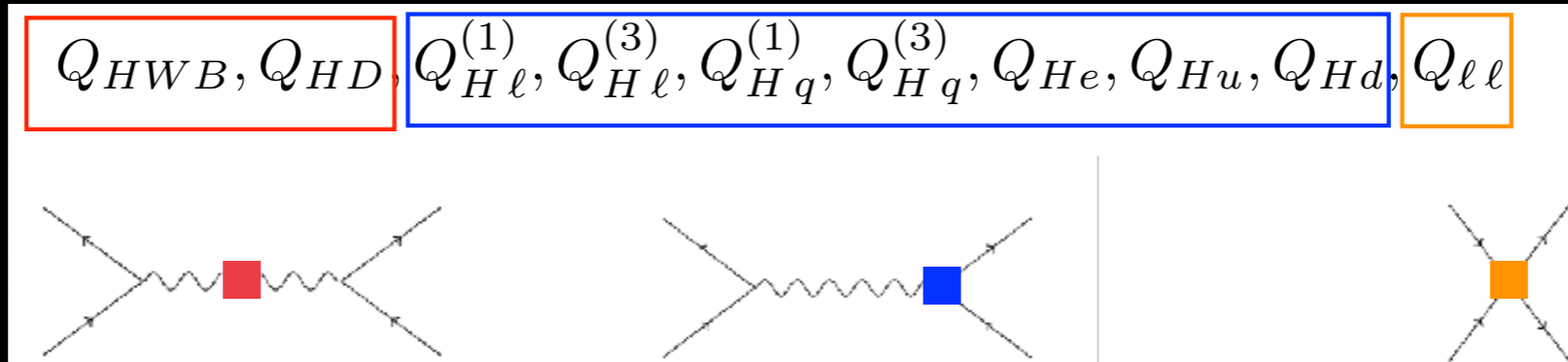
No linear correction required, statistical precision from E/p constrains the bias to <0.8 MeV



Measurement updates

Method or technique	impact
Detailed treatment of parton distribution functions	+3.5 MeV
Resolved beam-constraining bias in CDF reconstruction	+10 MeV
Improved COT alignment and drift model [65]	uniformity
Improved modeling of calorimeter tower resolution	uniformity
Temporal uniformity calibration of CEM towers	uniformity
Lepton removal procedure corrected for luminosity	uniformity
Higher-order calculation of QED radiation in J/ψ and Υ decays	accuracy
Modeling kurtosis of hadronic recoil energy resolution	accuracy
Improved modeling of hadronic recoil angular resolution	accuracy
Modeling dijet contribution to recoil resolution	accuracy
Explicit luminosity matching of pileup	accuracy
Modeling kurtosis of pileup resolution	accuracy
Theory model of p_T^W / p_T^Z spectrum ratio	accuracy
Constraint from p_T^W data spectrum	robustness
Cross-check of p_T^Z tuning	robustness

Electroweak observables at dimension 6



Parameter	Input Value
\hat{m}_Z	91.1875 ± 0.0021
\hat{G}_F	$1.1663787(6) \times 10^{-5}$
$\hat{\alpha}_{ew}$	$1/137.035999074(94)$

Observable	Experimental Value	Ref.	SM Theoretical Value	Ref.
\hat{m}_Z [GeV]	91.1875 ± 0.0021	[19]	–	–
\hat{m}_W [GeV]	80.385 ± 0.015	[49]	80.365 ± 0.004	[50]
Γ_Z [GeV]	2.4952 ± 0.0023	[19]	2.4942 ± 0.0005	[48]
R_ℓ^0	20.767 ± 0.025	[19]	20.751 ± 0.005	[48]
R_c^0	0.1721 ± 0.0030	[19]	0.17223 ± 0.00005	[48]
R_b^0	0.21629 ± 0.00066	[19]	0.21580 ± 0.00015	[48]
σ_h^0 [nb]	41.540 ± 0.037	[19]	41.488 ± 0.006	[48]
A_{FB}^ℓ	0.0171 ± 0.0010	[19]	0.01616 ± 0.00008	[32]
A_{FB}^c	0.0707 ± 0.0035	[19]	0.0735 ± 0.0002	[32]
A_{FB}^b	0.0992 ± 0.0016	[19]	0.1029 ± 0.0003	[32]

$$\frac{\delta m_W^2}{\hat{m}_W^2} = \hat{\Delta} \left[4C_{HWB} + \frac{c_{\hat{\theta}}}{s_{\hat{\theta}}} C_{HD} + 4 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{H\ell}^{(3)} - 2 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{\ell\ell} \right]$$

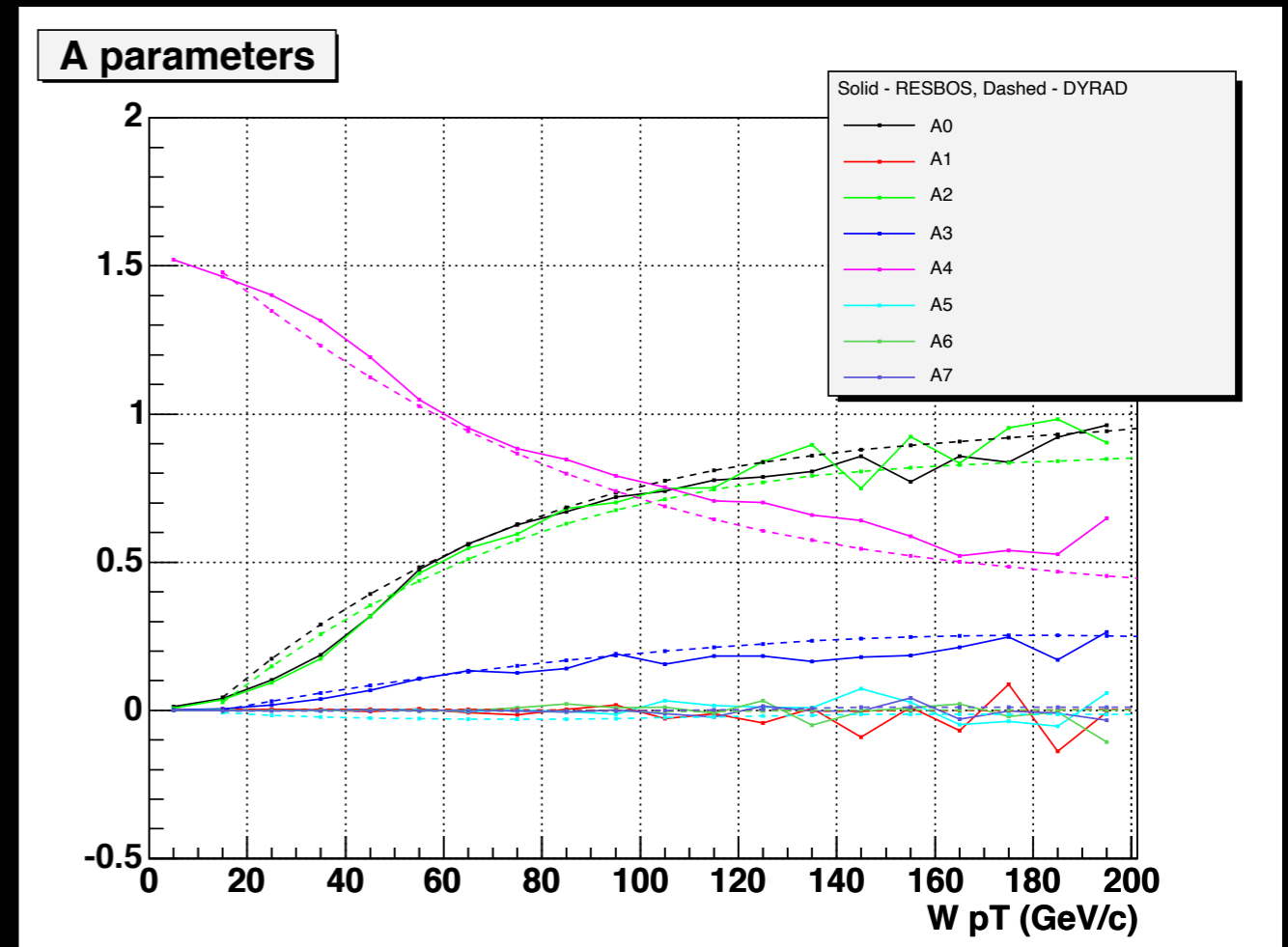
W boson mass fit results

Distribution	W -boson mass (MeV)	χ^2/dof
$m_T(e, \nu)$	$80\,429.1 \pm 10.3_{\text{stat}} \pm 8.5_{\text{syst}}$	39/48
$p_T^\ell(e)$	$80\,411.4 \pm 10.7_{\text{stat}} \pm 11.8_{\text{syst}}$	83/62
$p_T^\nu(e)$	$80\,426.3 \pm 14.5_{\text{stat}} \pm 11.7_{\text{syst}}$	69/62
$m_T(\mu, \nu)$	$80\,446.1 \pm 9.2_{\text{stat}} \pm 7.3_{\text{syst}}$	50/48
$p_T^\ell(\mu)$	$80\,428.2 \pm 9.6_{\text{stat}} \pm 10.3_{\text{syst}}$	82/62
$p_T^\nu(\mu)$	$80\,428.9 \pm 13.1_{\text{stat}} \pm 10.9_{\text{syst}}$	63/62
combination	$80\,433.5 \pm 6.4_{\text{stat}} \pm 6.9_{\text{syst}}$	7.4/5

Distribution	M_W (MeV)	$\chi^2/\text{d.o.f.}$
$W \rightarrow e\nu$		
m_T	80408 ± 19	52/48
p_T^ℓ	80393 ± 21	60/62
p_T^ν	80431 ± 25	71/62
$W \rightarrow \mu\nu$		
m_T	80379 ± 16	57/48
p_T^ℓ	80348 ± 18	58/62
p_T^ν	80406 ± 22	82/62

Angular coefficients in decay

$$\frac{d^4\sigma}{dQ_T^2 dy d\phi d(\cos\theta)} = \frac{3}{16\pi} \frac{d^2\sigma}{dQ_T^2 dy} \times \left[(1 + \cos^2\theta) + \frac{A_0}{2} (1 - 3\cos^2\theta) - A_1 Q \sin 2\theta \cos\phi + \frac{A_2}{2} \sin^2\theta \cos 2\phi + A_3 \sin\theta \cos\phi - A_4 Q \cos\theta + A_5 \sin^2\theta \sin 2\phi - A_6 Q \sin 2\theta \sin\phi + A_7 \sin\theta \sin\phi \right]$$



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thesis (2006)