

GRAVITON-PHOTON MIXING AND FUTURE LABORATORY AXION SEARCHES

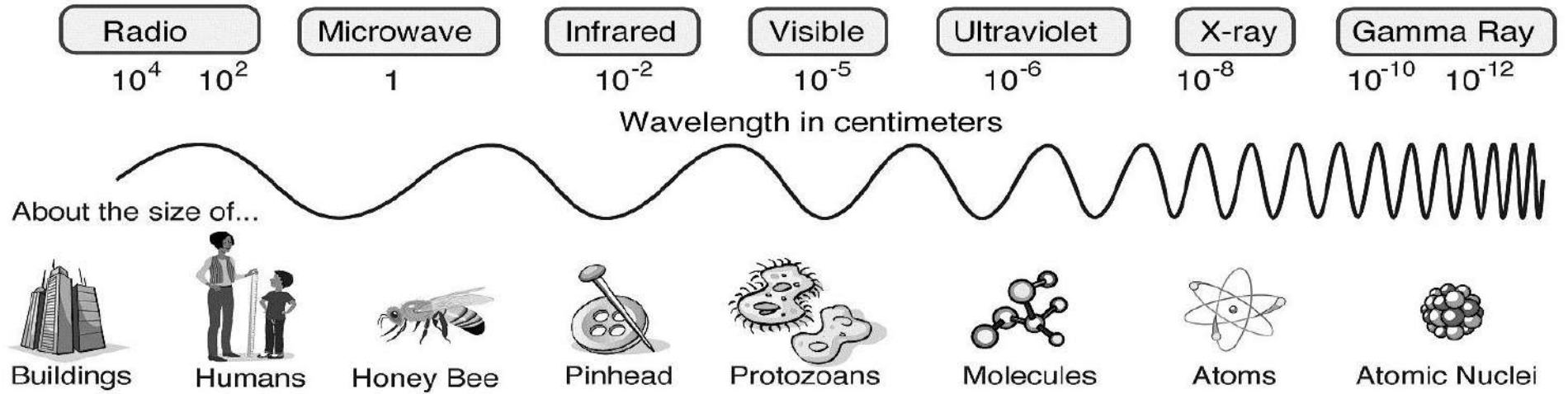
Aldo Ejlli

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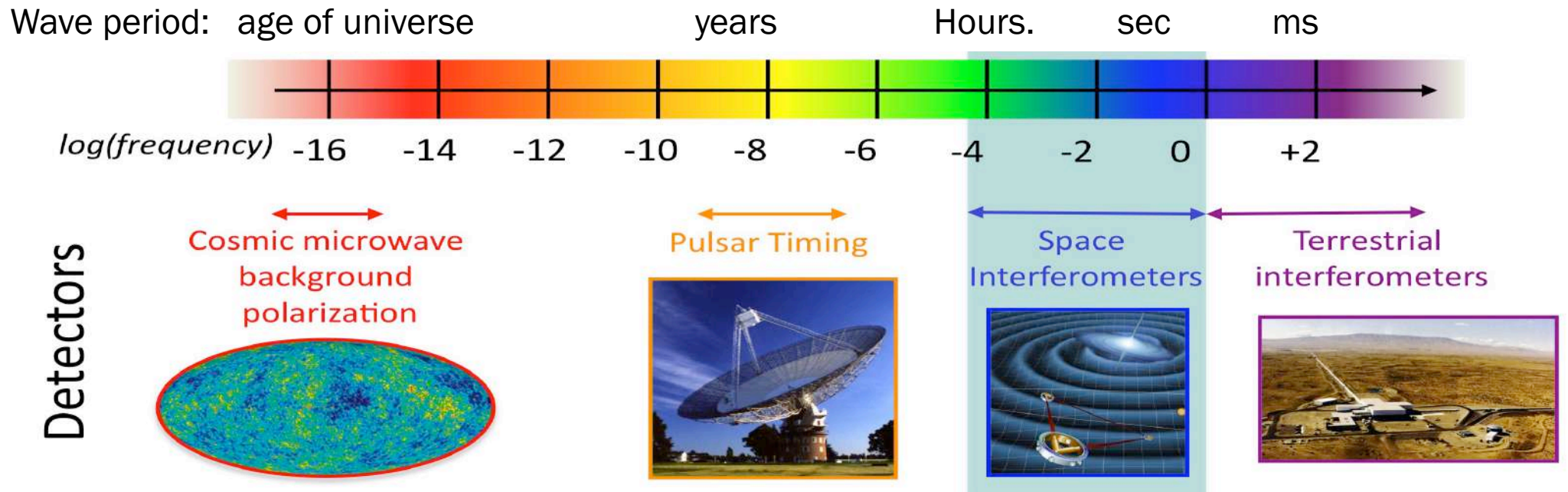
02/02/2022



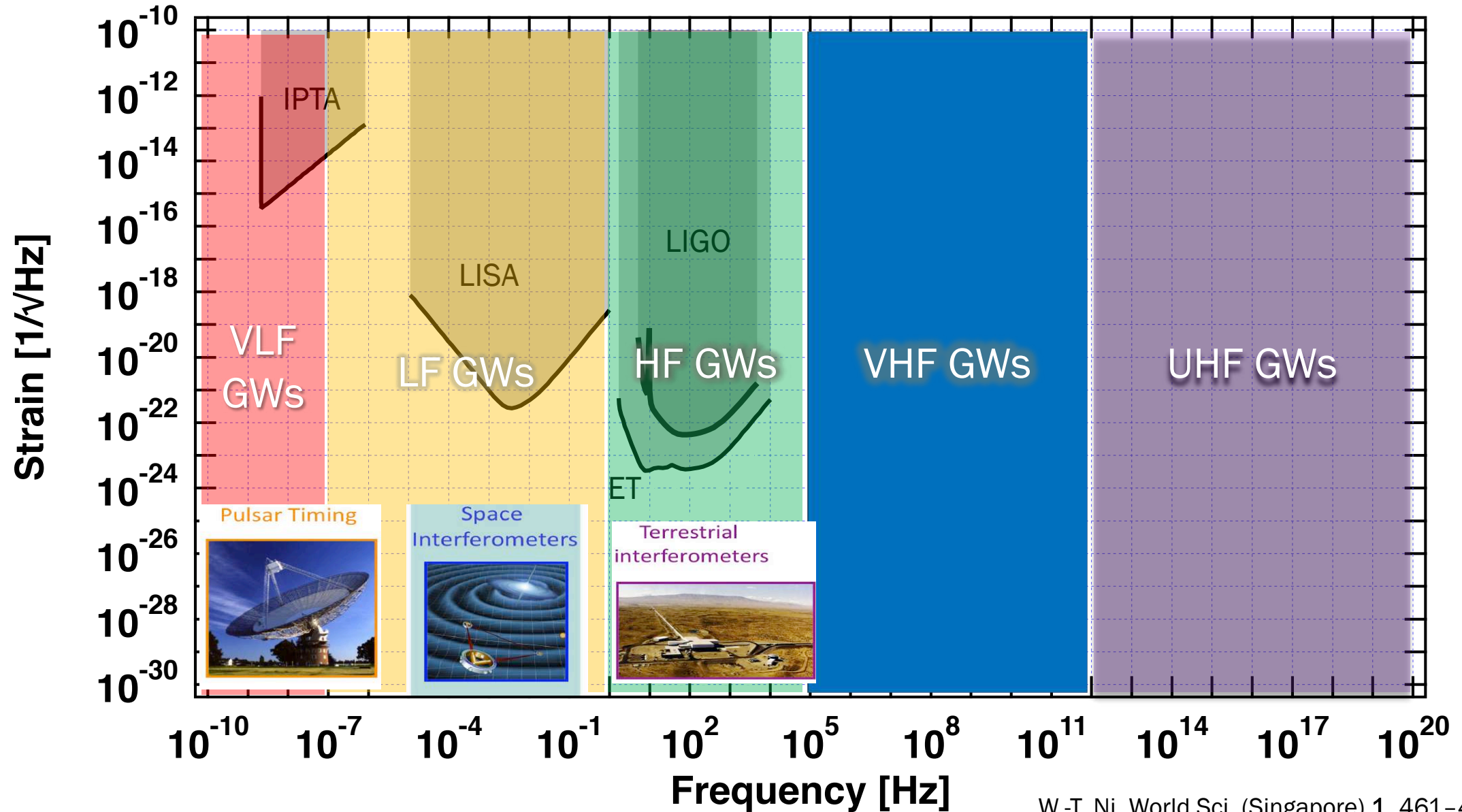
EM radiation

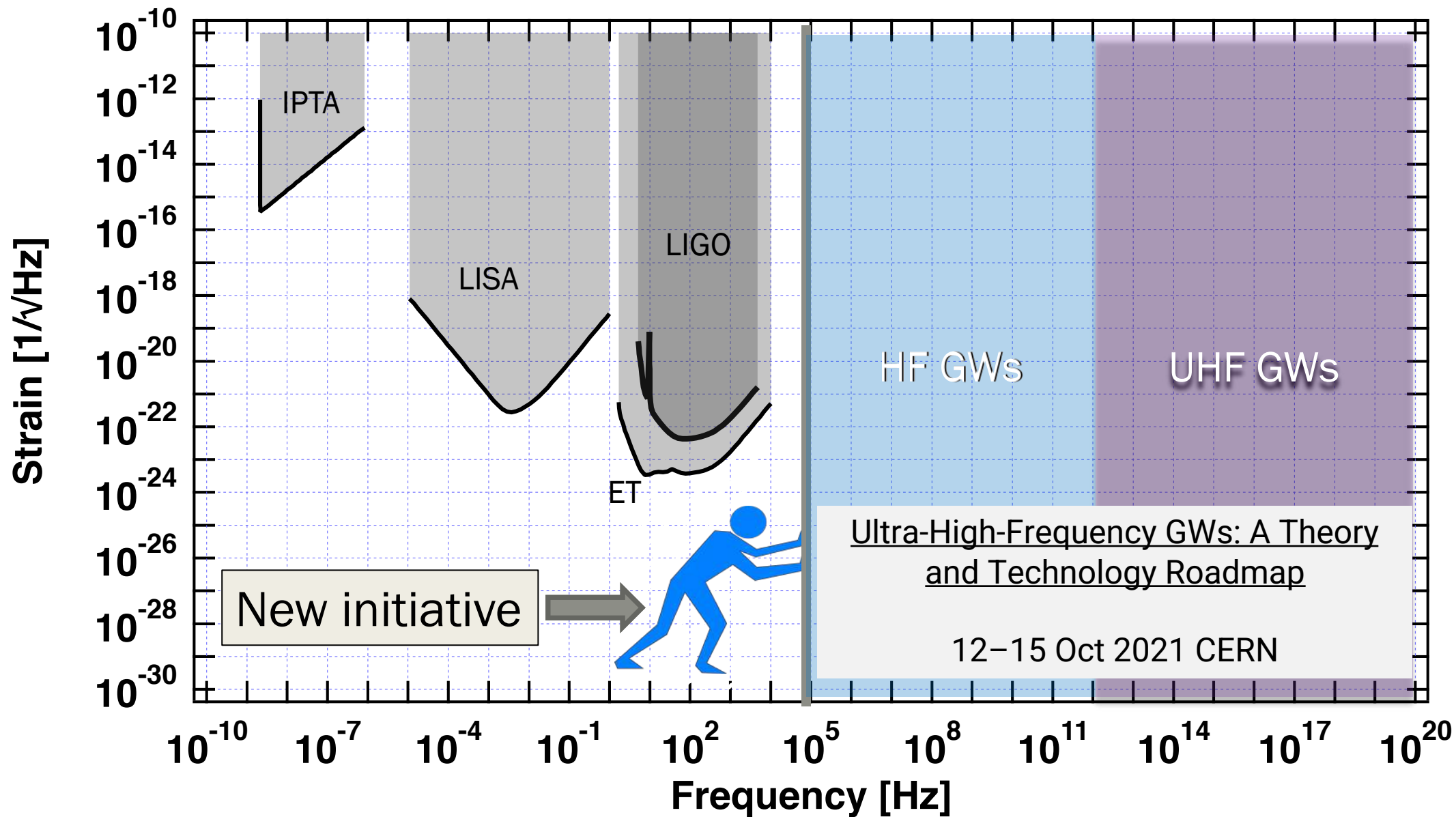


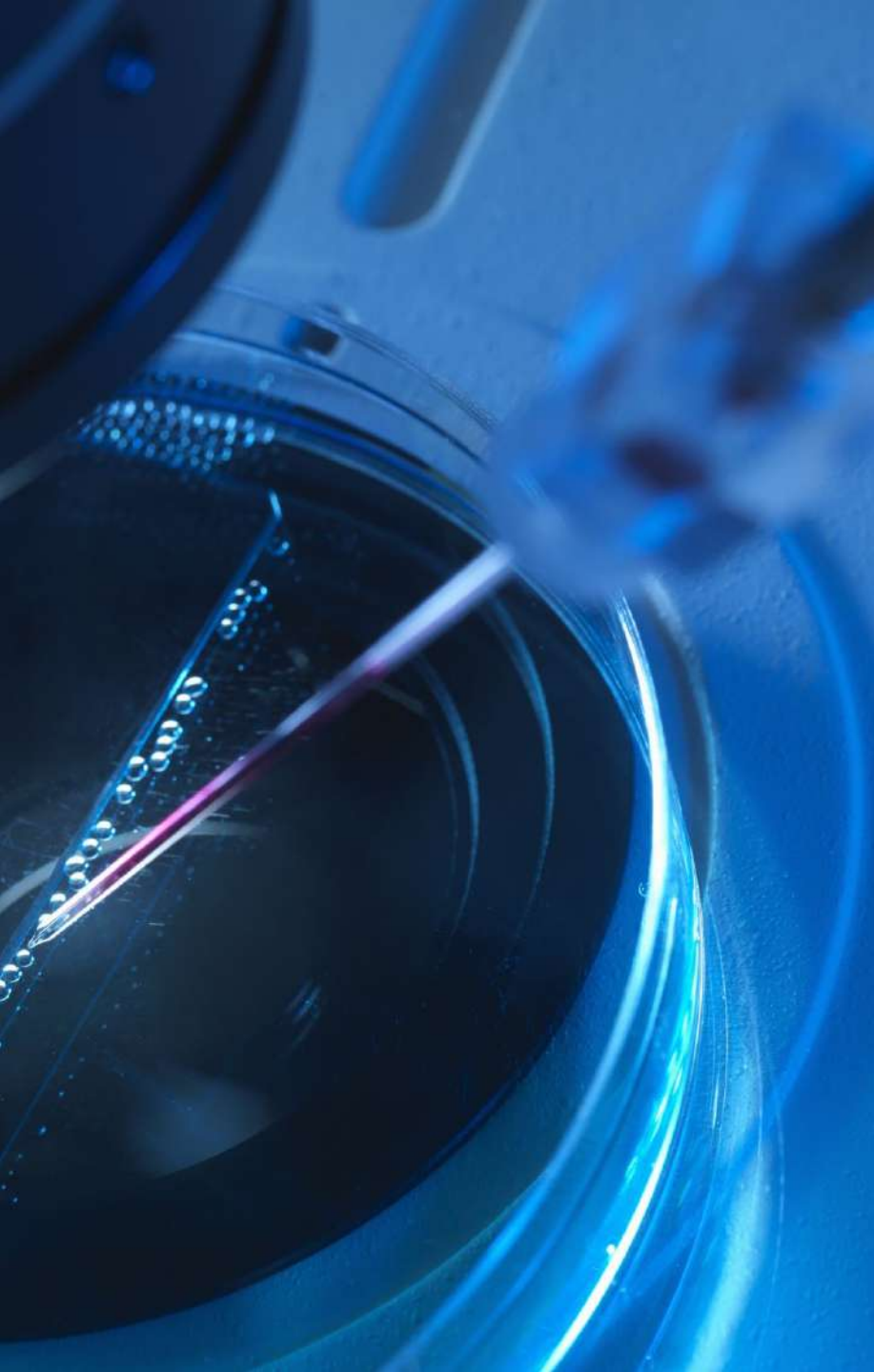
GW radiation



Definition







GW UHF: new experimental proposals

- Laser interferometers
- Optically levitated sensors
- Polarisation rotation
- Microwave resonant cavities
- GW magnon resonance
- Magnetic conversion: inverse Gertsenshtein effect
- ...

Outline

Magnetic conversion of GWs in static magnetic field

Axion experiments and magnetic conversion

Experimental UHF GWs upper limits

Prospect of UHF GWs in upgraded axion experiments

HF GWs using interferometry

Conclusions



MAGNETIC CONVERSION?

Magnetic conversion: not a new idea

Electromagnetic waves (photons) can transform into gravitational waves (gravitons) in the presence of a constant external magnetic field, Gertsenshtein (1962), Lupanov (1967).

The reverse process $g \rightarrow \gamma$ was considered by Mitskevich (1969), Boccaletti, De Sabbata, Fortini and Gualdi (1970), Zel'dovich (1973) etc.

For an extended region of a magnetic field in vacuum, there are coherent oscillations of GW in EM and vice versa in complete analogy with neutrino oscillations.



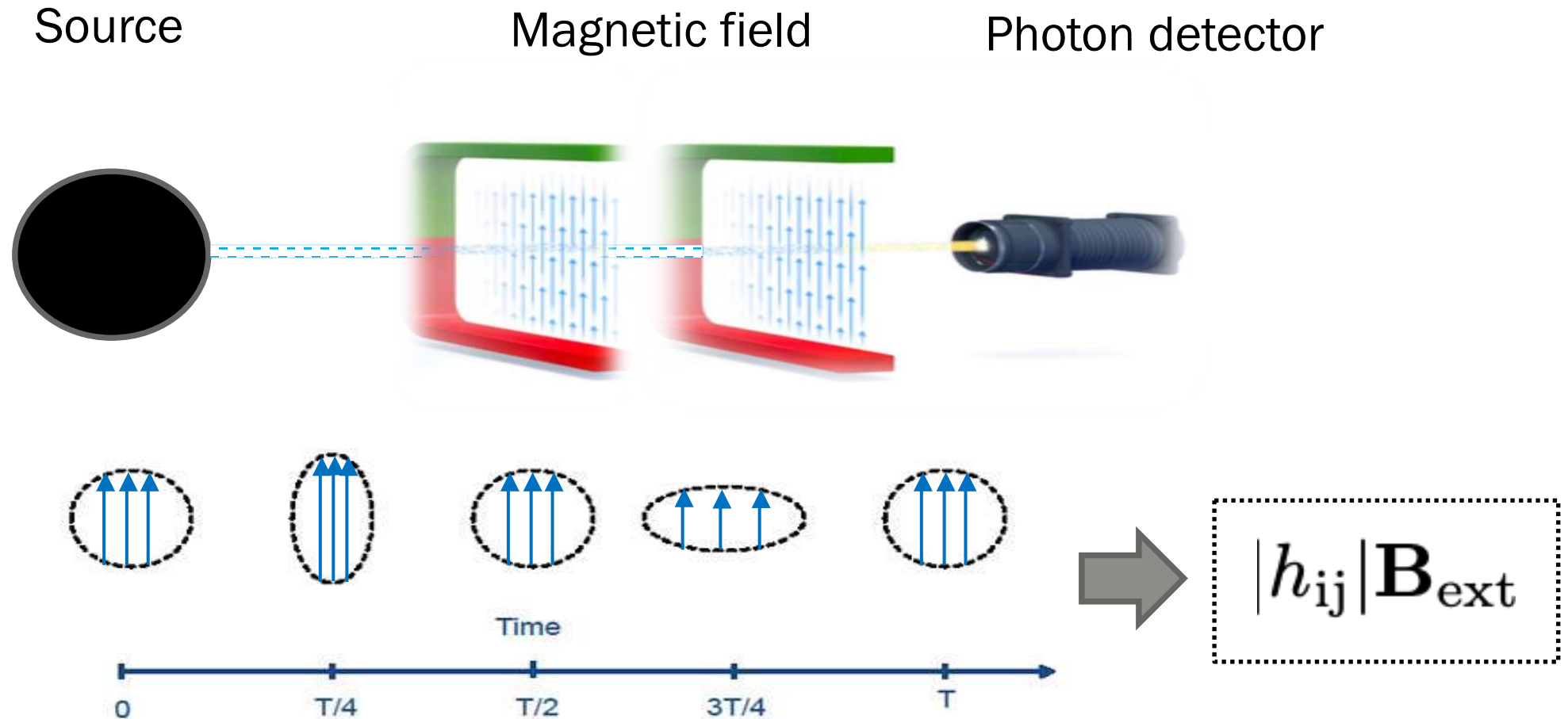
Credit Mike Cruise

Laboratory magnetic conversion detection

- Examples of an experimental conceptual design Prof. Mike Cruise
- Requirements: single photon detectors, aperture, field strength, cross section and directionality.

Magnetic conversion (Inverse Gertsenshtein effect)

- Gravitational-wave propagating in magnetic fields convert into photons.
Gertsenshtein, Sov. Phys., JETP 14, 84 (1962), G. A. Lupanov JETP 25, 76 (1967)

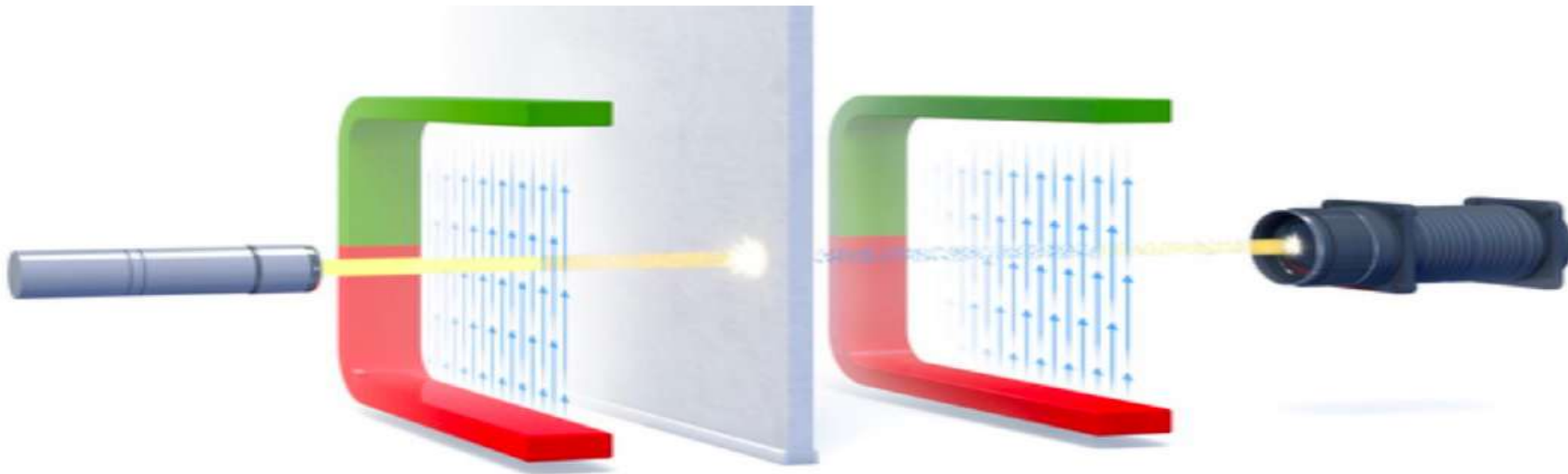




AXION EXPERIMENTS

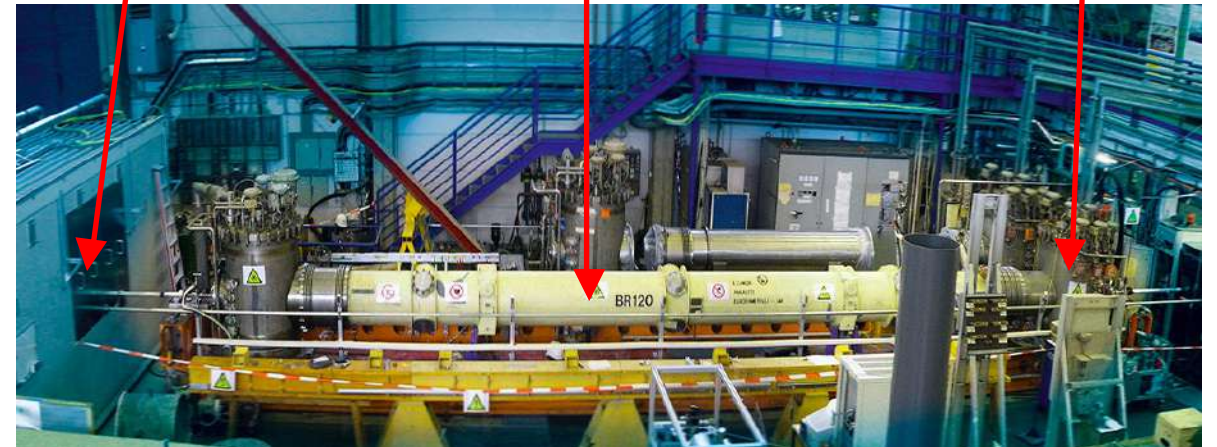
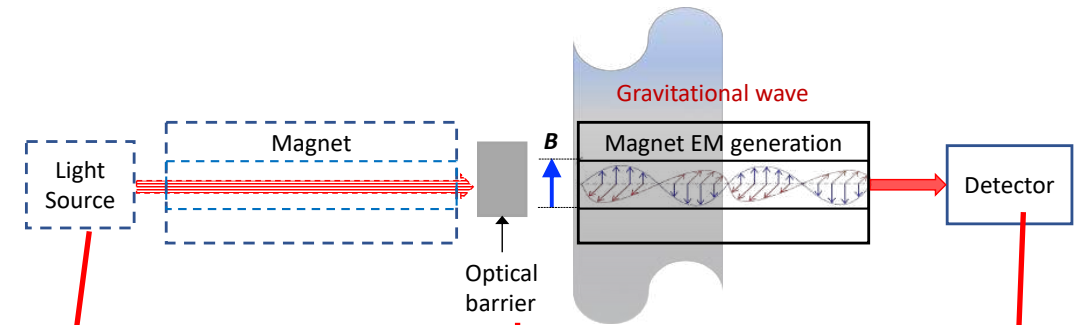
Axion search using laboratory static magnetic fields

- Axions are generated in the magnetic field coupled to two photons.
- Axions, in the second region of the magnetic field, decay into photons.



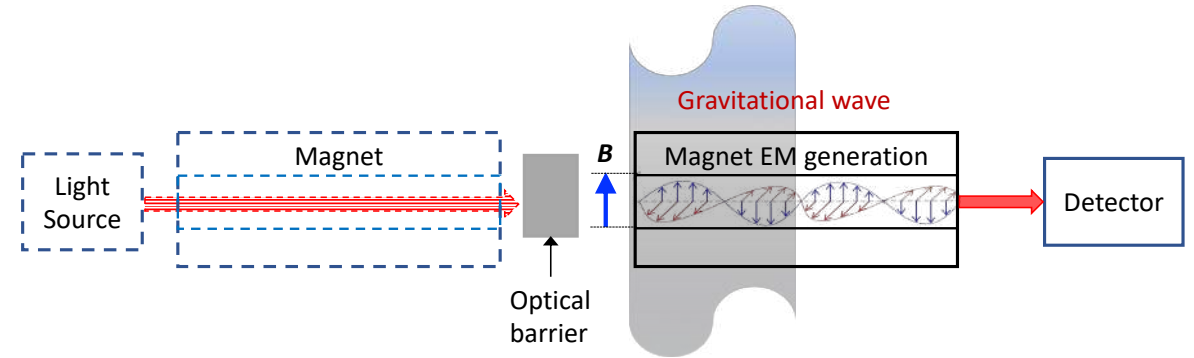
ALPS (Axion-Like Particle Search) DESY Germany

- Magnet provided from HERA particle accelerator working at liquid helium (4 K).
- Magnetic field: $B=5$ T.
- Length: $L=2\times 4.3$ m.
- Photodetector @ $\lambda = 532$ nm PIXIS CCD.
- Data acquisition 2009-2010.
- Excluded detection @ 95% confidence interval.

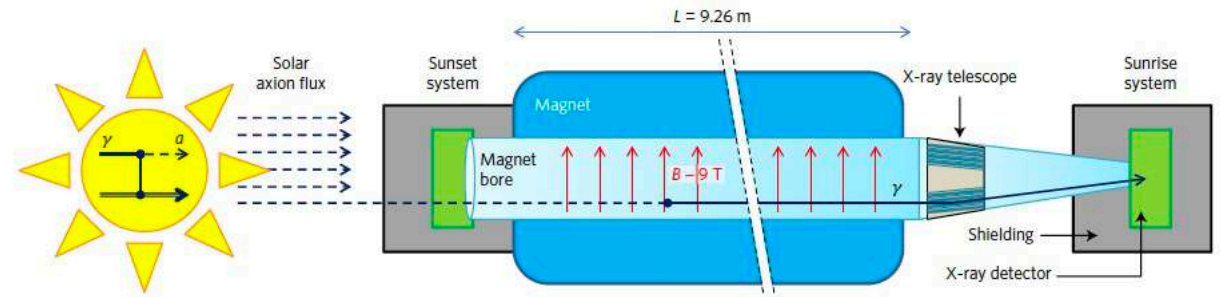


OSQAR (Optical Search of QED, Axion and photon Regeneration) CERN Switzerland

- Magnets provided from spare LHC particle accelerator working @ superfluid helium (2 K).
- Magnetic field Field: $B = 9$ T.
- Magnet length: $L = 14.3$ m.
- Photodetector @ $\lambda = 532$ nm.
- Data acquisition 2014-2015.
- Excluded detection @ 95% confidence interval.



CAST (CERN Axion Solar Telescope) CERN Switzerland



- Magnet provided from spare LHC particle accelerator working @ superfluid helium (2 K).
- Magnetic field: $B = 9$ Tesla.
- Length: $L = 9$ m.
- X-Ray detector @ $\lambda = 3$ nm.
- Data acquisition 2013-2015.
- Excluded detection @ 95% confidence interval.



GWs upper limits: ALPS, OSQAR, CAST

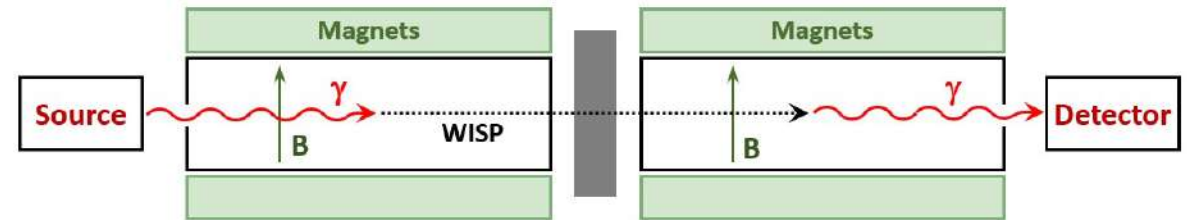
Detectors

- Cannot point deliberately to the emitting sources, except CAST
- GWs upper limits at Ultra-High-Frequencies (UHF): optical 5×10^{14} Hz and X-ray 10^{18} Hz

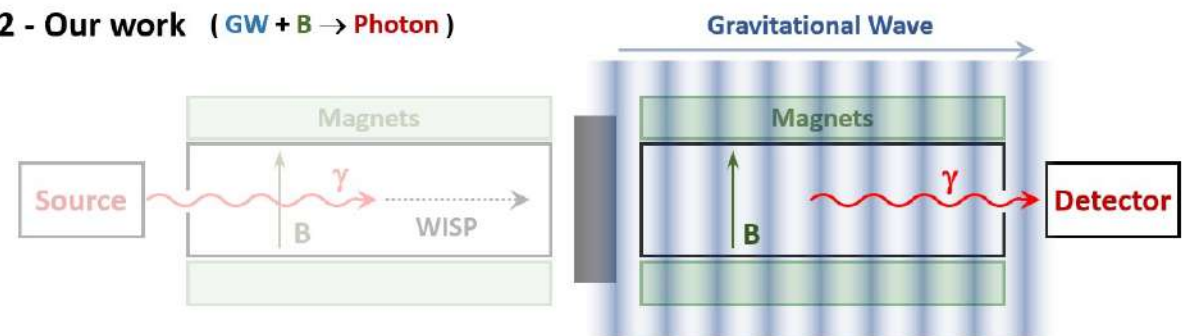
Suited sources?

- Requirements: stochastic, isotropic, stationary, and Gaussian gravitational-waves.

1 - ALPS/OSQAR ($\text{Photon} + B \rightarrow \text{WISP} \rightarrow \text{WISP} + B \rightarrow \text{Photon}$)



2 - Our work ($\text{GW} + B \rightarrow \text{Photon}$)



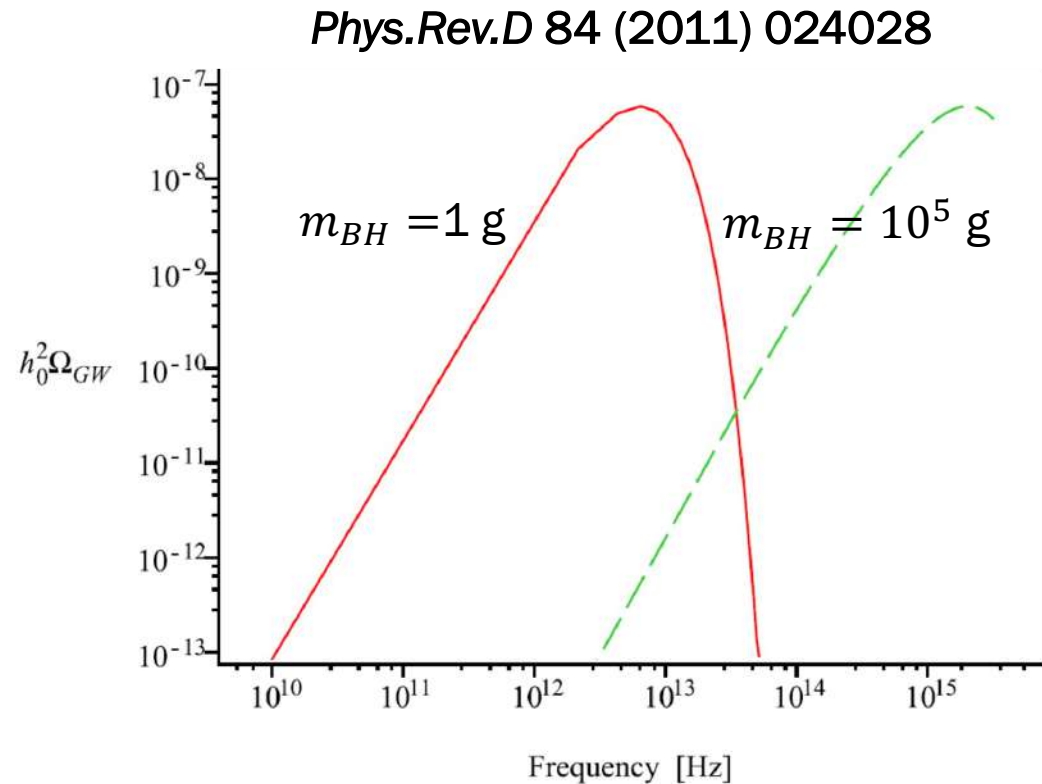
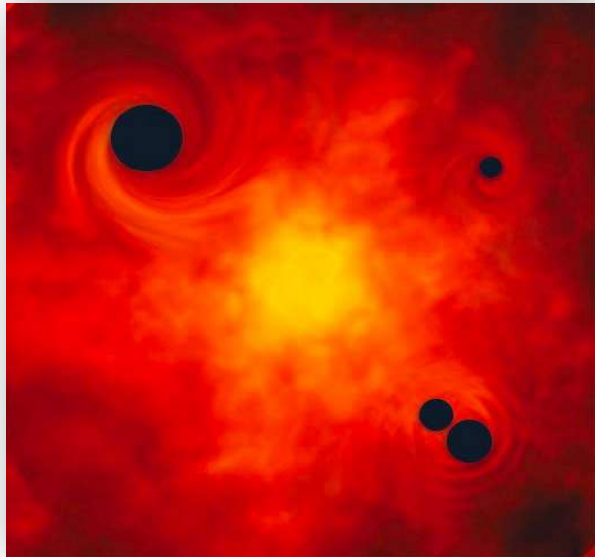


UHF GWS SOURCES

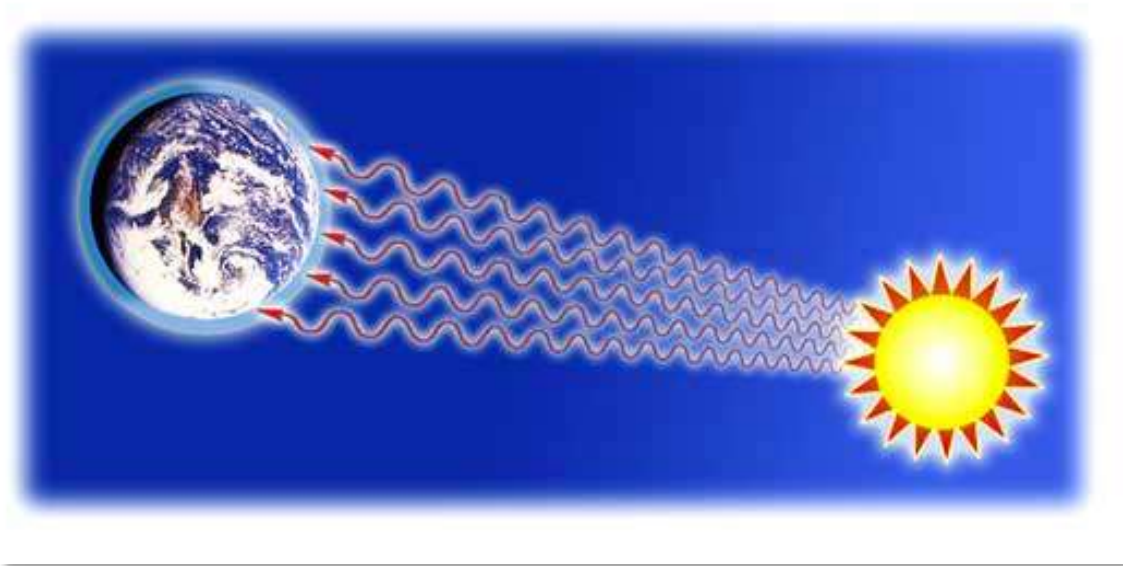
UHF GW sources: early universe

Primordial BH collisions and evaporations

- Cosmological energy density of the order of $h_0^2 \Omega_{GW}(f_{\text{peak}}) \approx 10^{-7}$

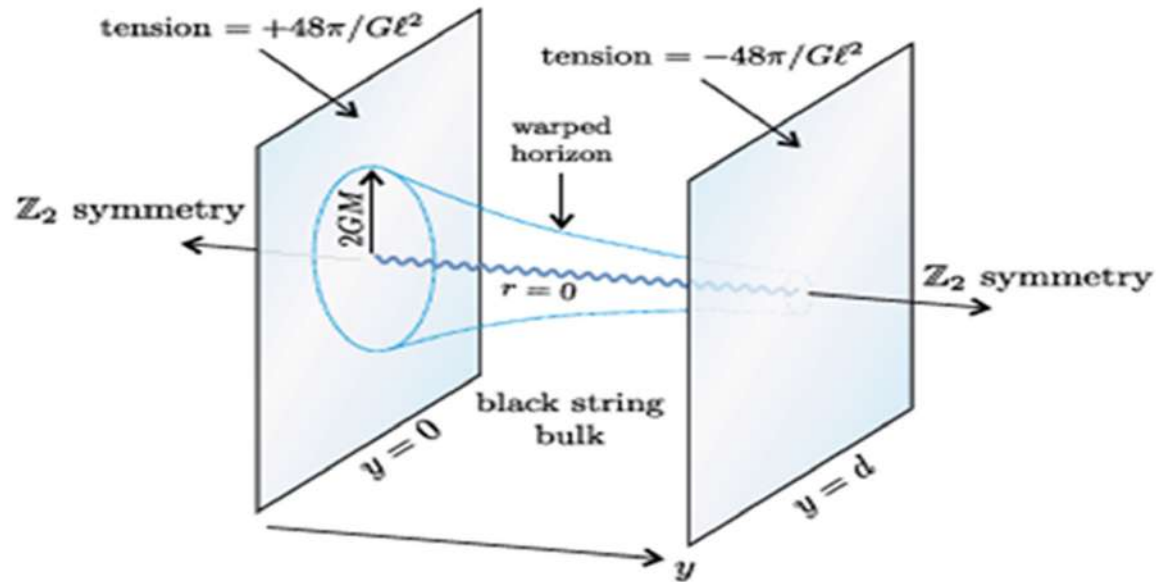


UHF GW sources: thermal plasma in the sun



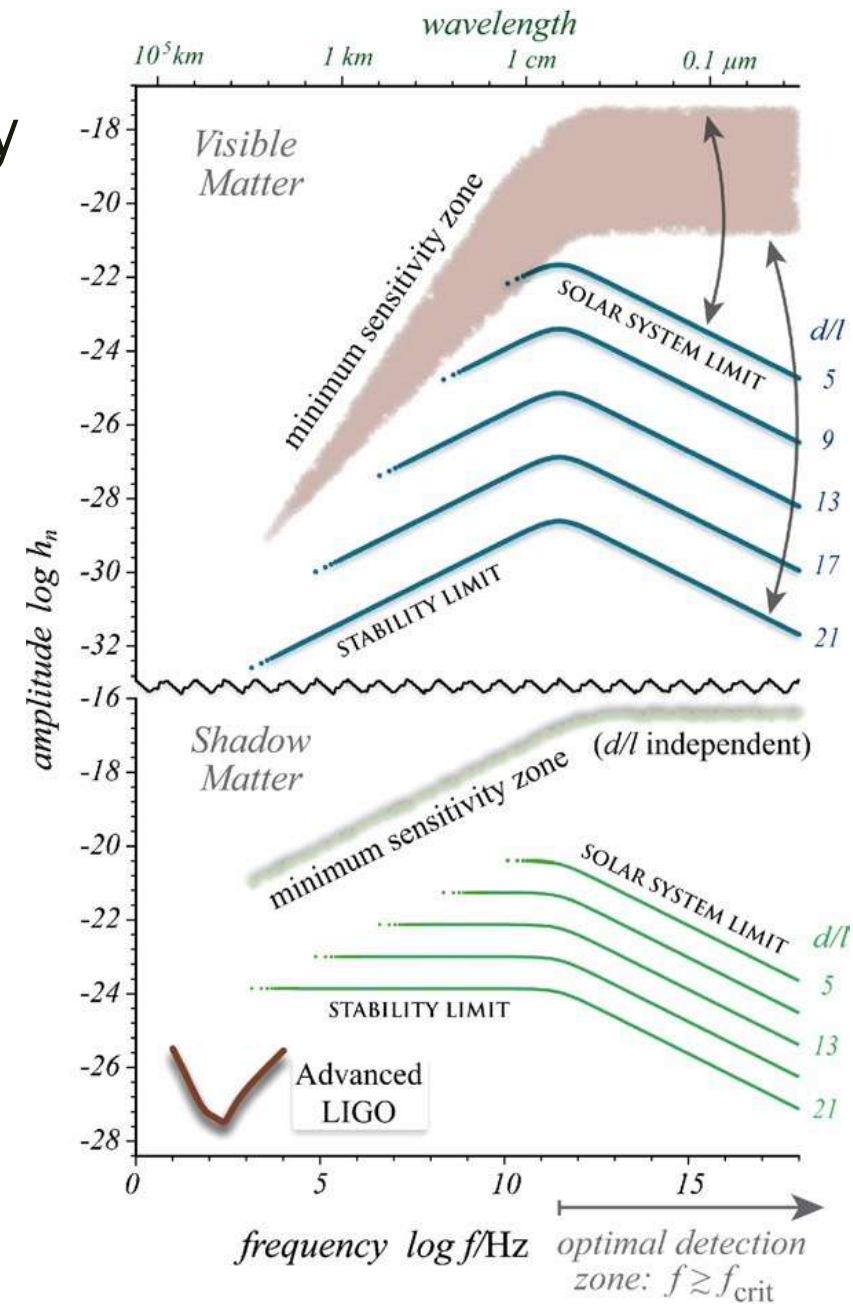
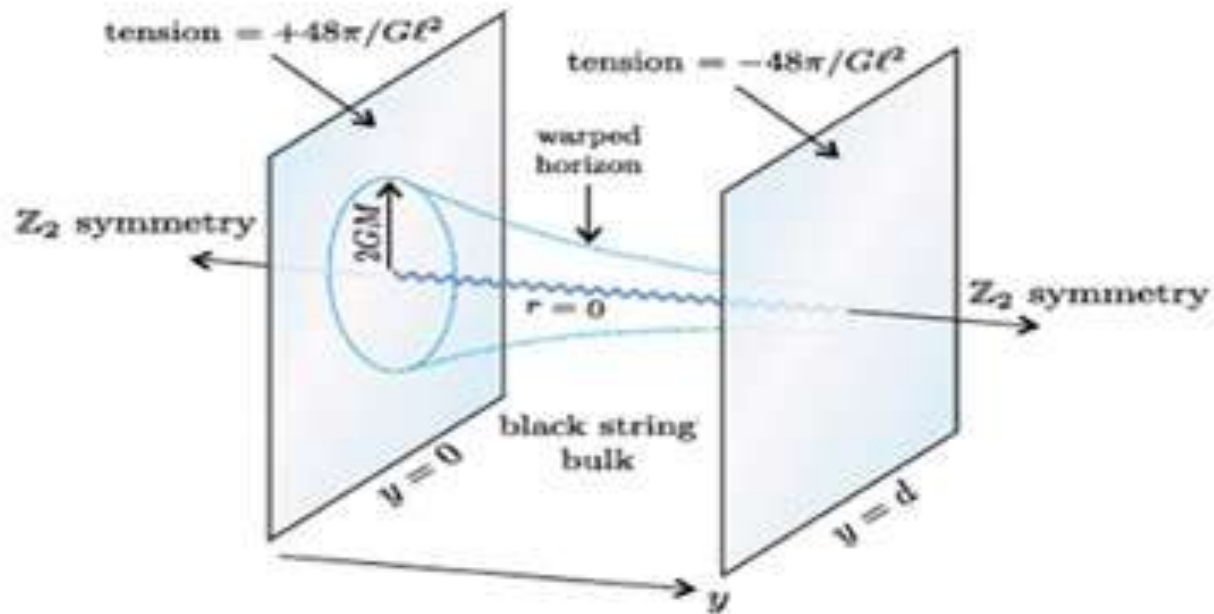
- Gravitational radiation emitted by Coulomb collision in plasma
- Hydrogen plasma in the solar core
- Collision frequency 10^{15} Hz
- Thermal collisions in the solar core produce about 10^8 watts of gravitational radiation

UHF GW sources: BH-BH collisions in 5D gravity



- Seahra and Clarkson have calculated the GW emission in 5-D gravity when stellar mass black holes fall into a black hole.
- The normal LF radiation from such a system is emitted plus an excitation of the brane separation itself

UHF GW sources: BH-BH collisions in 5D gravity





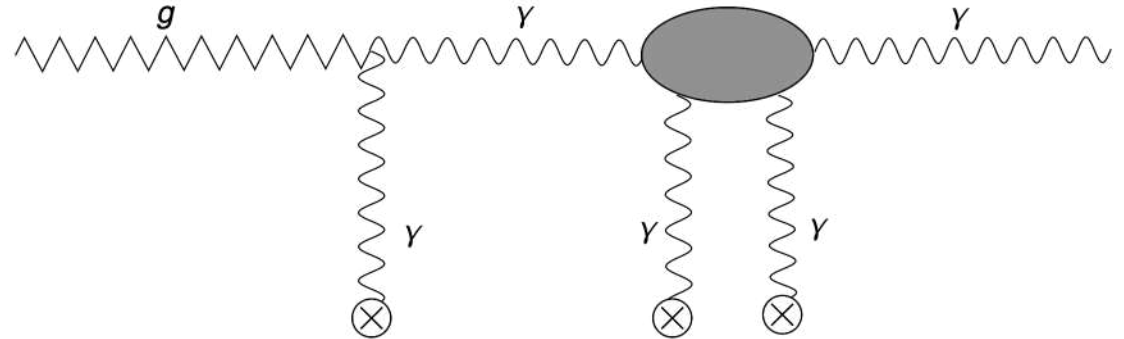
MAGNETIC CONVERSION IN AXION EXPERIMENTS

GWs propagating in static magnetic fields

$$S = \int d^4x \sqrt{-g} \mathcal{L}$$

$$\mathcal{L} = \mathcal{L}_{\text{gr}} + \mathcal{L}_{\text{em}}$$

$$\mathcal{L}_{\text{gr}} = \frac{1}{\kappa^2} R, \quad \mathcal{L}_{\text{em}} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{2} \int d^4x' A_\mu(x) \Pi^{\mu\nu}(x, x') A_\nu(x')$$

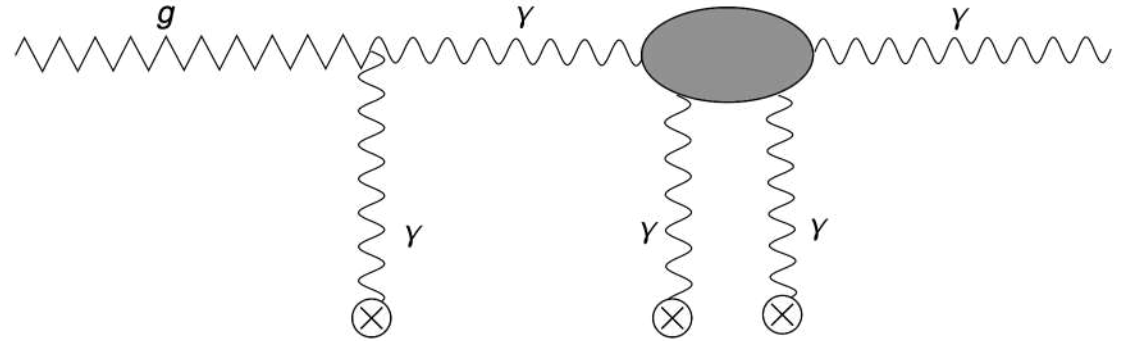


$$\begin{aligned} \nabla^2 A^0 &= 0, \\ \square A^i + \left(\int d^4x' \Pi^{ij}(x, x') A_j(x') \right) + \partial^i \partial_\mu A^\mu &= \kappa \partial_\mu [h^{\mu\beta} \bar{F}_\beta^i - h^{i\beta} \bar{F}_\beta^\mu], \\ \square h_{ij} &= -\kappa (B_i \bar{B}_j + \bar{B}_i B_j + \bar{B}_i \bar{B}_j), \end{aligned}$$

GWs propagating in static magnetic fields

$$S = \int d^4x \sqrt{-g} \mathcal{L}$$

$$\mathcal{L} = \mathcal{L}_{\text{gr}} + \mathcal{L}_{\text{em}}$$



$$(\omega + i\partial_z)\Psi(z, \omega, \hat{z})\mathbf{I} + M(z, \omega)\Psi(z, \omega, \hat{z}) = 0 \quad \Psi(z, \omega, \hat{z}) = (h_x, h_+, A_x, A_y)^T$$

$$M(z, \omega) = \begin{pmatrix} 0 & 0 & -iM_{g\gamma}^x & iM_{g\gamma}^y \\ 0 & 0 & iM_{g\gamma}^y & iM_{g\gamma}^x \\ iM_{g\gamma}^x & -iM_{g\gamma}^y & M_x & M_{\text{CF}} \\ -iM_{g\gamma}^y & -iM_{g\gamma}^x & M_{\text{CF}}^* & M_y \end{pmatrix}$$

$$M_{g\gamma}^x = \kappa k \bar{B}_x / (\omega + k)$$

$$M_{g\gamma}^y = \kappa k \bar{B}_y / (\omega + k)$$

$$M_x = -\Pi_{xx} / (\omega + k)$$

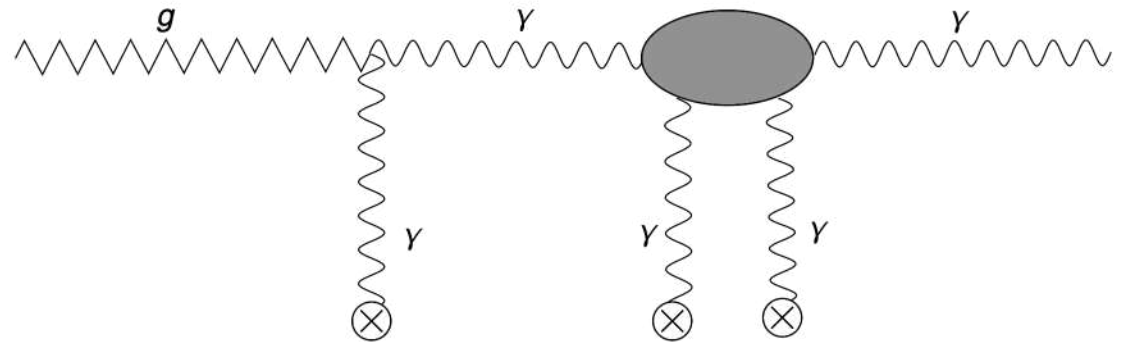
$$M_y = -\Pi_{yy} / (\omega + k)$$

$$M_{\text{CF}} = -\Pi_{xy} / (\omega + k)$$

GWs propagating in static magnetic fields

$$S = \int d^4x \sqrt{-g} \mathcal{L}$$

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$$M_{g\gamma}^x = \kappa k \bar{B}_x / (\omega + k)$$

~~$$M_{g\gamma}^y = \kappa k \bar{B}_y / (\omega + k)$$~~

$$M_x = -\Pi_{xx} / (\omega + k)$$

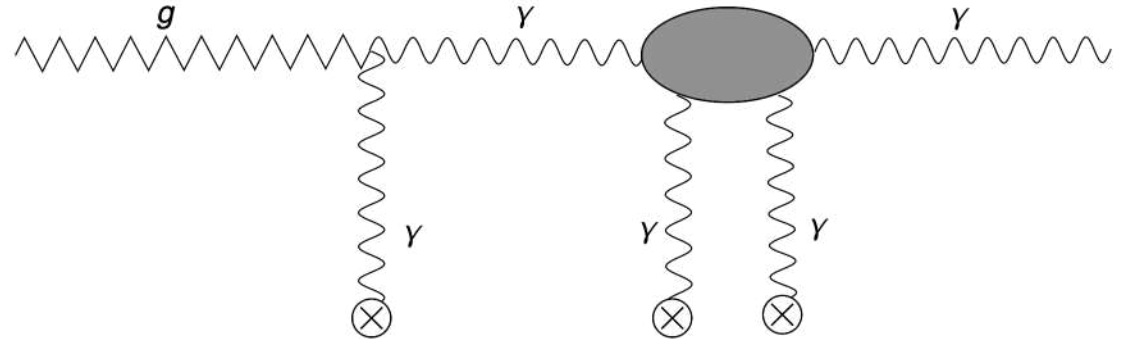
$$M_y = -\Pi_{yy} / (\omega + k)$$

~~$$M_{\text{CF}} = \Pi_{xy} / (\omega + k)$$~~

GWs propagating in static magnetic fields

$$S = \int d^4x \sqrt{-g} \mathcal{L}$$

$$\mathcal{L} = \mathcal{L}_{\text{gr}} + \mathcal{L}_{\text{em}}$$



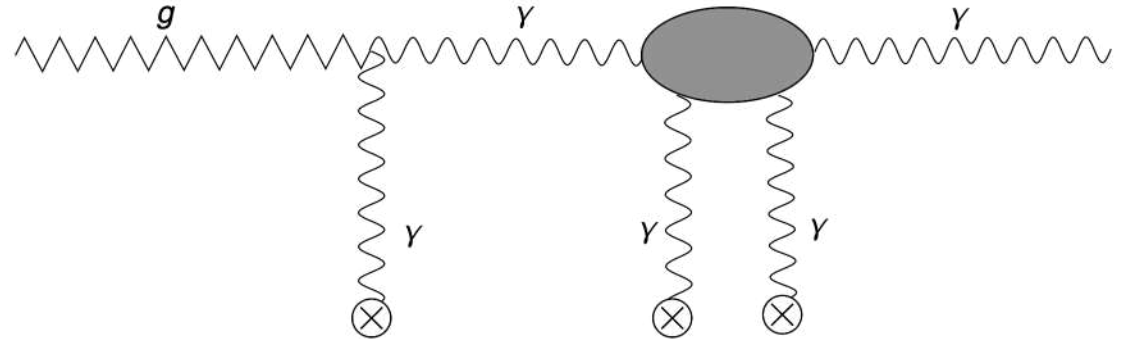
$$\begin{aligned}
 h_{\times}(z, \omega, \hat{z}) &= \left[\cos(\Delta_x z) - i \frac{M_x \sin(\Delta_x z)}{2\Delta_x} \right] e^{i(\omega+M_x/2)z} h_{\times}(0, \omega, \hat{z}) + \frac{M_{g\gamma}^x \sin(\Delta_x z)}{\Delta_x} e^{i(\omega+M_x/2)z} A_x(0, \omega, \hat{z}), \\
 h_{+}(z, \omega, \hat{z}) &= \left[\cos(\Delta_y z) - i \frac{M_y \sin(\Delta_y z)}{2\Delta_y} \right] e^{i(\omega+M_y/2)z} h_{+}(0, \omega, \hat{z}) - \frac{M_{g\gamma}^x \sin(\Delta_y z)}{\Delta_y} e^{i(\omega+M_y/2)z} A_y(0, \omega, \hat{z}), \\
 A_x(z, \omega, \hat{z}) &= -\frac{M_{g\gamma}^x \sin(\Delta_x z)}{\Delta_x} e^{i(\omega+M_x/2)z} h_{\times}(0, \omega, \hat{z}) + \left[\cos(\Delta_x z) + i \frac{M_x \sin(\Delta_x z)}{2\Delta_x} \right] e^{i(\omega+M_x/2)z} A_x(0, \omega, \hat{z}), \\
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 \end{aligned}$$

$$\Delta_{x,y} \equiv \frac{\sqrt{M_{x,y}^2 + 4(M_{g\gamma}^x)^2}}{2}$$

GWs propagating in static magnetic fields

$$S = \int d^4x \sqrt{-g} \mathcal{L}$$

$$\mathcal{L} = \mathcal{L}_{\text{gr}} + \mathcal{L}_{\text{em}}$$



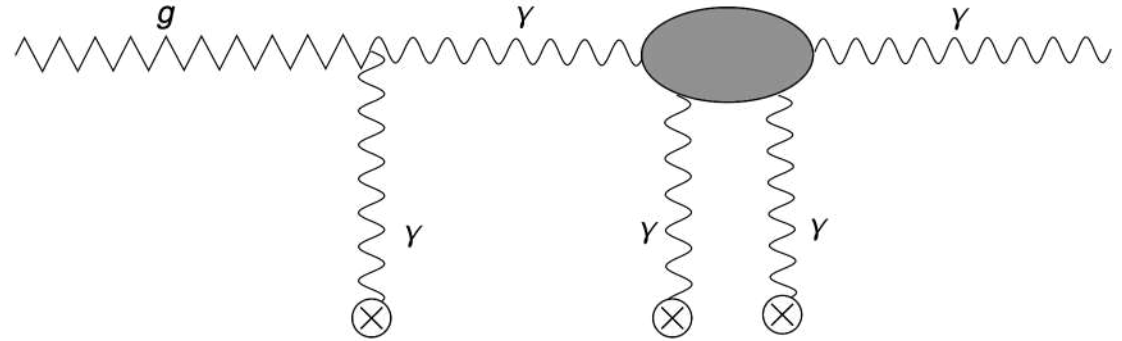
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 A_x(z, \omega, \hat{z}) &= -\frac{M_{g\gamma}^x \sin(\Delta_x z)}{\Delta_x} e^{i(\omega+M_x/2)z} h_{\times}(0, \omega, \hat{z}) + \left[\cos(\Delta_x z) + i \frac{M_x \sin(\Delta_x z)}{2\Delta_x} \right] e^{i(\omega+M_x/2)z} A_x(0, \omega, \hat{z}), \\
 A_y(z, \omega, \hat{z}) &= \frac{M_{g\gamma}^y \sin(\Delta_y z)}{\Delta_y} e^{i(\omega+M_y/2)z} h_{+}(0, \omega, \hat{z}) + \left[\cos(\Delta_y z) + i \frac{M_y \sin(\Delta_y z)}{2\Delta_y} \right] e^{i(\omega+M_y/2)z} A_y(0, \omega, \hat{z}).
 \end{aligned}$$

$$\Delta_{x,y} \equiv \frac{\sqrt{M_{x,y}^2 + 4(M_{g\gamma}^x)^2}}{2}$$

GWs propagating in static magnetic fields

$$S = \int d^4x \sqrt{-g} \mathcal{L}$$

$$\mathcal{L} = \mathcal{L}_{\text{gr}} + \mathcal{L}_{\text{em}}$$



$$A_x(z, \omega, \hat{z}) = -\frac{M_{g\gamma}^x \sin(\Delta_x z)}{\kappa \Delta_x} e^{i(\omega + M_x/2)z} \tilde{h}_\times(0, \omega, \hat{z})$$

$$A_y(z, \omega, \hat{z}) = \frac{M_{g\gamma}^x \sin(\Delta_y z)}{\kappa \Delta_y} e^{i(\omega + M_y/2)z} \tilde{h}_+(0, \omega, \hat{z}).$$

GWs propagating in static magnetic fields

- EMWs flux: $\Phi_\gamma(z, t) \equiv \langle |E_x(z, t)|^2 \rangle + \langle |E_y(z, t)|^2 \rangle$
- Stochastic GWs tensor $\tilde{h}_{ij}(0, t) = \sum_{\lambda=x,+} \int_{-\infty}^{+\infty} \frac{d\omega}{2\pi} \int_{S^2} d^2\hat{n} \tilde{h}_\lambda(0, \omega, \hat{n}) e_{ij}^\lambda(\hat{n}) e^{-i\omega t}$
- Average value: $\langle \tilde{h}_{ij}(0, t) \tilde{h}^{ij}(0, t) \rangle \equiv 2 \int_0^{+\infty} d(\log \omega) h_c^2(0, \omega),$

Converted EMWs stochastic flux

$$\Phi_\gamma^{\text{graph}}(z, \omega_f; t) \simeq \int_{\omega_i}^{\omega_f} \frac{B^2 z^2 h_c^2(0, \omega) \omega}{4} d\omega$$

Measured EMWs flux from the CCD

$$\Phi_\gamma^{\text{CCD}}(z, \omega_f; t) = \int_{\omega_i}^{\omega_f} \frac{1}{A(z)} \frac{N(\omega, t) \omega}{\epsilon_\gamma(\omega)} d\omega$$

$$N(\omega, t) = N_{\text{exp}} / \Delta\omega$$

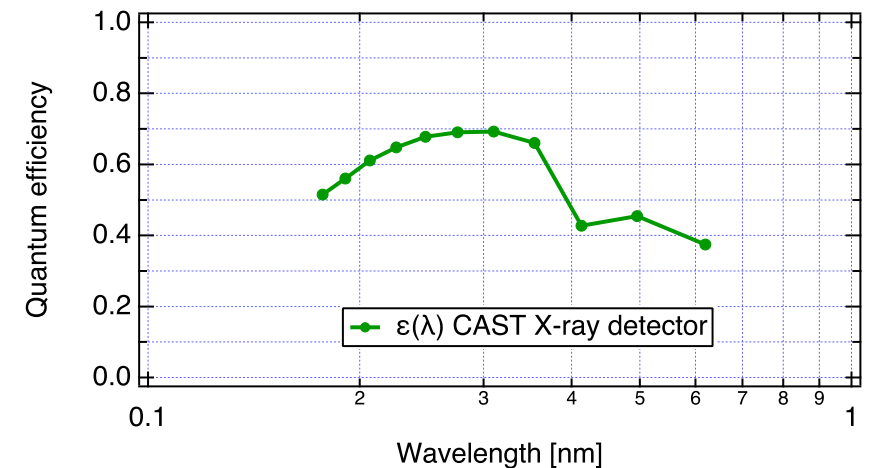
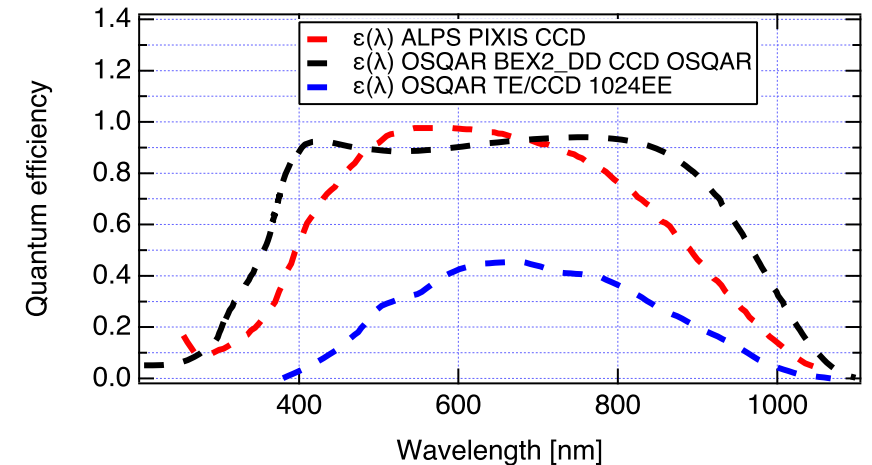
$$h_c^{\text{min}}(0, \omega) \simeq \sqrt{\frac{4 N_{\text{exp}}}{A B^2 L^2 \epsilon_\gamma(\omega) \Delta\omega}} \simeq 1.6 \times 10^{-16} \sqrt{\left(\frac{N_{\text{exp}}}{1 \text{ Hz}}\right) \left(\frac{1 \text{ m}^2}{A}\right) \left(\frac{1 \text{ T}}{B}\right)^2 \left(\frac{1 \text{ m}}{L}\right)^2 \left(\frac{1 \text{ Hz}}{\Delta f}\right) \left(\frac{1}{\epsilon_\gamma(\omega)}\right)}$$

Parameters necessary to compute the characteristic amplitude

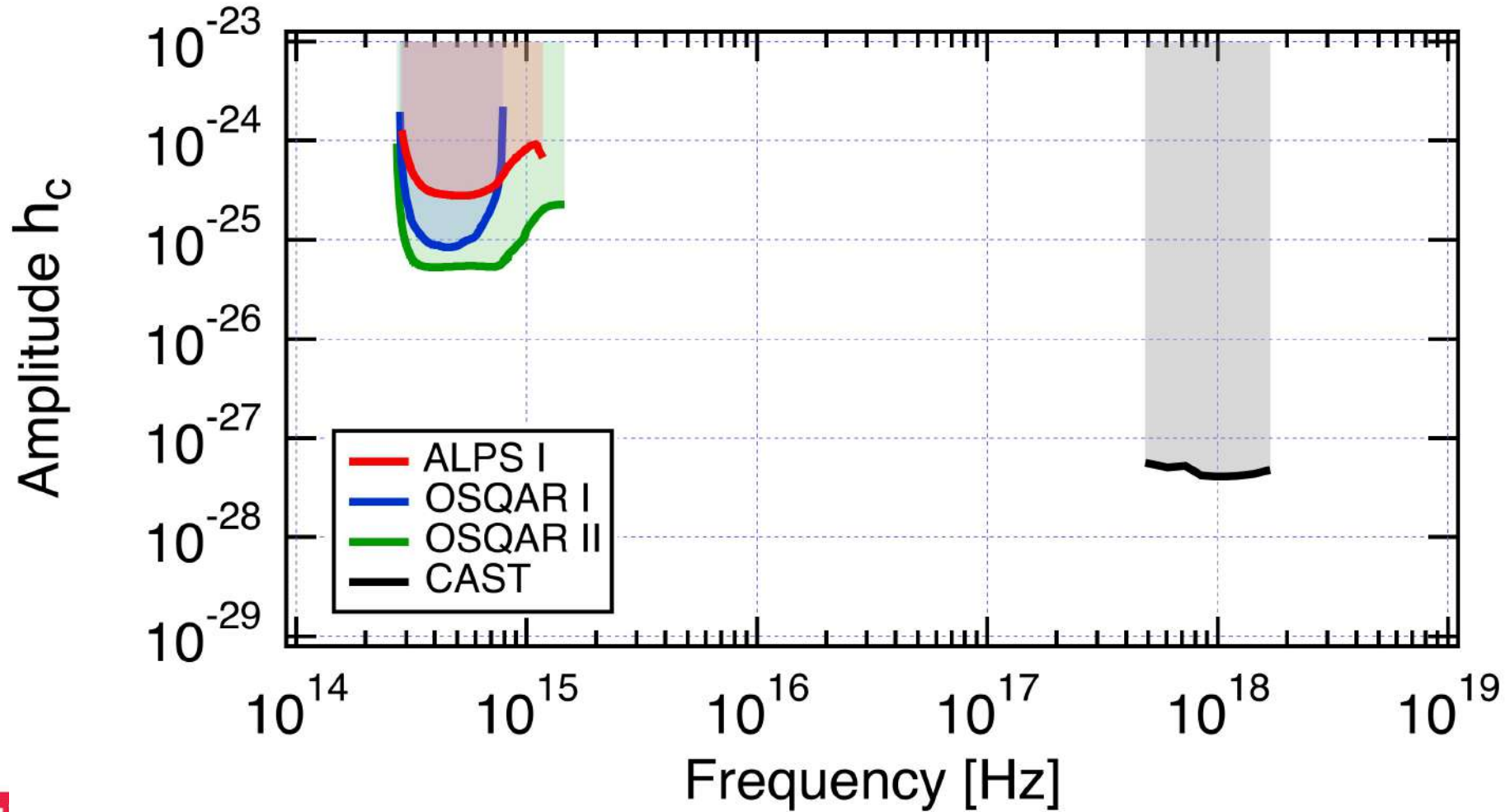
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- N_{exp} - detected number of photons per second,
- A - cross-section of the detector,
- B - magnetic field amplitude,
- L - distance extension of the magnetic field,
- $\epsilon_\gamma(\omega)$ - quantum efficiency of the detector,
- Δf - operation frequency of the CCD.

| | $\epsilon_\gamma(\omega)$ | N_{exp} (mHz) | A (m ²) | B (T) | L (m) | Δf (Hz) |
|----------|---------------------------|------------------------|-----------------------|---------|---------|--------------------|
| ALPS I | see Fig 2 | 0.61 | 0.5×10^{-3} | 5 | 9 | 9×10^{14} |
| OSQAR I | see Fig 2 | 1.76 | 0.5×10^{-3} | 9 | 14.3 | 5×10^{14} |
| OSQAR II | see Fig 2 | 1.14 | 0.5×10^{-3} | 9 | 14.3 | 1×10^{15} |
| CAST | see Fig 2 | 0.15 | 2.9×10^{-3} | 9 | 9.26 | 1×10^{18} |



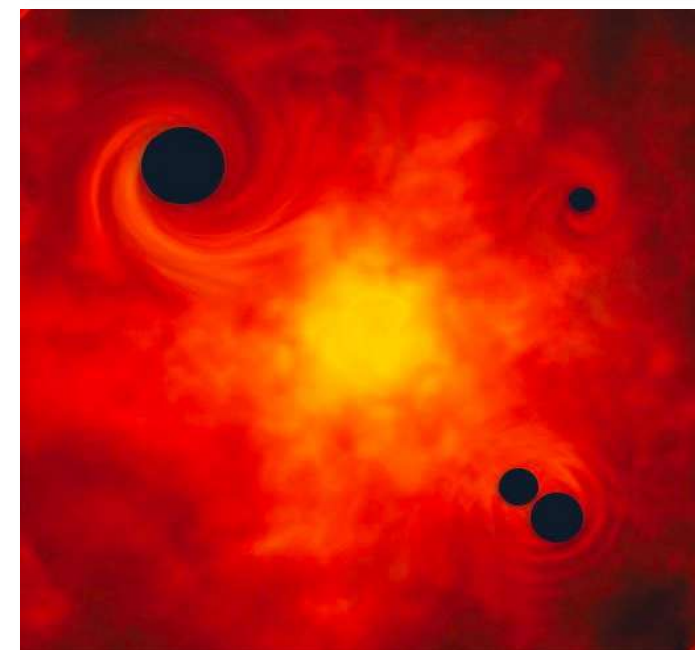
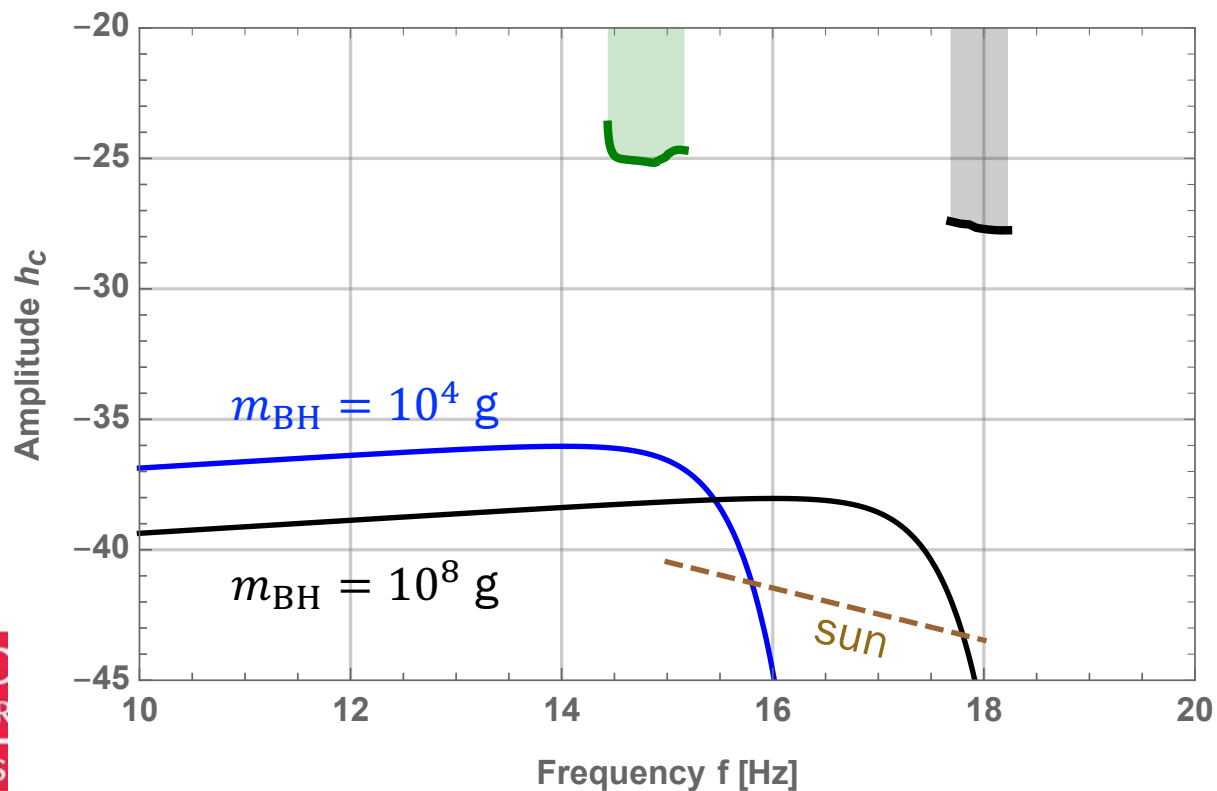
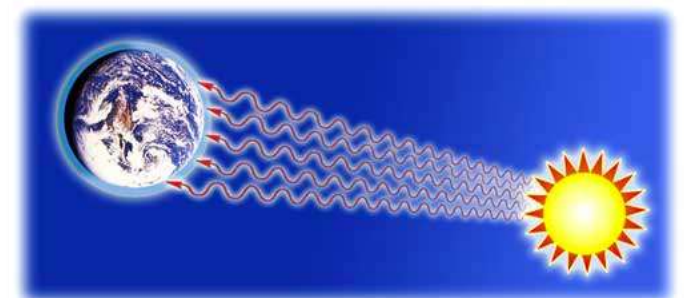
UHF GW characteristic amplitude upper limits



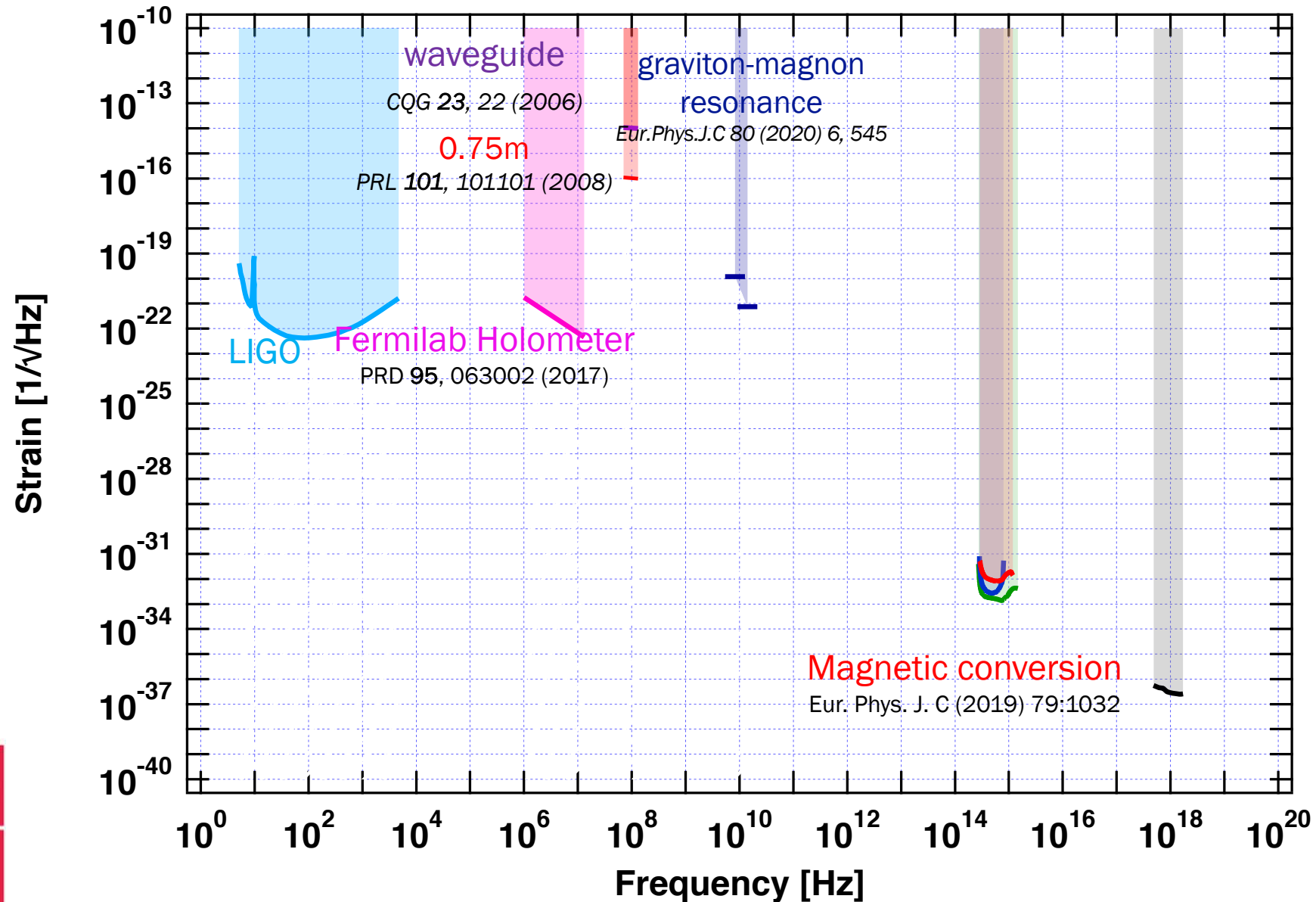
Primordial black hole evaporation and upper limits

- PBH evaporation: predicted stochastic isotropic UHF GWs background
- Sun: thermal activity generates UHF GWs.

$$\frac{d\rho_\gamma^{\text{Sun}}}{d(\log \omega)} \approx 5.7 \times 10^{-62} \text{ GeV}^4 \text{ @ Earth}$$



STRAIN UPPER LIMITS



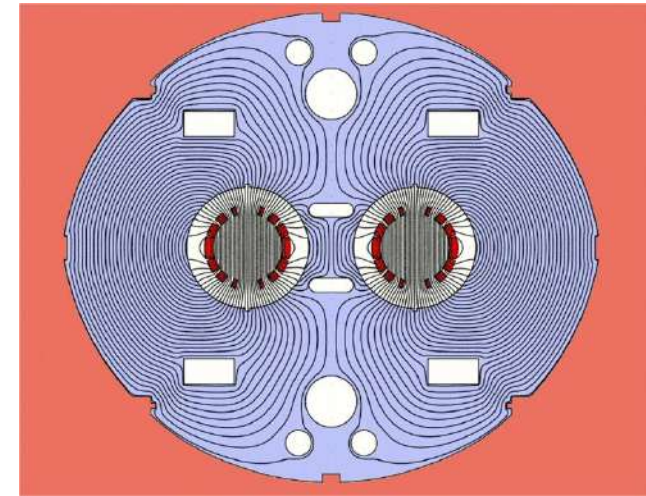


WHERE TO NEXT?

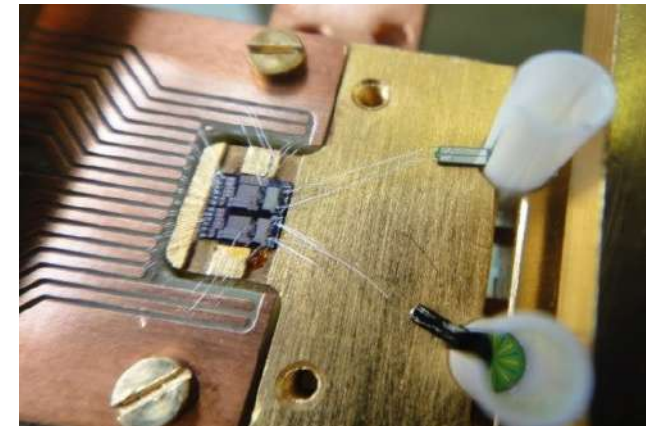
Graviton to photon conversion and synergies with next generation axion search experiments

$$h_c^{\min}(0, \omega) \simeq \sqrt{\frac{4 N_{\text{exp}}}{A B^2 L^2 \epsilon_\gamma(\omega) \Delta\omega}} \simeq 1.6 \times 10^{-16} \sqrt{\left(\frac{N_{\text{exp}}}{1 \text{ Hz}}\right) \left(\frac{1 \text{ m}^2}{A}\right) \left(\frac{1 \text{ T}}{B}\right)^2 \left(\frac{1 \text{ m}}{L}\right)^2 \left(\frac{1 \text{ Hz}}{\Delta f}\right) \left(\frac{1}{\epsilon_\gamma(\omega)}\right)}$$

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TES



ALPSII: Magnets installation



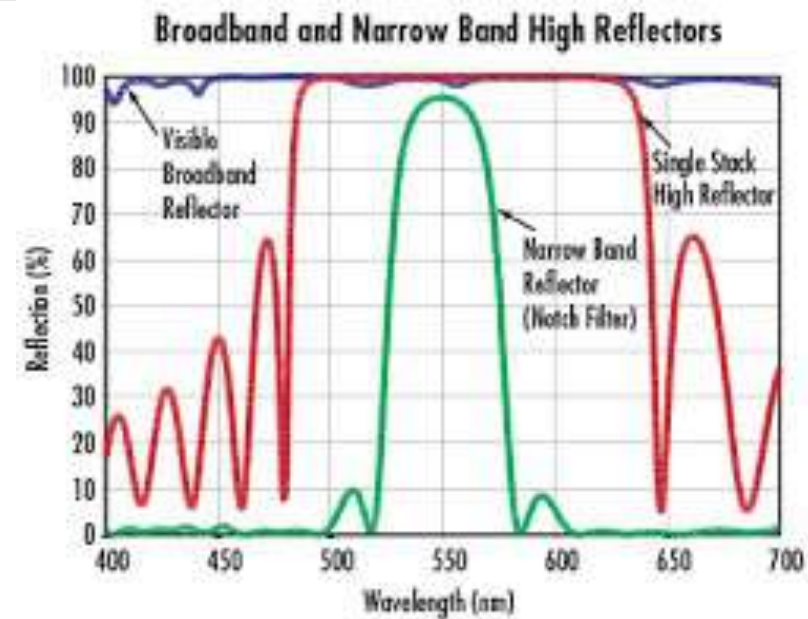
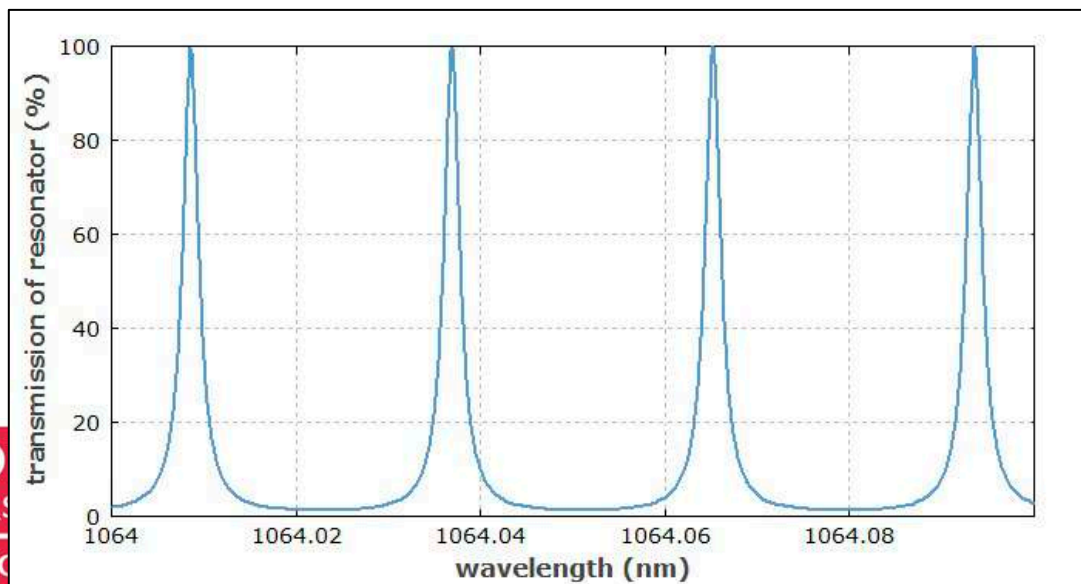
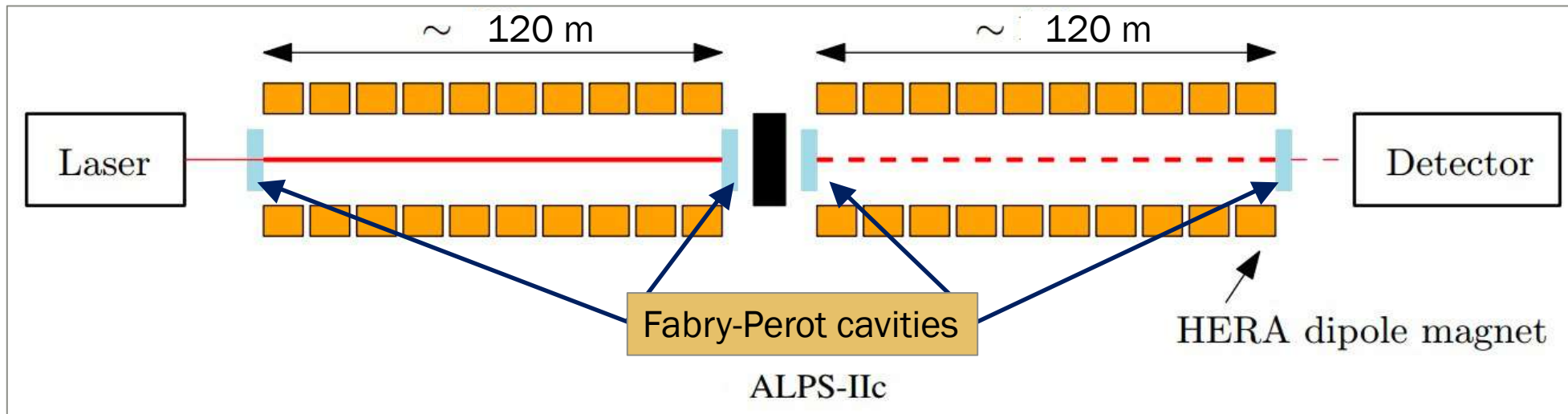
ALPS II under construction (Credit: DESY)

ALPS II

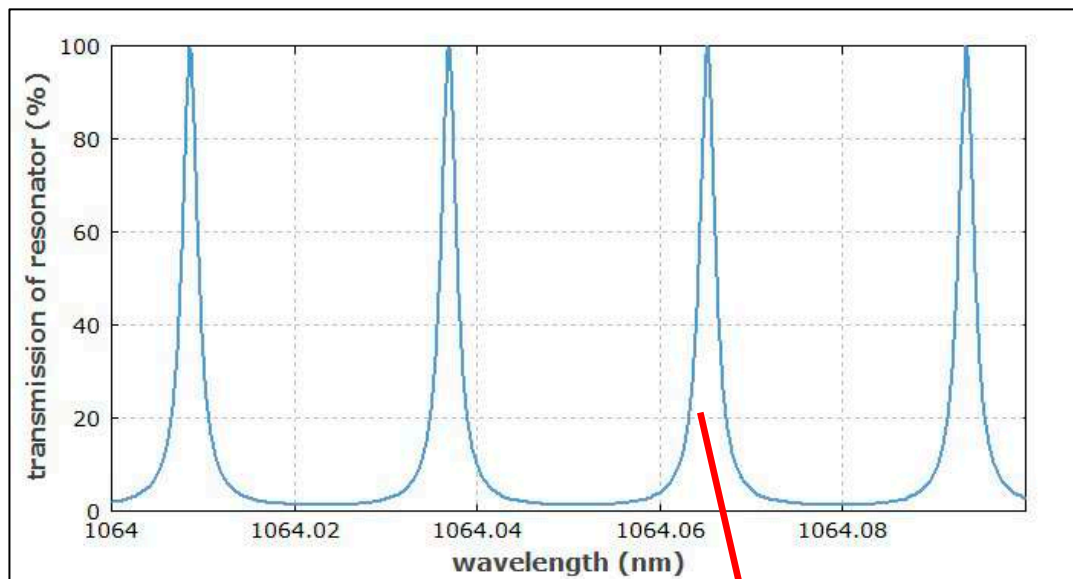
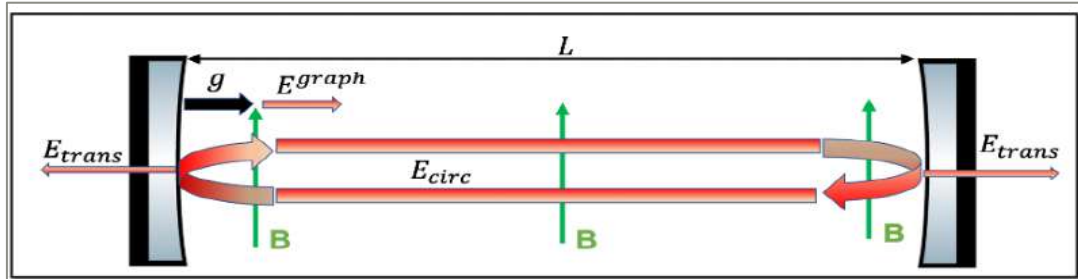


ALPS II under construction as of October 2020 (Credit: DESY)

ALPS II: Fabry-Perot cavities



Graviton-to-photon in the conversion Fabry-Perot cavity



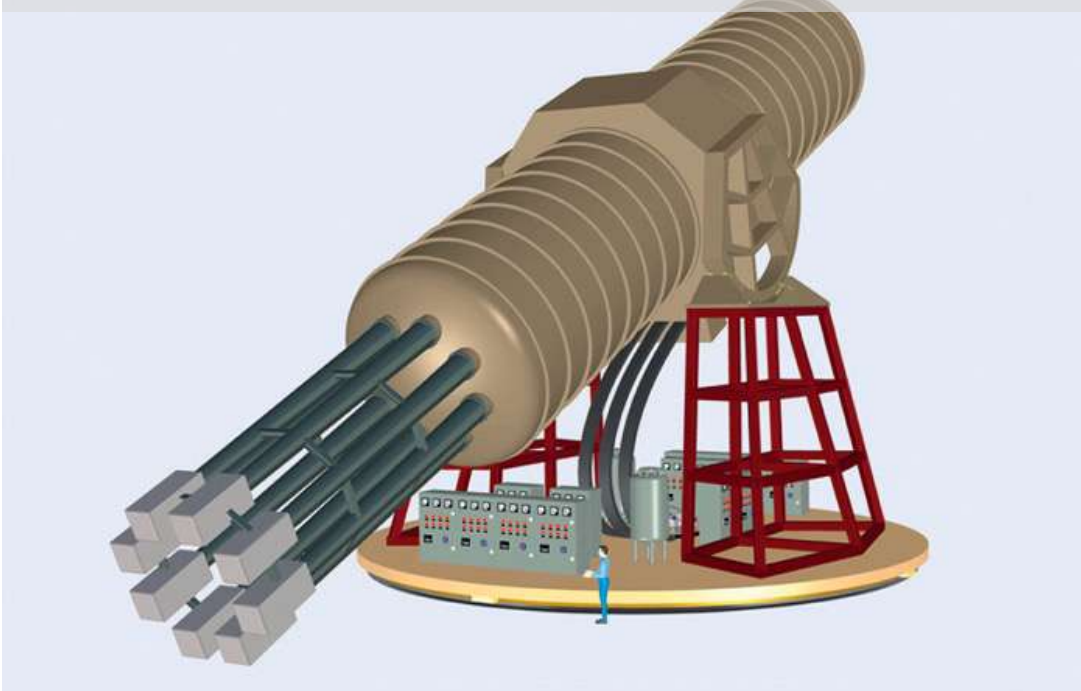
$$\begin{aligned}\vec{E}_{x,y}^{\text{circ}}(z,t) &= \vec{E}_{x,y}^{\text{graph}}(z,t) \left(1 + R e^{-i2\phi(\omega,L)} + \left(R e^{-i2\phi(\omega,L)} \right)^2 + \dots \right) \\ &= \vec{E}_{x,y}^{\text{graph}}(z,t) \sum_{n=0}^{\infty} \left(R e^{-i2\phi(\omega,L)} \right)^n \\ &= \vec{E}_{x,y}^{\text{graph}}(z,t) \frac{1}{1 - R e^{-i2\phi(\omega,L)}}\end{aligned}$$

$$\begin{aligned}\Phi_{\gamma}^{\text{trans}}(L, \omega_f; t) &= \int_{\omega_i}^{\omega_f} \frac{B_x^2 L^2 h_c(0, \omega)^2}{4} \frac{1 - R}{(1 - R)^2 + 4R \sin^2 [\phi(\omega, L)]} \omega d\omega. \\ &\frac{B_x^2 L^2 h_c(0, \omega)^2}{4} \frac{\mathcal{F}}{\pi} \omega \quad \text{for} \quad \phi(\omega, L_R) = n\pi\end{aligned}$$

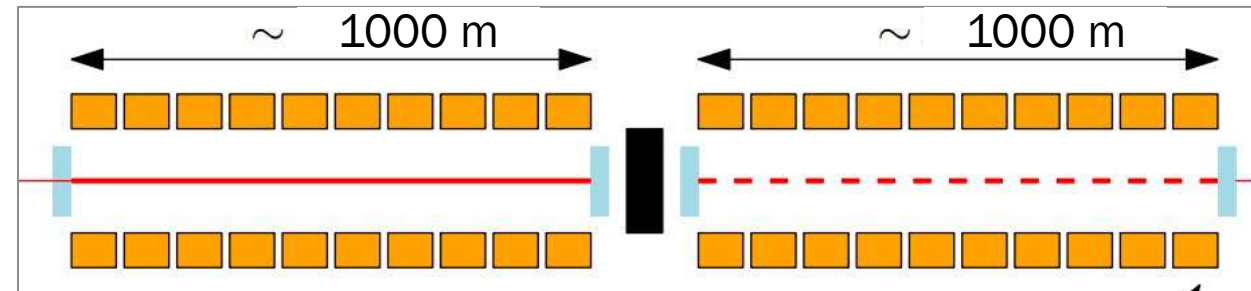
$$h_c^{\text{min}}(0, \omega^*) \simeq 2.8 \times 10^{-16} \sqrt{\left(\frac{1}{\mathcal{F}} \right) \left(\frac{N_{\text{dark}}}{1 \text{ Hz}} \right) \left(\frac{1 \text{ m}^2}{A} \right) \left(\frac{1 \text{ T}}{B} \right)^2 \left(\frac{1 \text{ m}}{L} \right)^2 \left(\frac{1 \text{ Hz}}{\Delta f} \right) \left(\frac{1}{\epsilon_{\gamma}(\omega)} \right)}$$

Future laboratory axion experiments: JURA, IAXO.

IAXO (Armengaud et al. *JINST* 9 T05002 (2014))

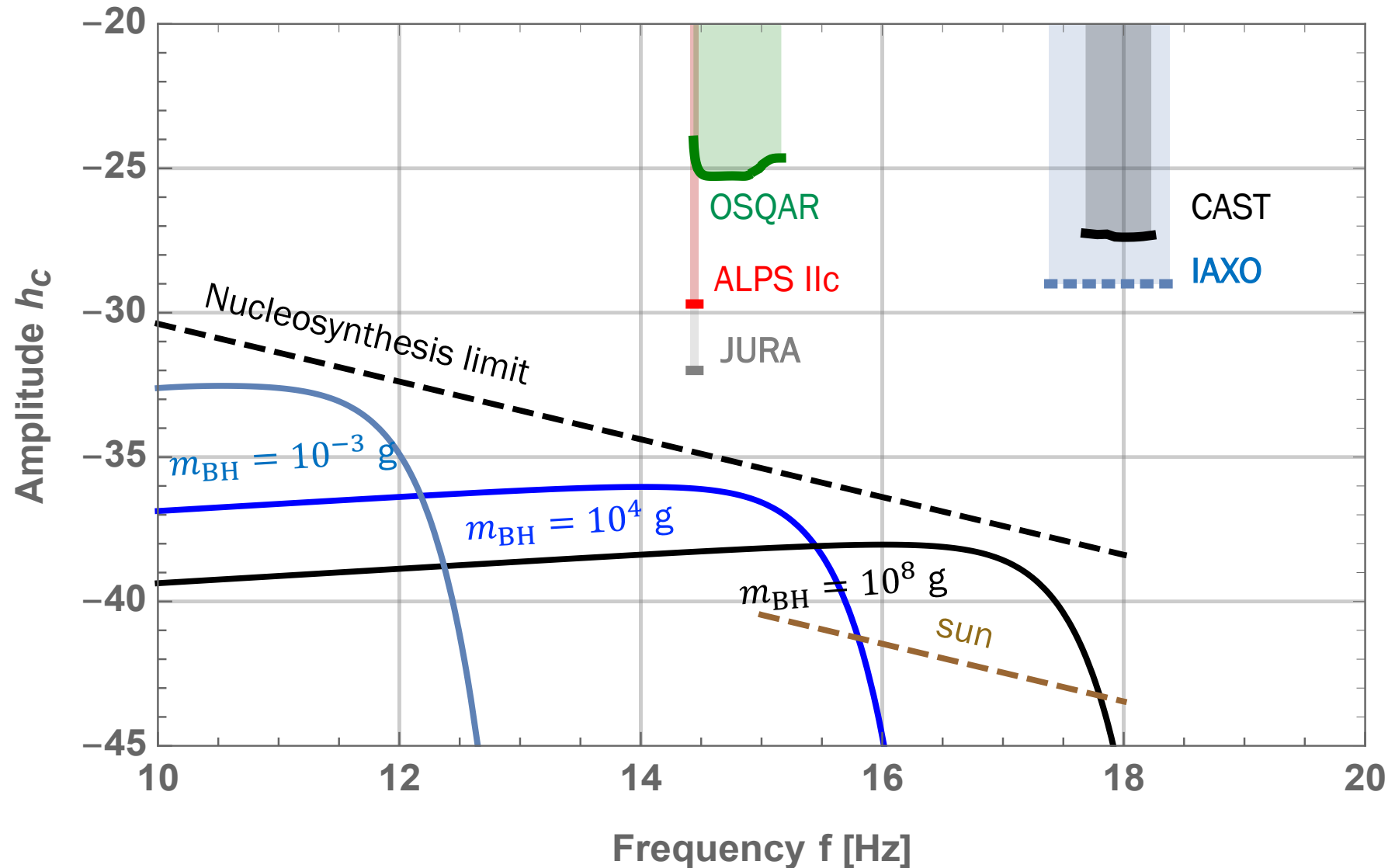


JURA



| | ϵ_γ | N_{dark} (Hz) | A (m ²) | B (T) | L (m) | \mathcal{F} |
|----------|-------------------|------------------------|----------------------------|---------|---------|---------------|
| ALPS IIc | 0.75 | $\approx 10^{-6}$ | $\approx 2 \times 10^{-3}$ | 5.3 | 120 | 40 000 |
| JURA | 1 | $\approx 10^{-6}$ | $\approx 8 \times 10^{-3}$ | 13 | 960 | 100 000 |
| IAXO | 1 | $\approx 10^{-4}$ | ≈ 21 | 2.5 | 25 | - |

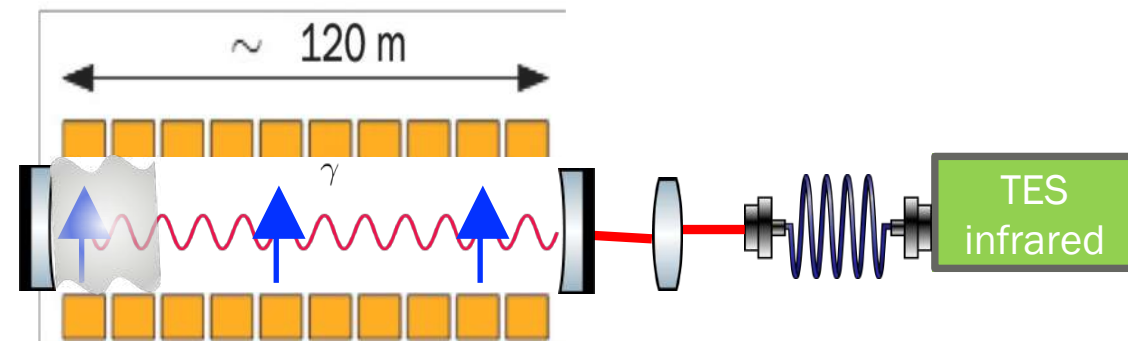
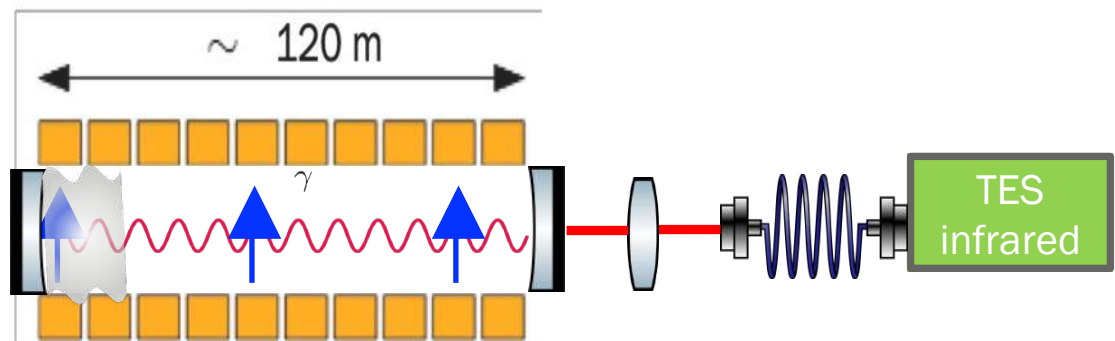
Prospects



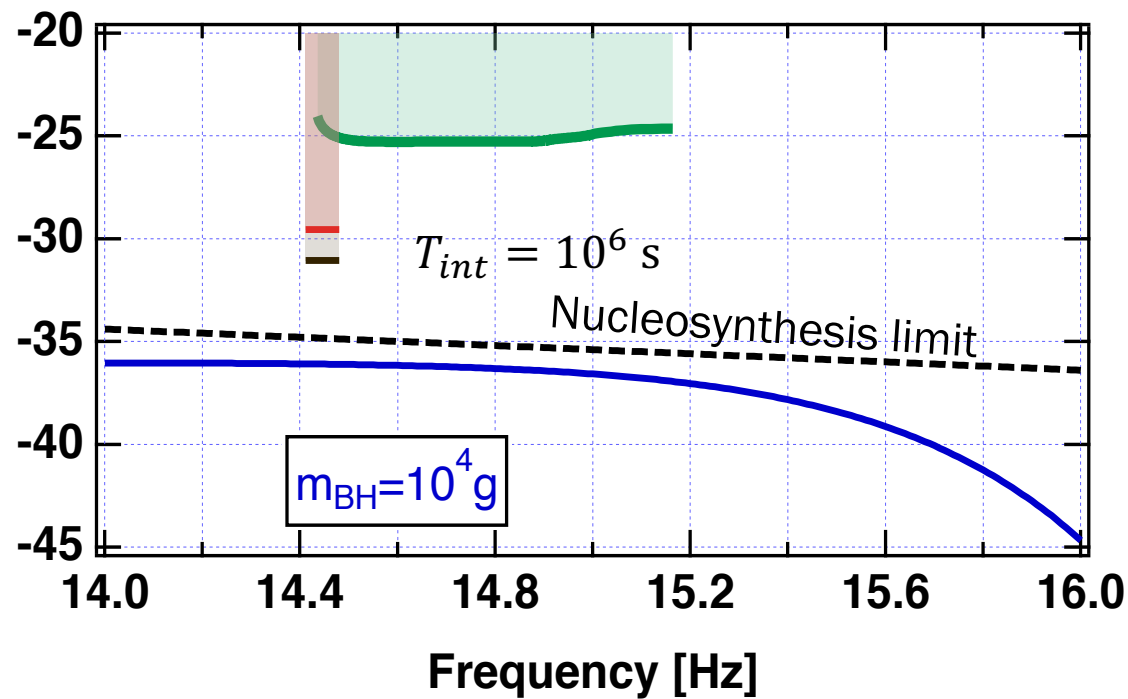
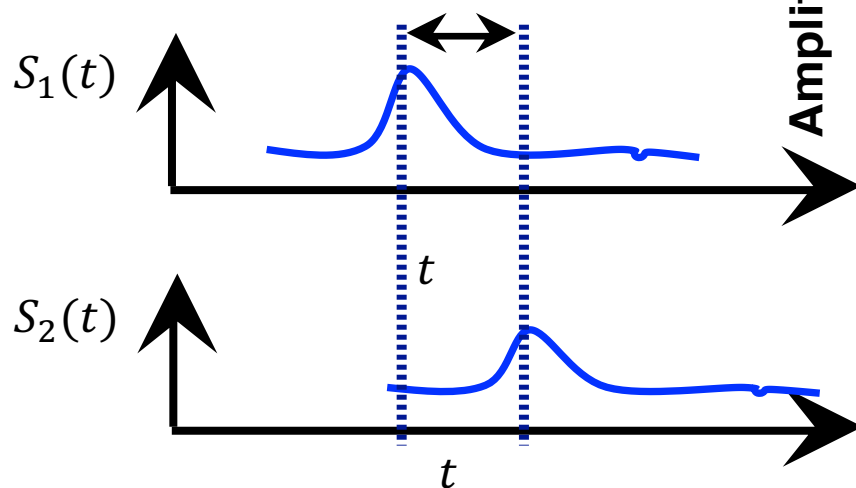


UPGRADES?

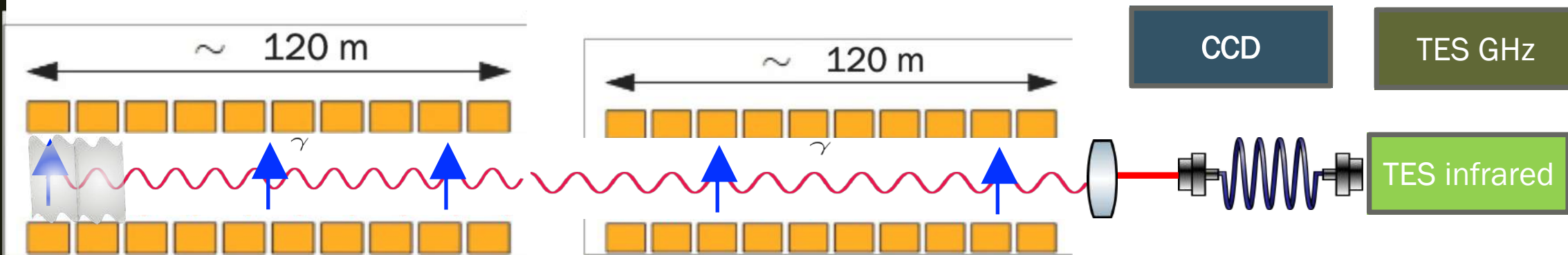
ALPS II: modifications



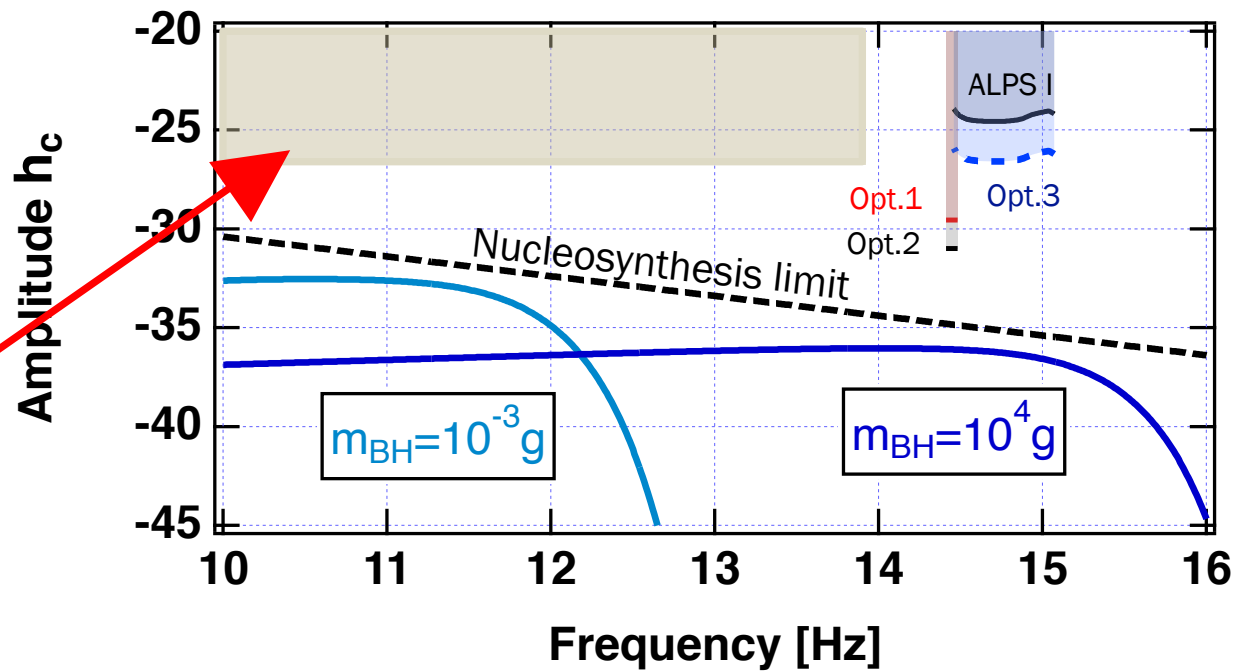
- Cross correlation
- Reduction background noise
- Possible identification of GW's transients



ALPS II without FP cavities

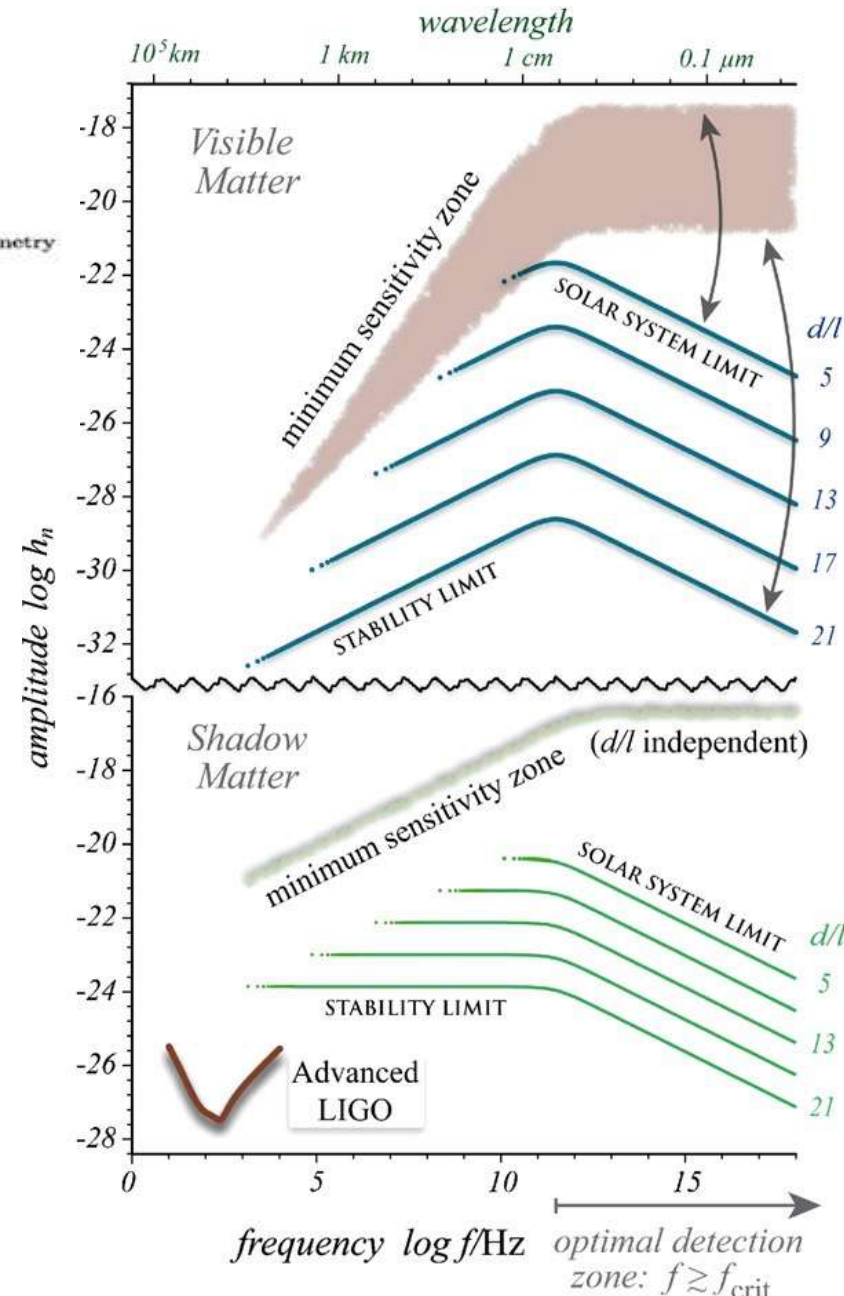
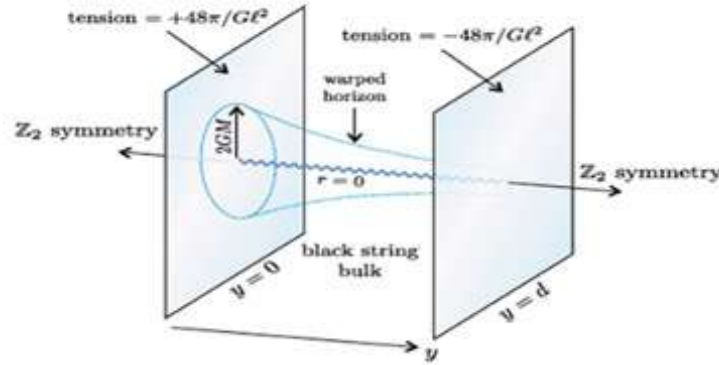


- Double length 2×10^6 m of the magnetic field.
- Possibility to investigate new frequency regions
- Interesting region in the GHz!

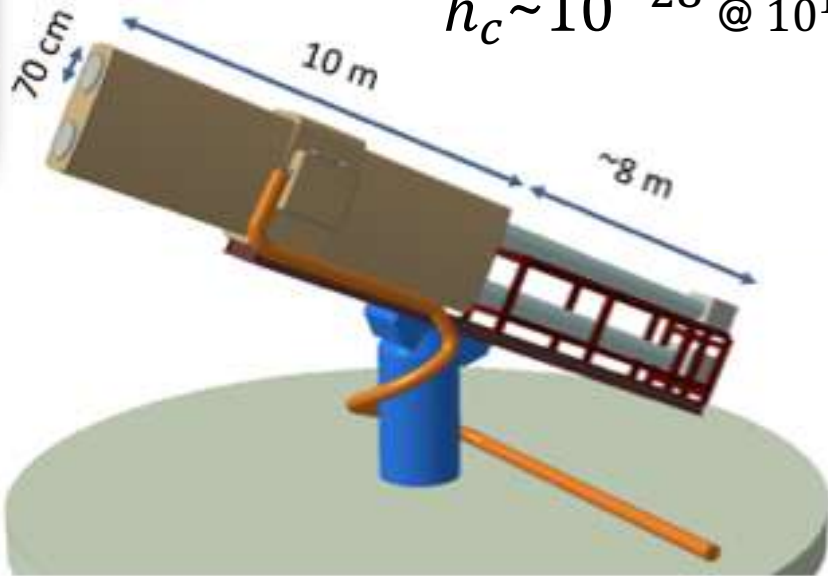


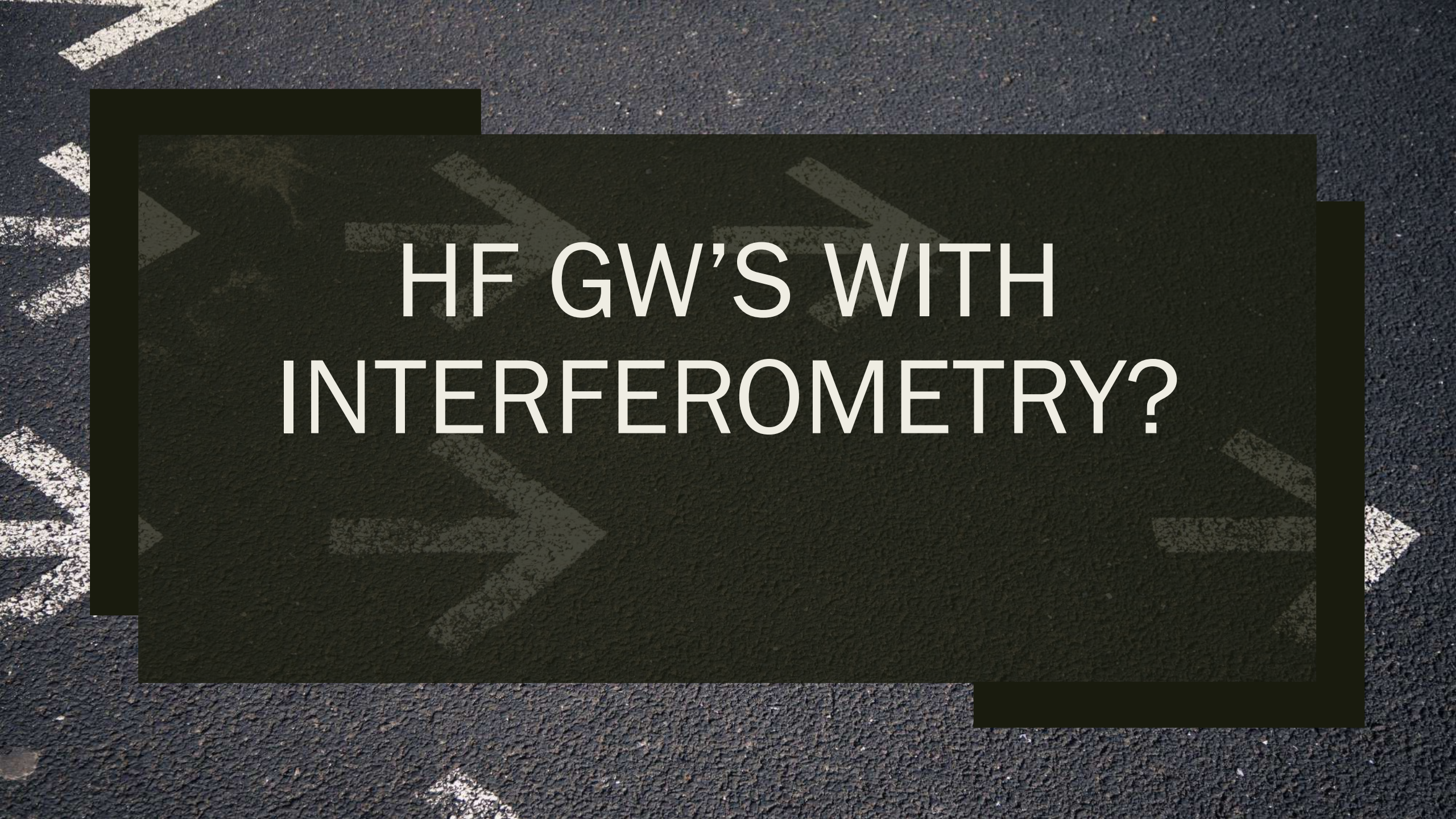
Baby IAXO, IAXO

- Pointing: rotatable platform
- BH-BH collisions in higher dimensional gravity



$10 \times \text{CAST } (B^2 L^2 A)$
 $h_c \sim 10^{-28} @ 10^{17} - 10^{18} \text{ Hz}$

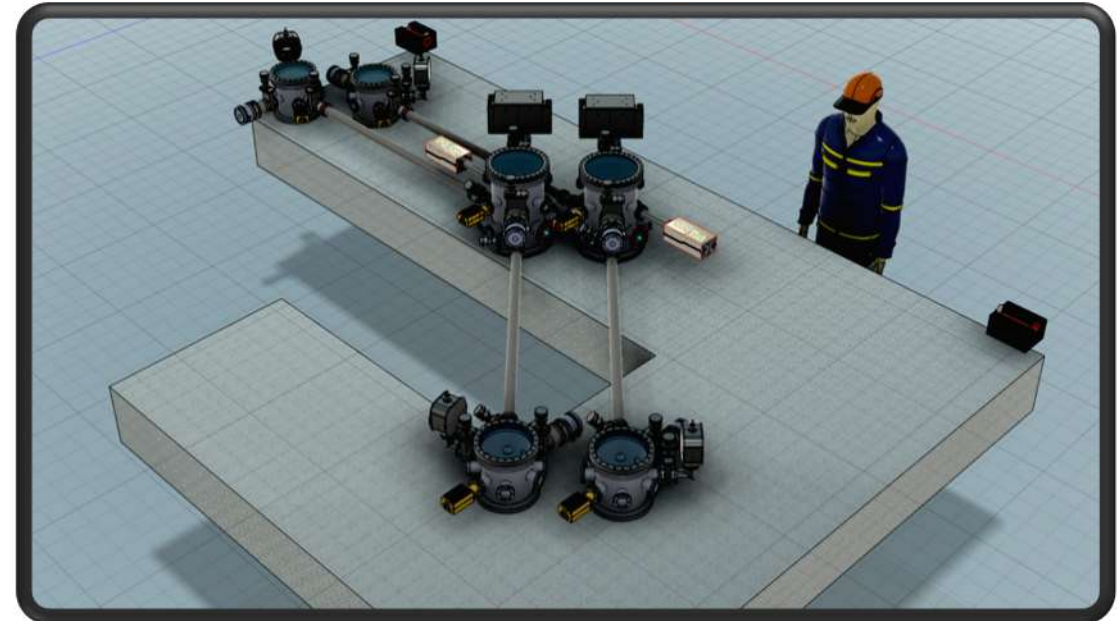
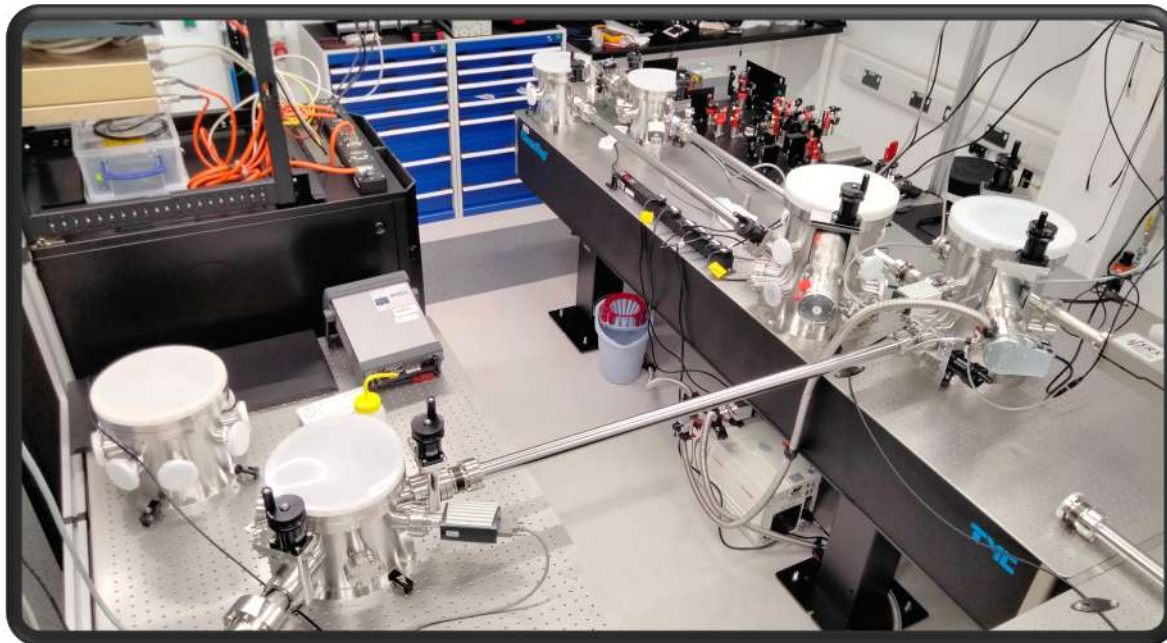




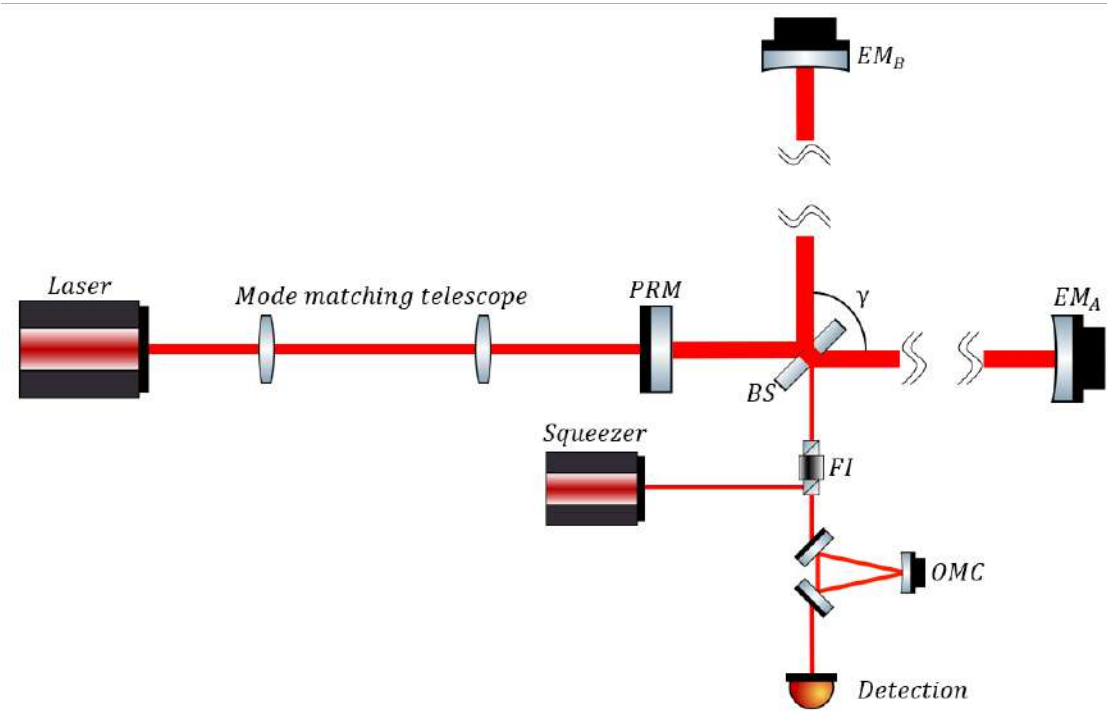
HF GW'S WITH INTERFEROMETRY?

Co-located interferometry up to 250 MHz at Cardiff University

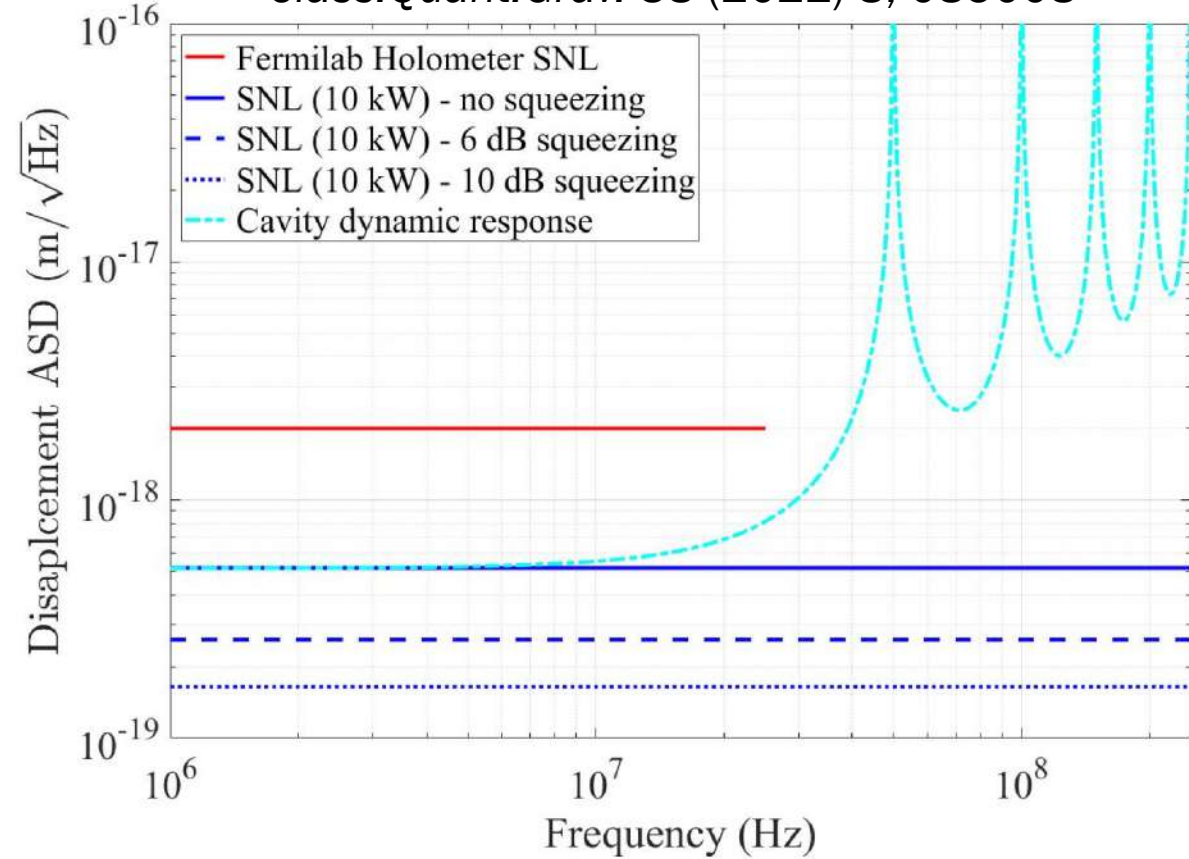
- Quantization of space-time (main scientific goal)
- Dark matter searches
- High-frequency gravitational waves (1 - 250 MHz)



Co-located interferometry up to 250 MHz



Class.Quant.Grav. 38 (2021) 8, 085008



Conclusions

Axion search experiments ALPS I, OSQAR and CAST, set first upper limits on stochastic UHF GWs.

The upgraded ALPS II, Baby-IAXO/IAXO, provide infrastructure to improve the existing upper limits for stochastic UHF GWs.

Minor modifications of axion experiments could improve sensitivity to UHF GWs.

Axion search experiments are also being identified as novel UHF GW detectors.



THANK YOU FOR
YOUR ATTENTION